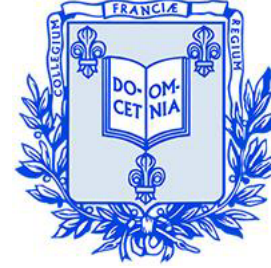
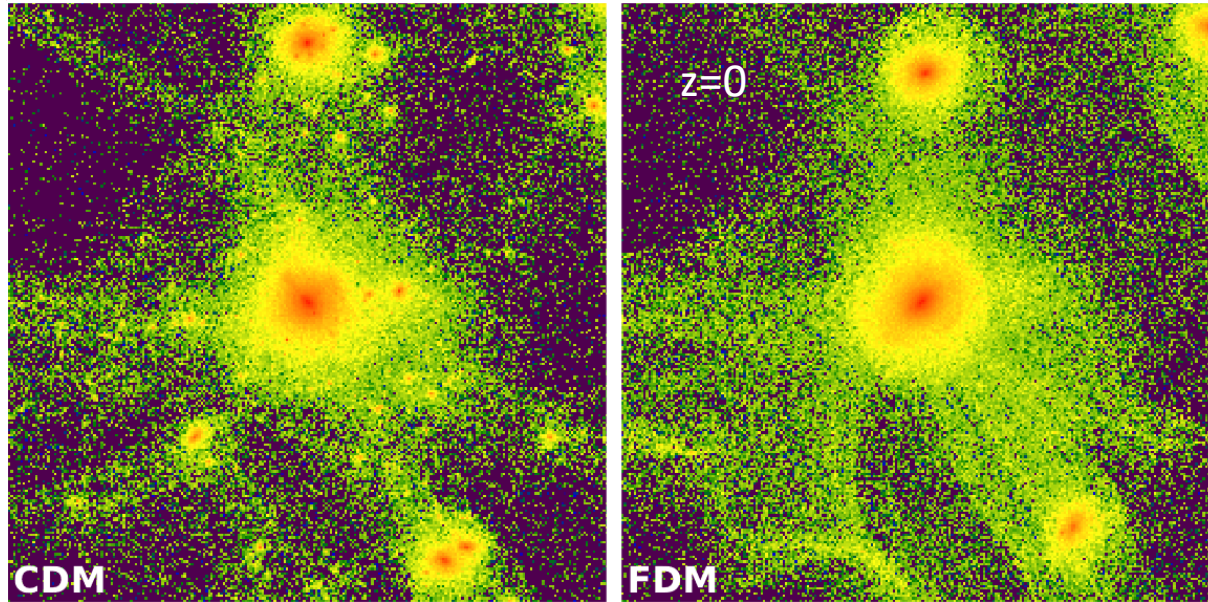


The dark matter puzzle



COLLÈGE
DE FRANCE
— 1530 —

Chaire Galaxies et Cosmologie



Ultra-Light Axions (ULA)
Scalar-field, non-interacting

WIMPS

Schwabe & Niemeyer 2022

Françoise Combes
July, 2023

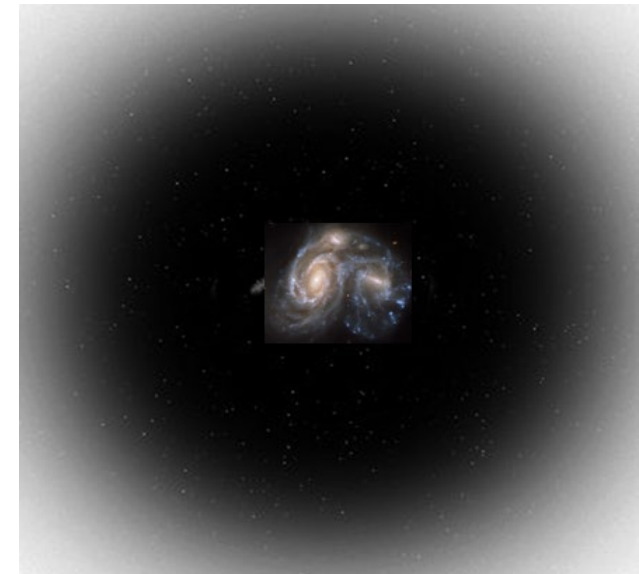
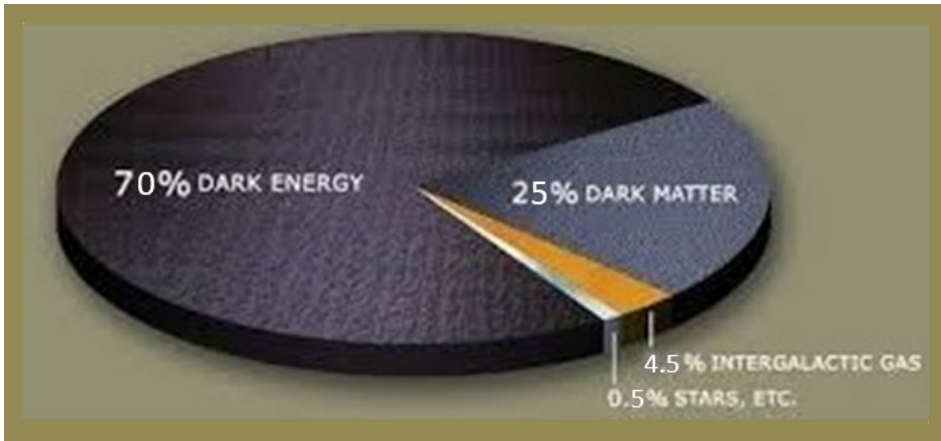


Abell 2218

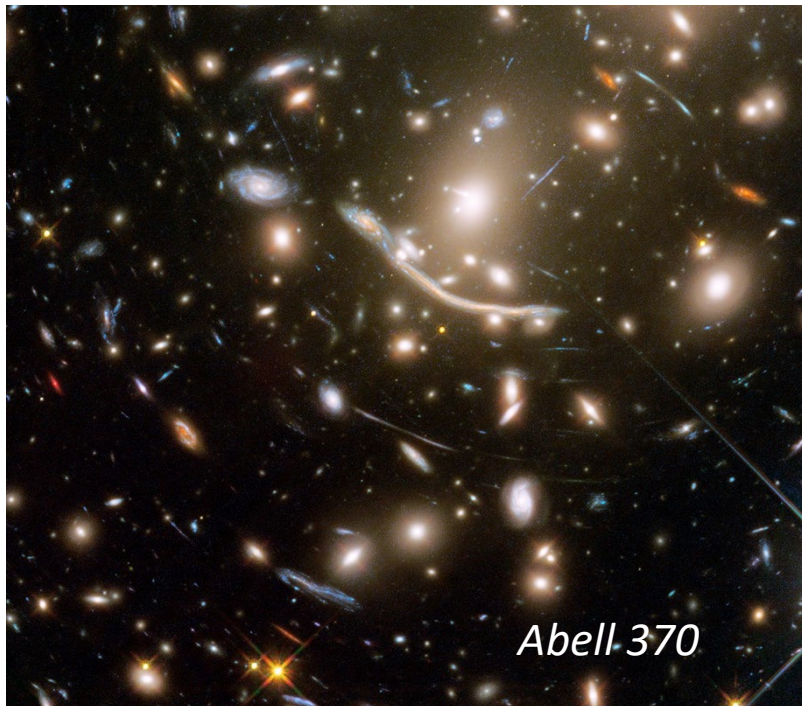


Where is the dark matter?

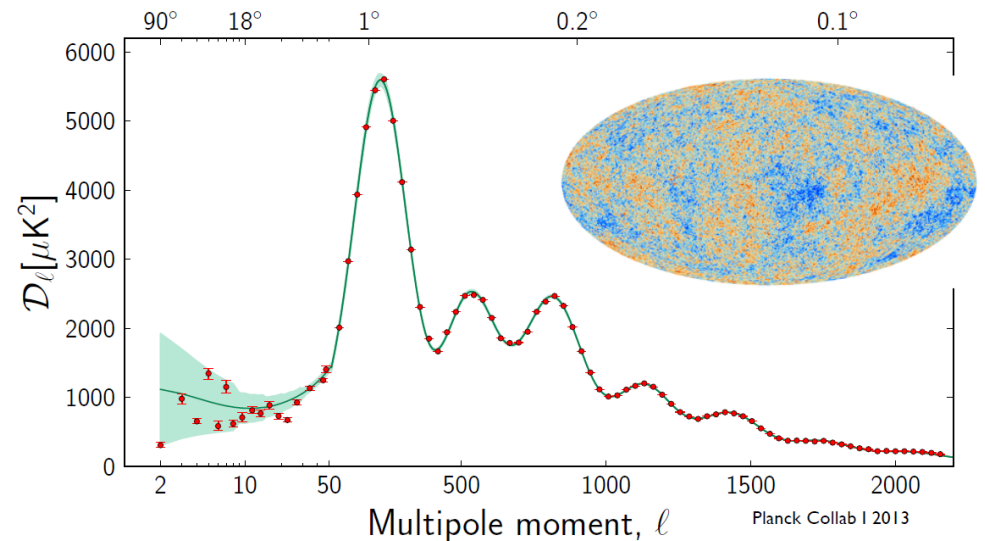
Galaxies



Galaxy clusters



Planck : power spectrum $\Omega_b, \Omega_m, \Omega_\Lambda$



The WIMP miracle

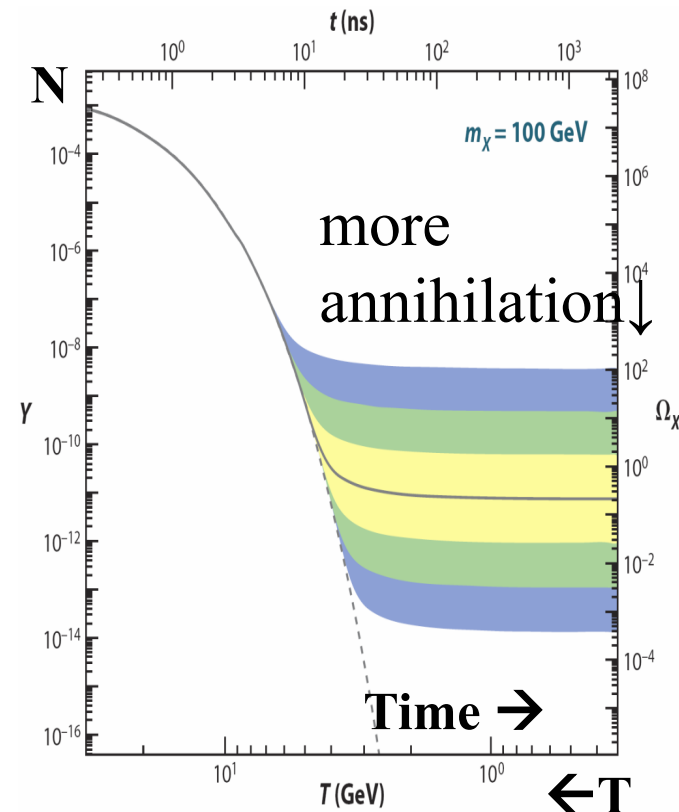
Possible to obtain the required abundance of dark matter with particles of mass ~ 100 GeV, with the **weak interaction force** annihilation rate $\langle\sigma v\rangle \sim 3 \cdot 10^{-26} \text{ cm}^3/\text{s}$

In early Universe, abundance of particles is « frozen », they decouple when their interaction

$$n \langle\sigma v\rangle \sim 1/t_{\text{hubble}}$$

Coincidence: corresponds to the lightest particle of super-symmetry (neutralino)

**But in LHC: no super-symmetry,
No new particle!**



Particles beyond standard model?

	fermions (3 générations de la matière)			bosons (forces)	
	I	II	III		
masse →	2,4 MeV/c ²	1,27 GeV/c ²	171,2 GeV/c ²	0	électromagnétisme
charge →	2/3	2/3	2/3	0	
spin →	1/2	1/2	1/2	1	
nom →	u up	c charm	t top	γ photon	
Quarks	4,8 MeV/c ²	104 MeV/c ²	4,2 GeV/c ²	0	interaction forte
	-1/3	-1/3	-1/3	0	
	1/2	1/2	1/2	1	
nom	d down	s strange	b bottom	g gluon	
Leptons	<2,2 eV/c ²	<0,17 MeV/c ²	<15,5 MeV/c ²	91,2 GeV/c ²	interaction faible
	0	0	0	0	
	1/2	1/2	1/2	1	
nom	ν _e neutrino électronique	ν _μ neutrino muonique	ν _τ neutrino tauique	Z ⁰ boson Z ⁰	
	0,511 MeV/c ²	105,7 MeV/c ²	1,777 GeV/c ²	80,4 GeV/c ²	interaction faible
	-1	-1	-1	±1	
	1/2	1/2	1/2	1	
	e électron	μ muon	τ tau	W [±] boson W	

From the Big-Bang

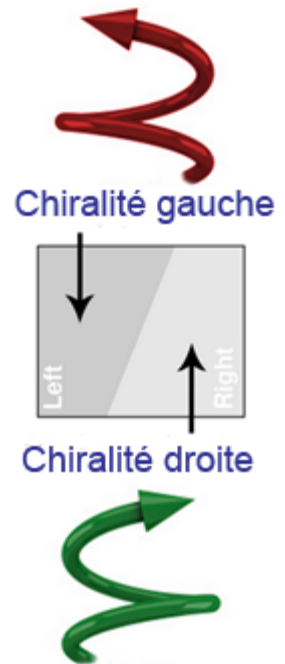
~400 photons /cm³

~300 neutrinos /cm³

0,1 billions of billions/s
cross us

→ Search for
WIMPS
since 1985

Extension to
sterile neutrinos?



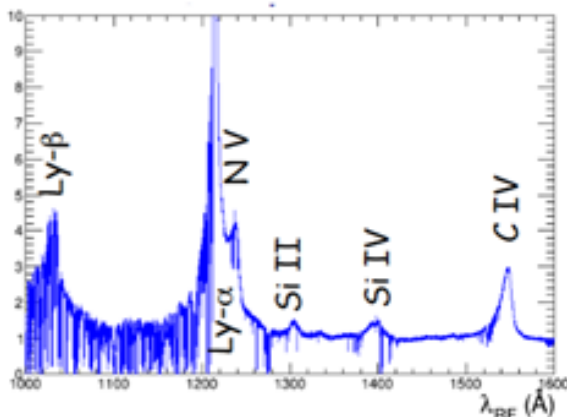
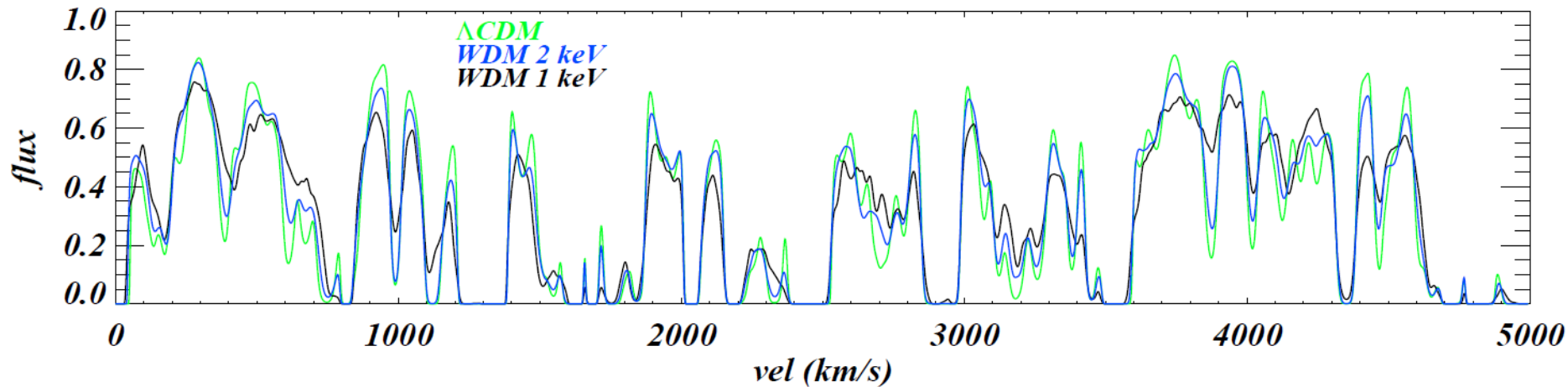
<0.0001 eV	~keV	~0.01 eV	~GeV	~0.04 eV	~GeV
0	N ₁	0	N ₂	0	N ₃
left	sterile neutrino	left	sterile neutrino	left	sterile neutrino
ν _e neutrino électronique		ν _μ neutrino muonique		ν _τ neutrino tauique	

Ly- α : constraints on $m(\text{warm})$



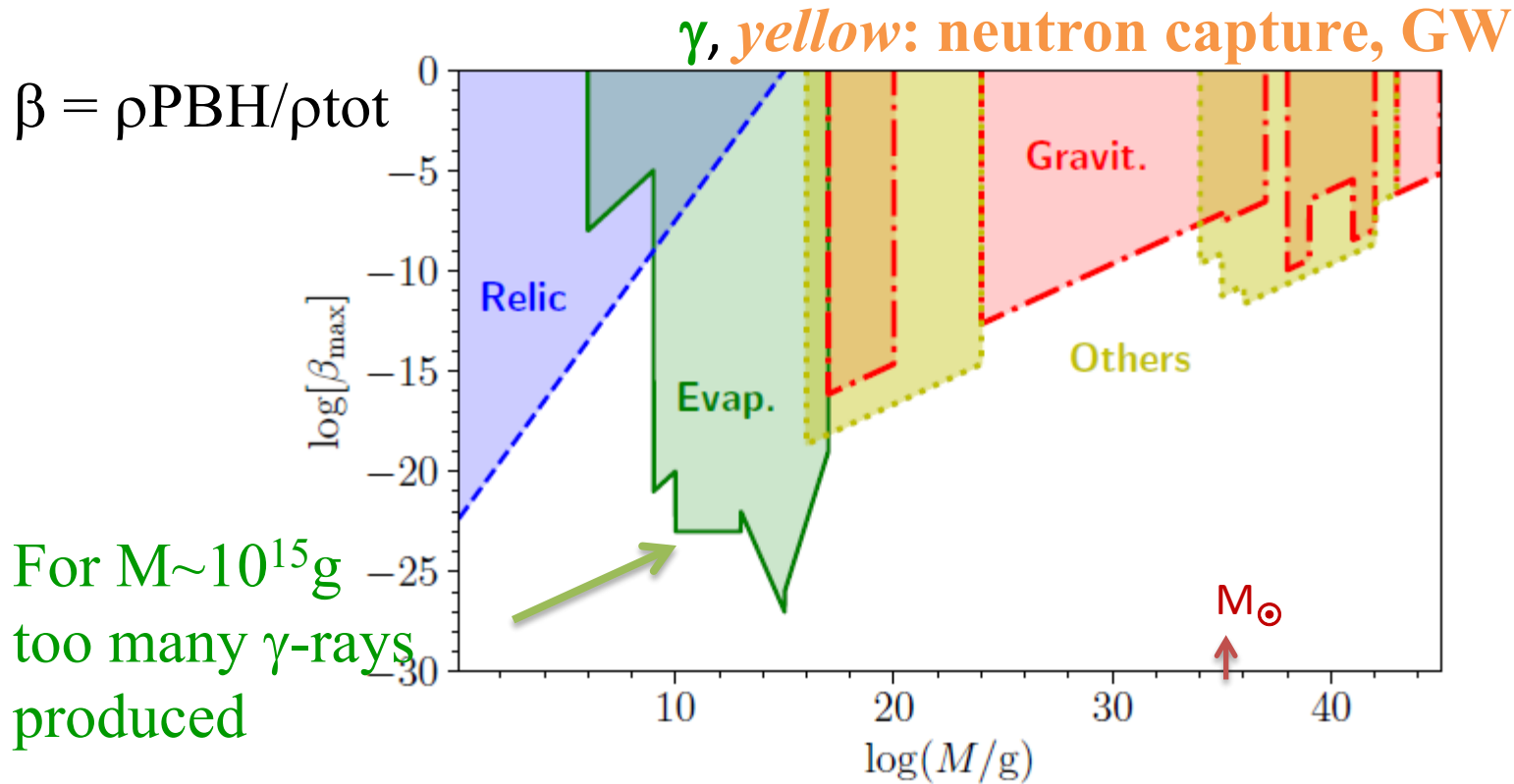
25 quasars $z > 4$: spectra obtained at Keck (*Viel et al 2013*)

Ly- α forest and comparison with simulations $m_{\text{WDM}} > 3.3 \text{ keV}$ (2σ)



$\text{WDM, } m_x > 4.65 \text{ keV}$ thermal relics
 $m_s > 29 \text{ keV}$ non-resonant production
Yeche et al (2017), Chabanier et al (2019)

Primordial Black holes



Since PBH form in the radiative era, they can be considered as non-baryonic, and =CDM

However, their mass is limited by MACHOS, EROS experiments

Small masses evaporate

Candidates for the dark matter

New physics, beyond the standard model SM

Kaluza-Klein DM in UED

Kaluza-Klein DM in RS (Randall-Sundrum)

Axion

Axino

Gravitino

Photino

SM Neutrino

Sterile Neutrino

Sneutrino

Light DM

Little Higgs DM

Wimpzillas

Cryptobaryonic DM

Q-balls

Champs (charged DM)

D-matter

Cryptons

Self-interacting

Superweakly interacting

Braneworld DM

Heavy neutrino

Neutralino (WIMP)

Messenger States in GMSB

Branons

Chaplygin Gas

Split SUSY

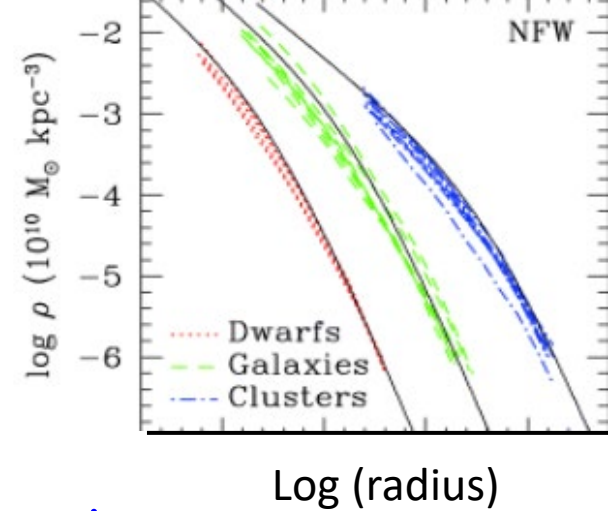
Primordial Black Holes

Mirror Matter

...

Fuzzy dark matter

Cusps exist in galaxy clusters, but not in galaxies
In dwarf galaxies, cores of ~ 1 kpc



Bosons generated in non-thermal mechanisms \rightarrow axions
(ALP, Marsh 2016) cold particles, which can collapse
BEC “Bose-Einstein condensate”, macroscopic state at low T

- Finite mass, very small, λ de Broglie, $\lambda_{\text{dB}} = h/m_a v$
 $\rightarrow \lambda_{\text{dB}} = 1-2$ kpc
- In fact $\lambda_{\text{dB}} \sim 1-2$ kpc for $m_a = 10^{-22}$ eV, and $v \sim 10$ km/s

For masses $m_a = 10^{-22}$ eV, quantum pressure prevents the formation of structures below $M_{\text{cut}} = 3 \cdot 10^8 m_{22}^{-3/2} M_{\odot}$ (Hui et al 2017)

A long history

Already 40 yrs!

Baldeschi, Gelmini, Ruffini (1983)

Galactic dark matter halos made of fermions of $m=10^{-3}$ eV,
or bosons of $m=10^{-24}$ eV



Mass-size relation for equilibrium

For $M \sim 10^{12} M_{\odot}$ $R \sim 30$ kpc

$$MR = 9.9 \hbar^2 / Gm^2$$

Sin (1994) rotation curves with pseudo Nambu-Goldstone boson

Hu et al (2000), are they self-interacting (SI) or not?

Scalar field SFDM \rightarrow SI-SFDM

Böhmer & Harko (2007)

Hui et al (2017) review and revisit the problem: $m > 10^{-21}$ eV

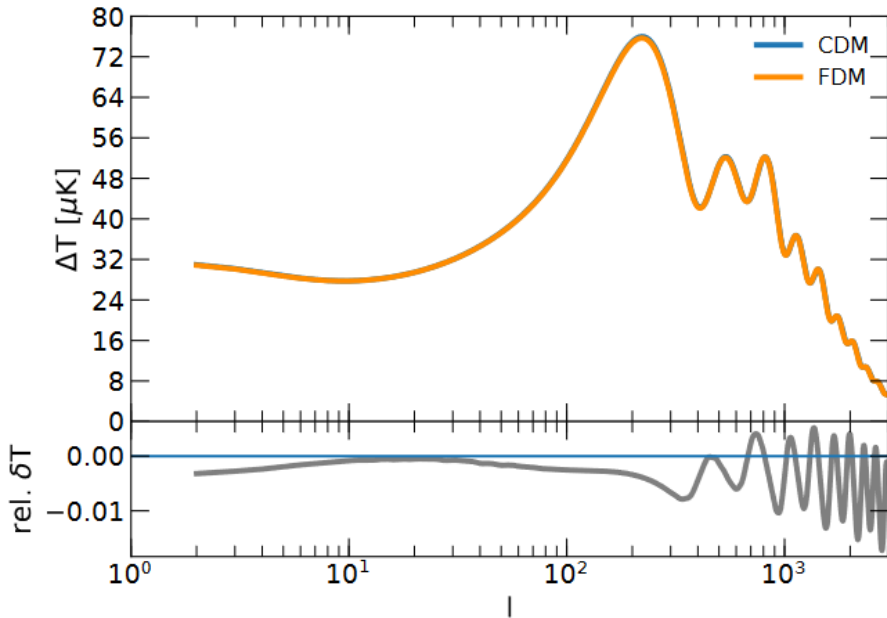
Fluctuation spectrum

Temperature anisotropies are undistinguishable from Λ CDM

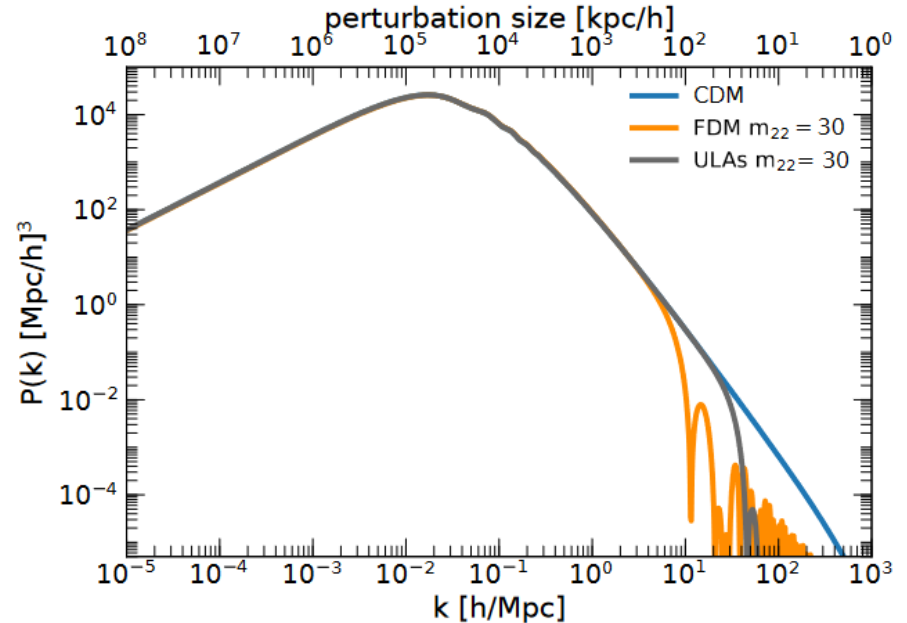
Foidl & Rindler-Daller 2022

Scalar-field DM (SFDM without self-interaction \rightarrow FDM)

Or Ultra-light actions (from QCD) \rightarrow cut the high spatial frequencies k

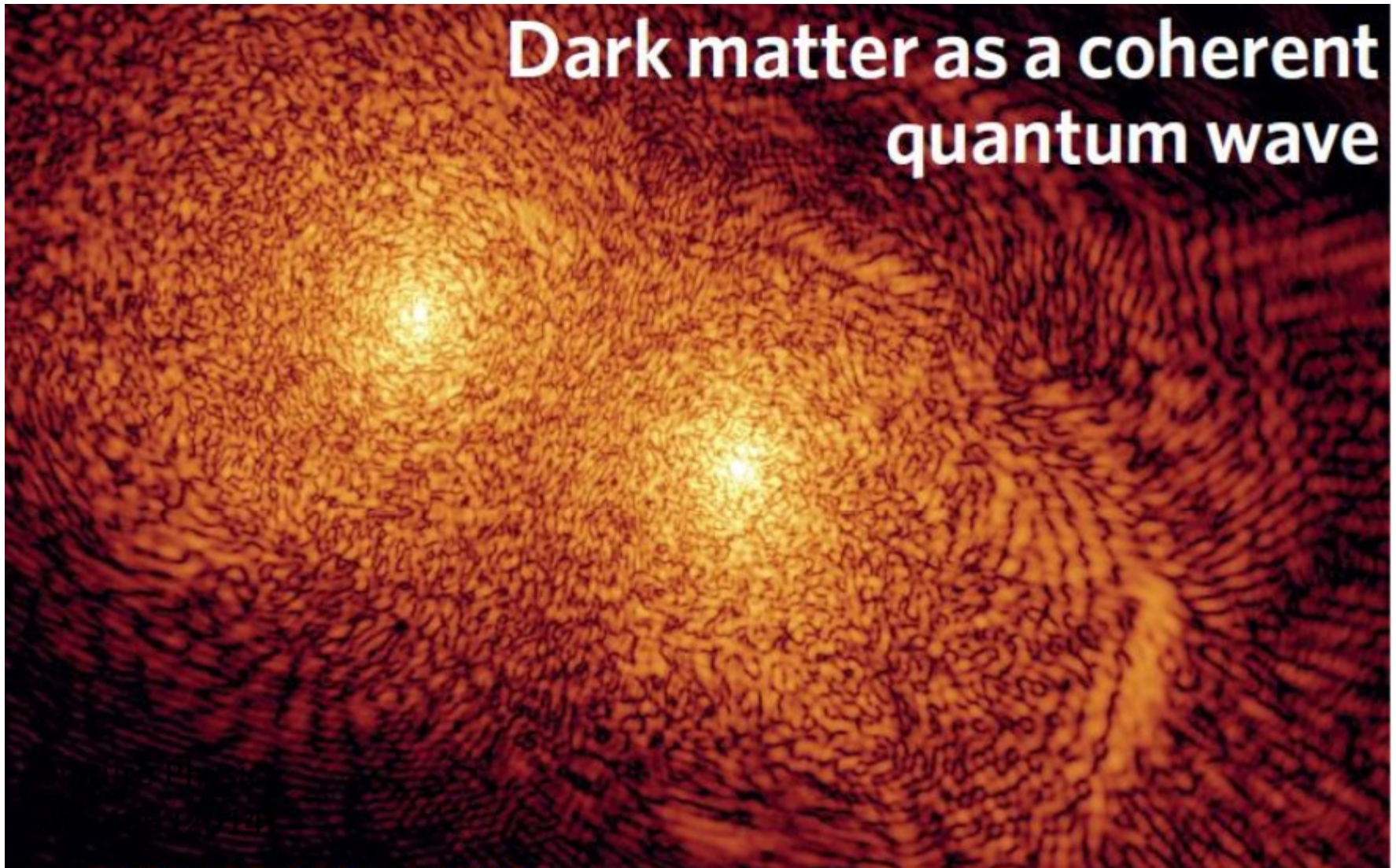


CMB acoustic modes



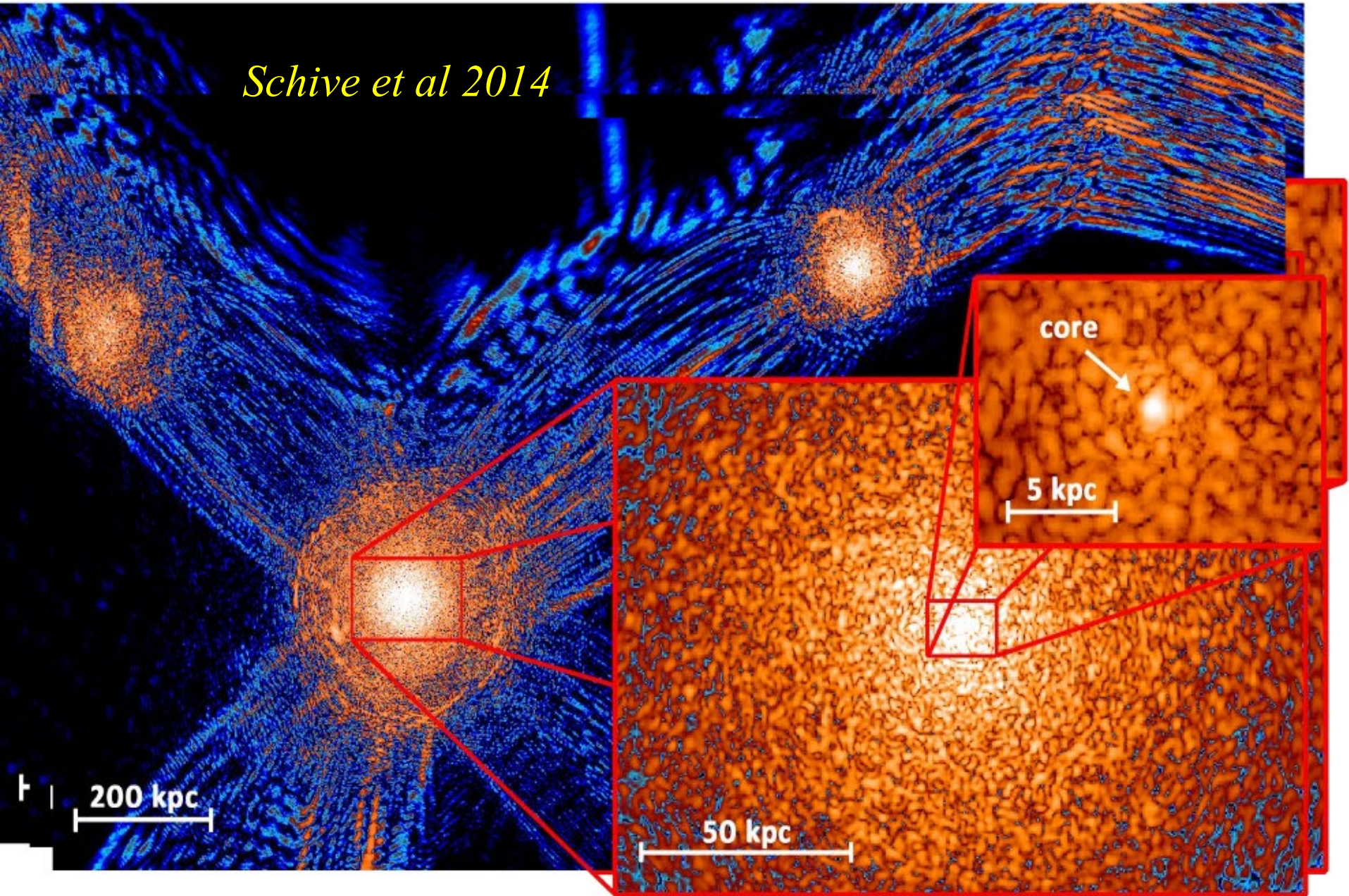
Simulations AMR: eq. Schrödinger- Poisson

Core= soliton, Halo= clumpy aspect + wavy (Schive +2014)



Quantum interferences: 9 orders of magnitude

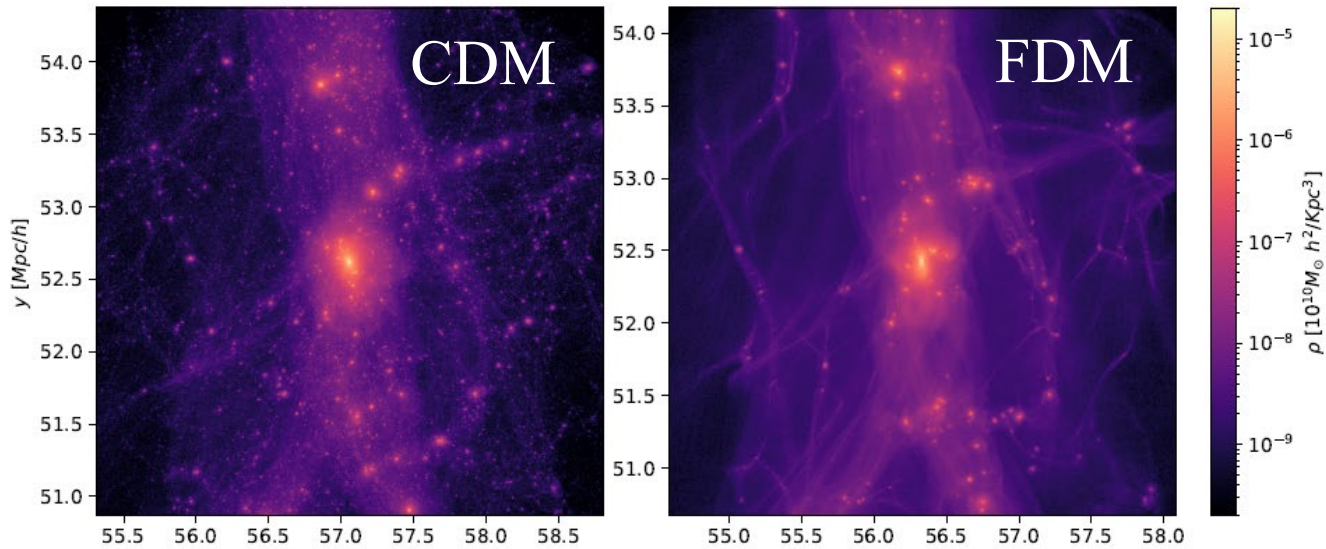
Schive et al 2014



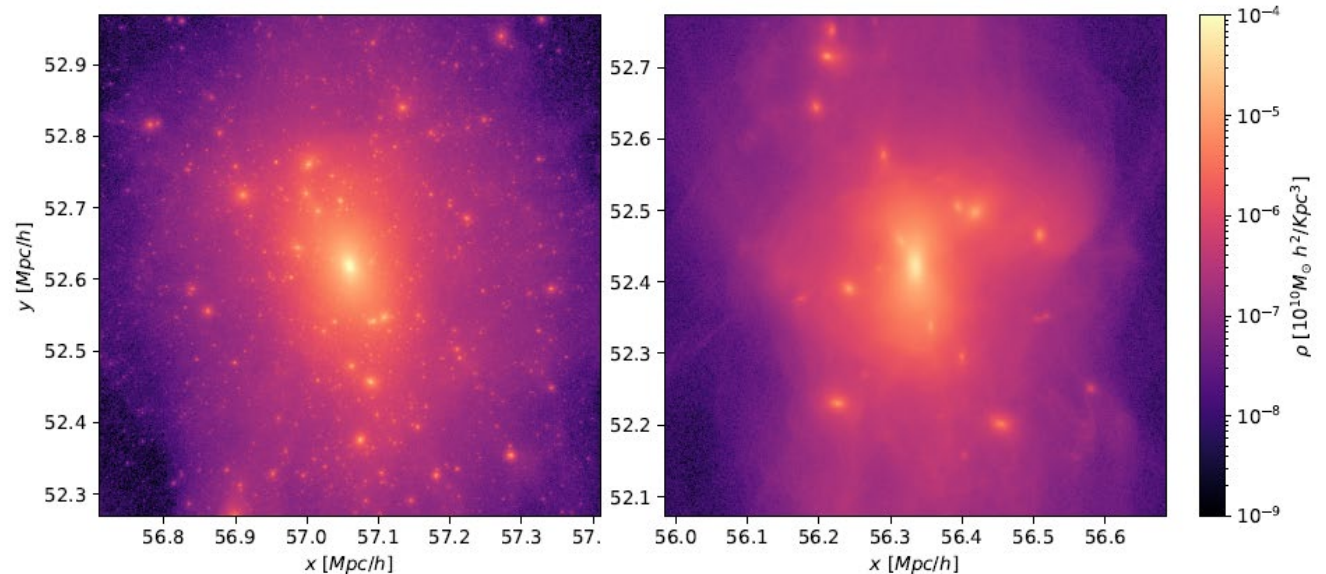
Milky Way: Aquarius, satellites

Nori et al 2023 AX-GADGET, compared with CDM

Expected scaling law $\rho_c \sim R_c^{-4}$ while observations say $\rho_c \sim R_c^{-1}$



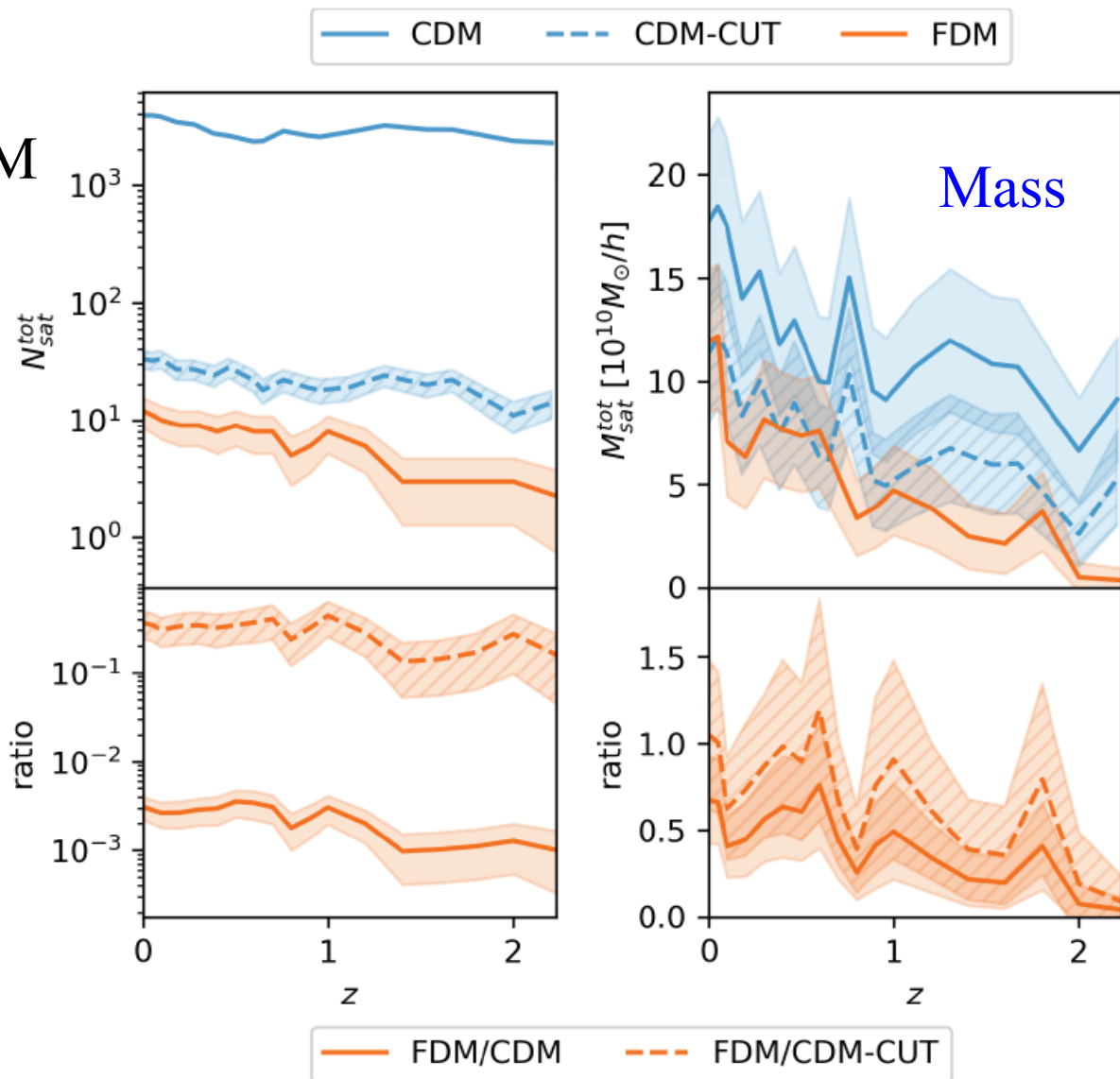
$\Sigma = 150 M_\odot / \text{pc}^2$
Donato et al 2009



Milky Way: Aquarius, satellites

Nori et al 2023

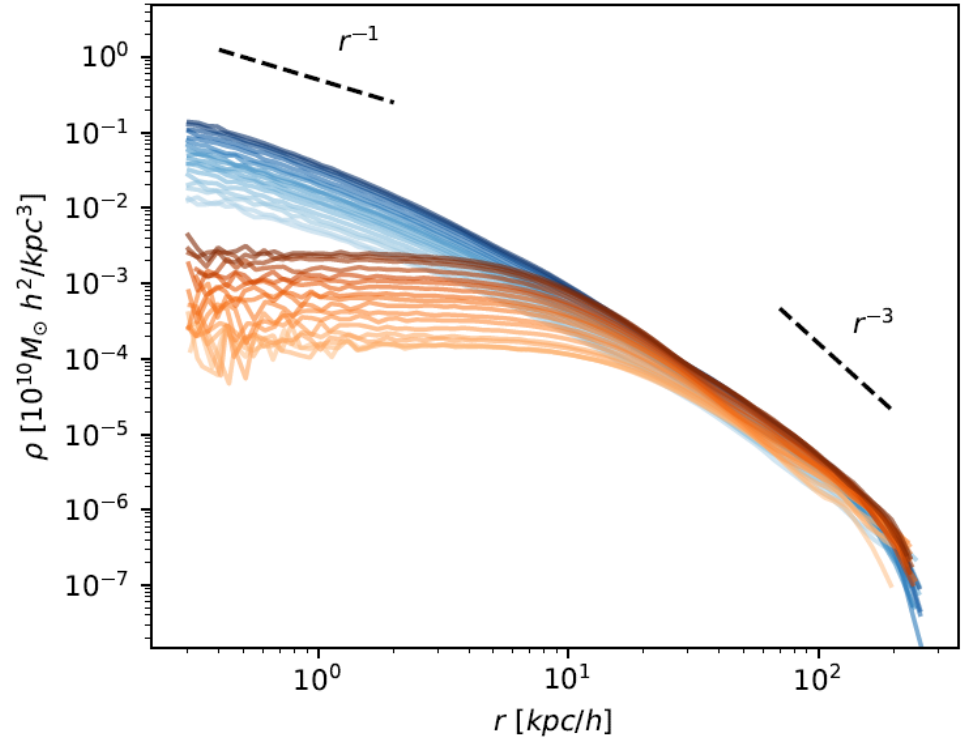
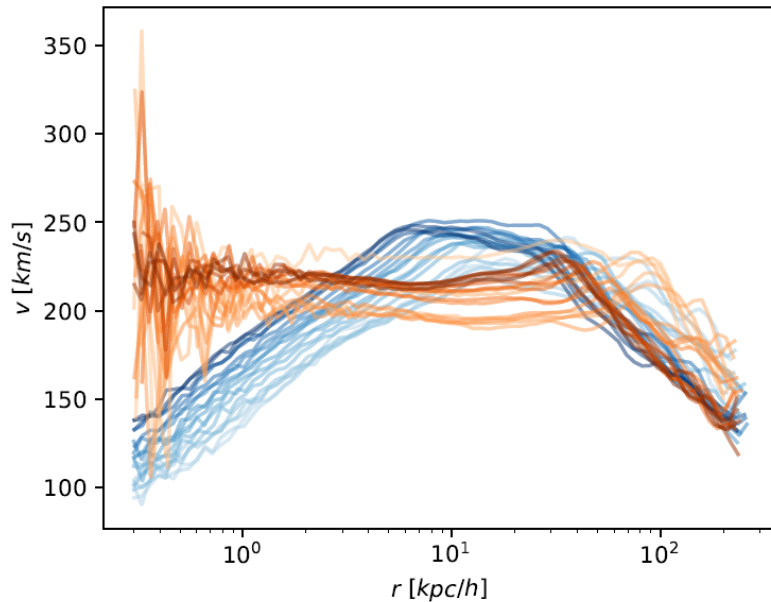
Comparison with CDM
and also when
 $M_{\text{sat}} > M_{\text{cut}}$ only
(CDM-CUT)



Evolution with redshift

Nori et al 2023

$z=4$ to $z=0$,
From light to dark lines

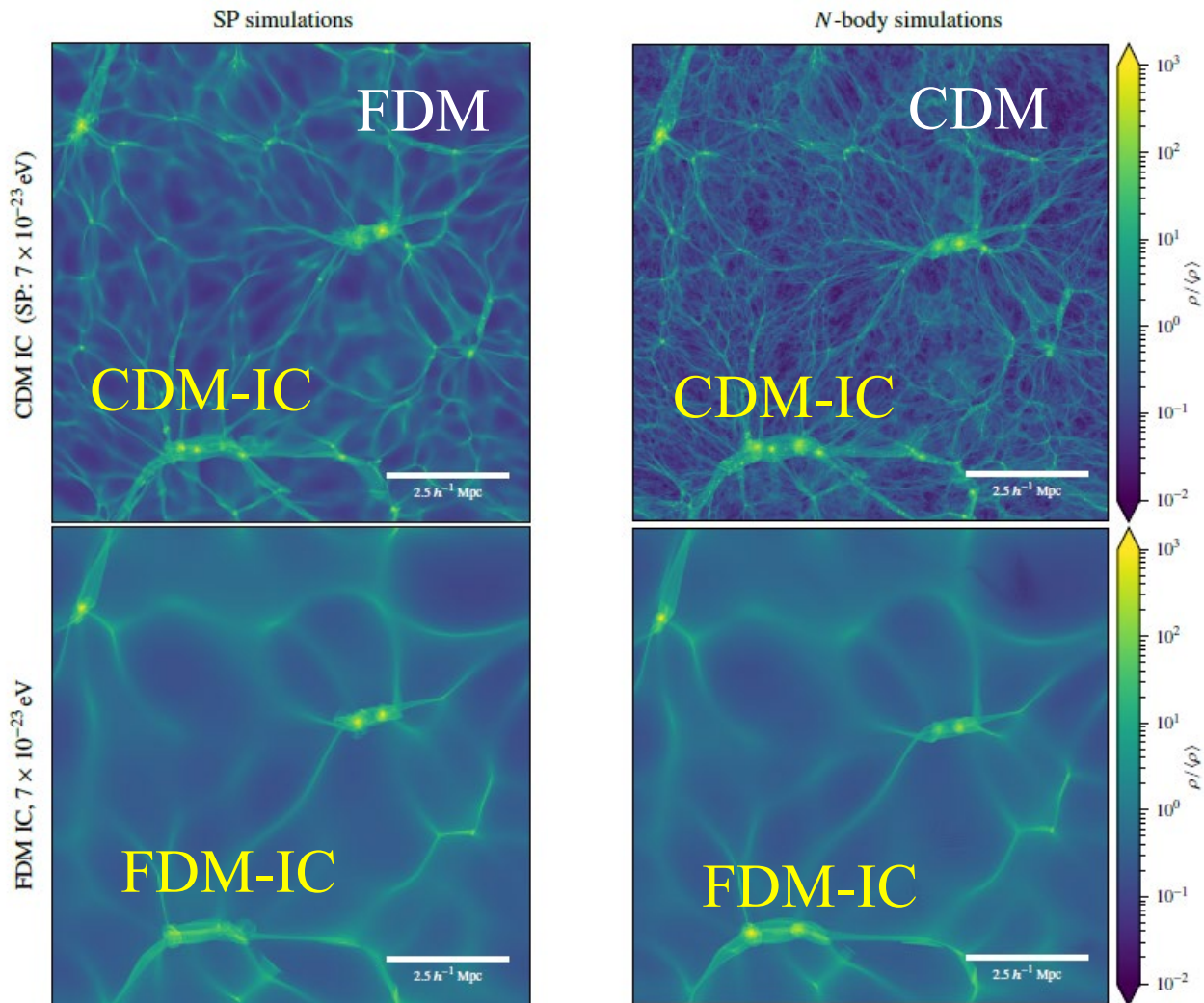


Even if density curves flatten
the asymptotic equilibrium
is not reached at $z=0$

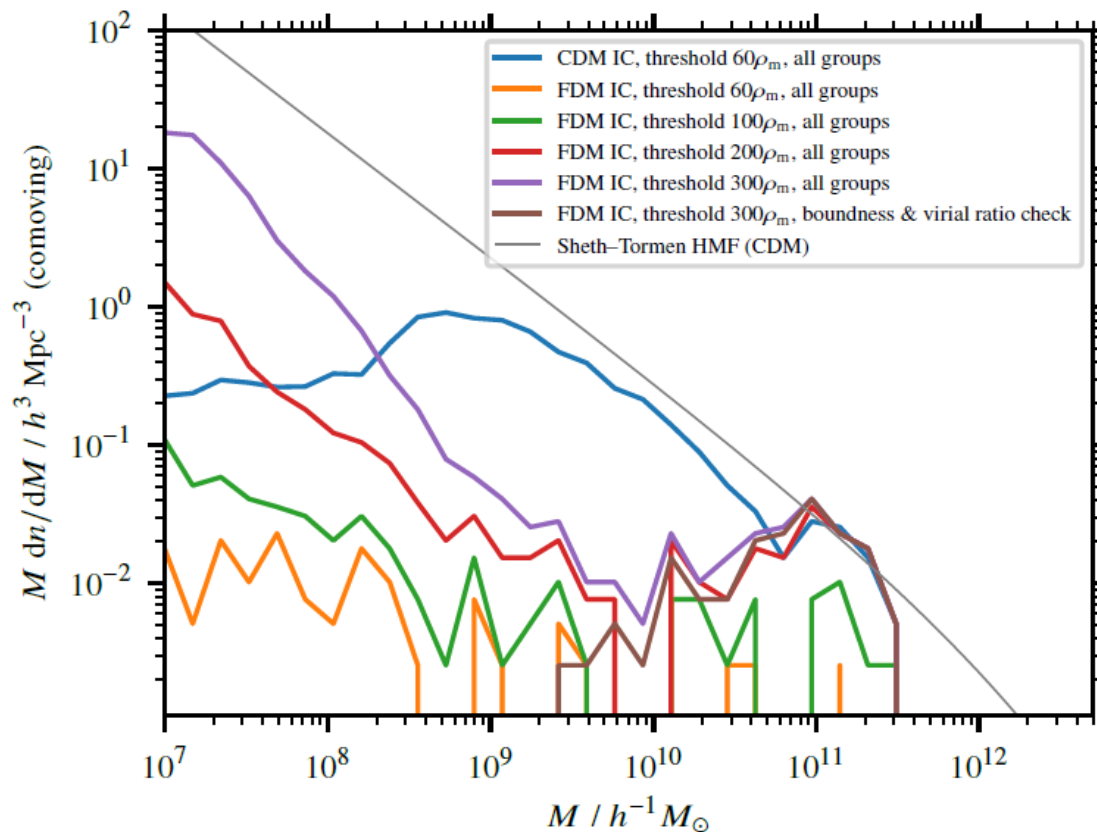
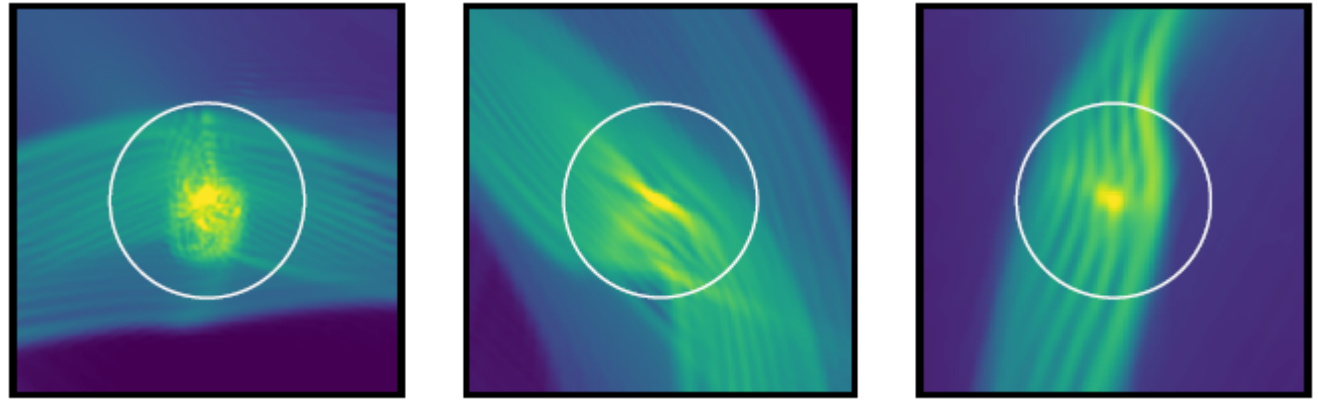
Halo mass function and filaments

May & Springel 2022 AxiREPO

Due to the mass cut-off, halos are linked with thin filaments



Filaments do not fragment!



May & Springel 2022

Search for structures
have to increase threshold

Big problem of resolution,
to resolve the
de Broglie length

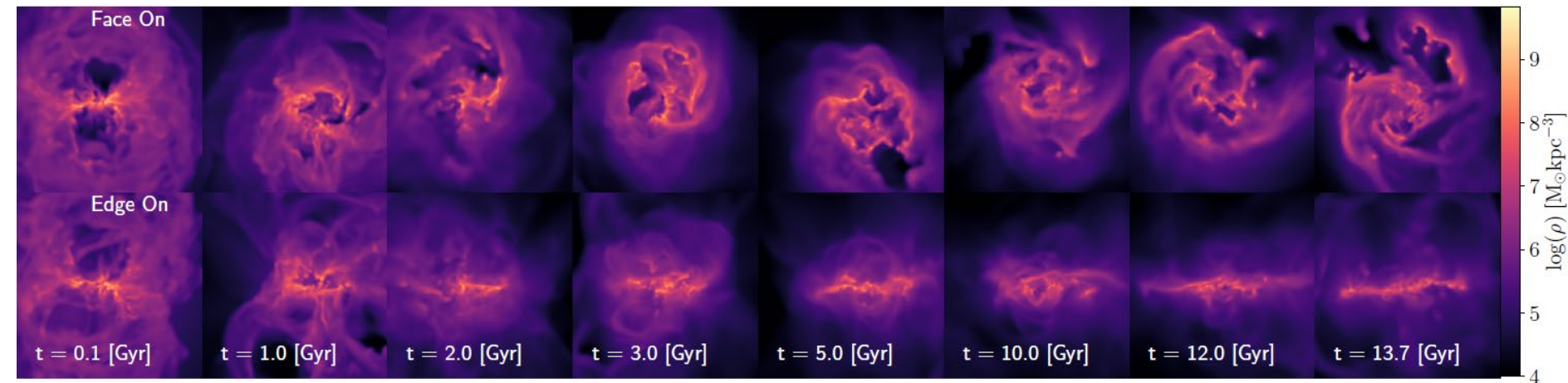
Simulations of a dwarf galaxy

Assuming gas and star formation, stochastic and stationary
Inducing fluctuations, different from white noise ($n=0$)

Ramses simulation of an isolated dwarf galaxy (Read et al 2016)

$M_{200} = 10^9 M_{\odot}$, $fg=0.15$, concentration 22.23

Cusp is mitigated in a Hubble time (*Hashim et al 2023*)

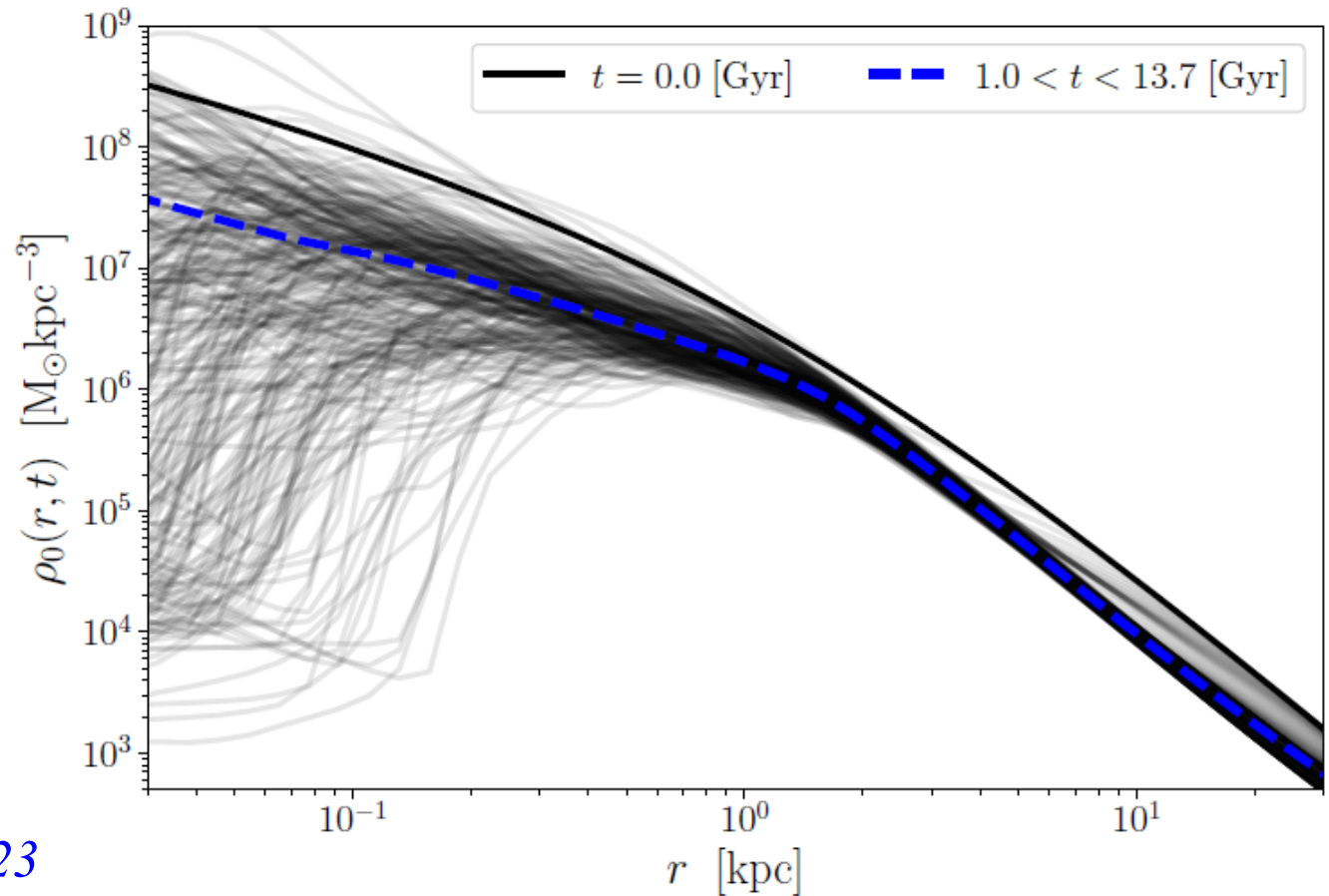


Box = 5kpc Important fluctuations due to SF, SN

Core formation ?

The slope of the radial density distribution is smoothed out, although not tending to a flat core

Trelax= 13.2 Gyr



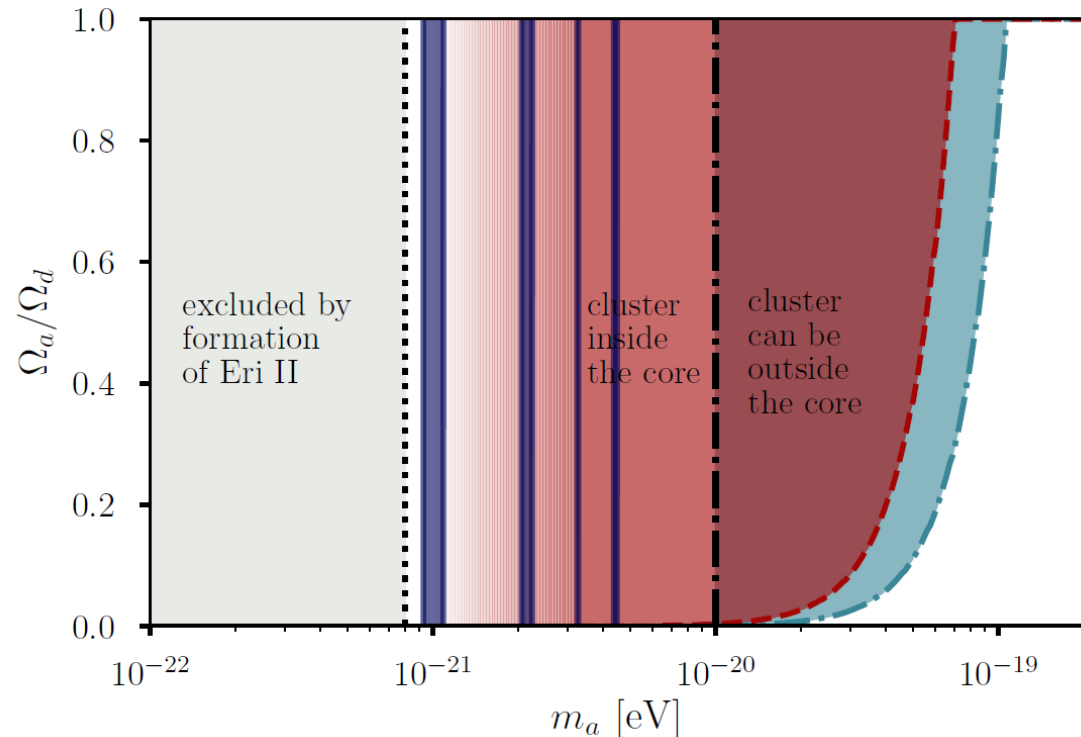
The case of Eridanus II

In this ultrafaint dwarf galaxy, there exists an old star cluster, whose existence and size put also a constraint

Heating due to core oscillations $\rightarrow m_a > 10^{-19}$ eV



Marsh & Niemeyer 2018



May be the region inside the core is not completely valid
There are resonances for the oscillations

High-z massive galaxies?

Gong et al 2022

JWST found numerous galaxies $7 < z < 11$

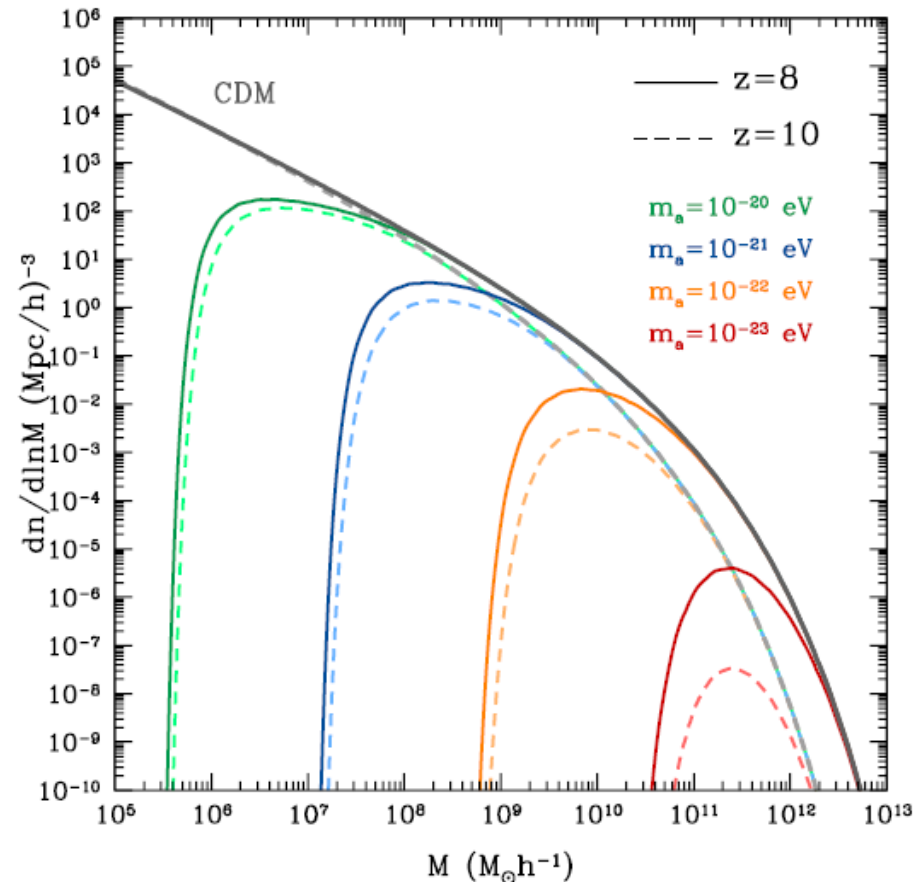
Big problem if star formation is made in the whole mass function of galaxies

→ Too many UV to reionize the Universe

Contradiction to Planck CMB

FDM, but also WDM with sterile neutrinos

→ Suppress small-mass galaxies



MOND = M**O**dified Newton Dynamics



At weak acceleration

$$a \ll a_0 \quad \text{MOND regime} \quad a = (a_0 a_N)^{1/2}$$

$$a \gg a_0 \quad \text{Newtonian} \quad a = a_N$$

$$a_0 = 10^{-10} \text{ m/s}^2 \sim 10^{-11} g$$

Milgrom (1983)

Asymptotically

$$a_N \sim 1/r^2 \rightarrow a \sim 1/r$$

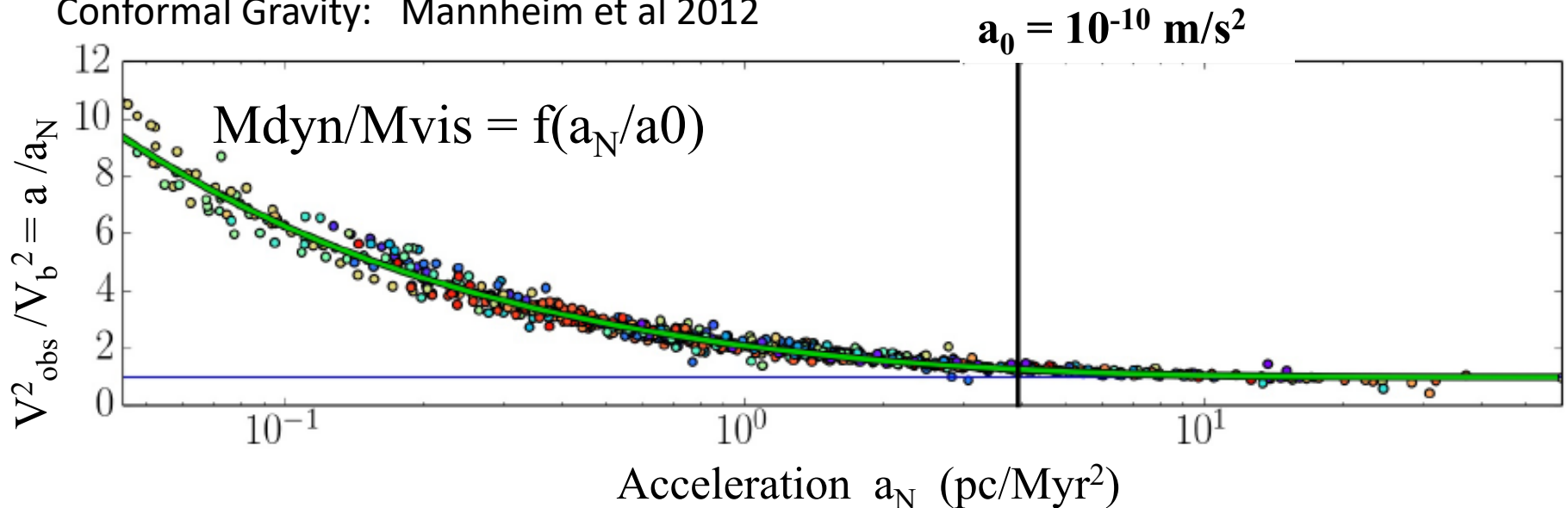
$$\rightarrow V^2 = \text{cste}$$

Covariant theory: TeVeS

\rightarrow Gravitational lenses

Bekenstein 2004

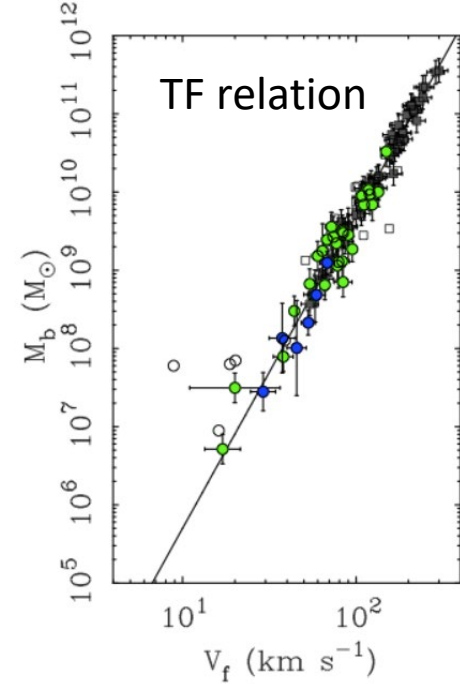
Conformal Gravity: Mannheim et al 2012



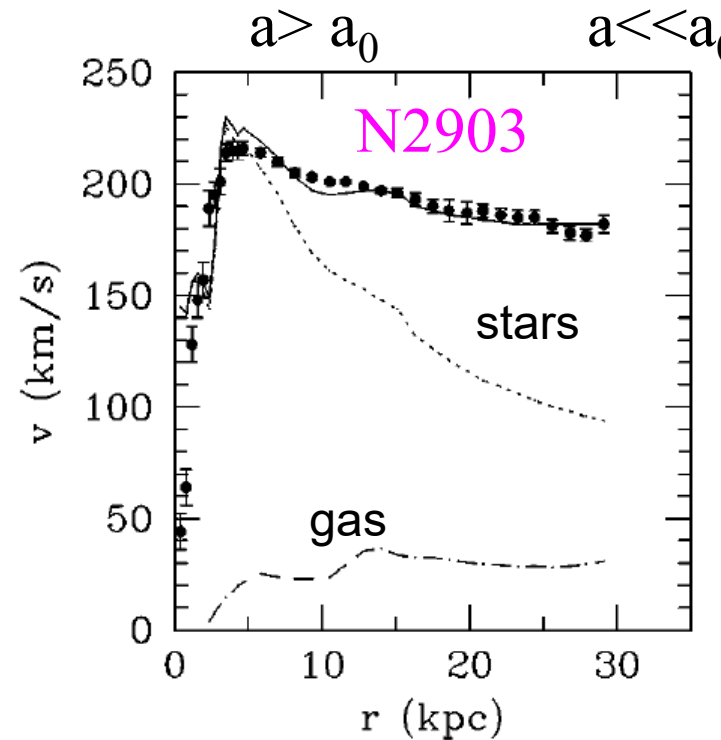
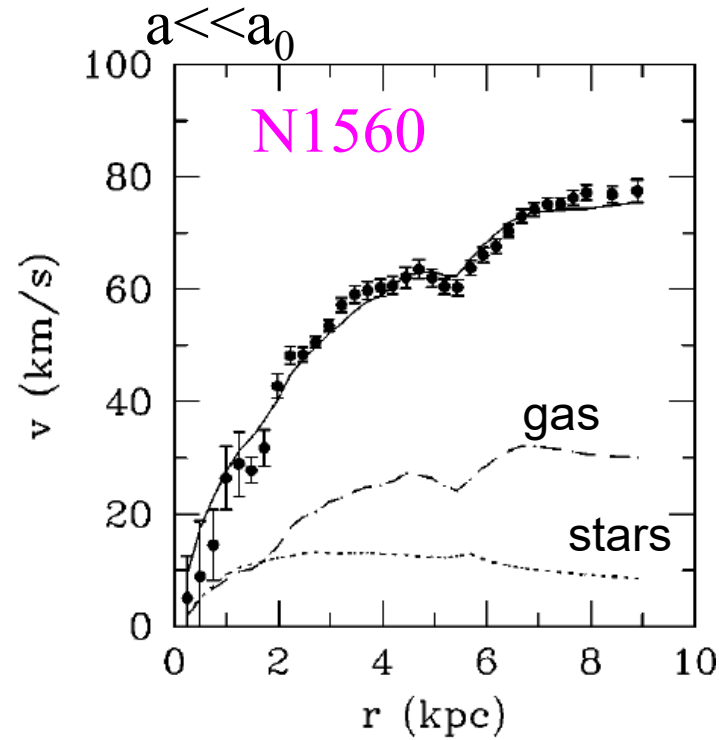
Success at weak surface densities

$\Sigma < \Sigma_0 \sim 150 M_\odot/\text{pc}^2$, \rightarrow the critical acceleration a_0

In particular dwarf galaxies



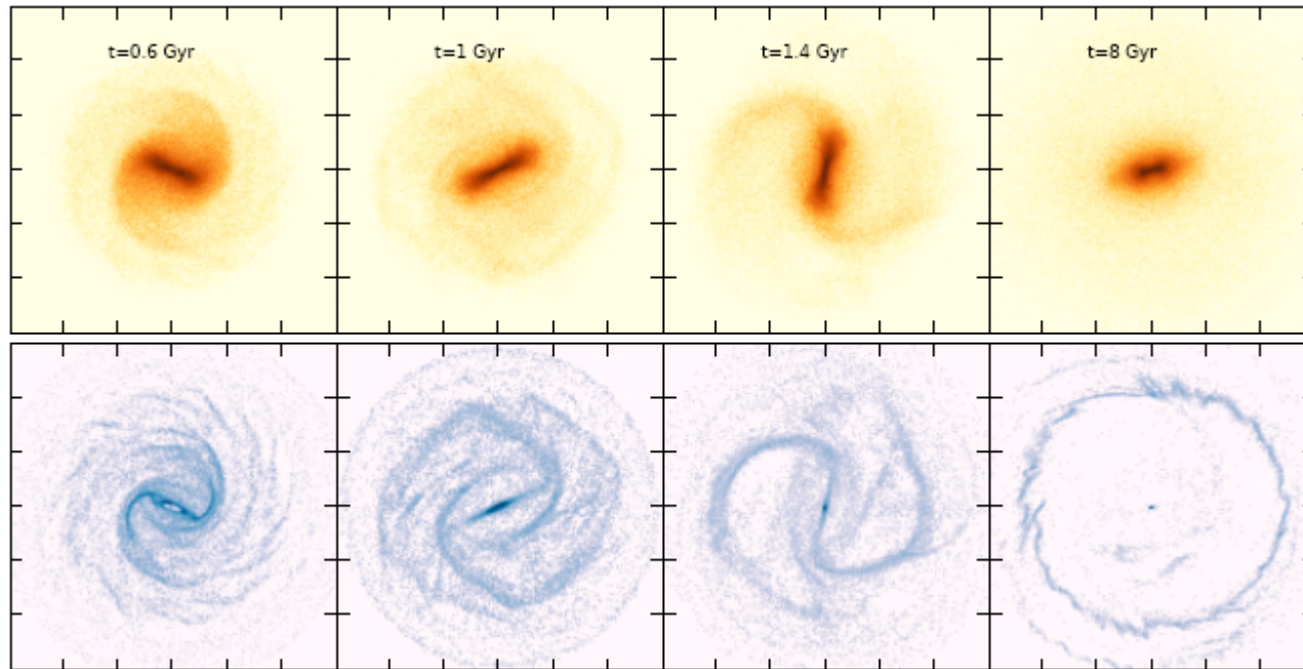
The rotation curves of all galaxy types



Influence of the dark halo ?

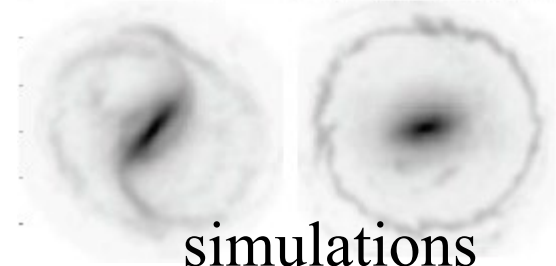
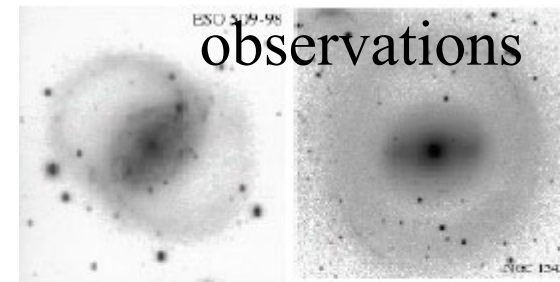
Dynamics of galaxies,

Formation of spirals and bars *Tiret & Combes 2007, 2008*



Stars

Gas

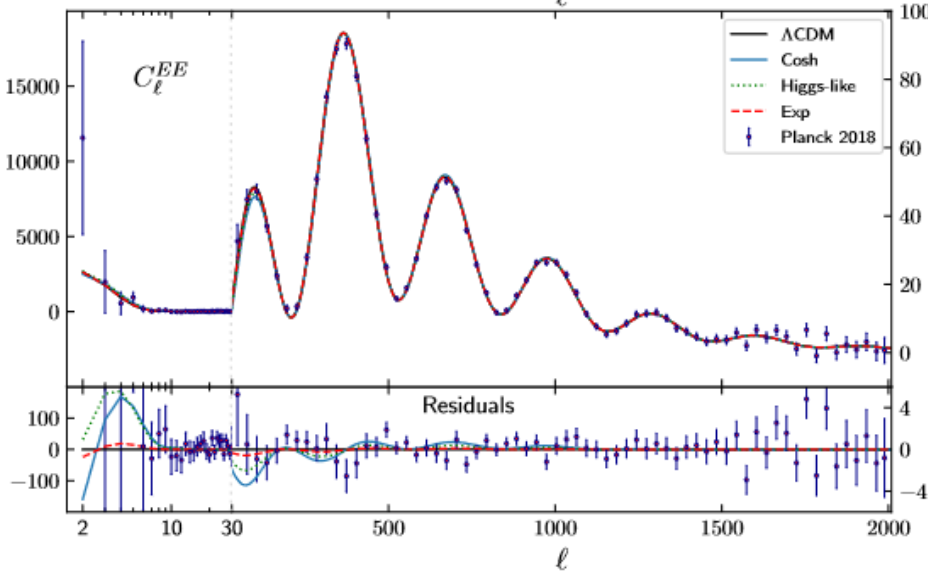
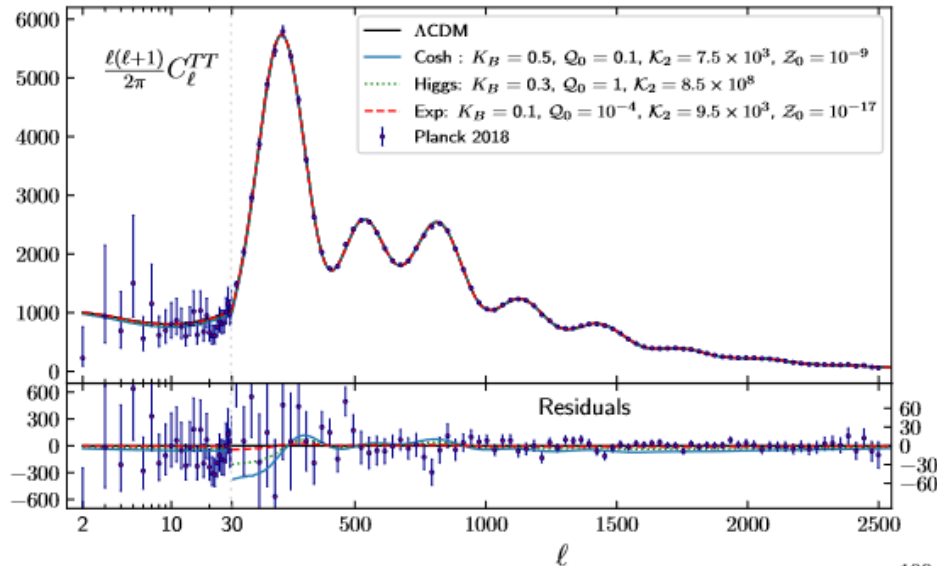


TeV S covariant theory → but unstable

ruled out by gravitational waves ($c_{\text{GW}} \neq c$)

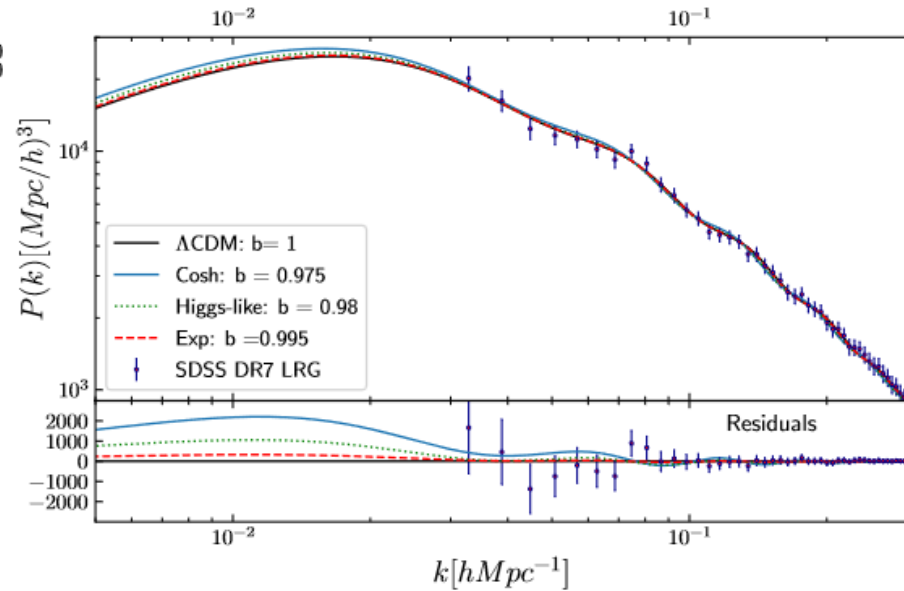
But Skordis et al 2019, new version, with $c_{\text{GW}} = c$

New theory with Vector field



Unit time-like vector
Gravitational lensing

$$c_{\text{GW}} = c$$



Skordis & Zlosnik 2021

Summary: axions or modified gravity?

Many constraints on the mass m_a , but not definitive

Some baryons+DM simulations (Aquarius, AX-Gadget, AxiREPO)

Approximations: cut-off of small structures (but negative pressure?)
SP fluid, Madelung approx, SI or not? Repulsive quantum force?

Interactions SMBH and soliton? (same order of masses)

Lyman- α forest? $\rightarrow m > 21 \cdot 10^{-22} \text{ eV}$ (*Nori et al 2019*)

Small halos (dwarfs) are less dense, larger cores

Massive halos, denser, unresolved solitons