

Investigating Kitaev physics in Co honeycomb-lattice oxides

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Spin wave calculations:

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Neutron/X-ray scattering:

Chris Stock (University of Edinburgh)

Jose Rodriguez, William Ratcliff (NIST)

Monica Jiménez-Ruiz (ILL)

Françoise Damay (Laboratoire Léon Brillouin)

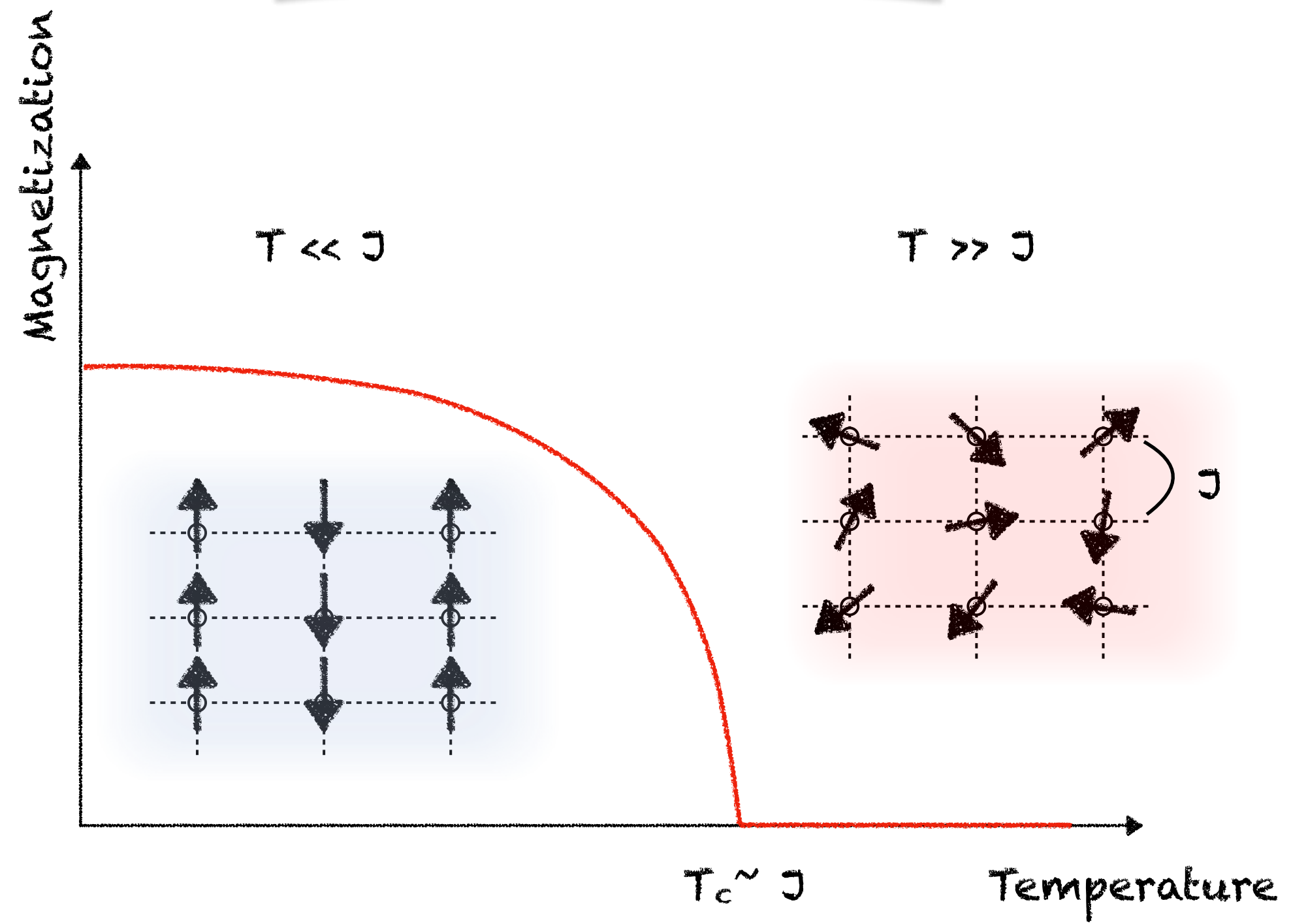
Victor Balédent (Laboratoire de Physique des Solides)



Beyond conventional magnetism

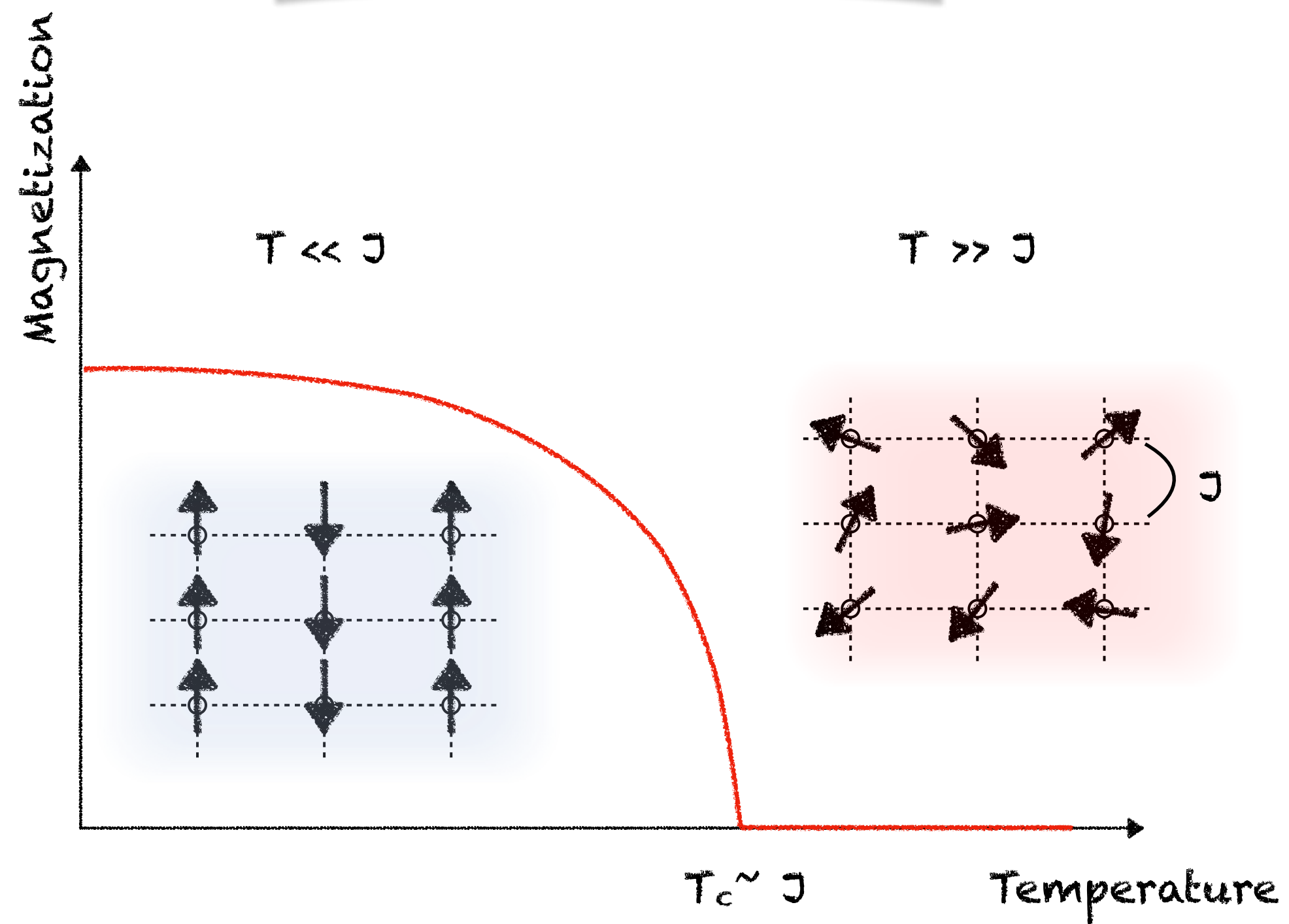


Conventional magnetic order
Landau's formalism

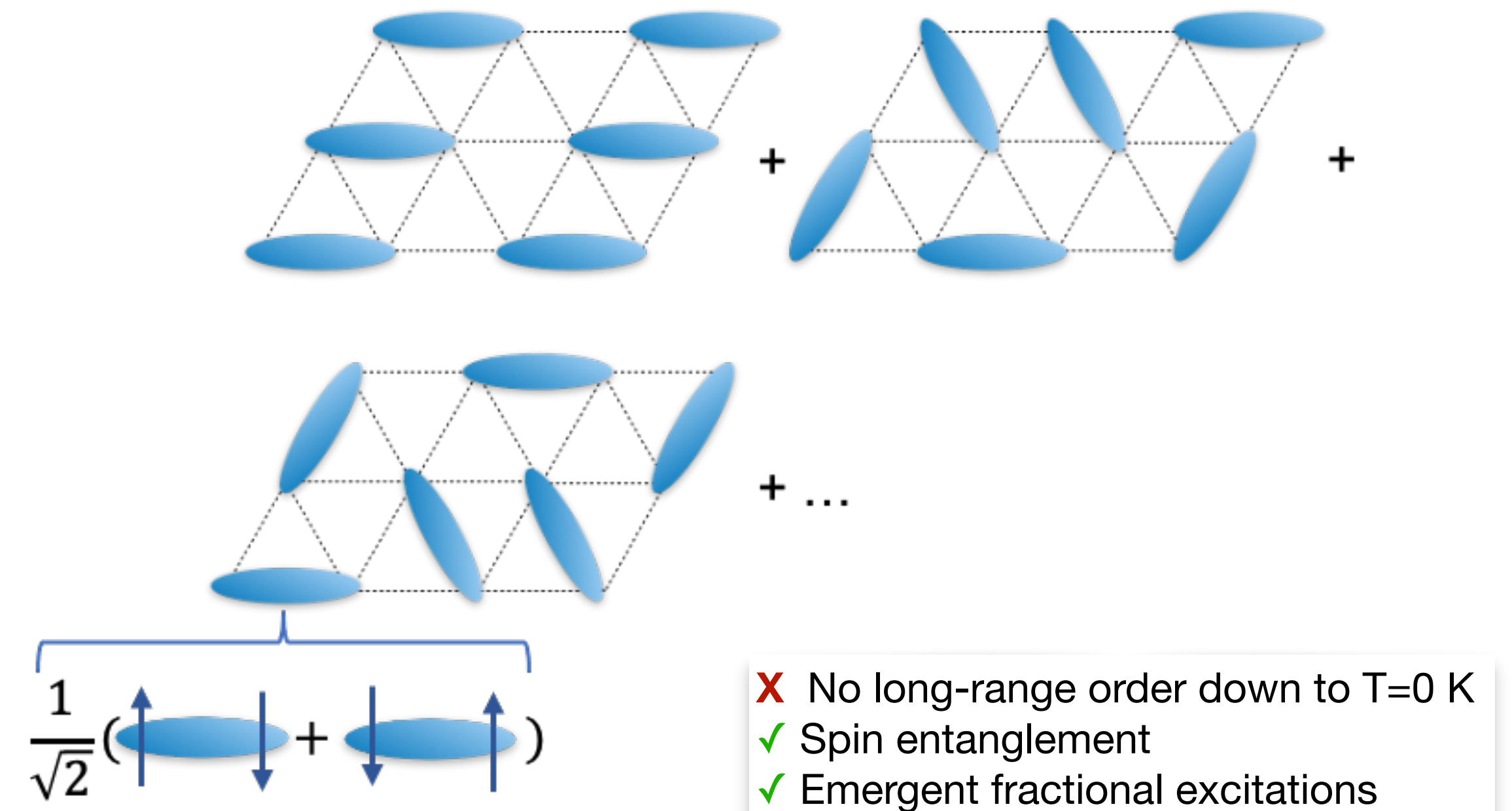




Conventional magnetic order
Landau's formalism



Quantum spin liquids
Beyond Landau's model



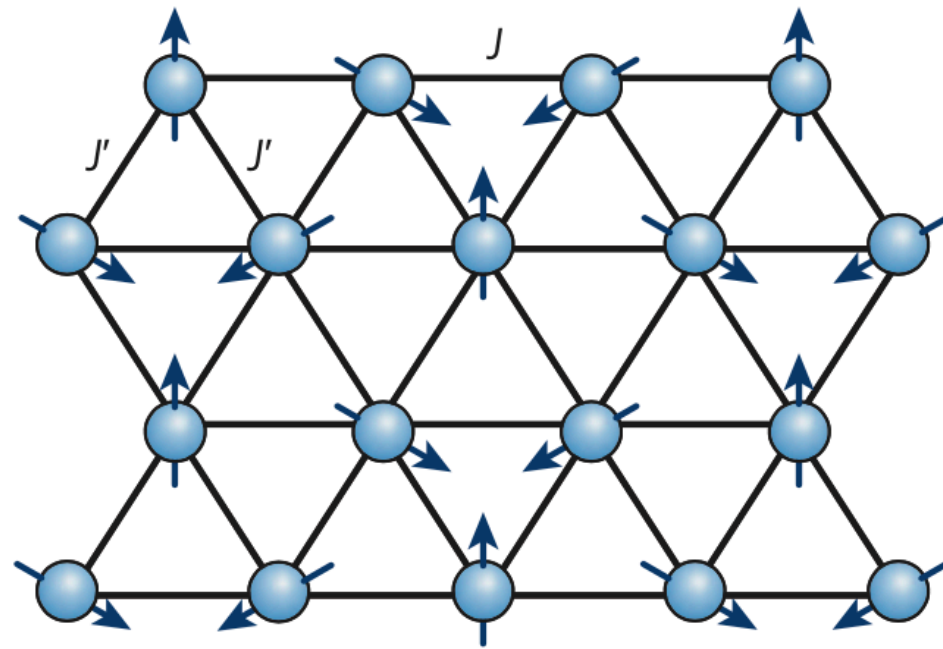
Why are quantum spin liquids interesting?



It's a new state of matter:

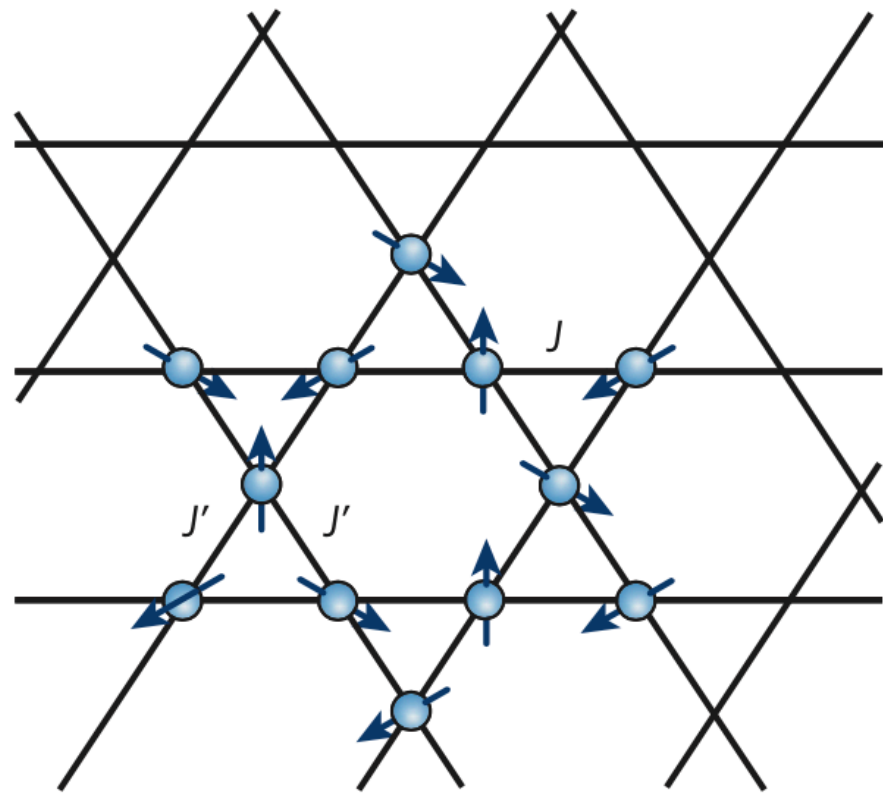
- Collective behaviours and emergent phenomena
 - Electromagnetism*
 - Quantum electrodynamics*
 - High energy physics...*
- How to classify these new states? Topological orders...
- Experimental challenge: what are the signatures?
- Very few experimental realizations in dimension $d > 1$

Achieving quantum spin liquids: geometrical frustration



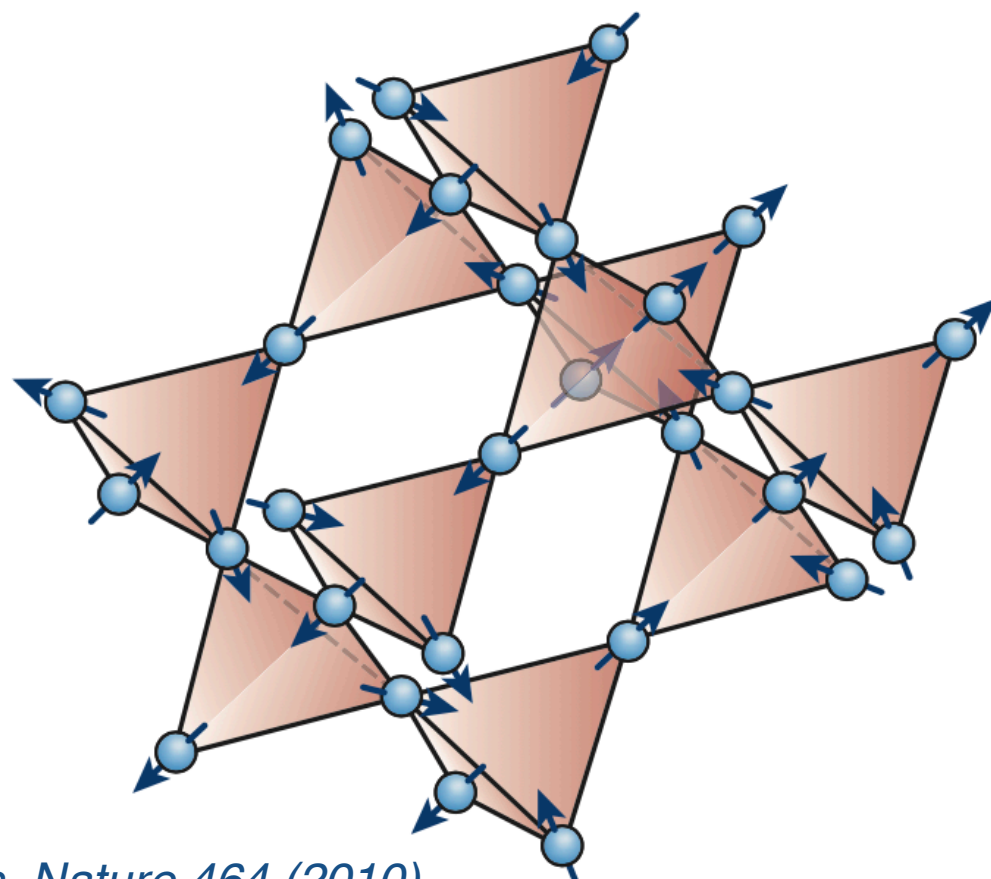
Triangular lattice

κ -(BEDT-TTF)₂Cu₂(CN)₃
EtMe₃Sb[Pd(dmit)₂]₂
Y. Shimizu et al., *Phys. Rev. Lett.* 91, 107001 (2003)
T. Itou et al., *Nature Physics* 6, 673 (2010)



Kagome lattice

Herbertsmithite ZnCu₃(OH)₆Cl₂
T.-H. Han et al., *Nature* 492, 504 (2012)
M. P. Shores et al., *J. Am. Chem. Soc.* 127, 13462 (2005)



Pyrochlore lattice

Pyrochlore Dy₂Ti₂O₇, Ho₂Ti₂O₇...
M. P. J. Gingras and P. A. McClarty, *Rep. Prog. Phys.* 77, 056501 (2014)

Hyperkagome Na₄Ir₃O₈
Y. Okamoto et al., *Phys. Rev. Lett.* 99, 137207 (2007)

A promising route: The Kitaev model on honeycomb lattice



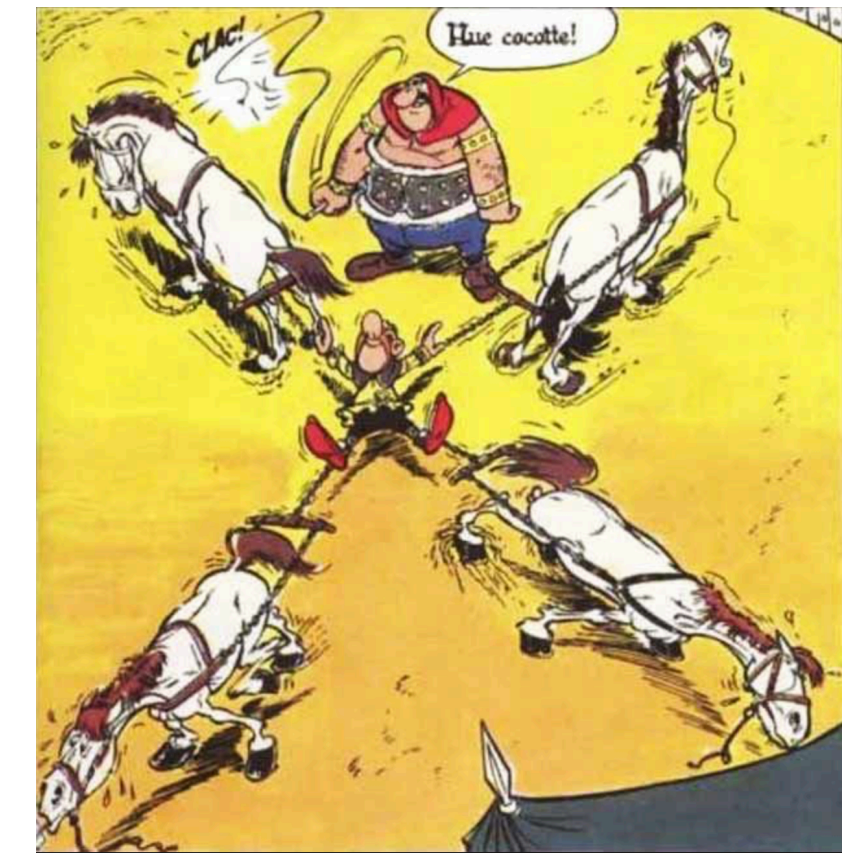
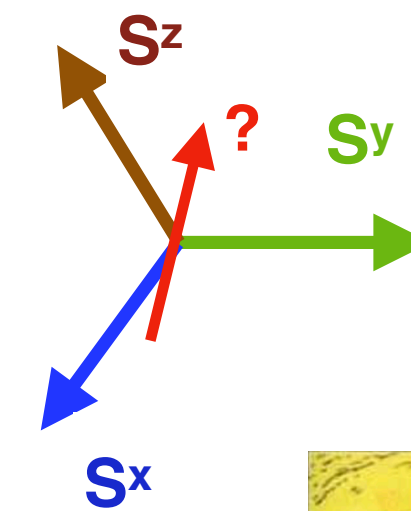
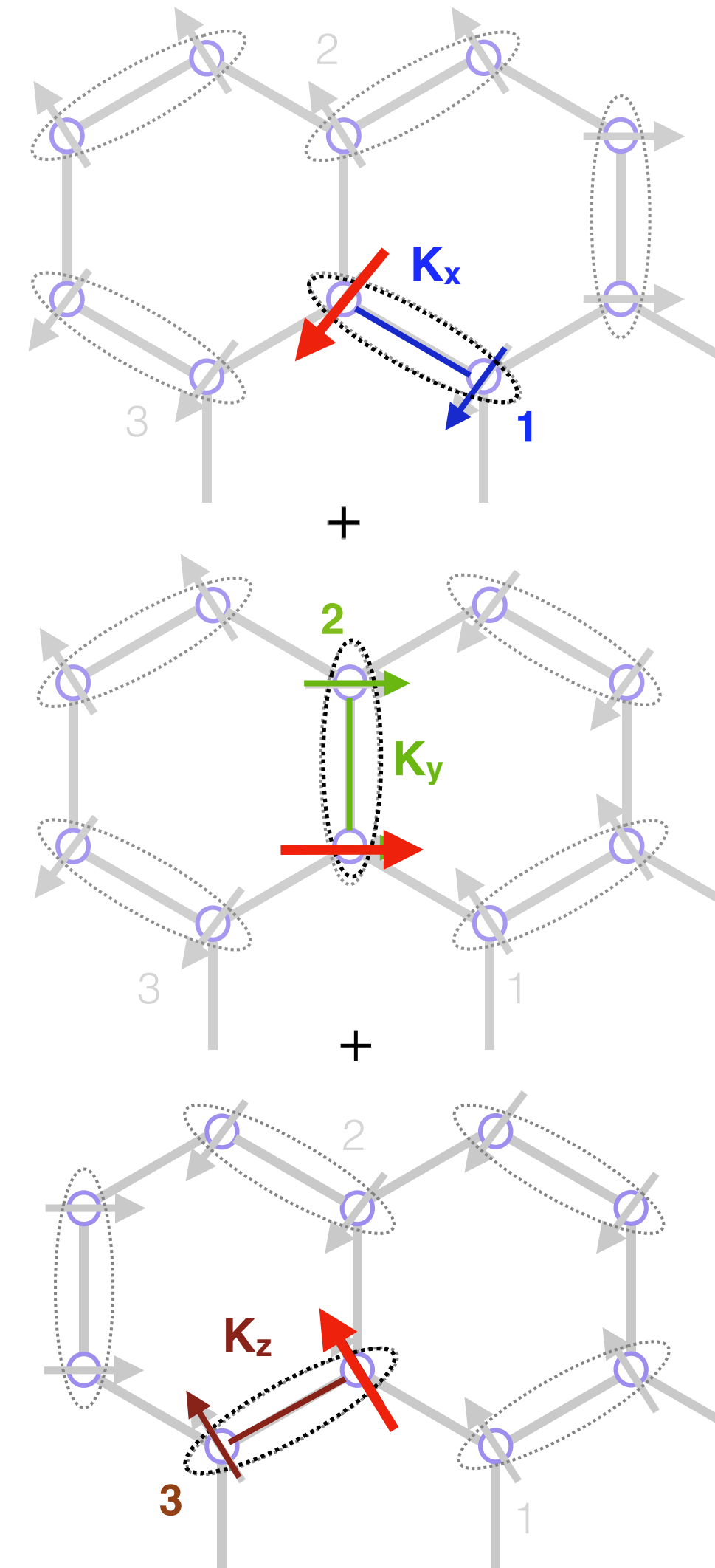
A. Kitaev, *Annals of Physics* 321 (2006)

- S=1/2 honeycomb lattice
- **Exact ground state : quantum spin liquid**
- Emergent fractional excitations: Majorana modes and flux excitations
- Rich phase diagram

Anisotropic bond-dependent interactions

$$H_{\text{Kitaev}} = - \sum_{i,\alpha=1,2,3} (K_x S_i^x S_\alpha^x + K_y S_i^y S_\alpha^y + K_z S_i^z S_\alpha^z)$$

An exact model

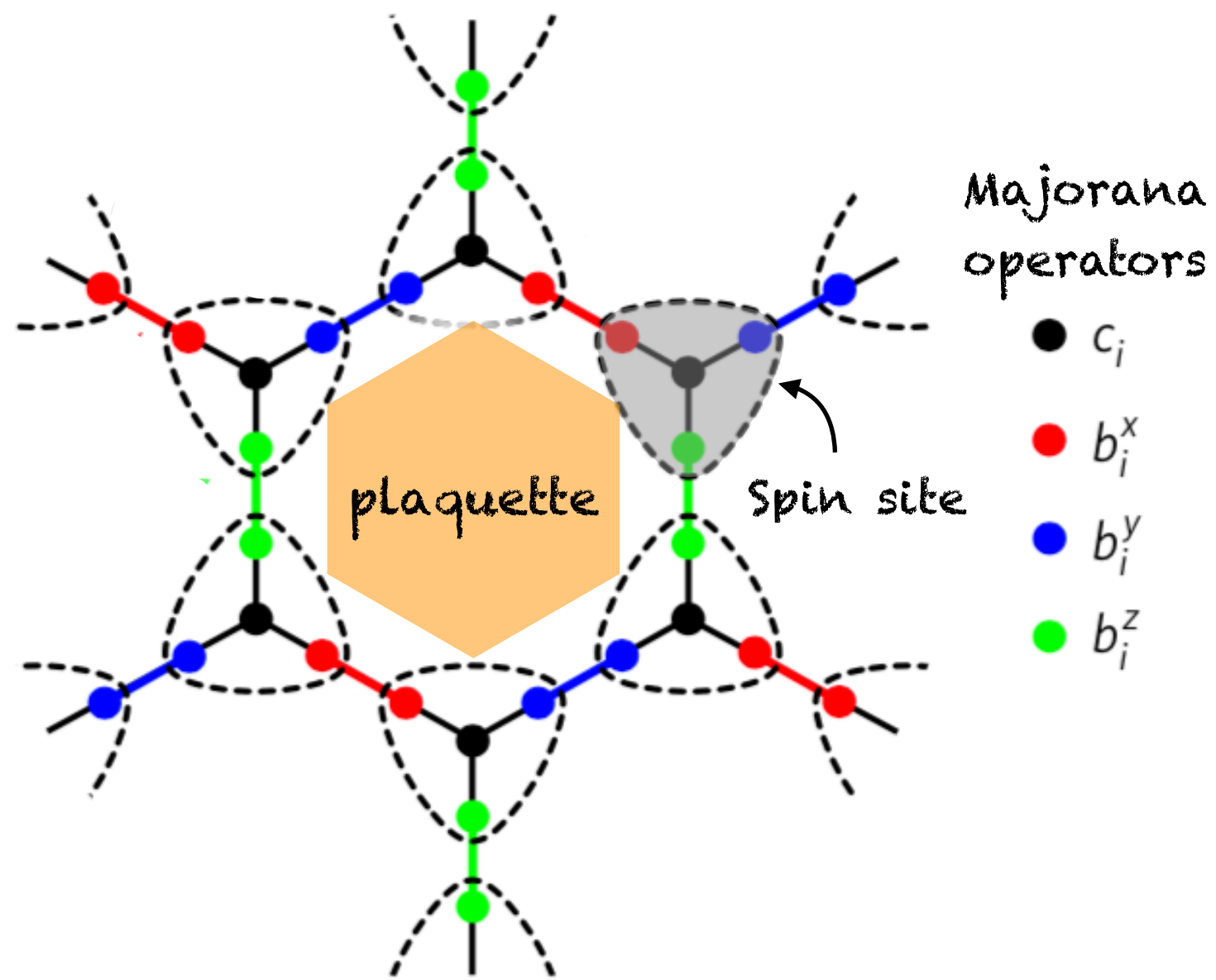


The Kitaev model



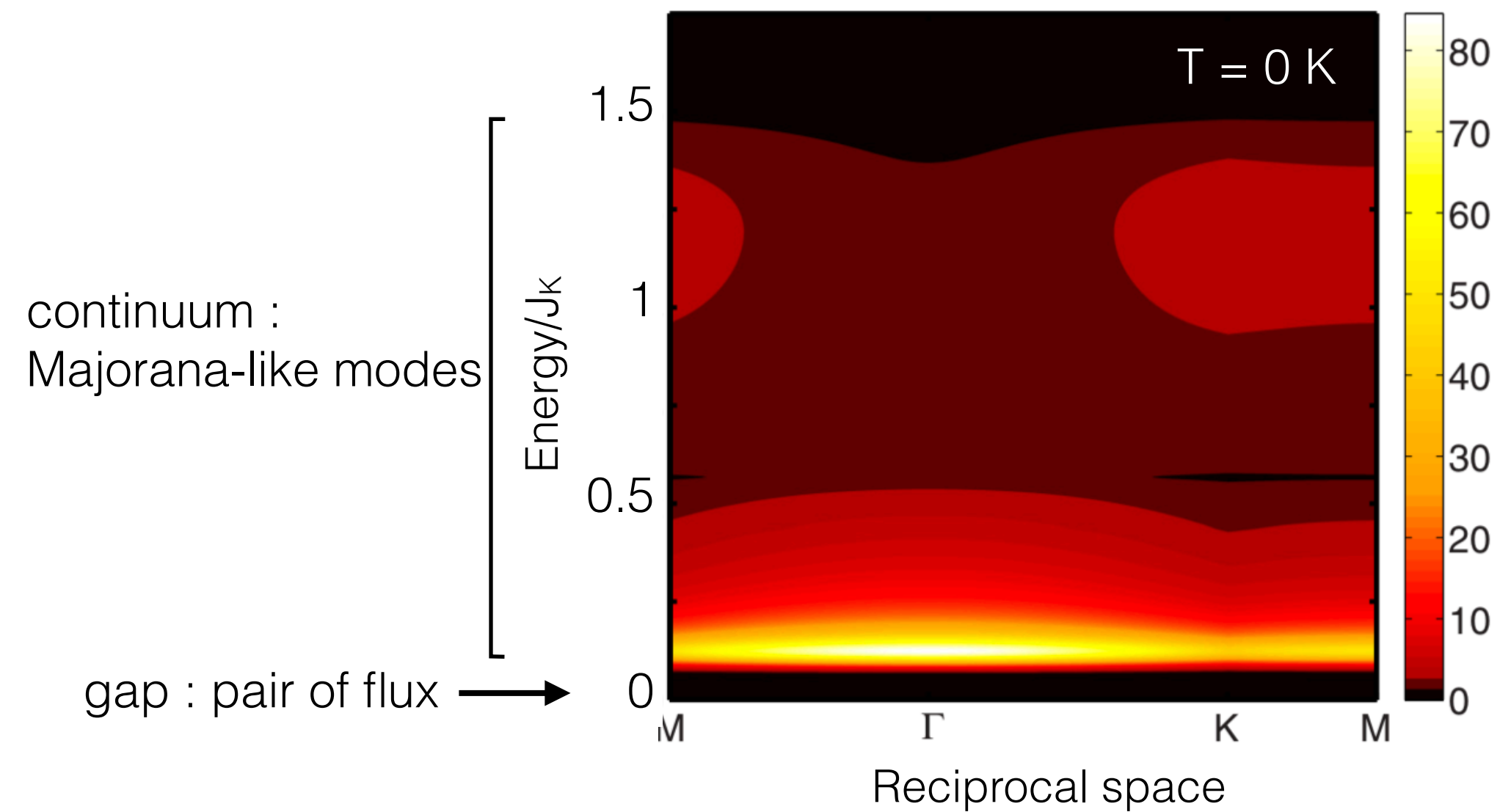
A. Kitaev, *Annals of Physics* 321 (2006)

- $S=1/2$ honeycomb lattice
- Exact ground state : quantum spin liquid
- **Emergent fractional excitations: Majorana modes and flux excitations**
- Rich phase diagram



S.-H. Do et al., *Nature Physics* 13, 1079 (2017)

Theoretical prediction for the dynamical structure factor in neutron scattering



J. Knolle et al., *Phys. Rev. B* (2015)

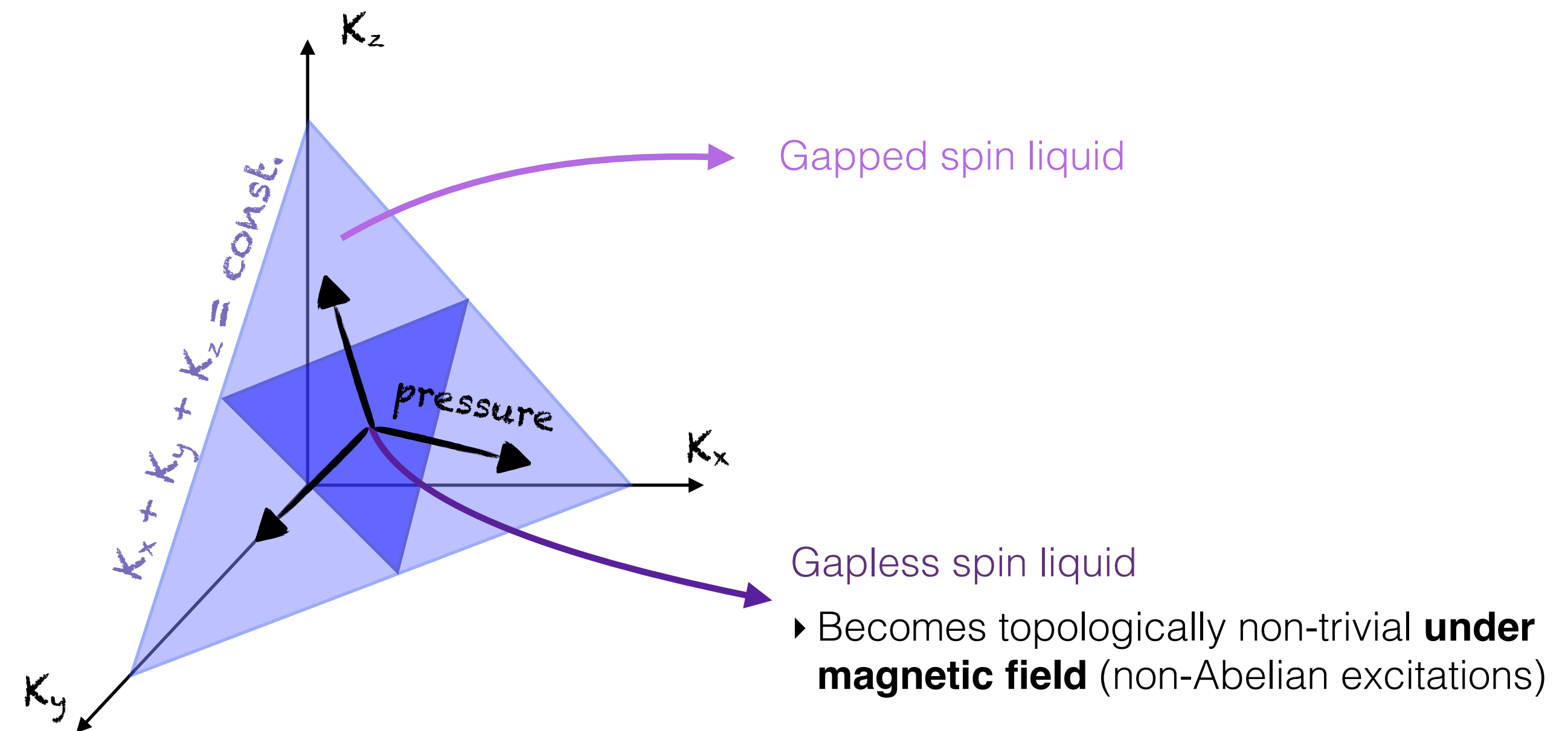
The Kitaev model



A. Kitaev, *Annals of Physics* 321 (2006)


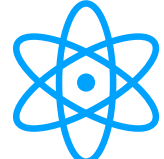


- $S=1/2$ honeycomb lattice
- Exact ground state : quantum spin liquid
- Emergent fractional excitations: Majorana modes and flux excitations
- **Rich phase diagram**

Tuning the ground state through external parameters
(magnetic field, pressure)





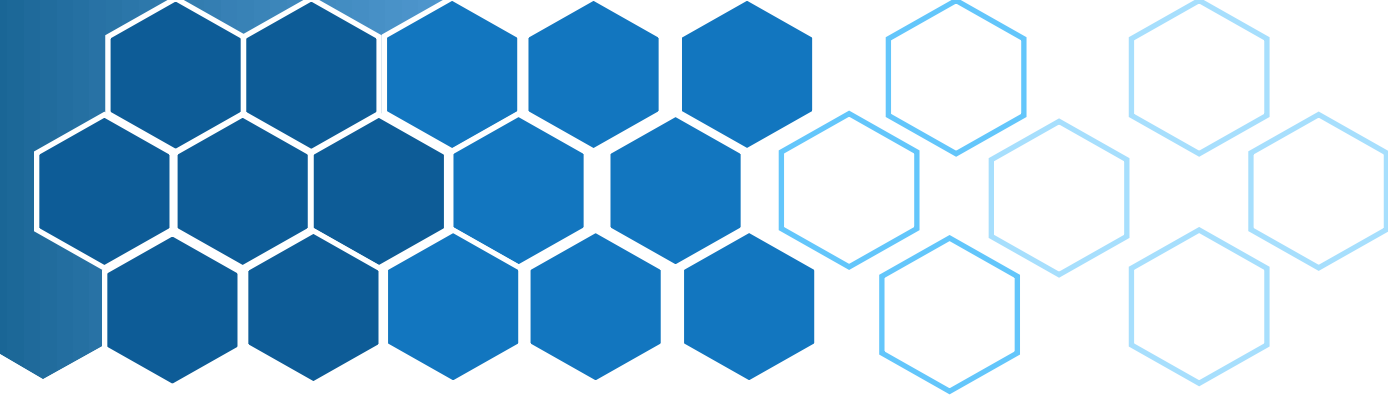
An alternative route to achieve quantum spin liquids

-  Exact solution : spin liquid ground state
-  Emergence of new fractional excitations with interesting statistical properties
-  Possibility to navigate between different QSL regimes with external parameters
-  Tools for quantum computing: the Toric code (c.f. *A. Kitaev, Annals of Physics 321 (2006)*)

C. Nayak et al., Rev. Mod. Physics 80, 3 (2008)
A. Stern, Nature 464, 7286 (2010)

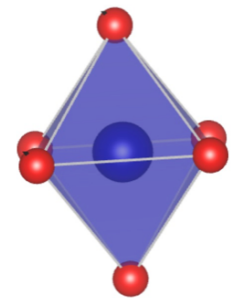


The Kitaev model: experimental realization?



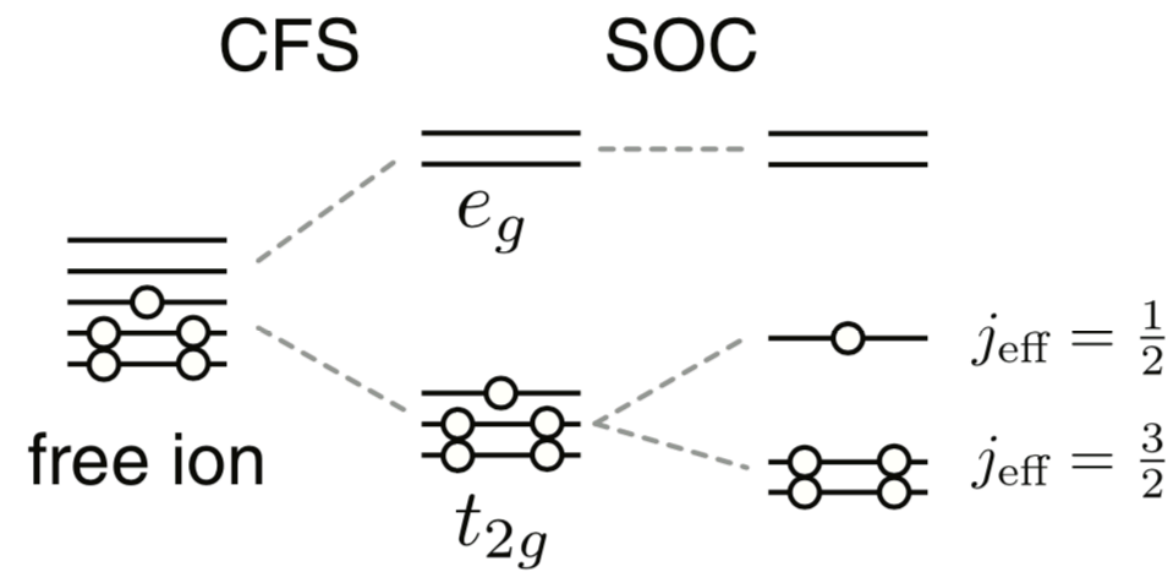
The Jackeli and Khaliullin proposal for experimental realization

G. Jackeli and G. Khaliullin, *Phys. Rev. Lett.* 102, 017205 (2009)



d⁵ metal transition in octahedral environment

Ir⁴⁺ (5d⁵), Ru³⁺ (4d⁵)



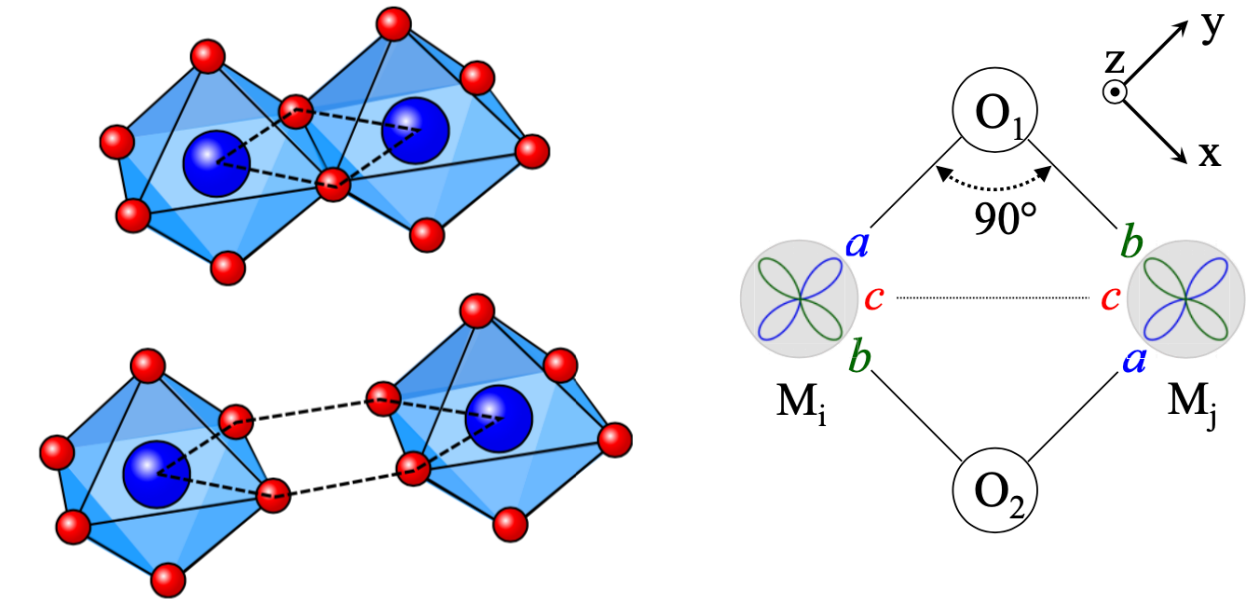
Spin-orbit coupling

$\lambda \sim 400\text{-}500\text{ meV}$ for *Ir⁴⁺*
 $\lambda \sim 100\text{ meV}$ for *Ru³⁺*

Hund's coupling

=

$j_{\text{eff}} = 1/2$ pseudospin with anisotropic exchange interactions



Edge-sharing octahedra

Suppress super-exchange processes

Material candidates:

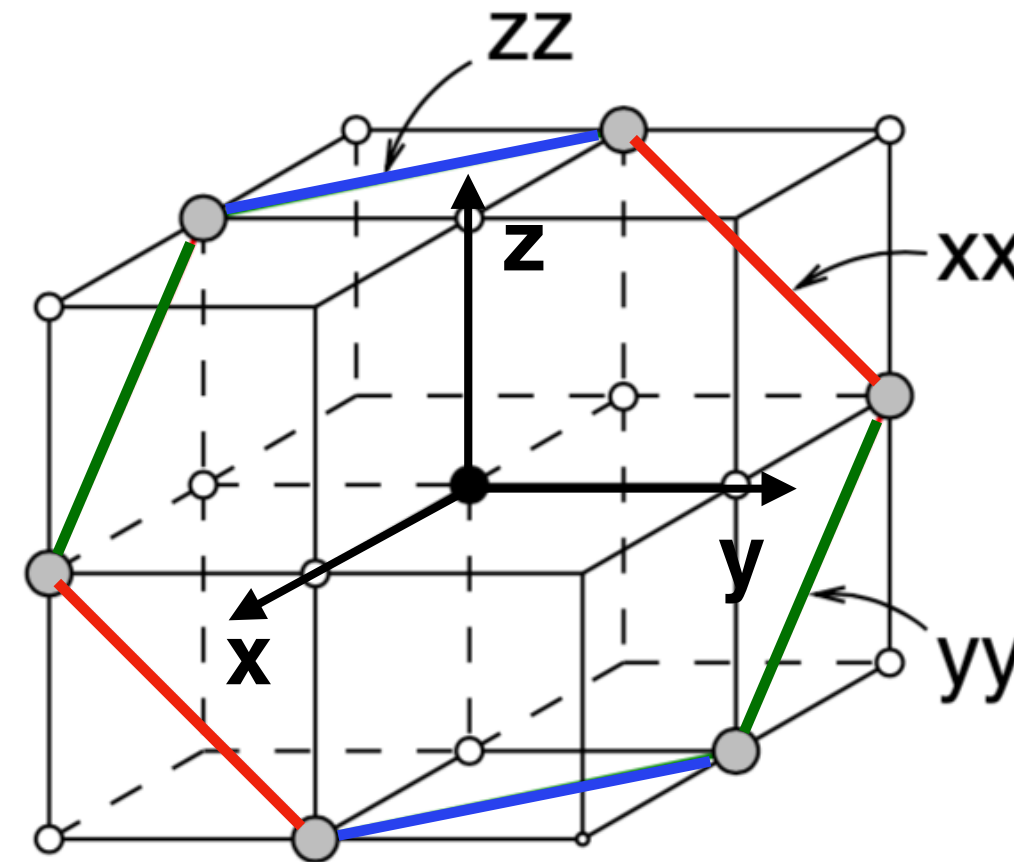
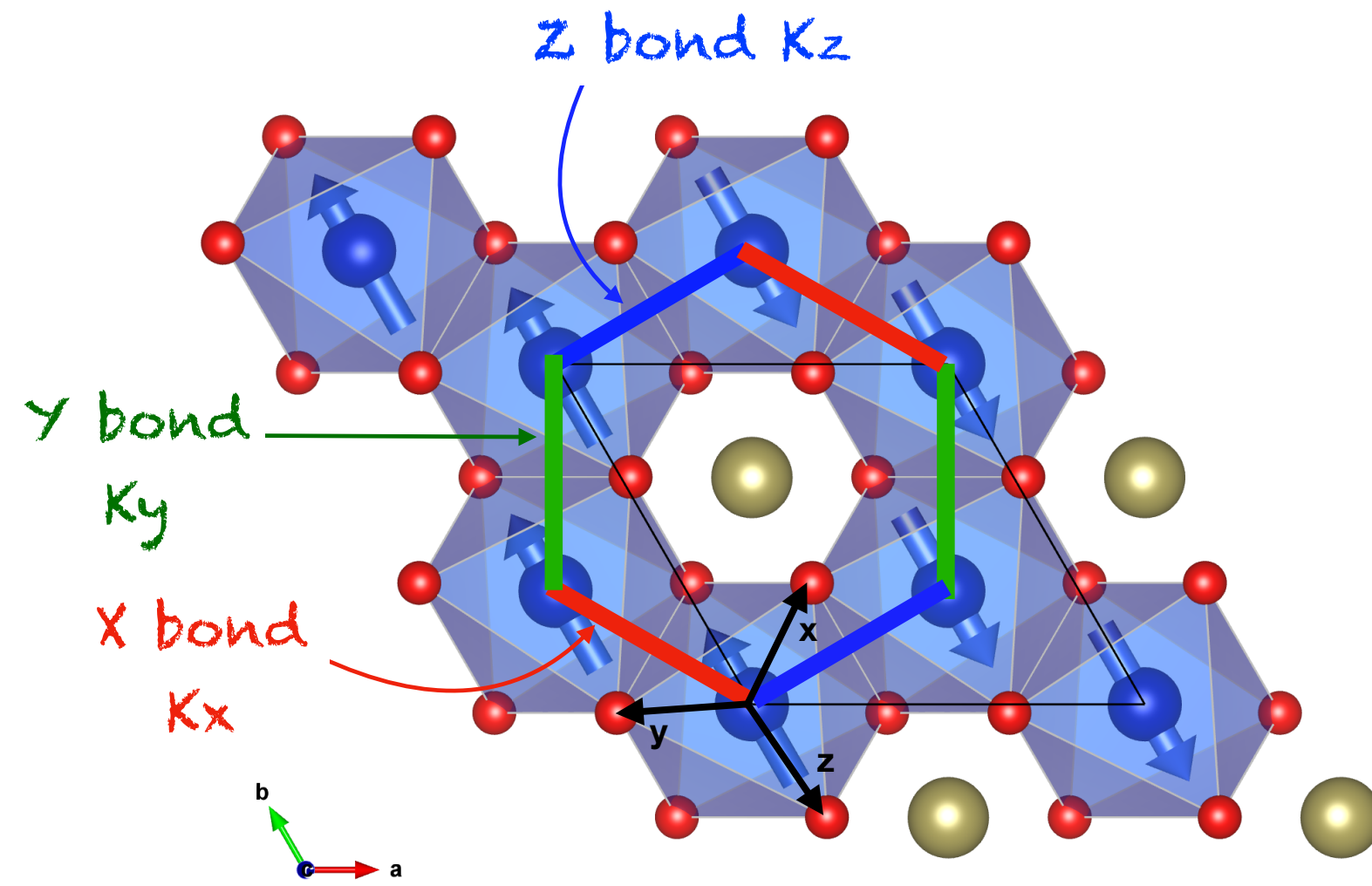
α -RuCl₃, Na₂IrO₃, α -Li₂IrO₃, Li₂RhO₃ ...

S. M. Winter et al., J. Phys.: Condens. Matter 29, 493002 (2017)

The Kitaev model: experimental realization?



Bond-dependent Kitaev interactions



Anisotropic bond-dependent interactions

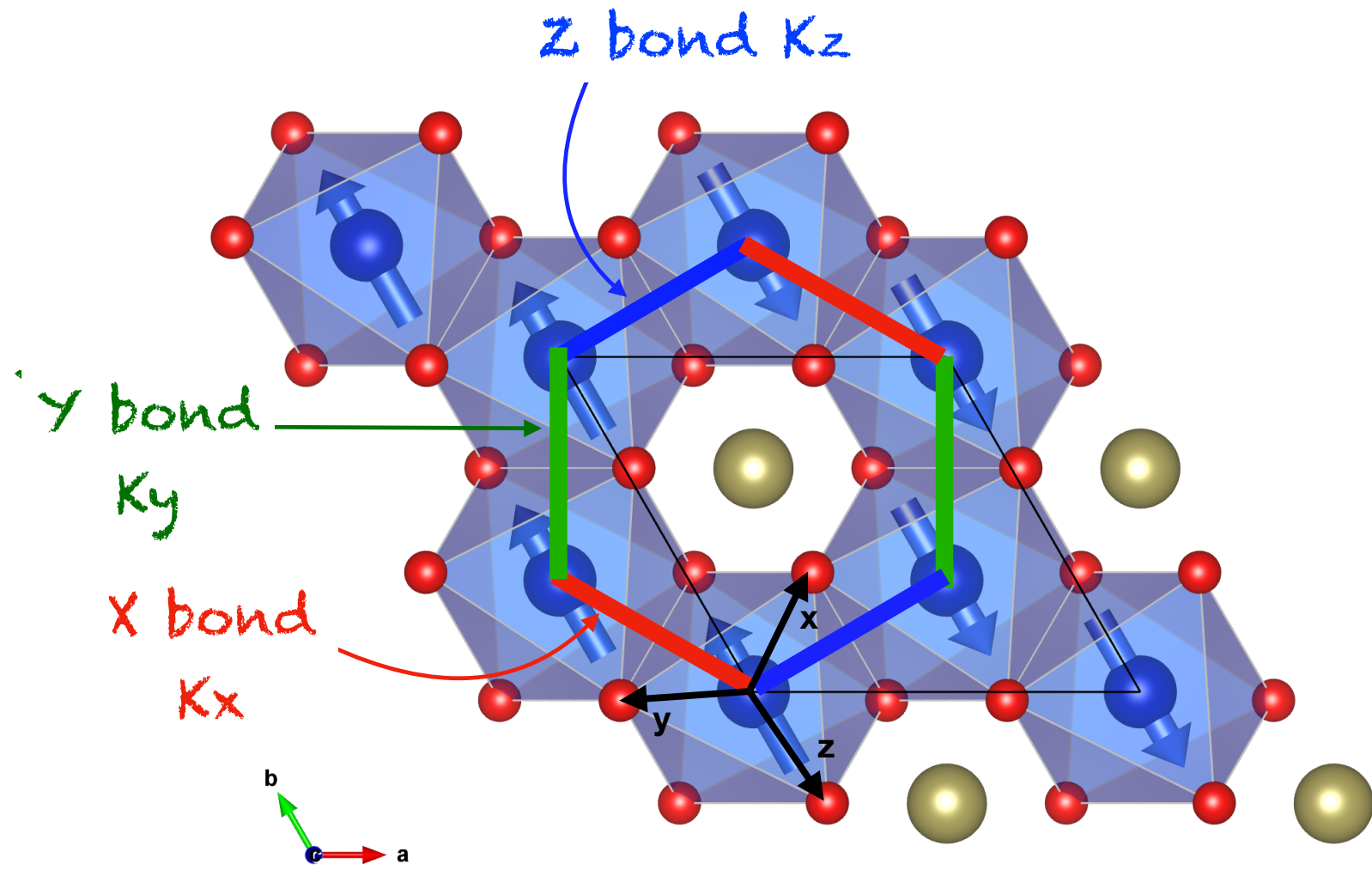
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→ Kitaev quantum spin liquid

The Kitaev model: experimental realization?

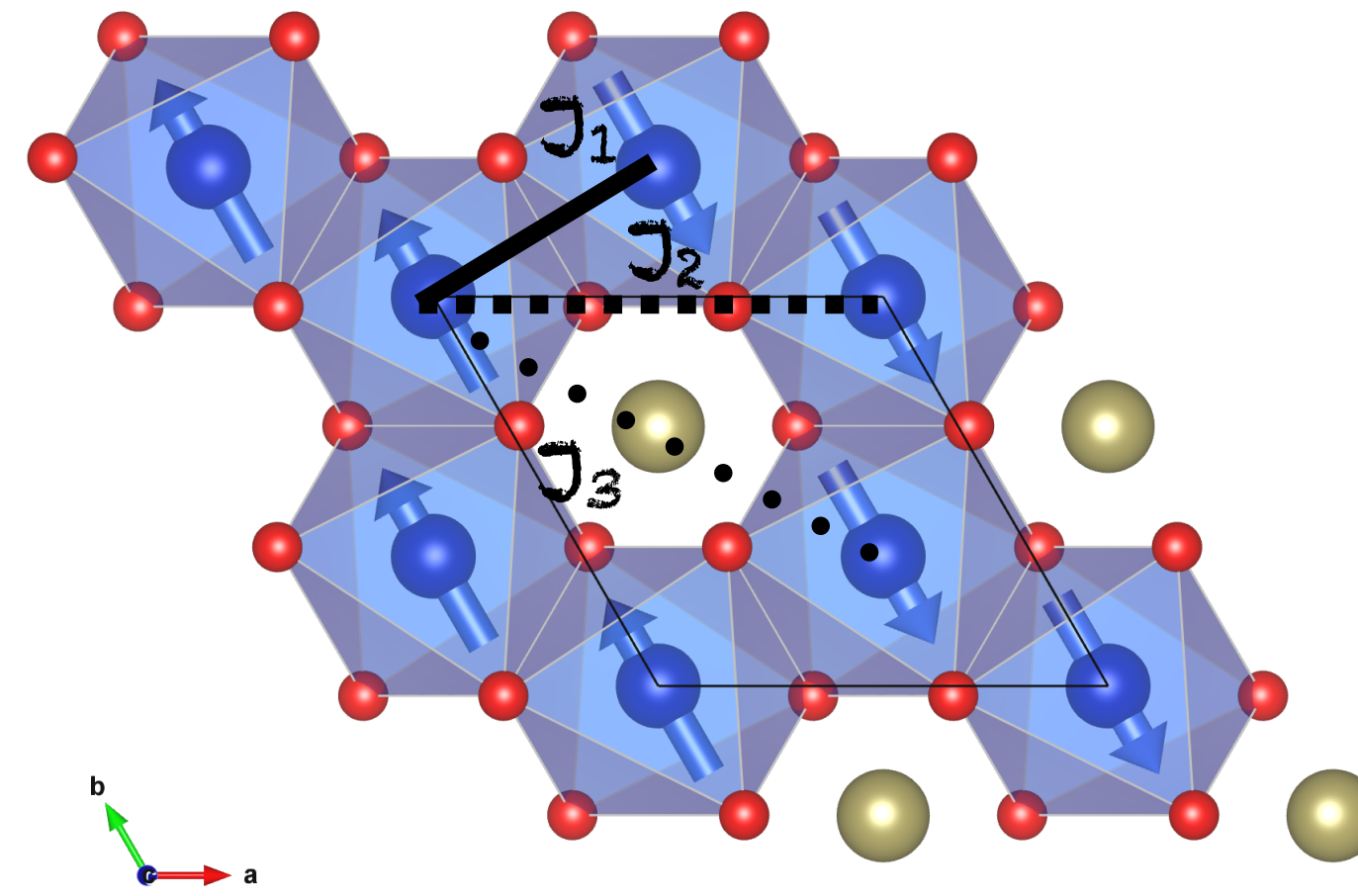


Bond-dependent Kitaev interactions



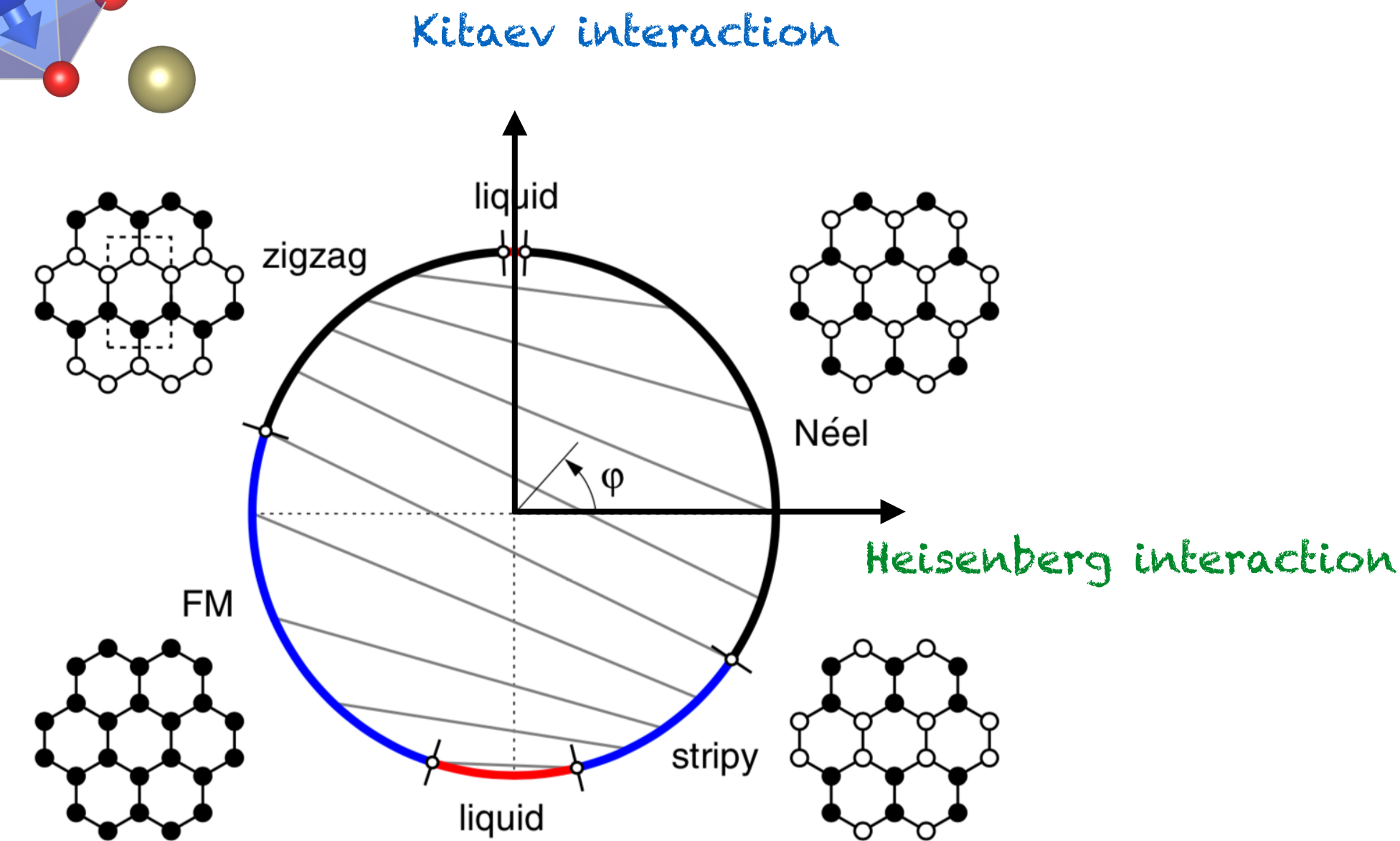
AND

Isotropic Heisenberg interactions



- ▶ Direct exchange
- ▶ Distortions : bond angles away from 90°

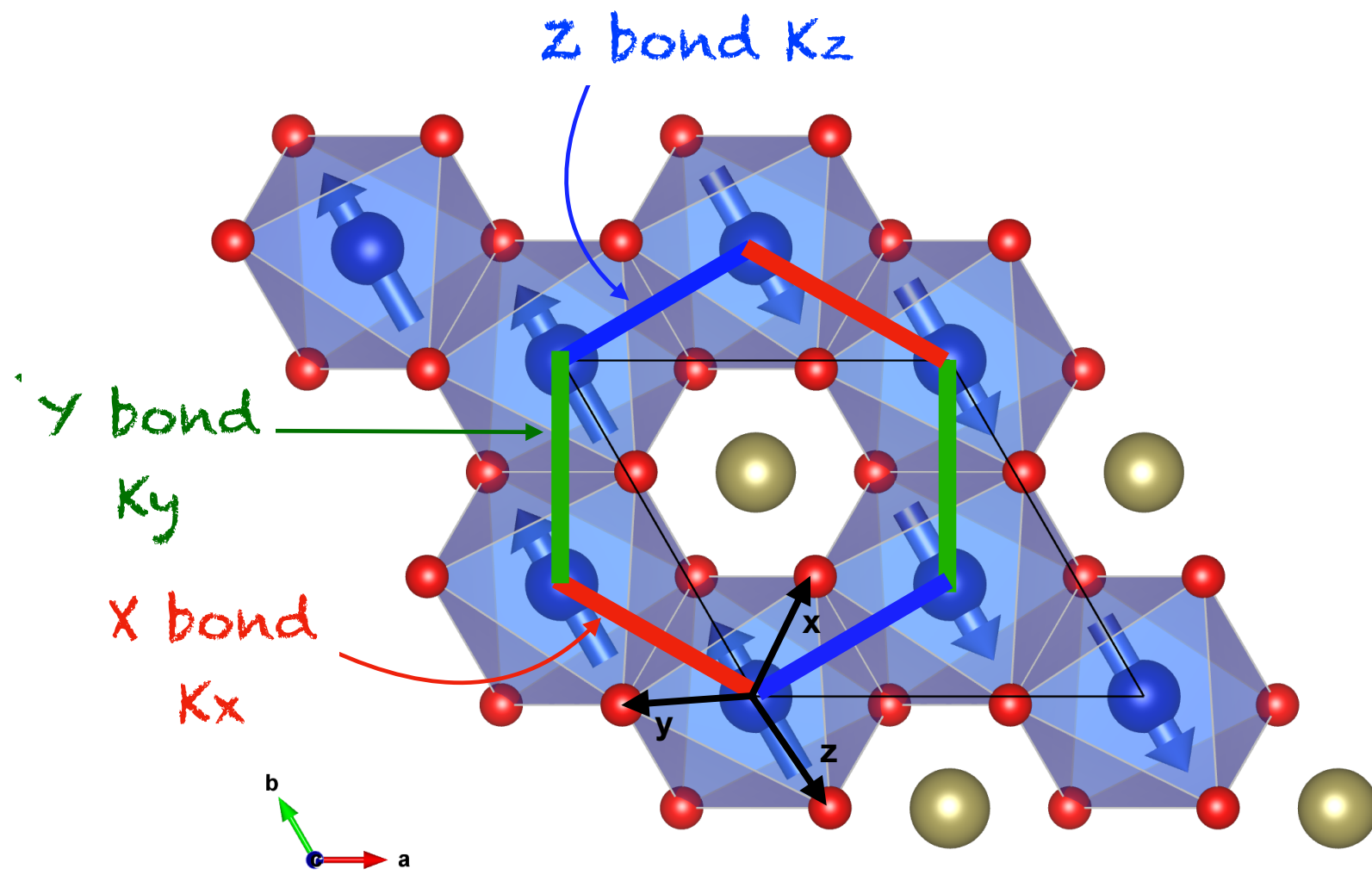
➔ Long-range magnetic order at low temperature



The Kitaev model: experimental realization?

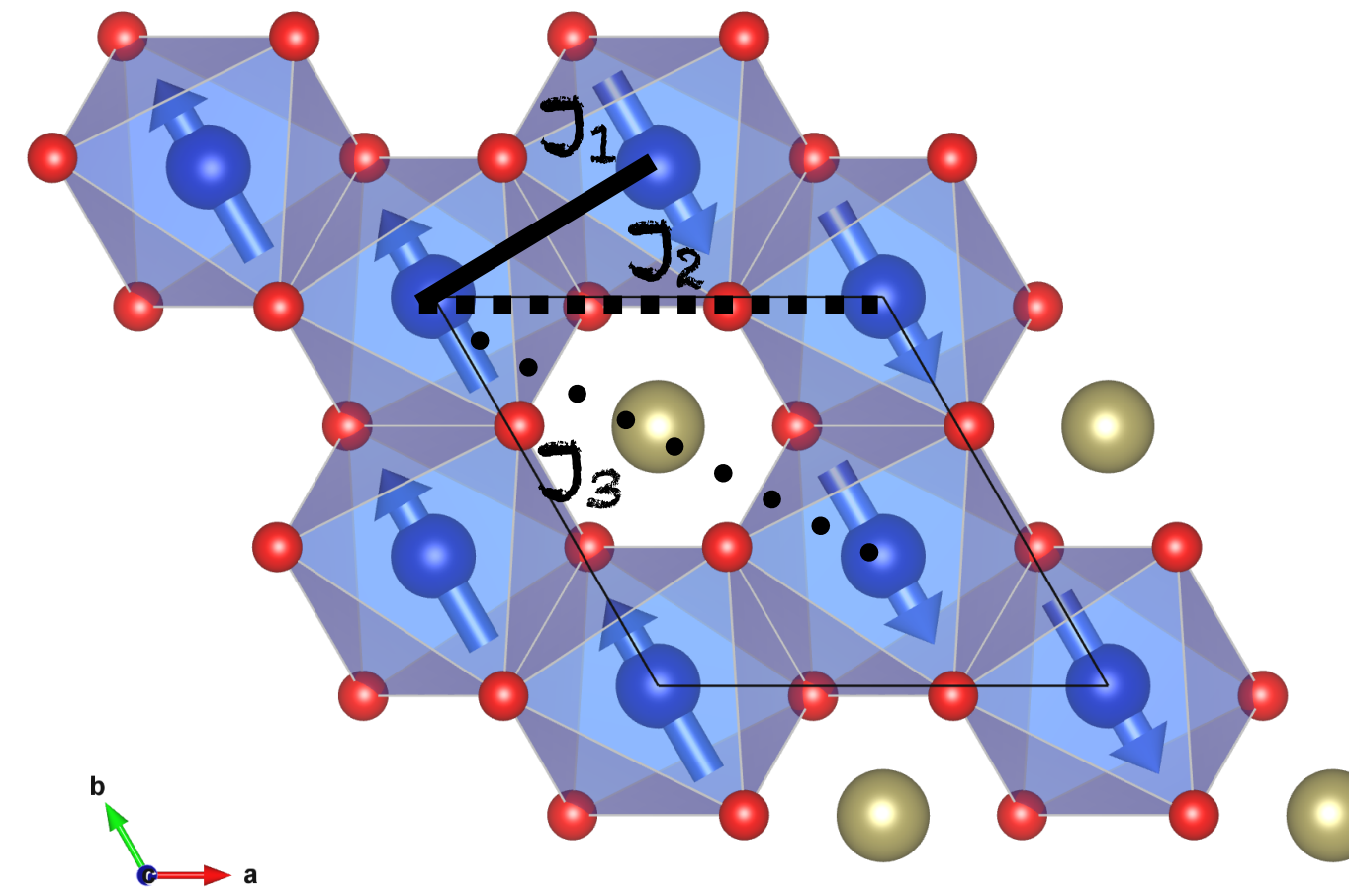


Bond-dependent Kitaev interactions



AND

Isotropic Heisenberg interactions



- ▶ Direct exchange
- ▶ Distortions : bond angles away from 90°

➔ Long-range magnetic order at low temperature

Exchange tensor:

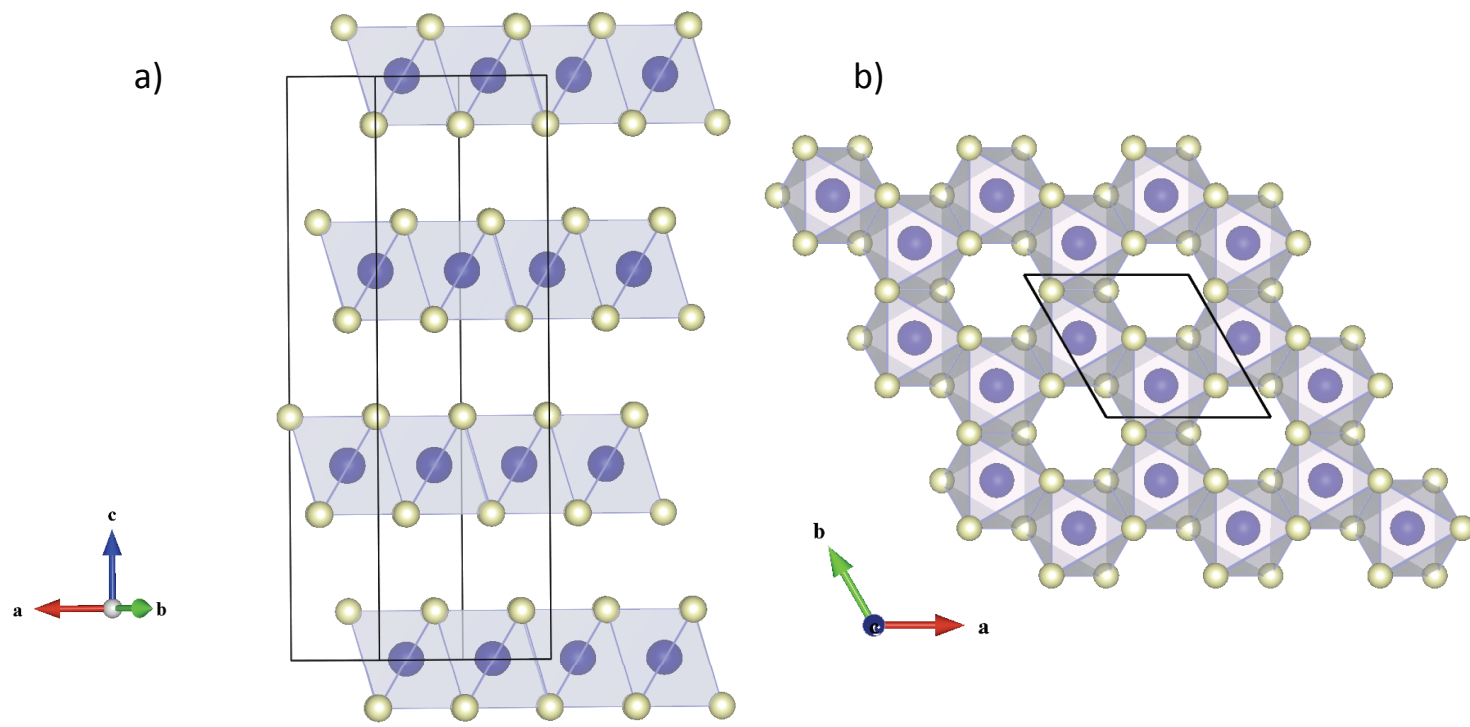
$$\begin{pmatrix} K_x + J & \Gamma + \Gamma' & \Gamma + \Gamma' \\ \Gamma + \Gamma' & K_y + J & \Gamma + \Gamma' \\ \Gamma + \Gamma' & \Gamma + \Gamma' & K_z + J \end{pmatrix}$$

P. A. Maksimov et al., Phys. Rev. Research 2, 03311 (2020)
H. Liu et al., Phys. Rev. Letters 125, 047201 (2020)

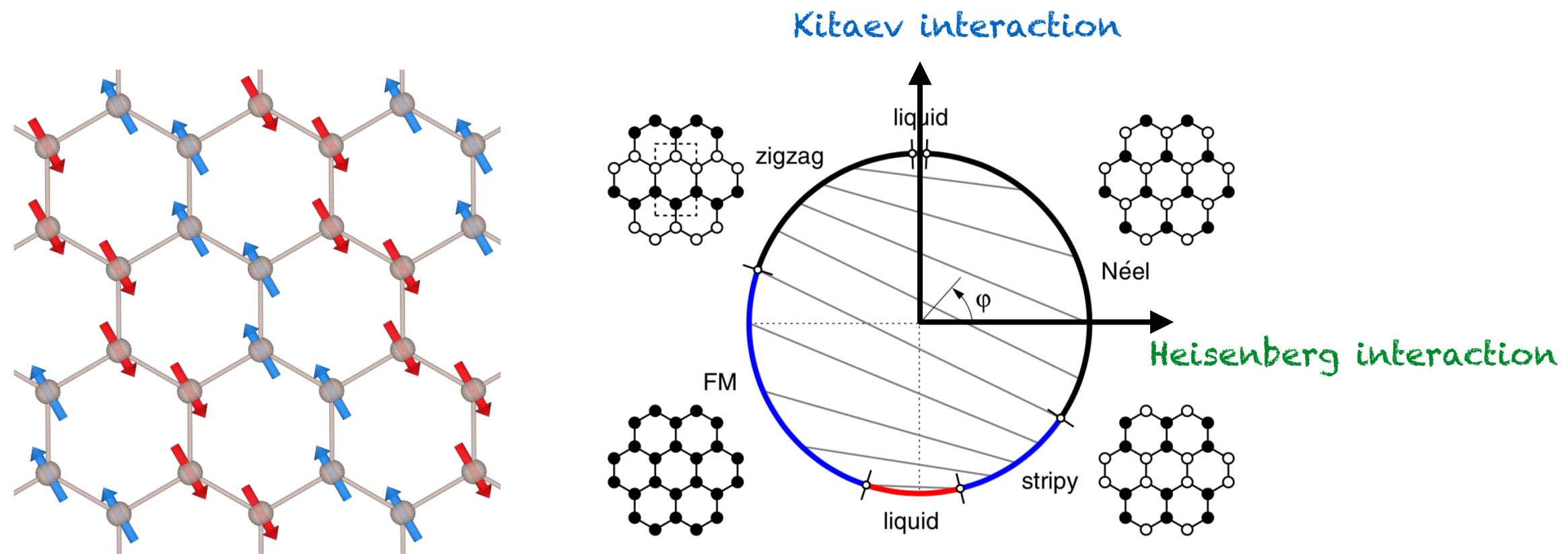
A promising material candidate: α - RuCl_3



A Van der Waals crystal



Zigzag magnetic order



J. A. Sears, M. Songvilay et al., Phys. Rev. B 91, 144420 (2015)

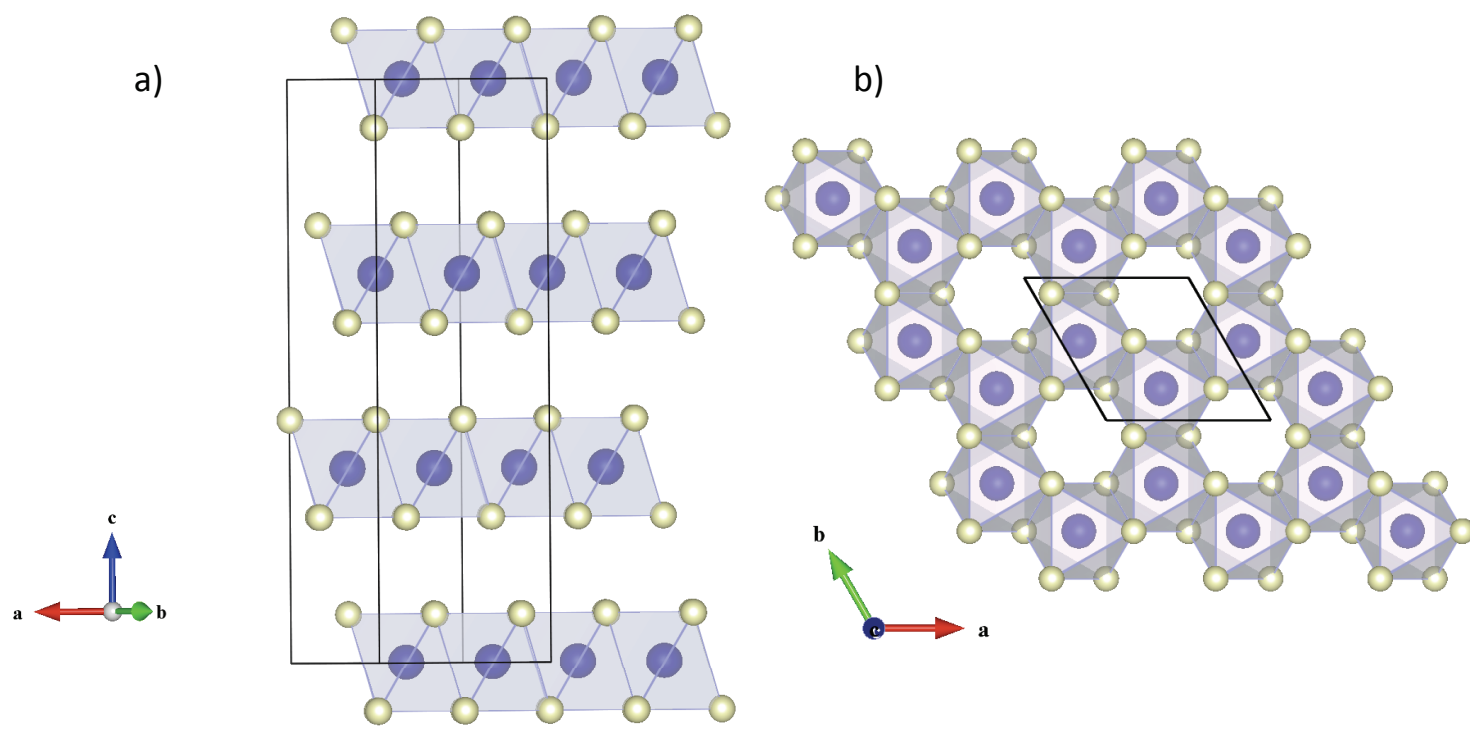
R. D. Johnson et al., Phys. Rev. B 92, 235119 (2015)

A. Banerjee et al., Nat. Mat. 15, 733 (2016)

A promising material candidate: α -RuCl₃



A Van der Waals crystal

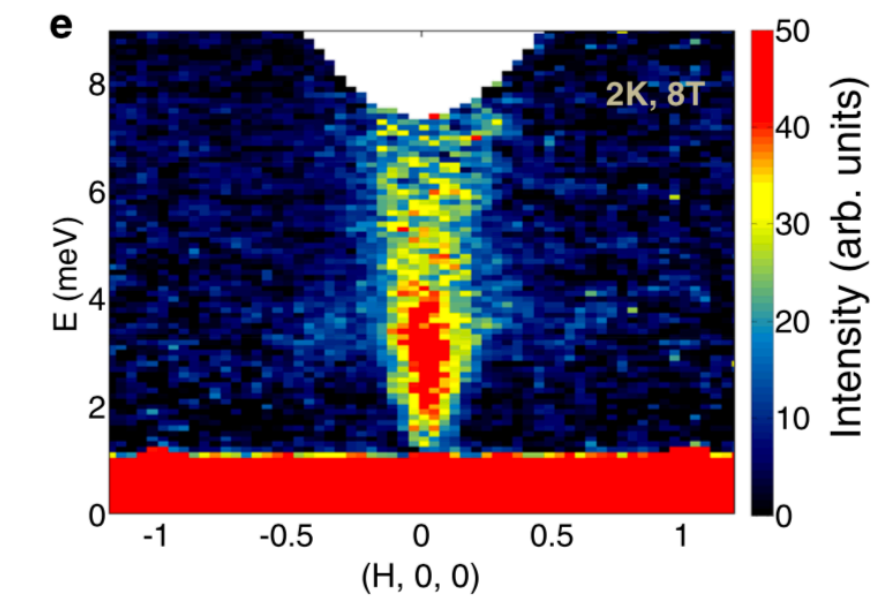
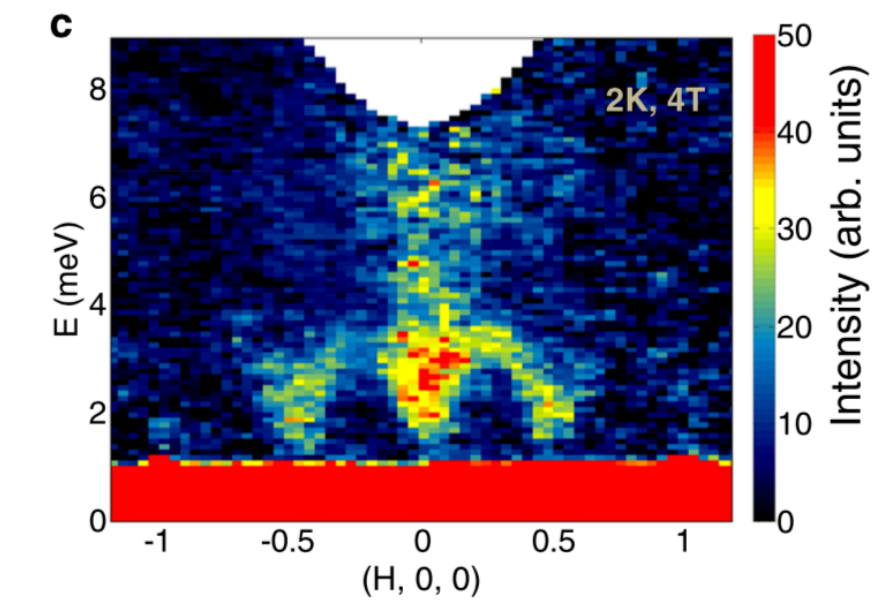
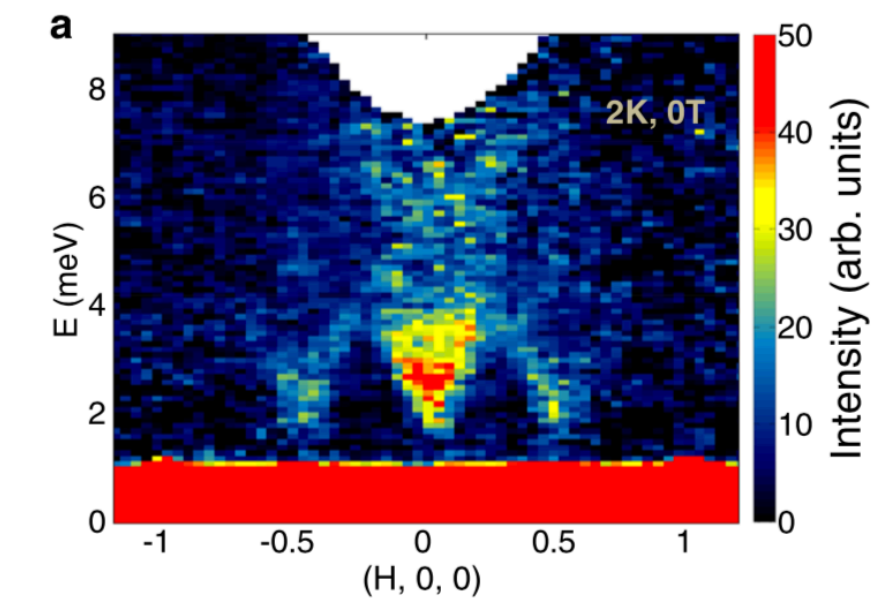
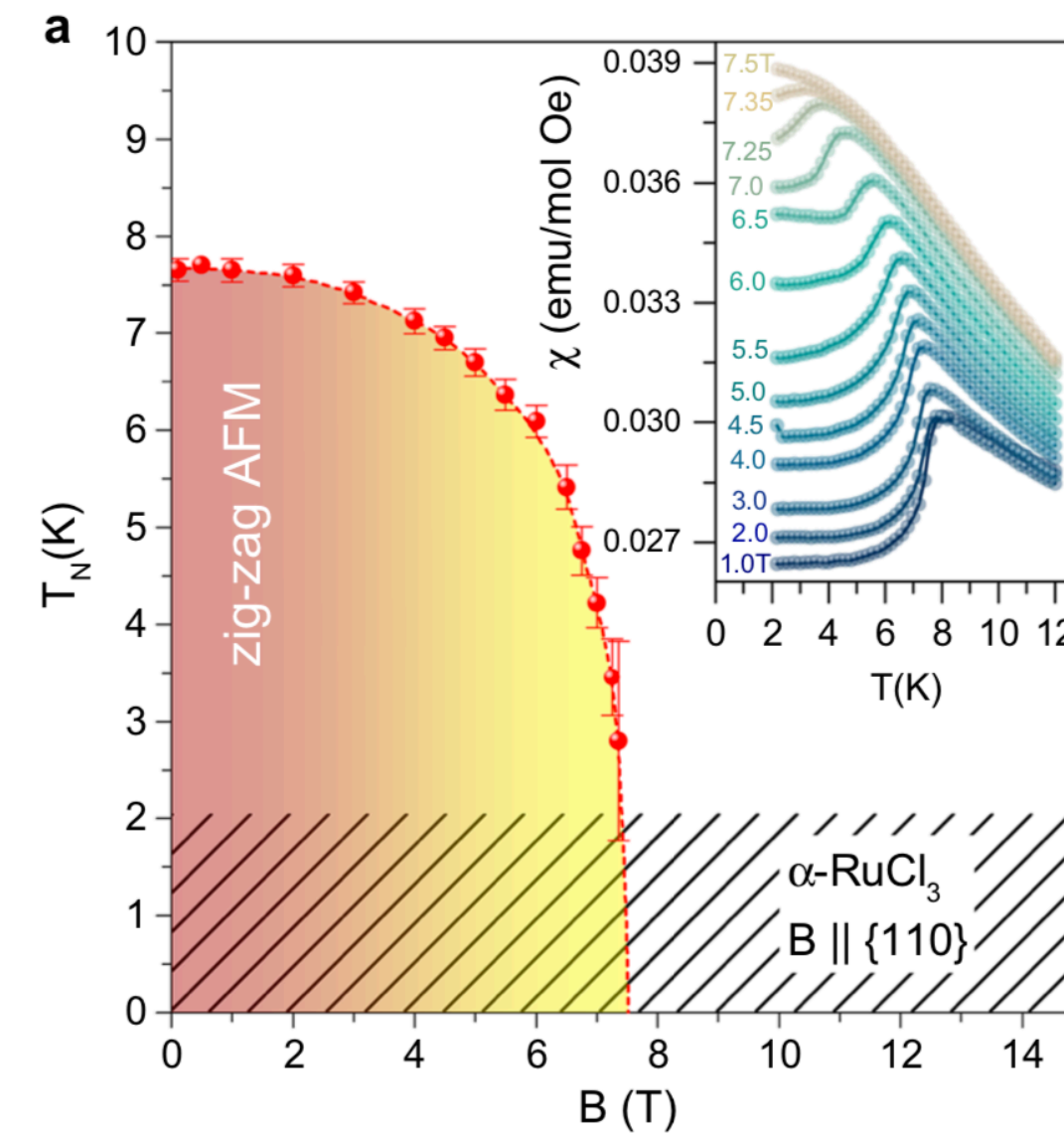
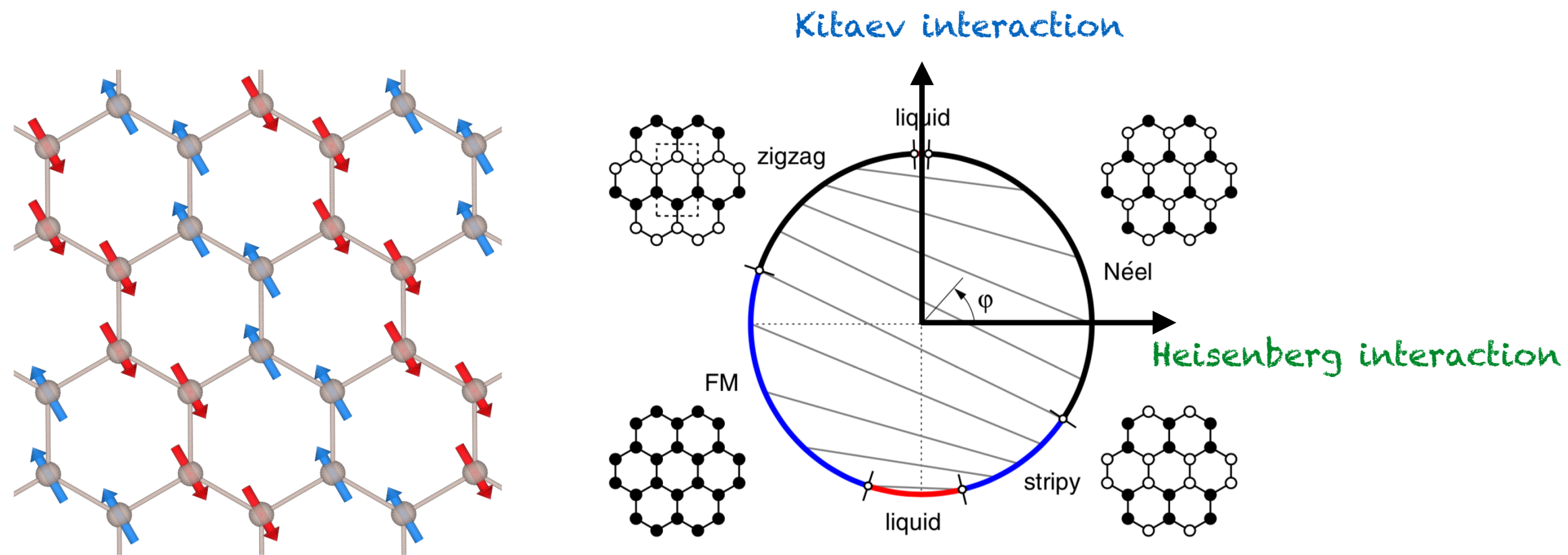


Possible field-induced quantum spin liquid state

- Suppression of magnetic order (in-plane field)
- gapped continuum of excitations (neutron scattering)

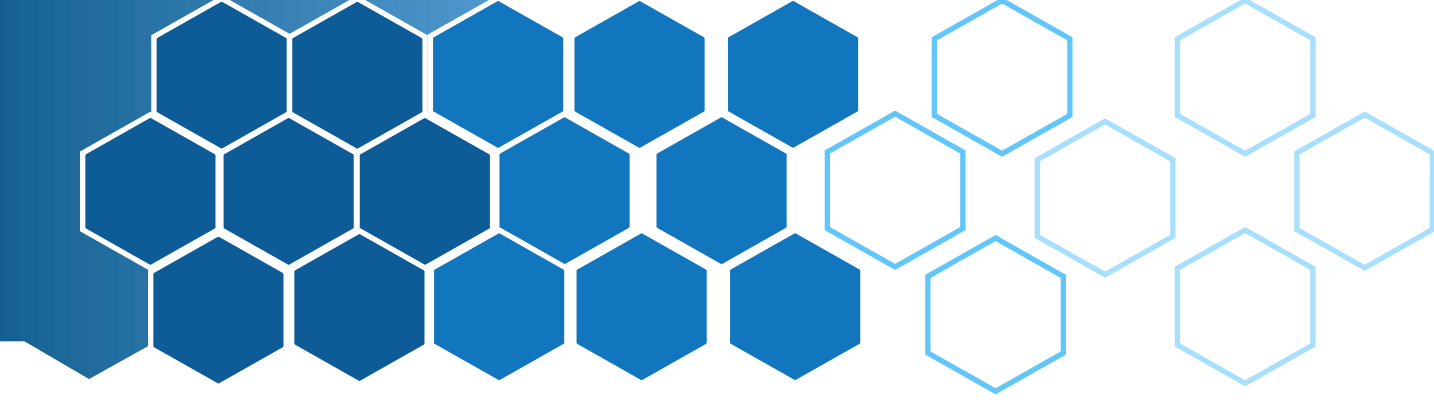
J. A. Sears et al., Phys. Rev. B 95, 180411(R) (2017)
A. Banerjee et al., npj Quantum Materials 3, 8 (2018)

Zigzag magnetic order

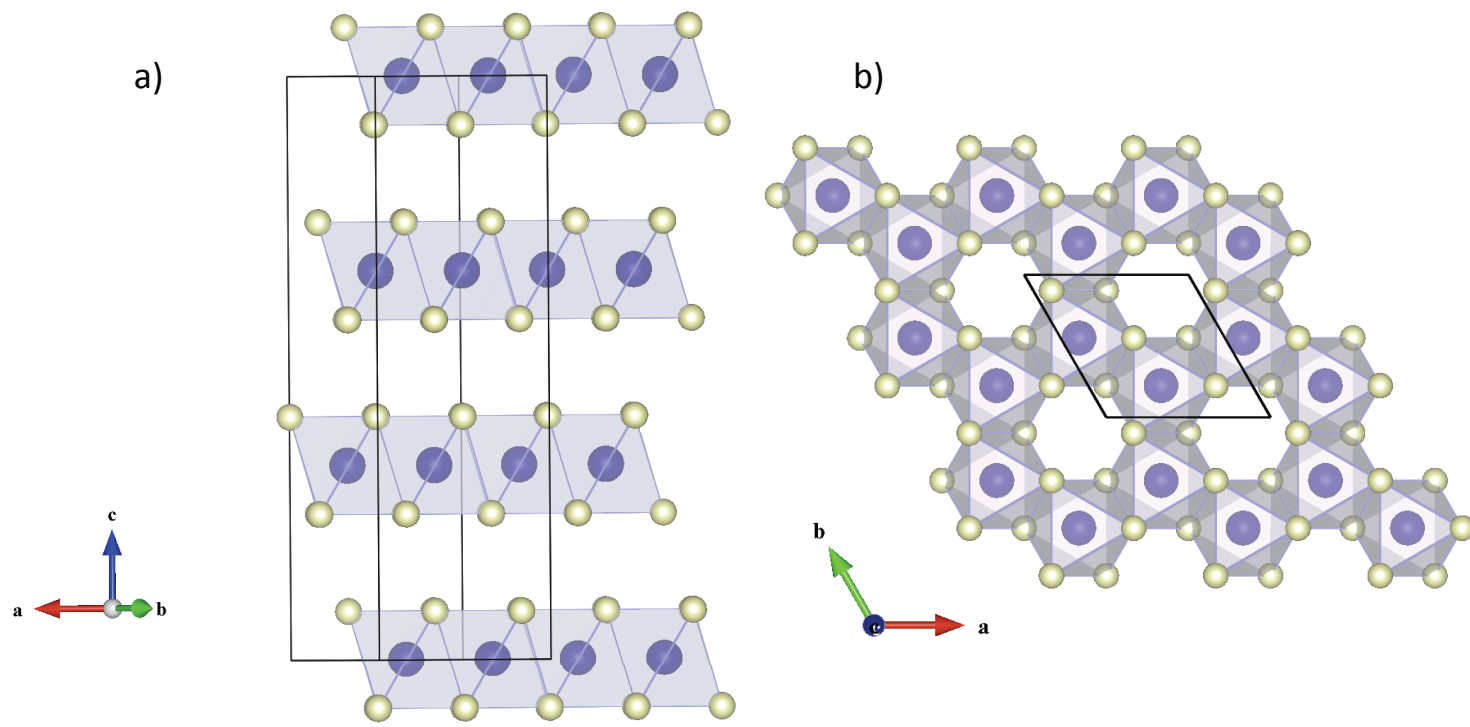


J. A. Sears, M. Songvilay et al., Phys. Rev. B 91, 144420 (2015)
R. D. Johnson et al., Phys. Rev. B 92, 235119 (2015)
A. Banerjee et al., Nat. Mat. 15, 733 (2016)

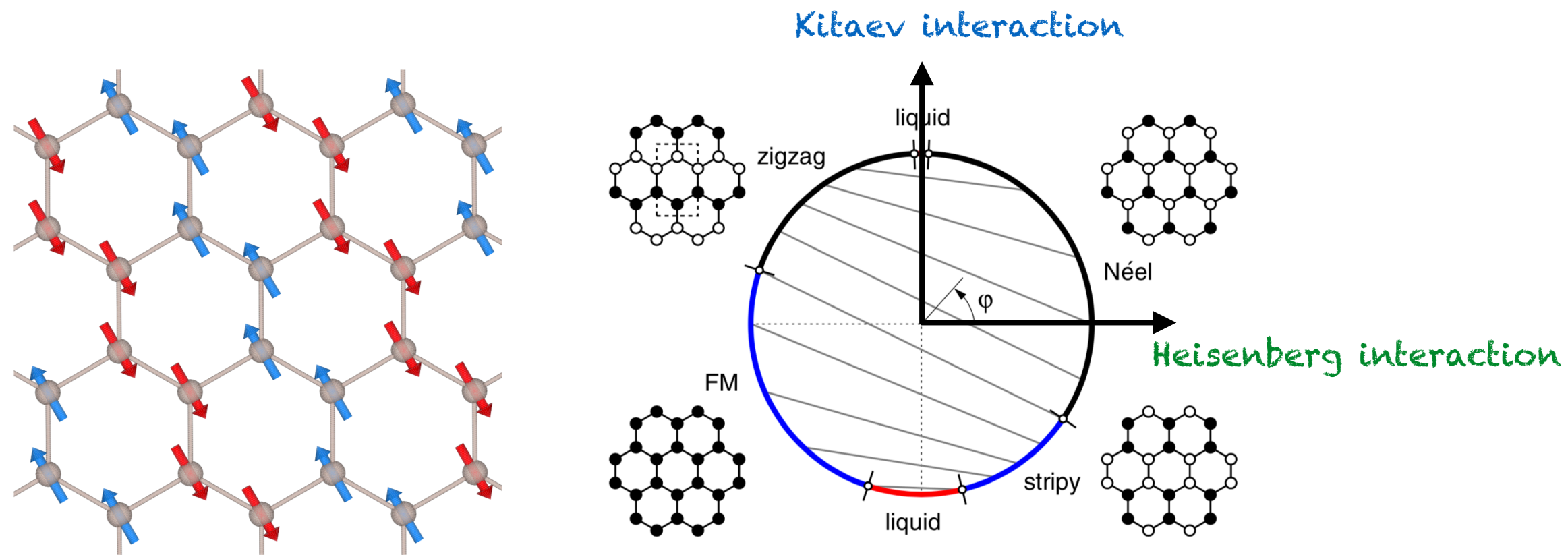
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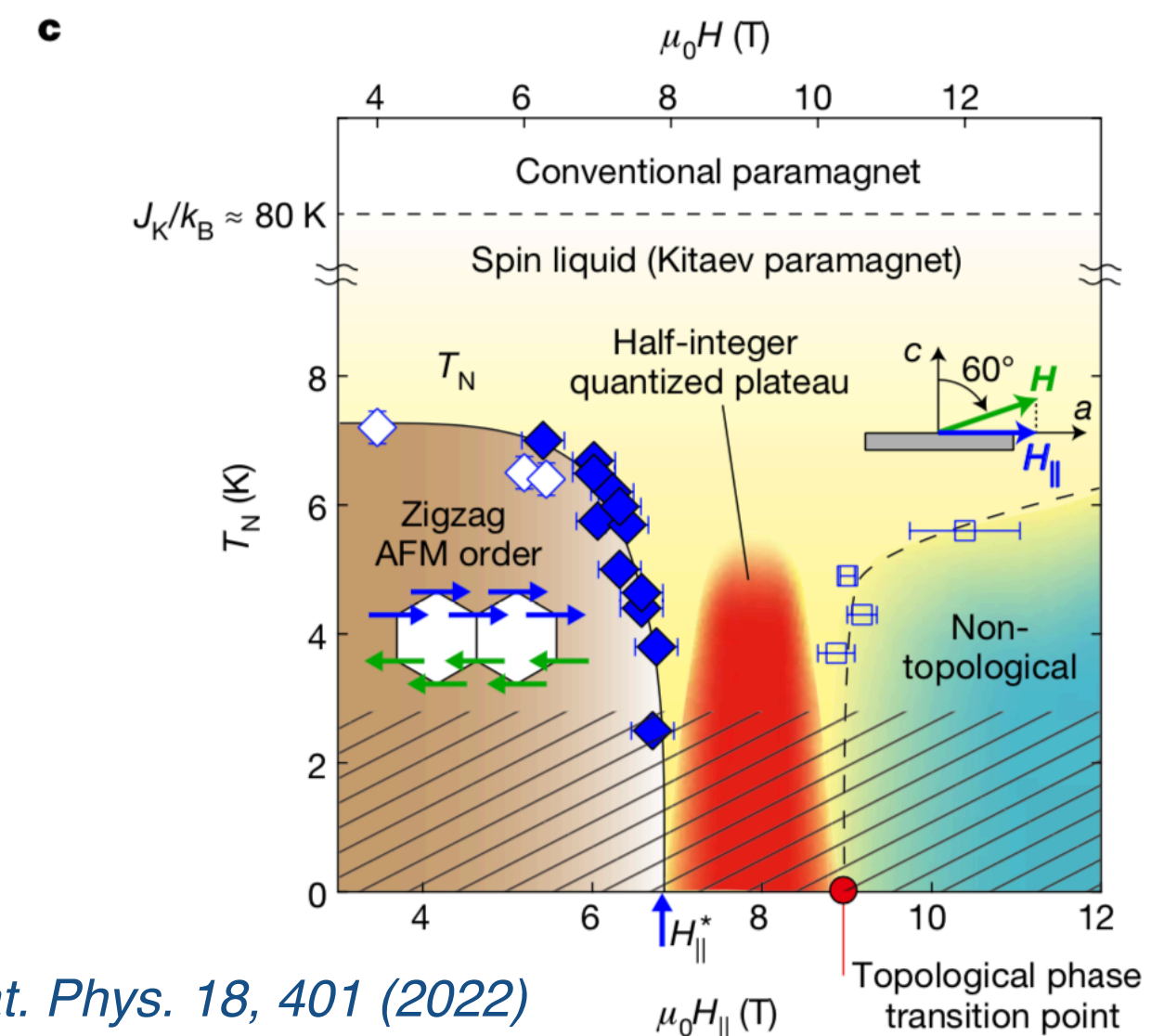
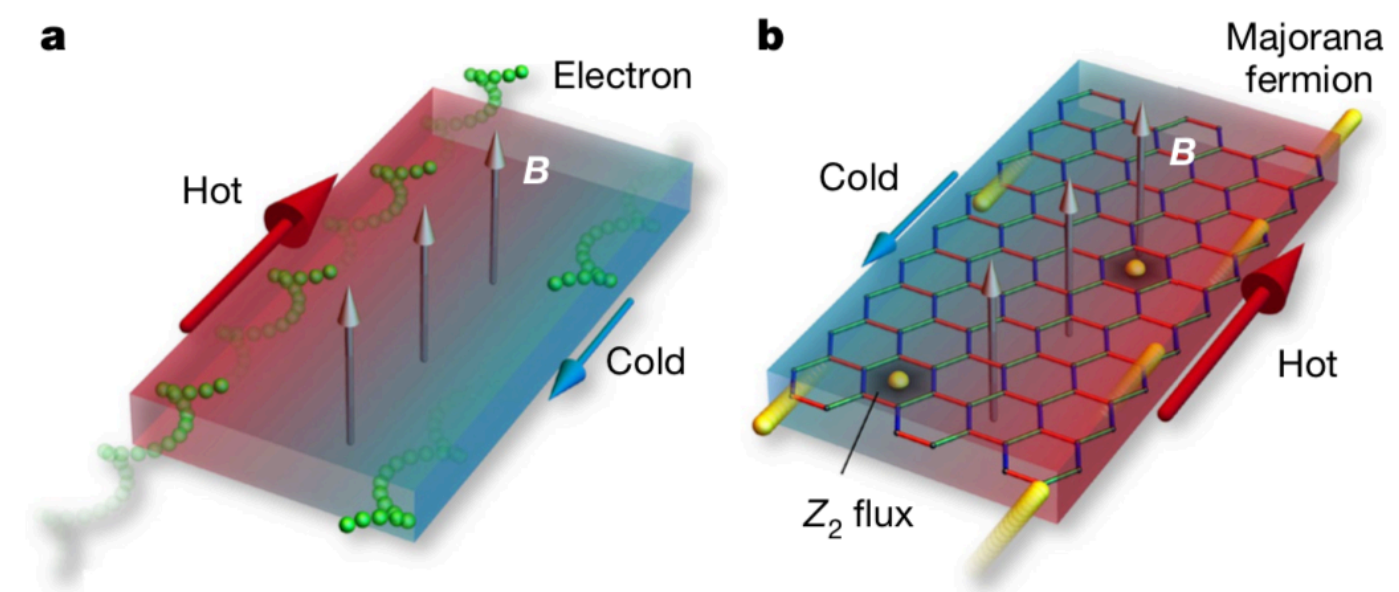
R. D. Johnson et al., Phys. Rev. B 92, 235119 (2015)

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Half-integer thermal hall conductance : evidence for edge current Majorana-like excitations ?

► **Topological phase under magnetic field ?**

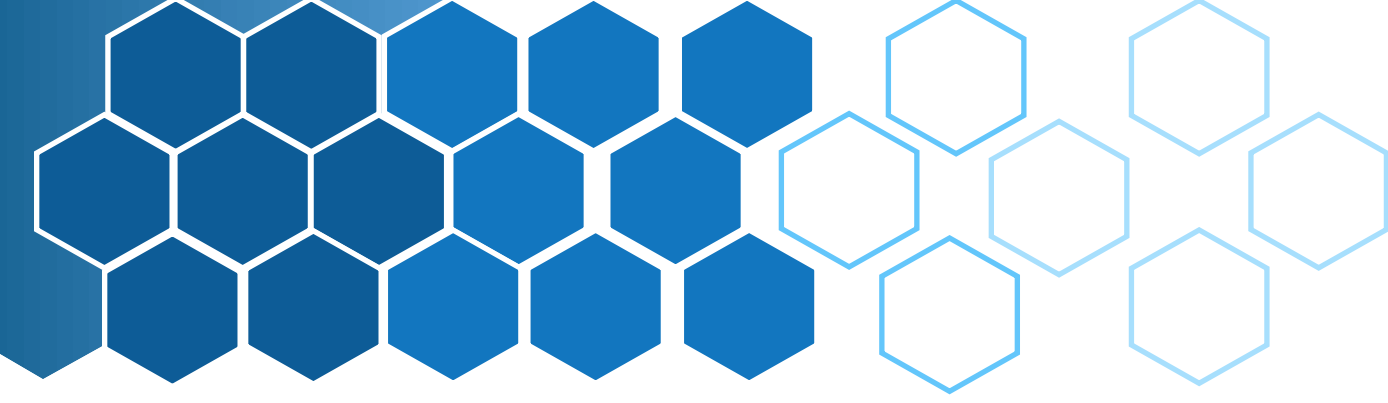
Y. Kasahara et al., Nature 559, 7713 (2018)



J. Bruin et al., Nat. Phys. 18, 401 (2022)

T. Yokoi et al., Science 373, 6554 (2021)

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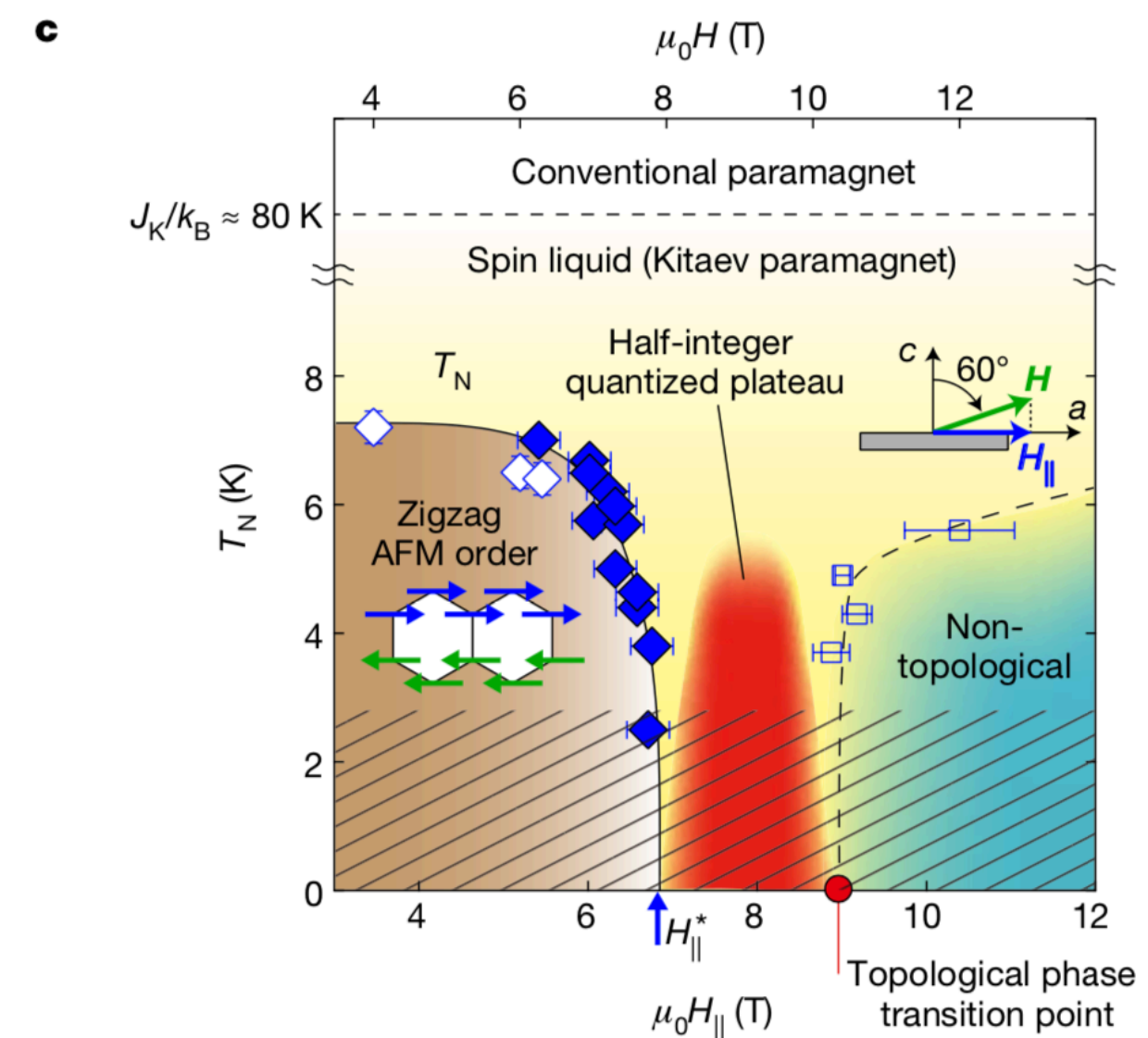
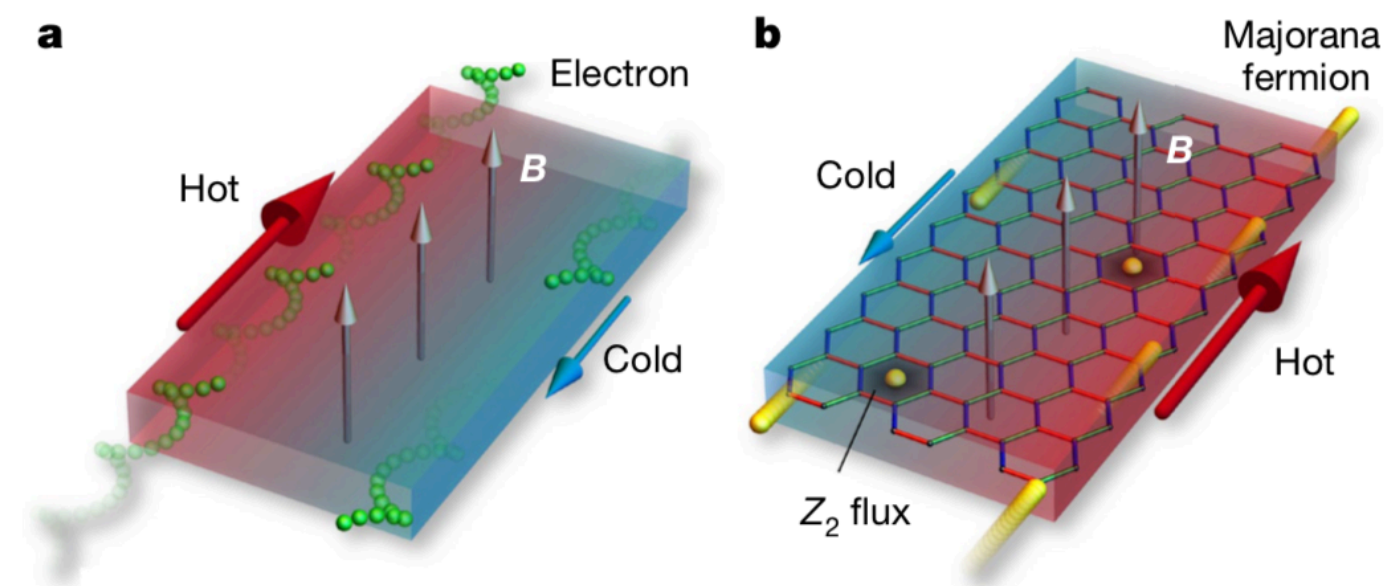
➔ Other contributions to the thermal Hall effect?

E. Zhang et al., Phys. Rev. B 103, 174402 (2021)

➔ Possible strong contribution of the phonons to the thermal Hall conductivity?

R. Hentrich et al., Phys. Rev. Lett. 120, 117204 (2018)

E. Lefrançois et al., Phys. Rev. X 12, 021025 (2022)



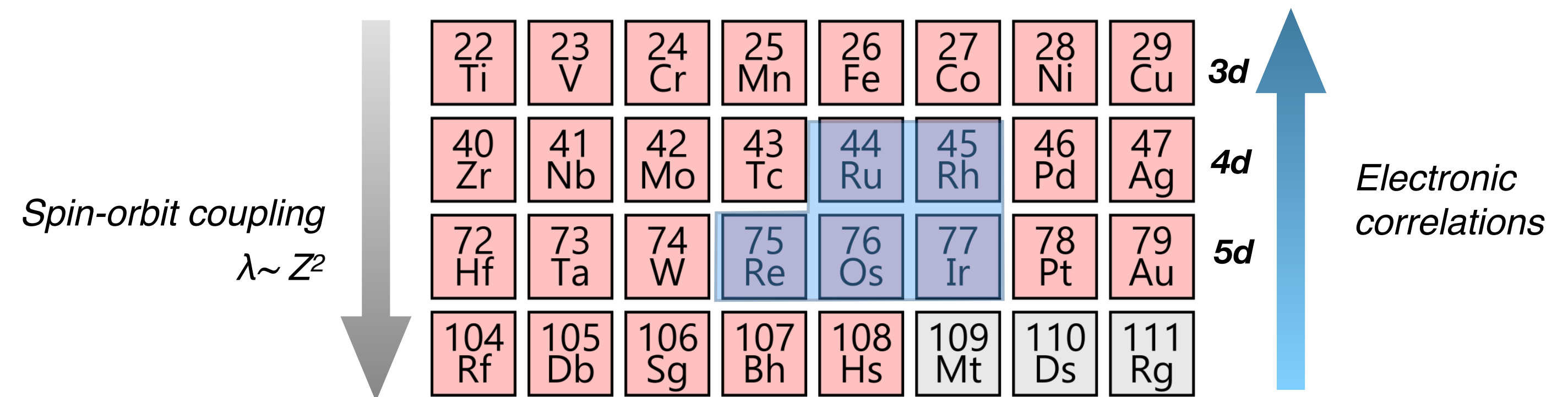
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Beyond the Jackeli-Khaliullin proposal :

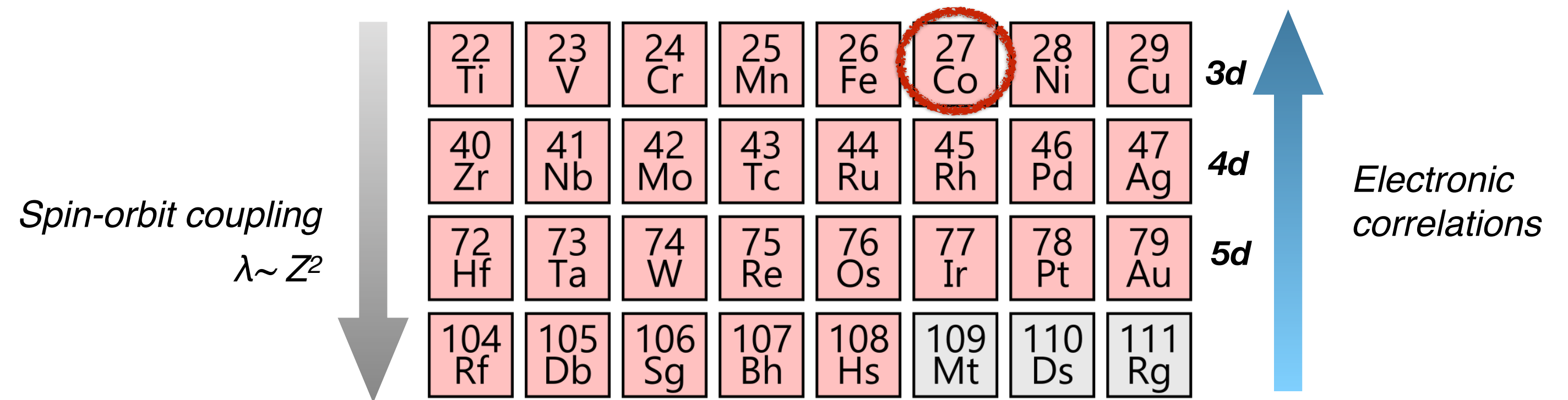
- ✓ Spin-orbit coupling/electron correlations : 3d transition metals, rare-earth, spin value...
- ✓ Other structures : organic materials, 3D lattices, triangular lattices...





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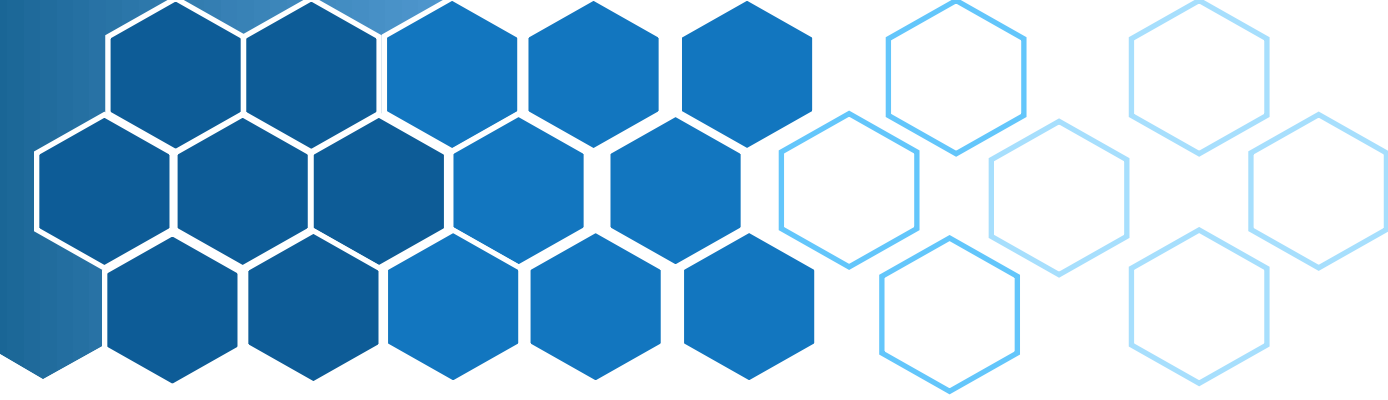


H. Liu and G. Khaliullin, Phys. Rev. B 97, 014407 (2018)

R. Sano et al., Phys. Rev. B 97, 014408 (2018)

H. Liu et al., Phys. Rev. Letters 125, 047201 (2020)

Beyond the Jackeli-Khaliullin proposal: cobalt materials



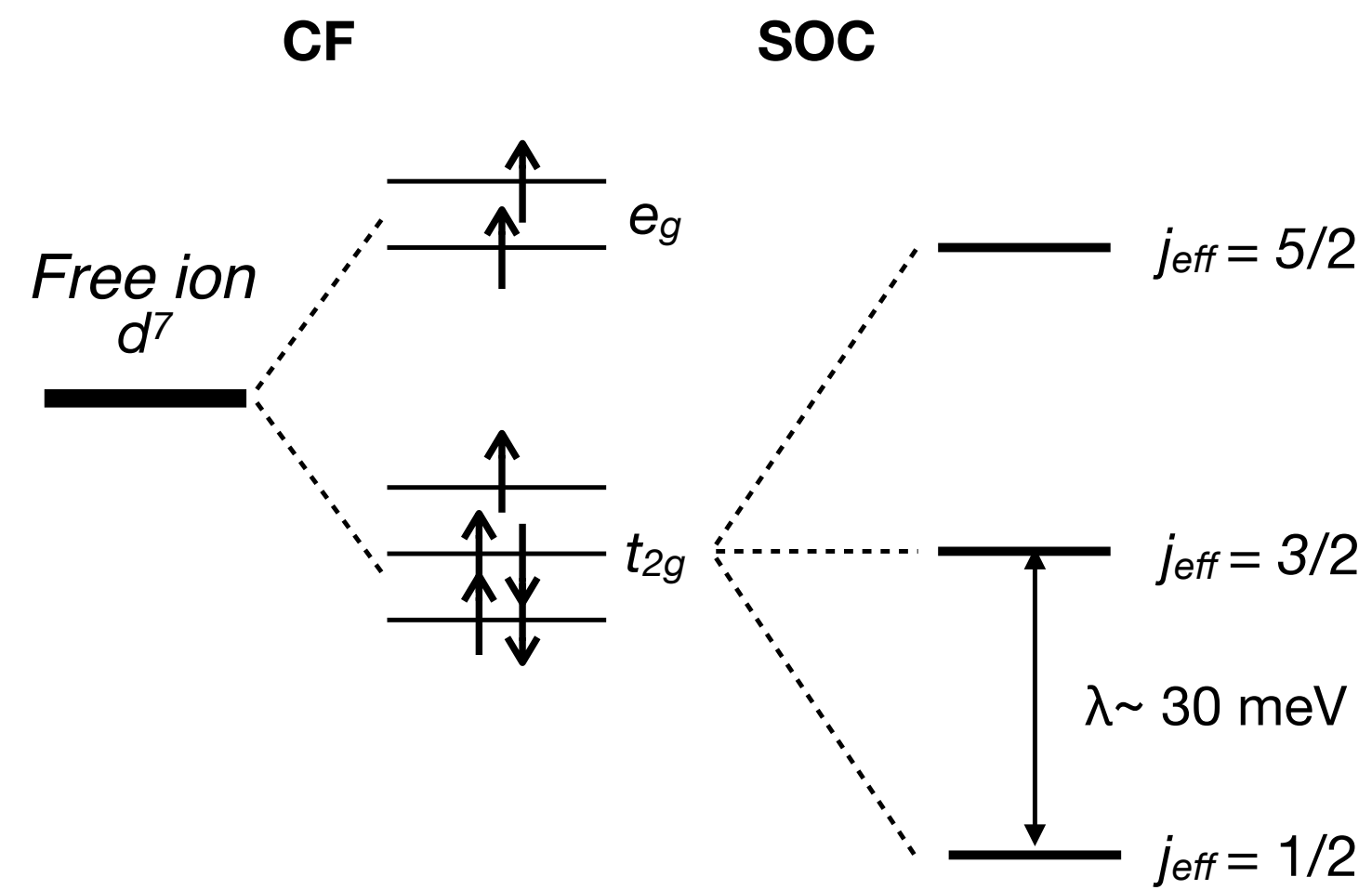
► Theoretical proposal to realise the Kitaev model in high-spin d7 systems

H. Liu and G. Khaliullin, Phys. Rev. B 97, 014407 (2018)

R. Sano et al., Phys. Rev. B 97, 014408 (2018)

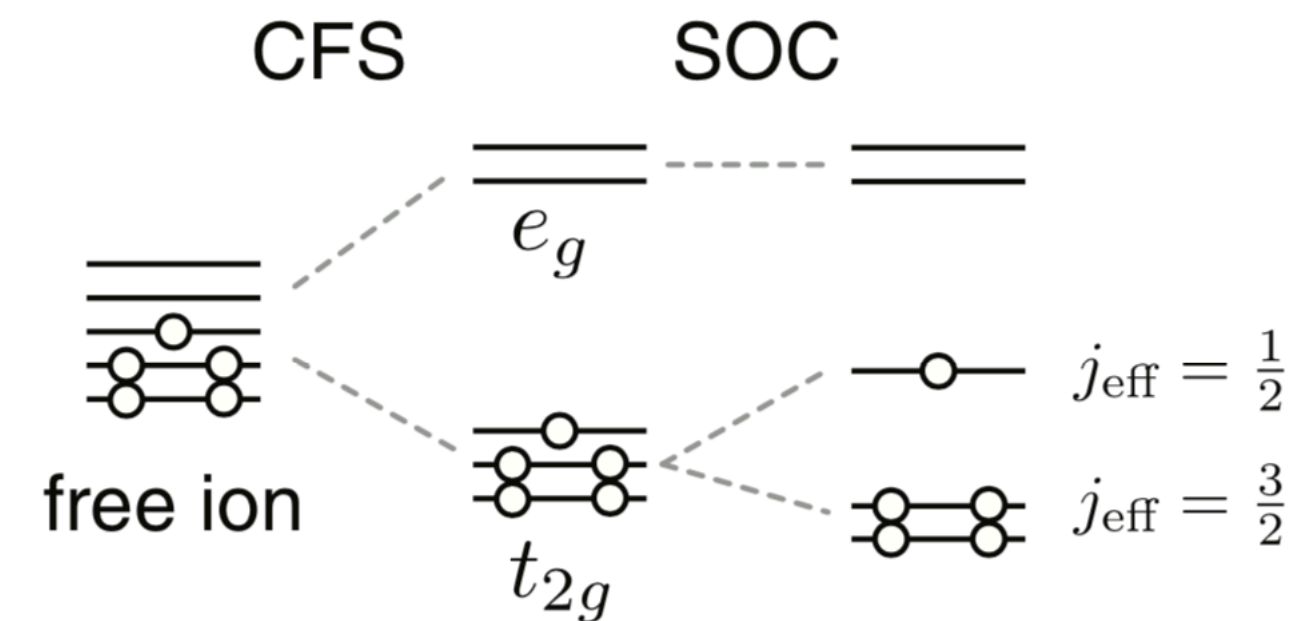
H. Liu et al., Phys. Rev. Letters 125, 047201 (2020)

Co²⁺ in octahedral environment : high spin 3d⁷ configuration (S = 3/2, L = 1)

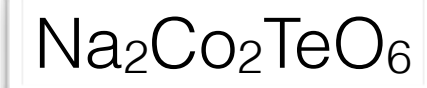
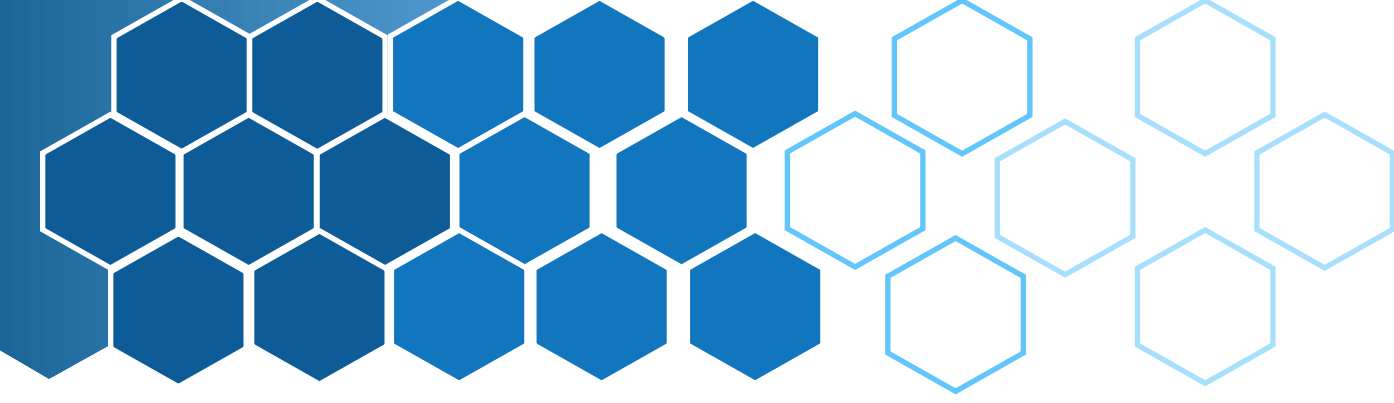


VS

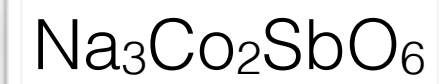
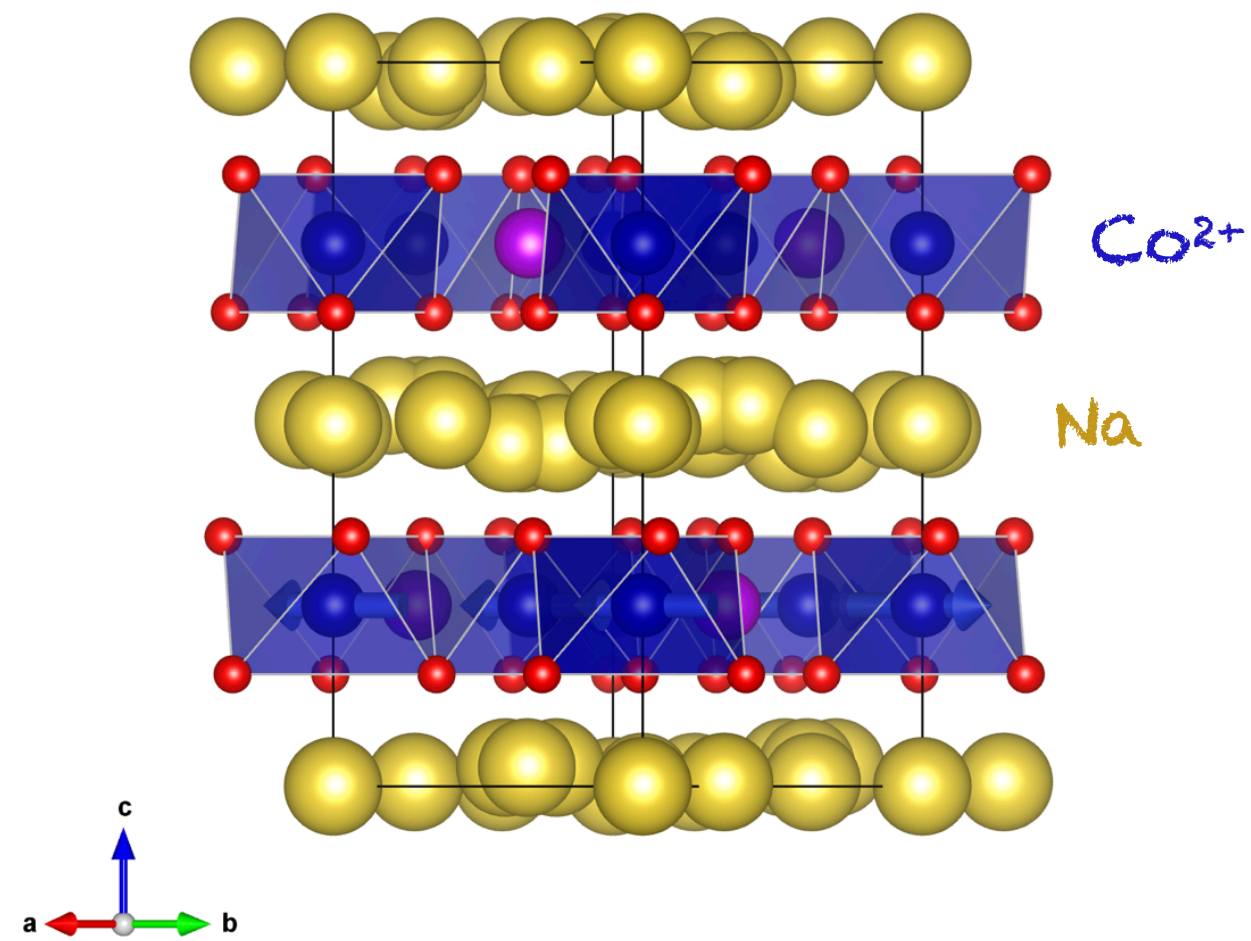
Ir⁴⁺ in octahedral environment: 5d⁵ configuration



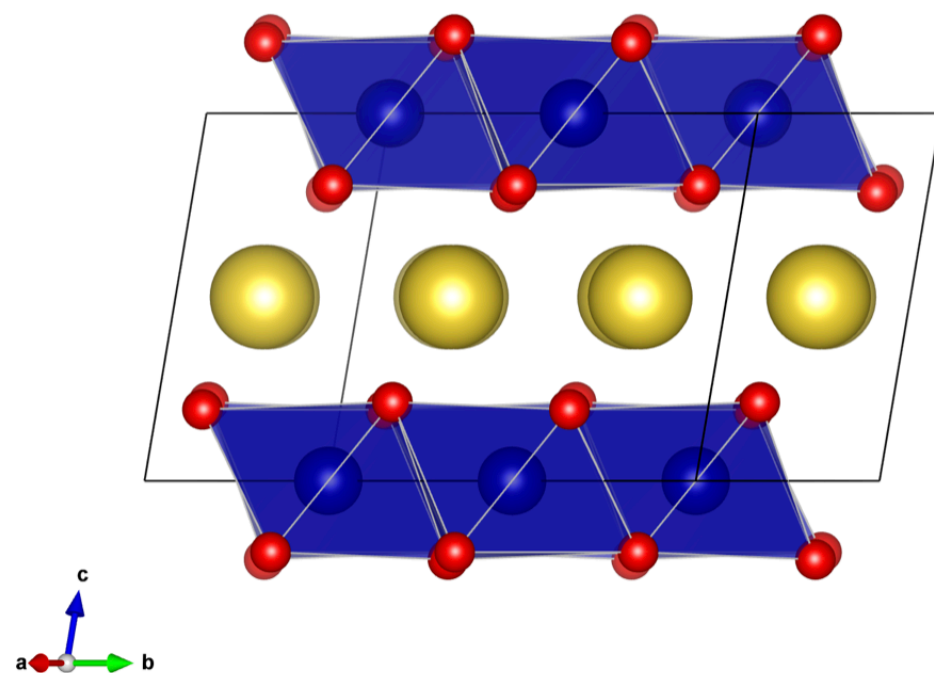
S. M. Winter et al., J. Phys.: Condens. Matter 29, 493002 (2017)



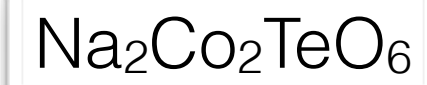
space group : $P6_322$ (hexagonal)



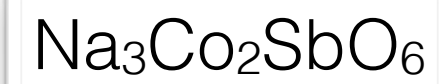
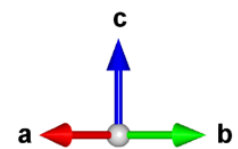
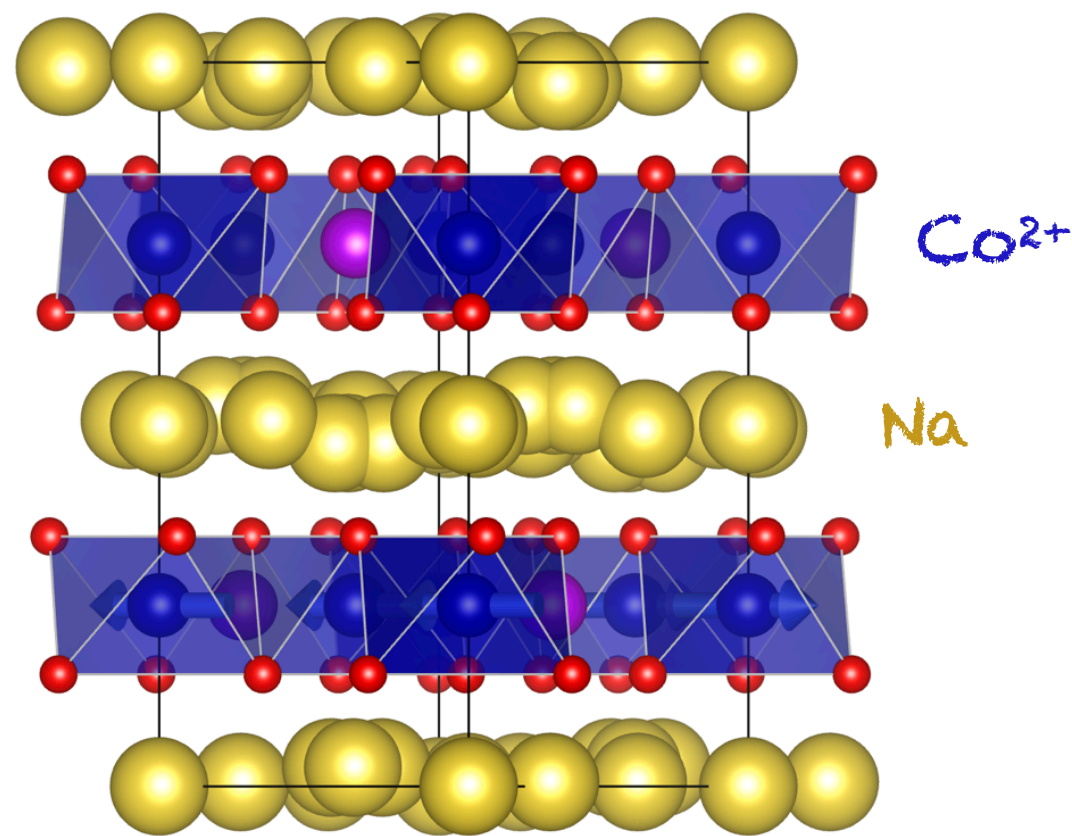
space group : $C2/m$ (monoclinic)



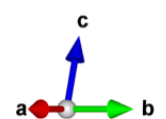
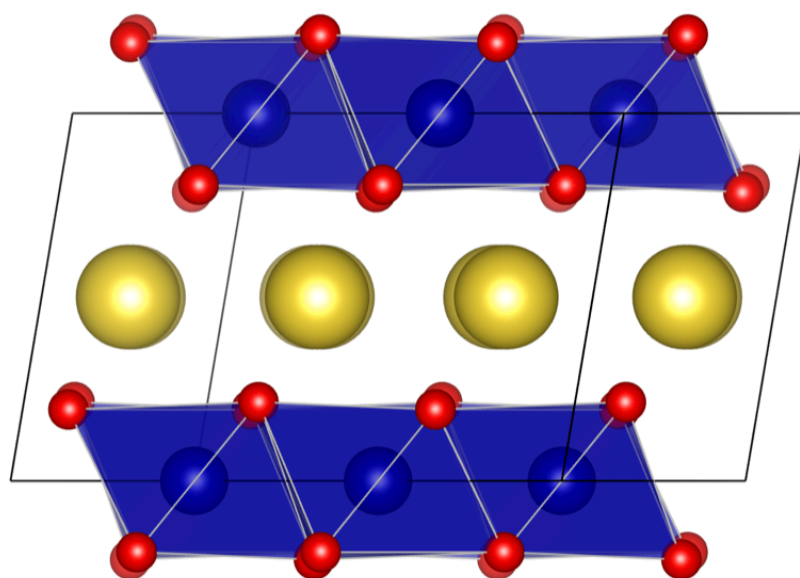
E. Lefrançois et al., Phys. Rev. B 94, 214416 (2016)
A. K. Bera et al., Phys. Rev. B 95, 094424 (2017)
C. Wong et al., J. Sol. State. Chem. 243 (2016)
J.-Q Yan et al., Phys. Rev. Mat. 3, 074405 (2019)



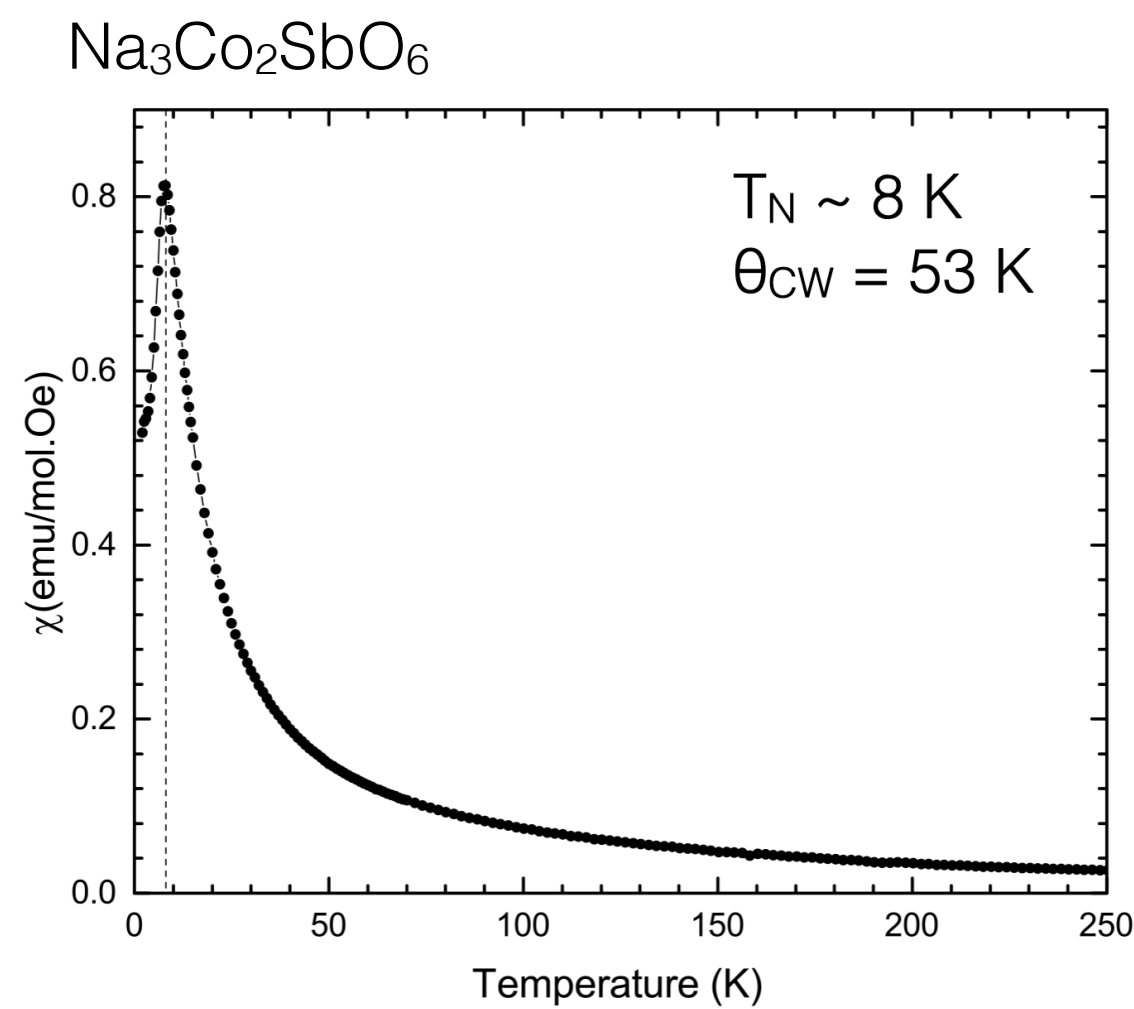
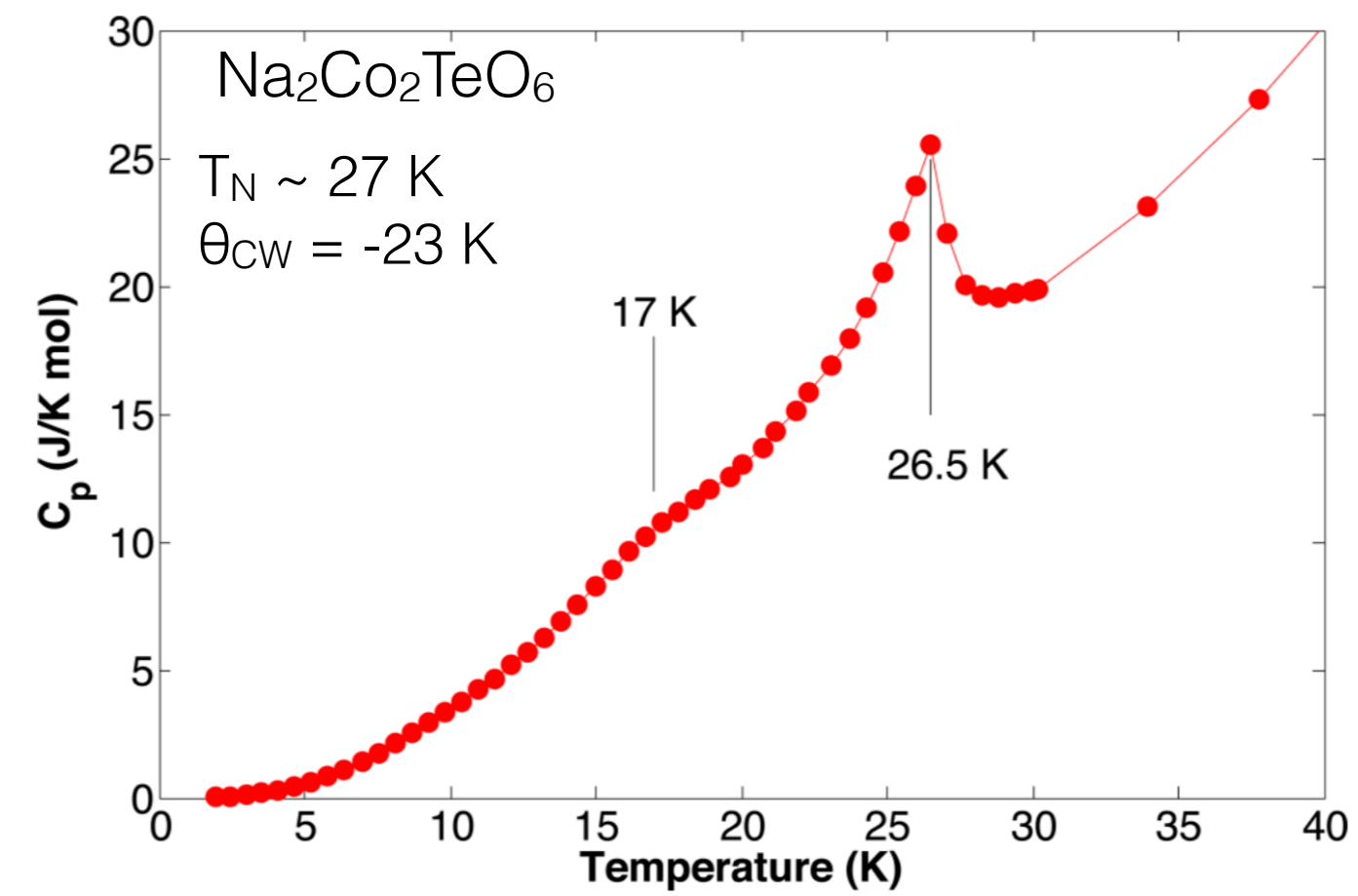
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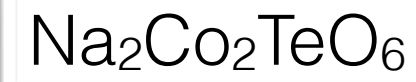
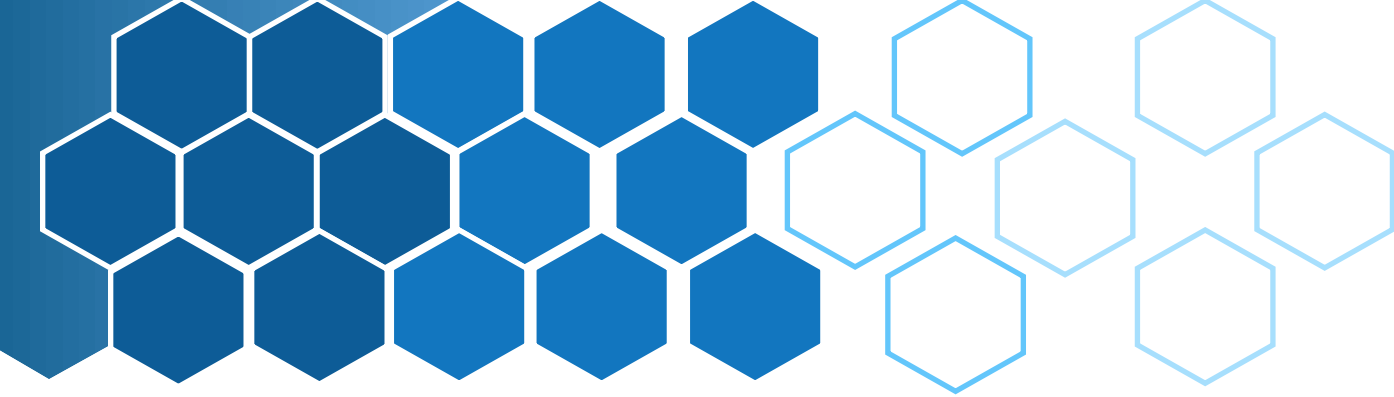
space group : $C2/m$ (monoclinic)



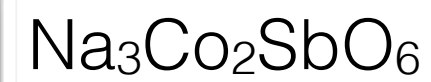
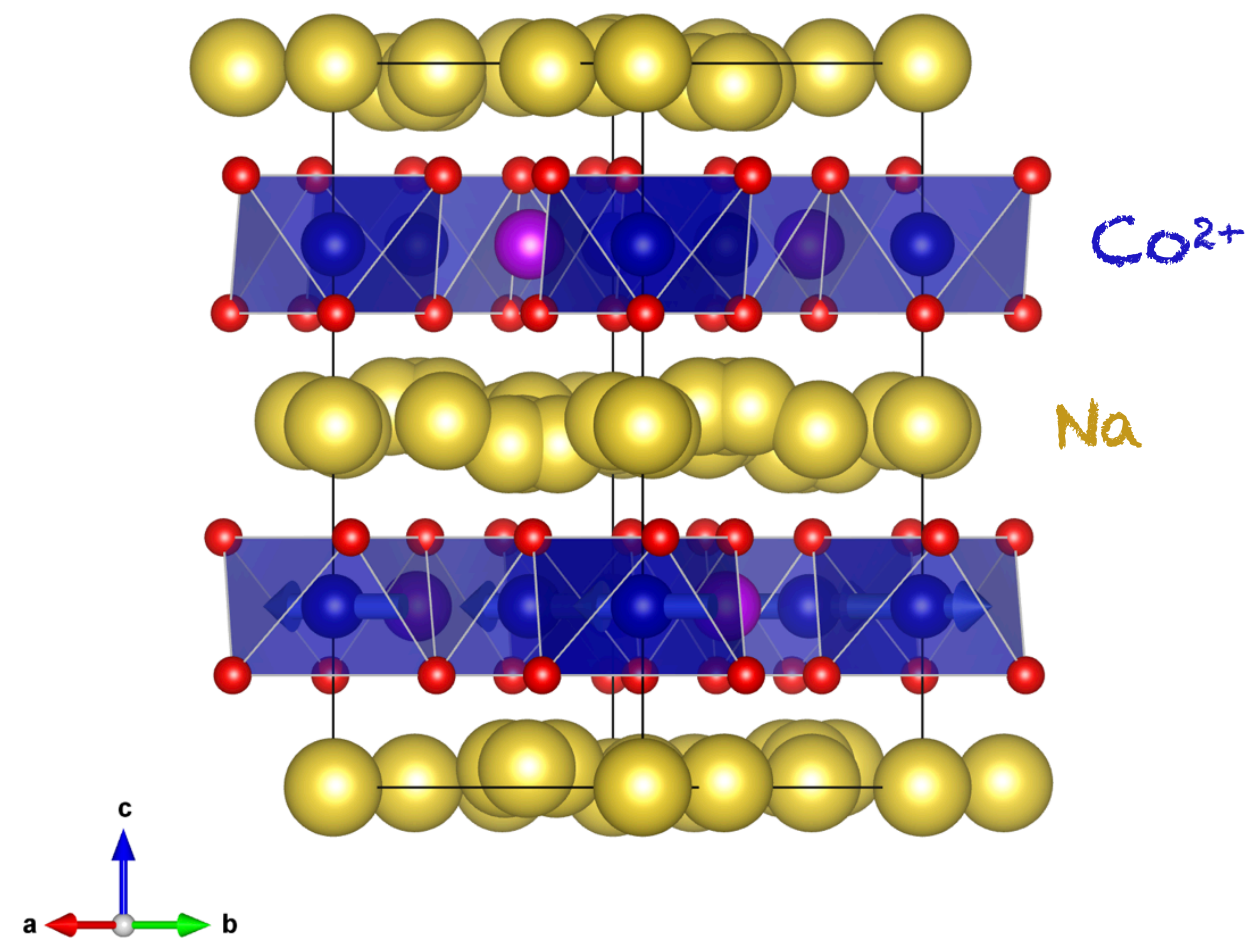
Magnetic properties



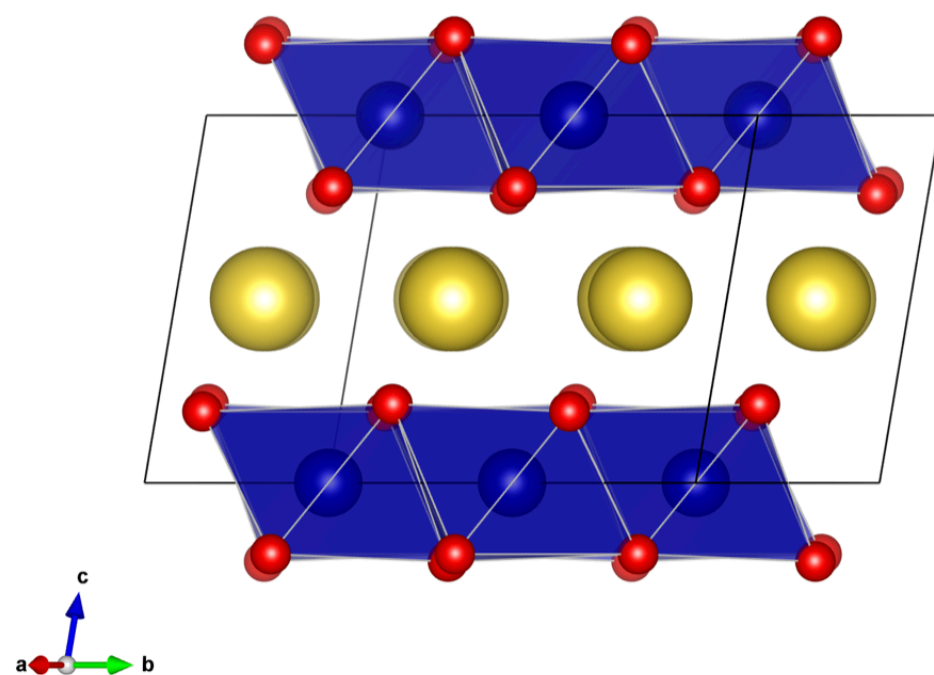
E. Lefrançois et al., Phys. Rev. B 94, 214416 (2016)
A. K. Bera et al., Phys. Rev. B 95, 094424 (2017)
C. Wong et al., J. Sol. State. Chem. 243 (2016)
J.-Q Yan et al., Phys. Rev. Mat. 3, 074405 (2019)



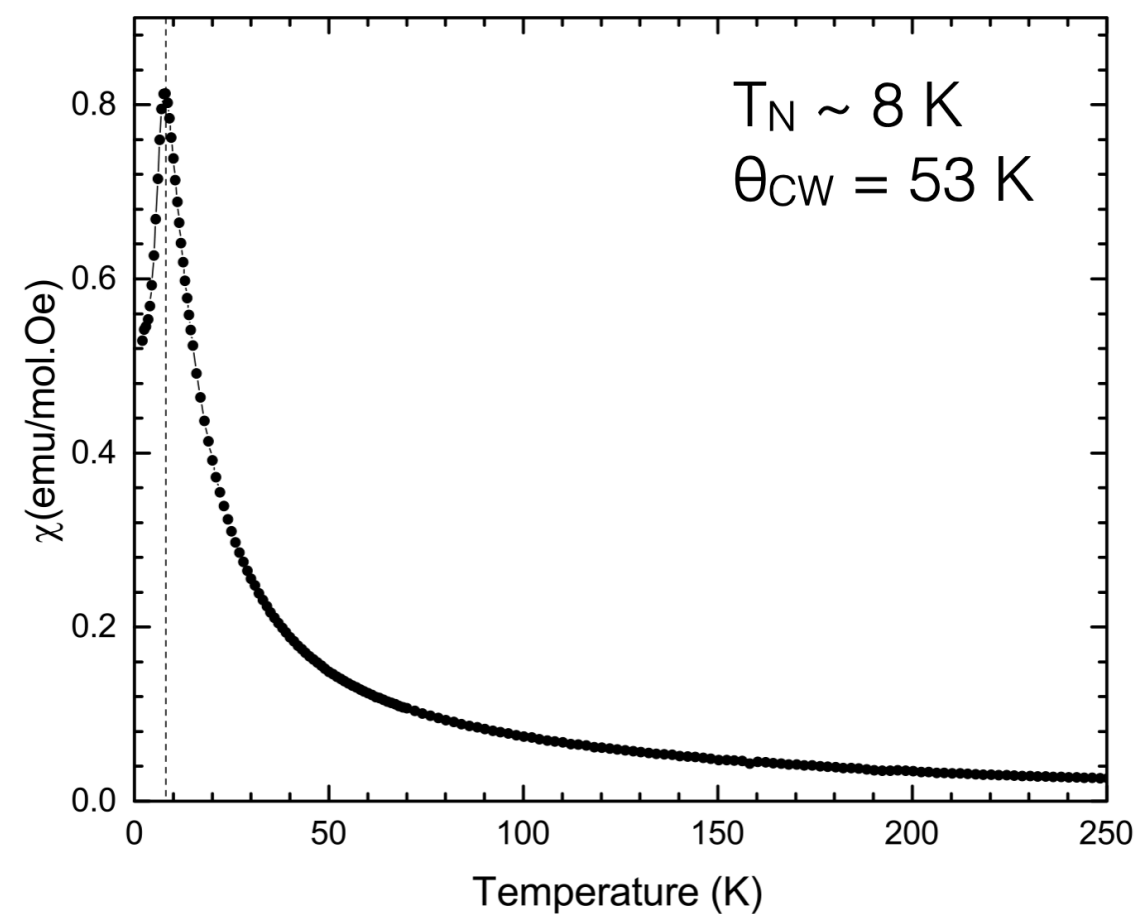
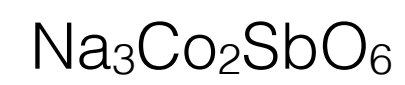
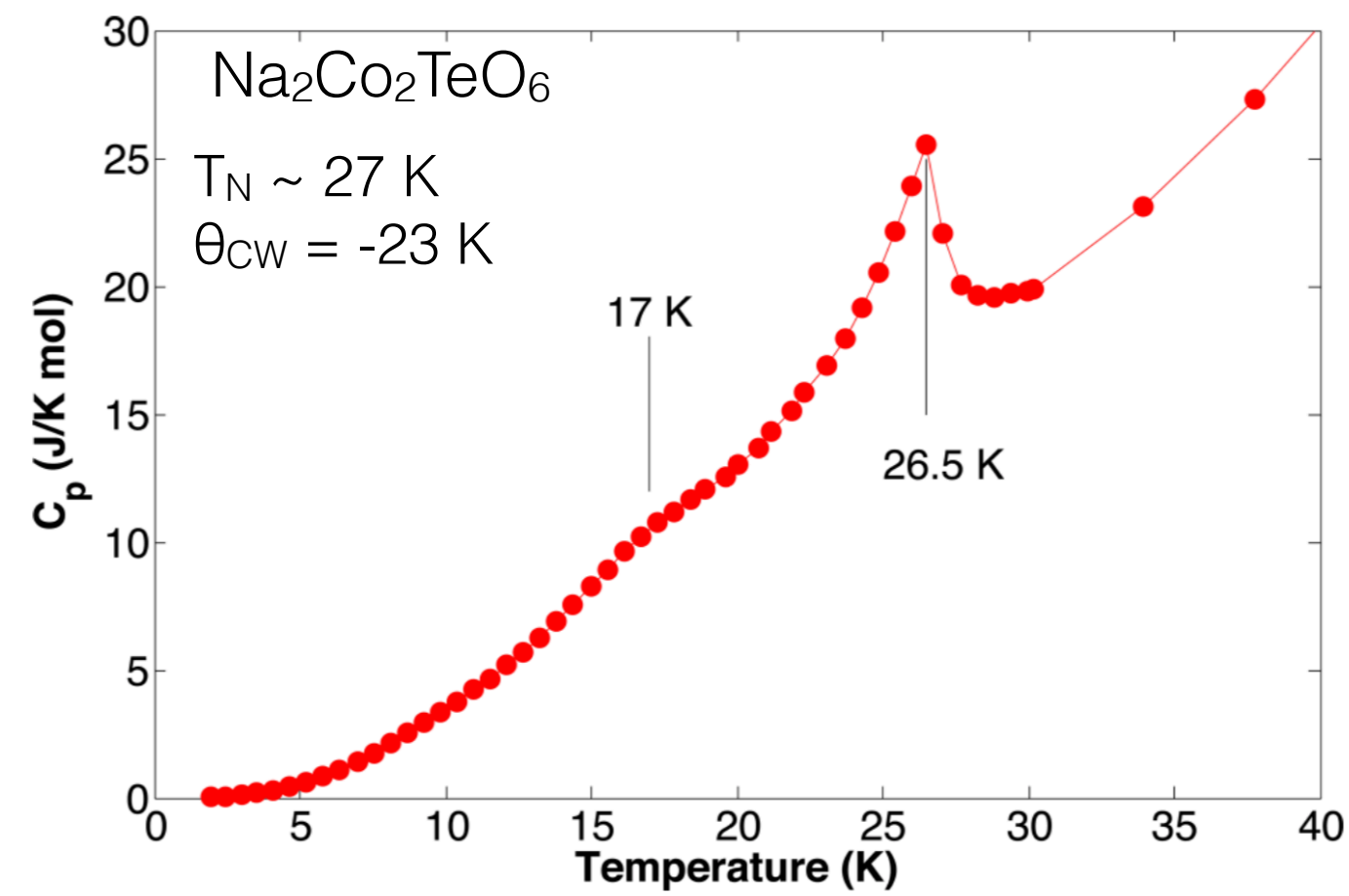
space group : $P6_322$ (hexagonal)



space group : $C2/m$ (monoclinic)

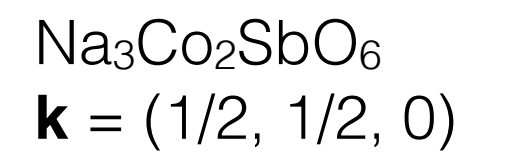
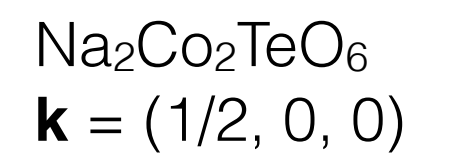
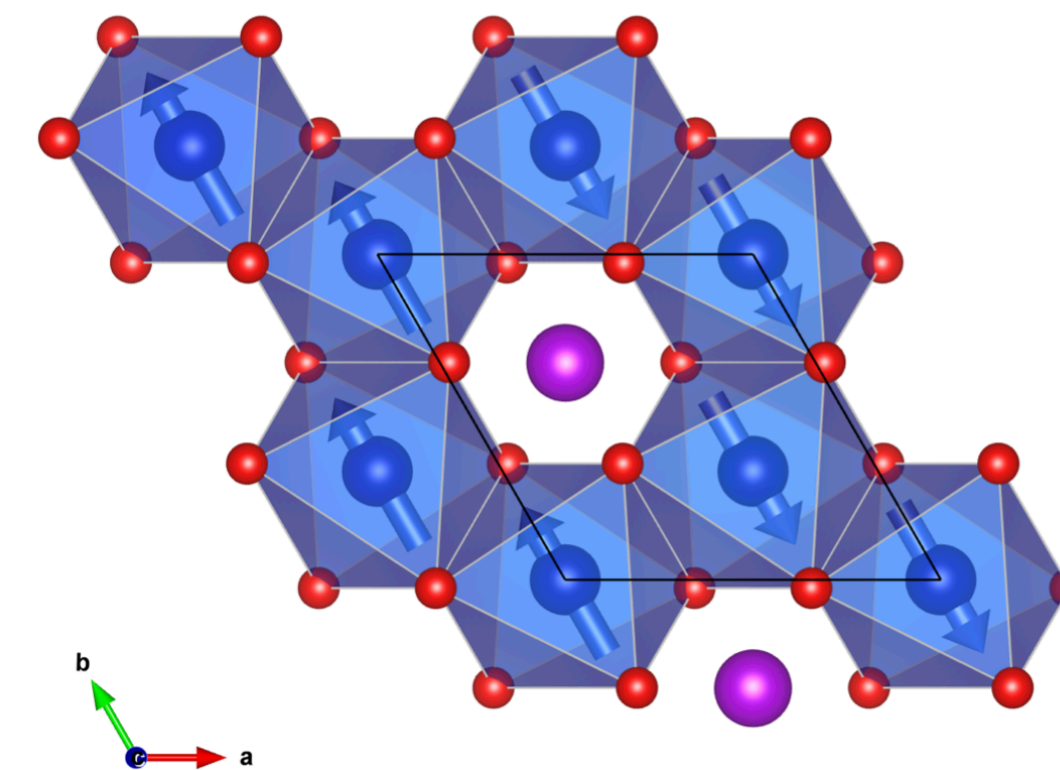


Magnetic properties



- ▶ Zigzag magnetic order at low temperature
- ▶ Anisotropic correlation lengths for $\text{Na}_2\text{Co}_2\text{TeO}_6$: short-range inter-plane correlations $J_{\text{int}}/J \sim 0.01$

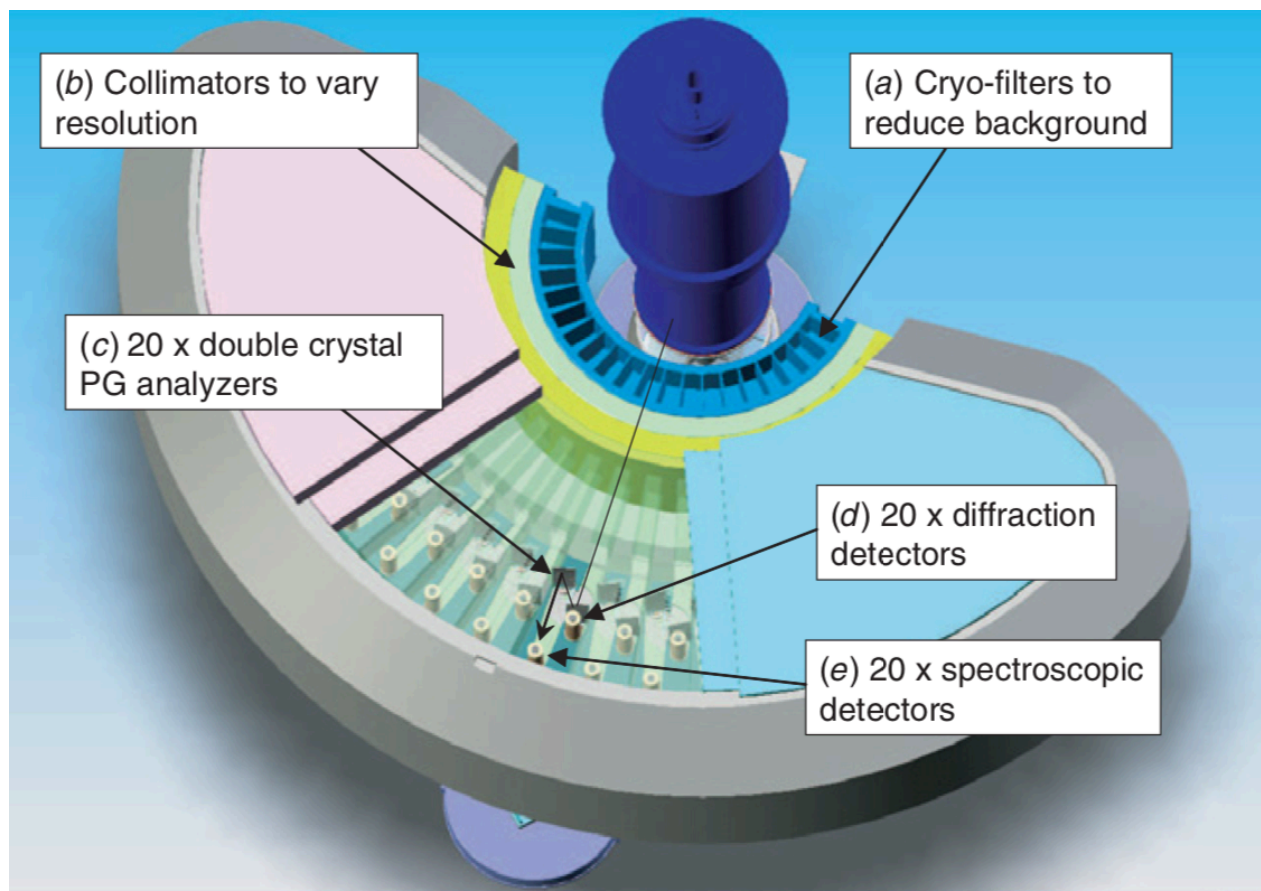
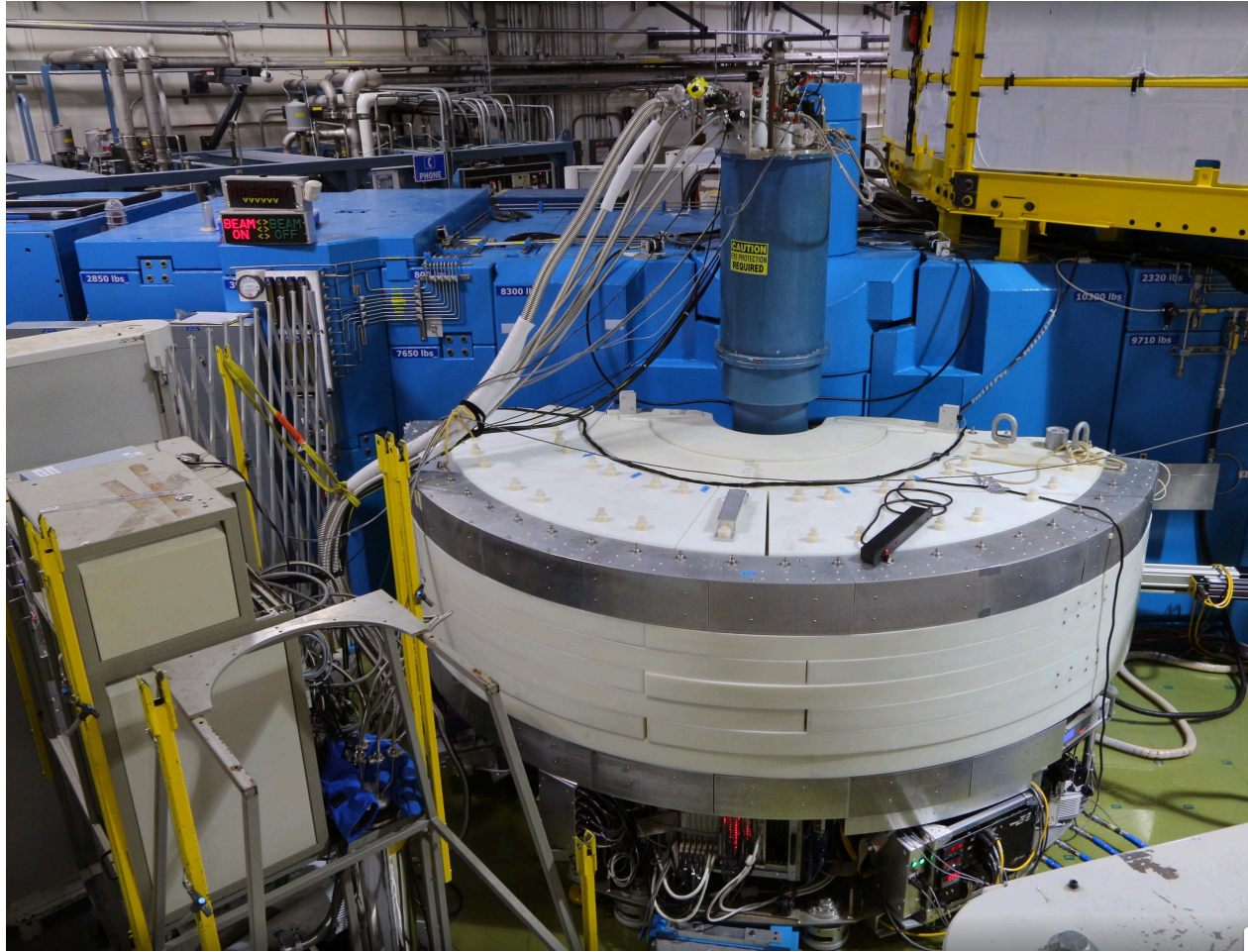
Magnetic structure determined by neutron powder diffraction (D1B, ILL - France)



E. Lefrançois et al., Phys. Rev. B 94, 214416 (2016)
A. K. Bera et al., Phys. Rev. B 95, 094424 (2017)
C. Wong et al., J. Sol. State. Chem. 243 (2016)
J.-Q Yan et al., Phys. Rev. Mat. 3, 074405 (2019)



MACS: Multi-Axis Crystal Spectrometer



Neutron scattering, an ideal tool for magnetic excitations:

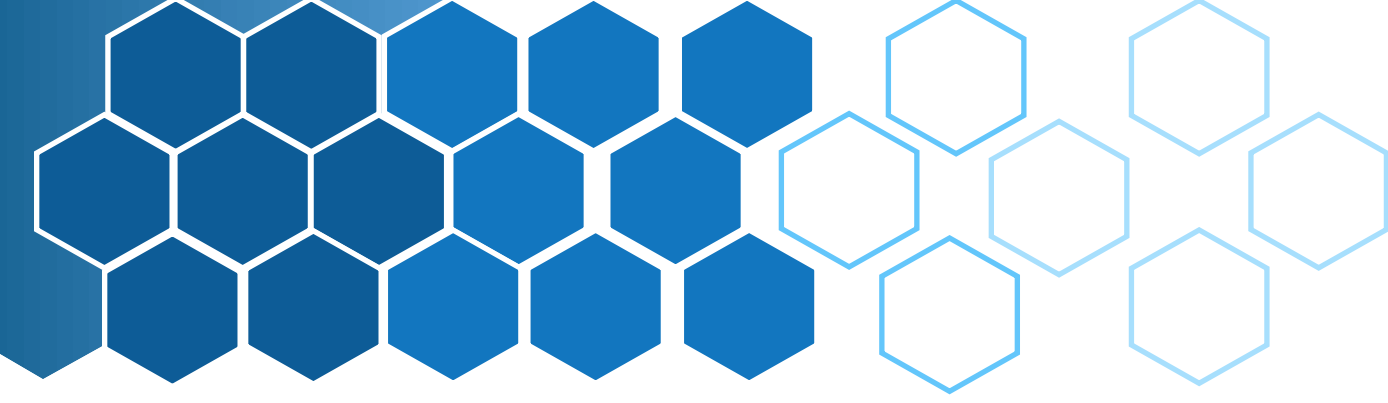
- ▶ No charge : probes the bulk and not the surface
- ▶ Interaction with matter : nuclear and magnetic contribution
- ▶ Energy of thermal neutrons : few meV
- ▶ Cross-section directly proportional to spin-spin correlation function
- ▶ Allows measurements throughout the reciprocal space

Momentum and energy conservation

$$\vec{Q} = \vec{k}_i - \vec{k}_f$$

$$E = \hbar\omega = E_i - E_f = \frac{\hbar^2}{2m}(k_i^2 - k_f^2)$$

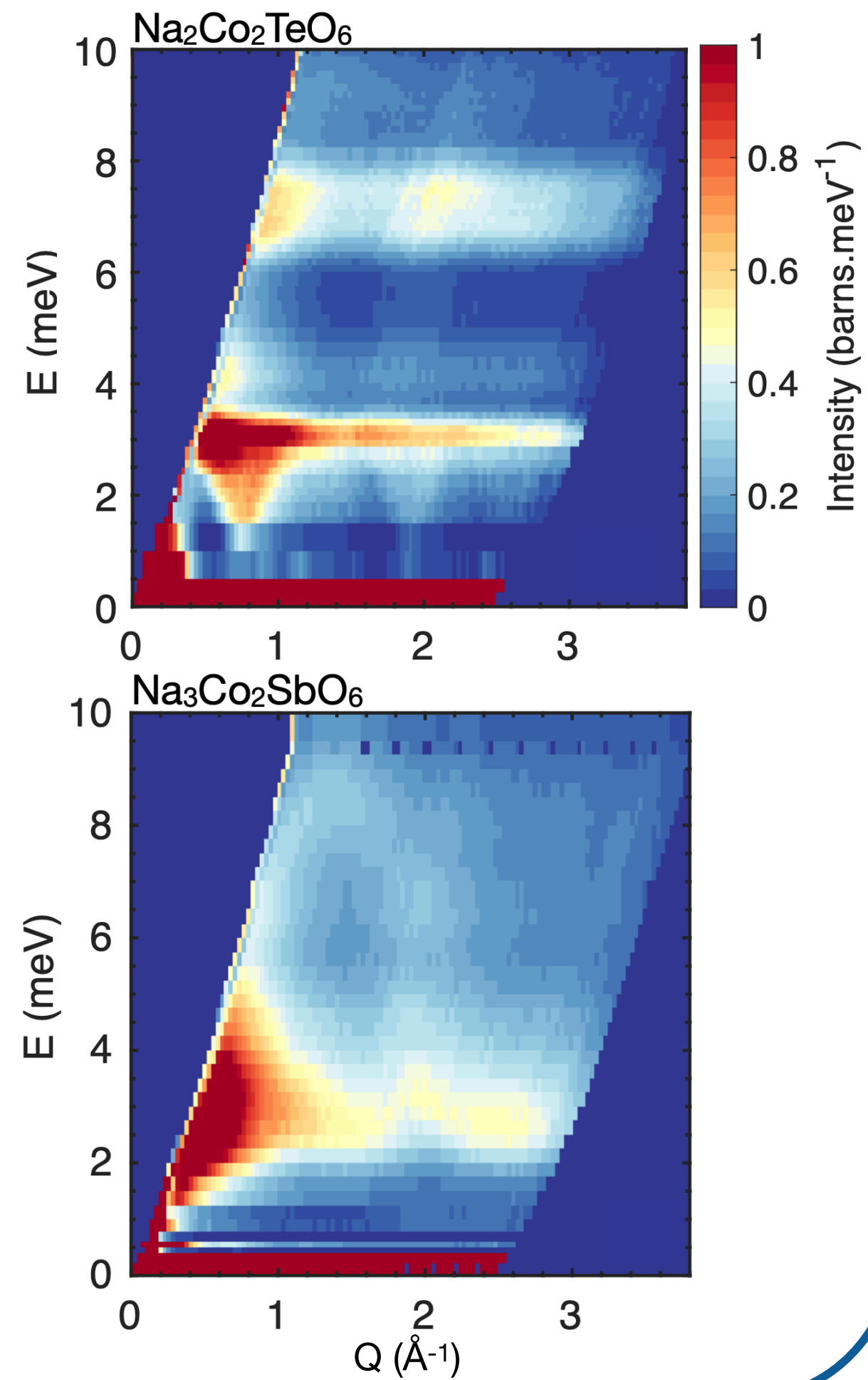
Neutron inelastic study (powder)



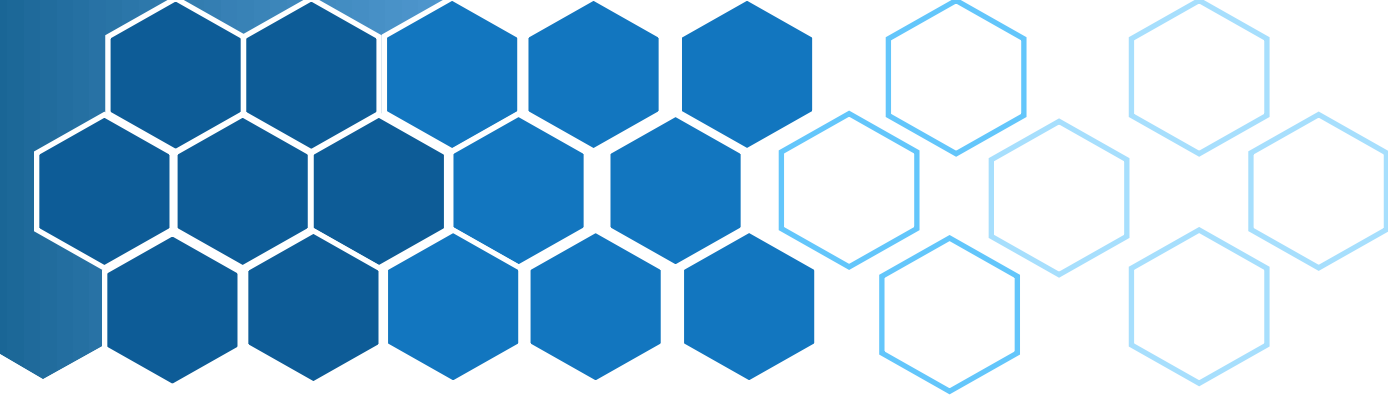
Low Energy:

- Excitations within the $j_{\text{eff}} = 1/2$ manifolds : exchange interactions

MACS (NIST), $E_f = 5 \text{ meV}$
 $T = 1.5 \text{ K}$



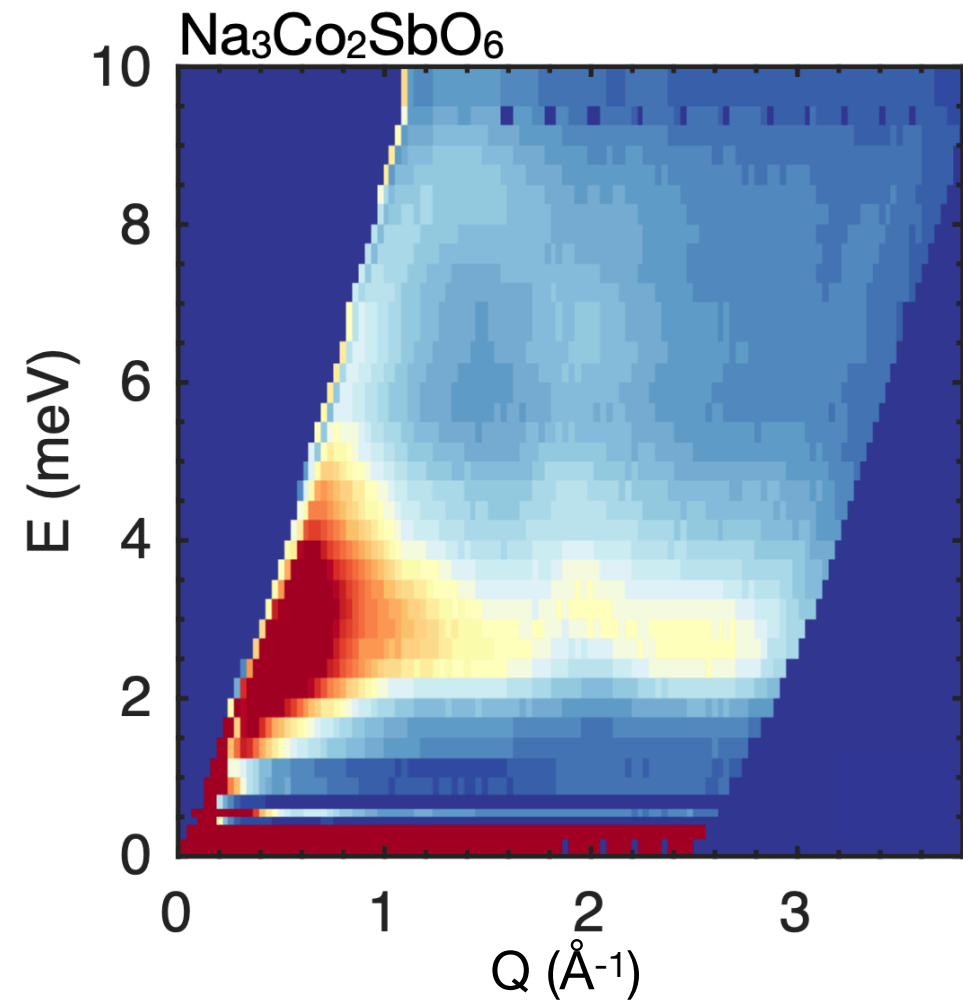
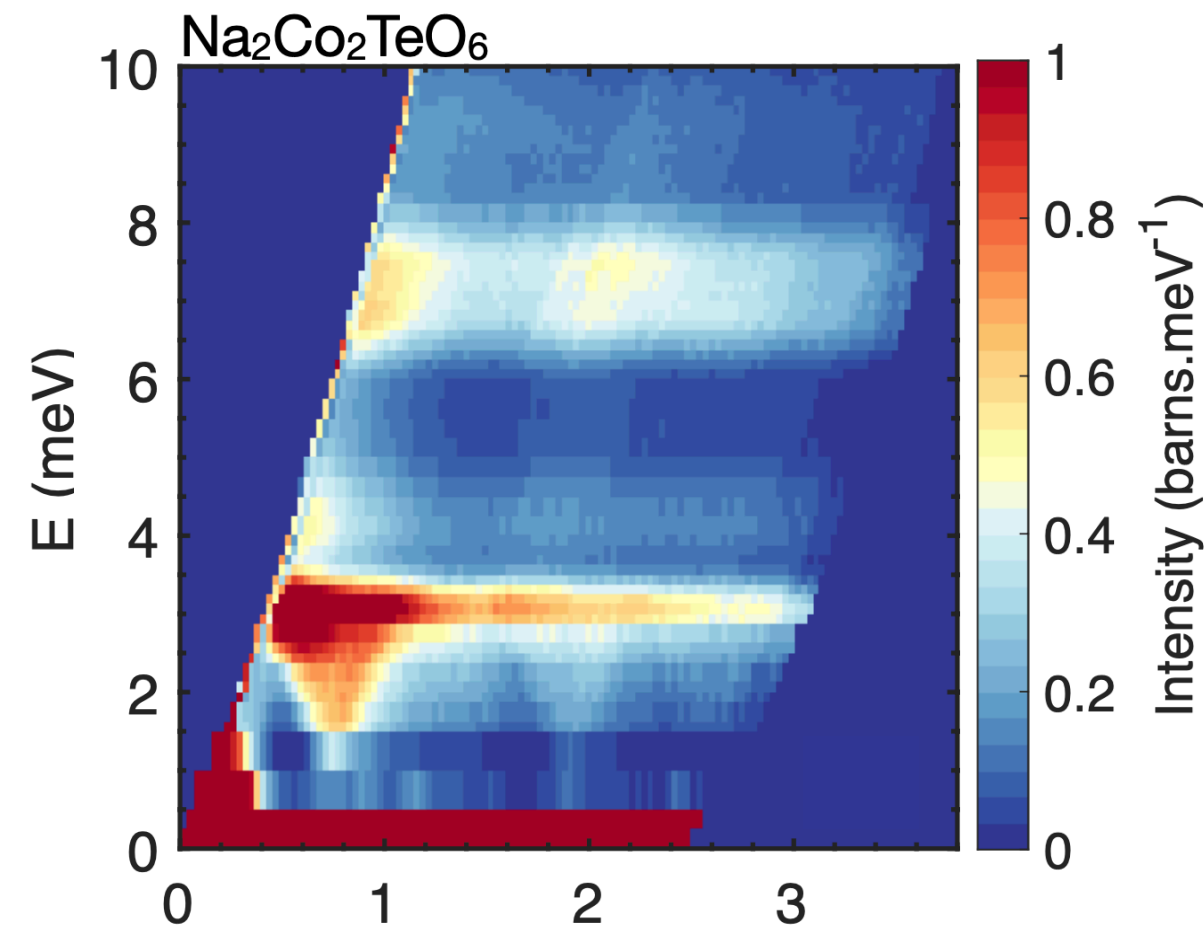
Testing the spin model : spin wave calculations



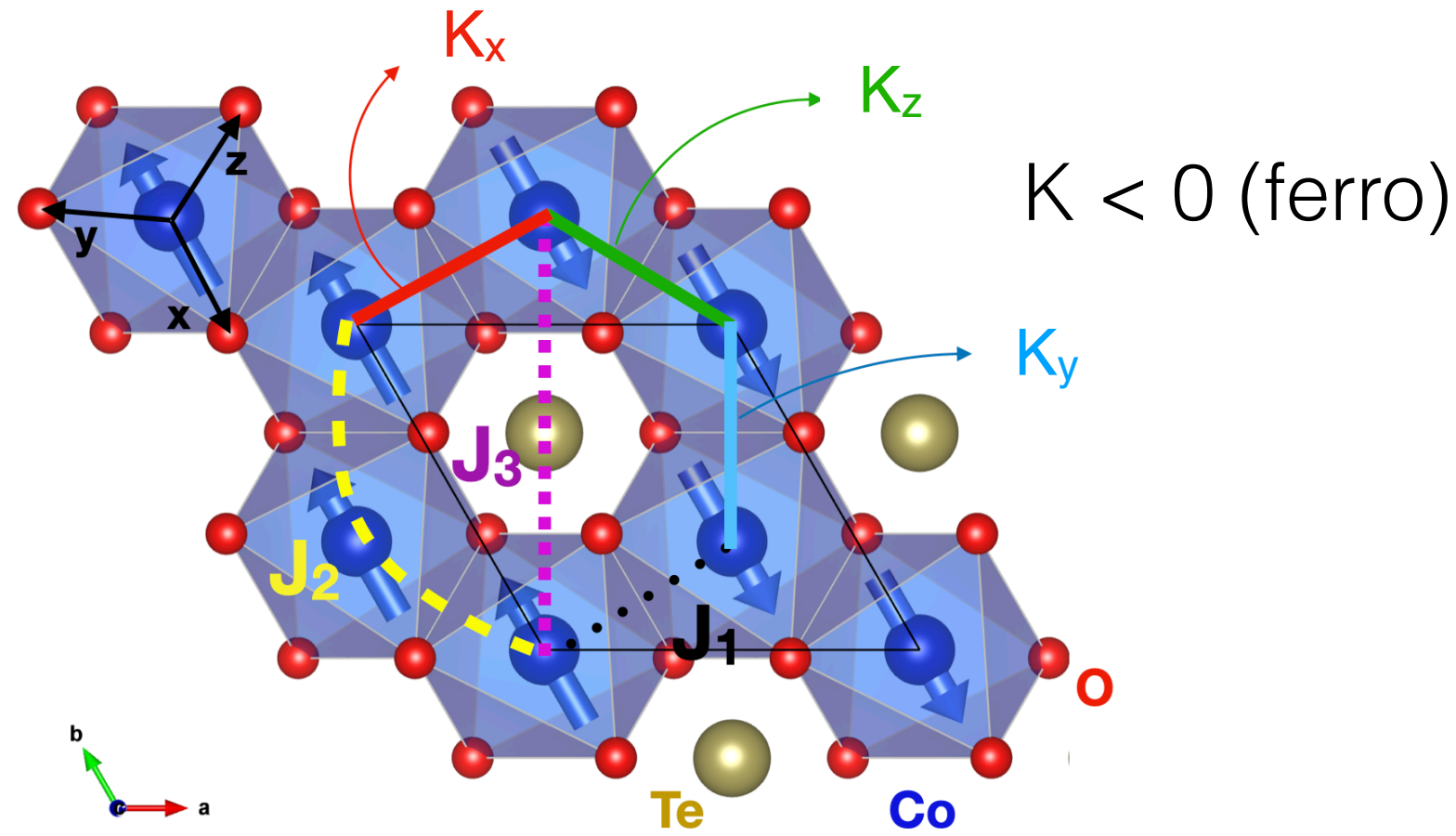
Low Energy:

- Excitations within the $j_{\text{eff}} = 1/2$ manifolds : exchange interactions

MACS (NIST), $E_f = 5 \text{ meV}$
 $T = 1.5 \text{ K}$



Spin Hamiltonian : Kitaev-Heisenberg model



$$H_{K-H} = \sum_{n=1}^3 J_n \sum_{i,j} \mathbf{S}_i \cdot \mathbf{S}_j + \sum_{i,j} K S_i^\gamma S_j^\gamma$$

$$+ \sum_{i,j} \Gamma (S_i^\alpha S_j^\beta + S_i^\beta S_j^\alpha)$$

$$+ \sum_{i,j} \Gamma' (S_i^\alpha S_j^\gamma + S_i^\gamma S_j^\alpha + S_i^\beta S_j^\gamma + S_i^\gamma S_j^\beta),$$

$$\{\alpha, \beta, \gamma\} = \{y, z, x\}, \{z, x, y\}, \{x, y, z\}$$

H. Liu et al., Phys. Rev. Letters 125, 047201 (2020)

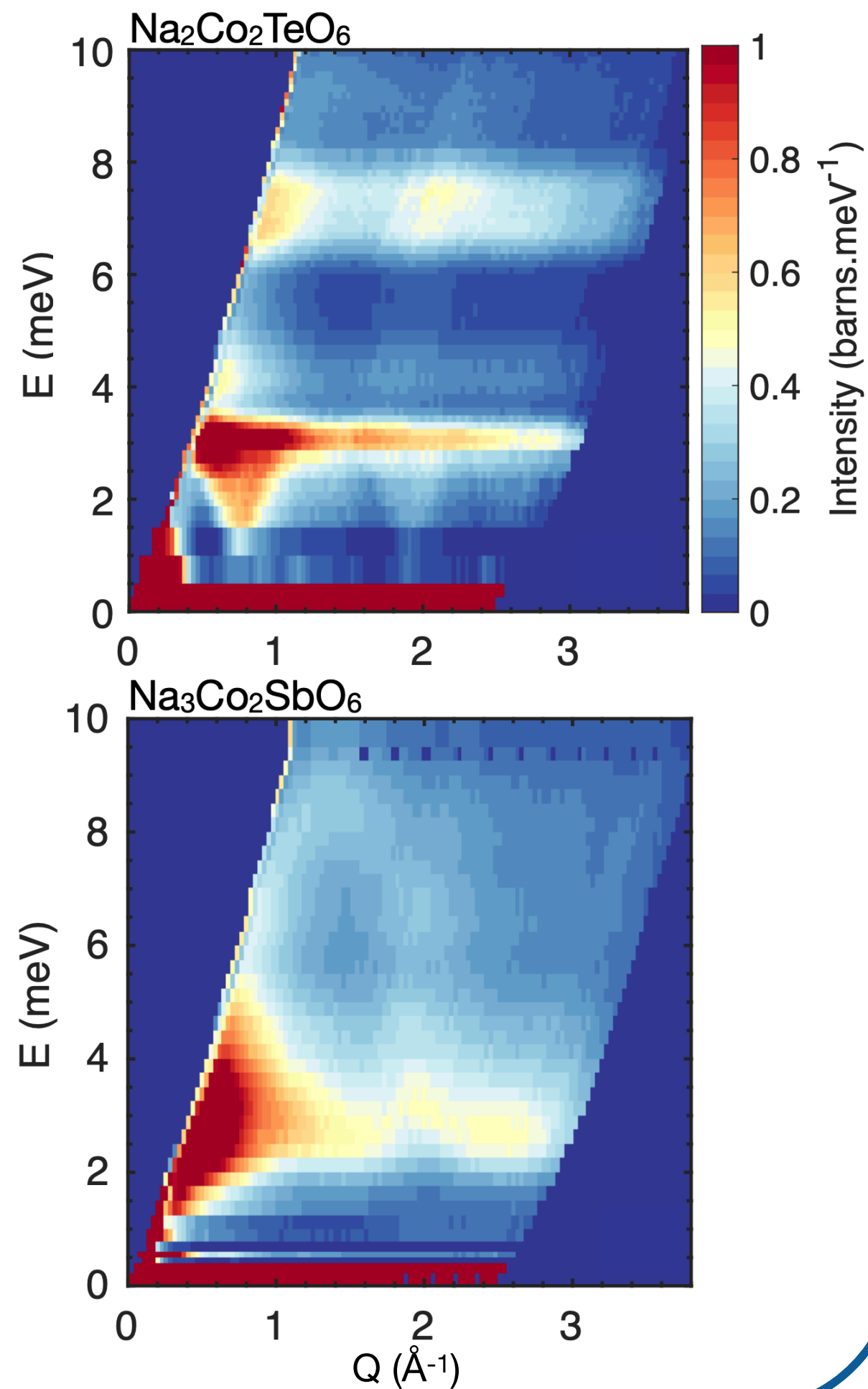
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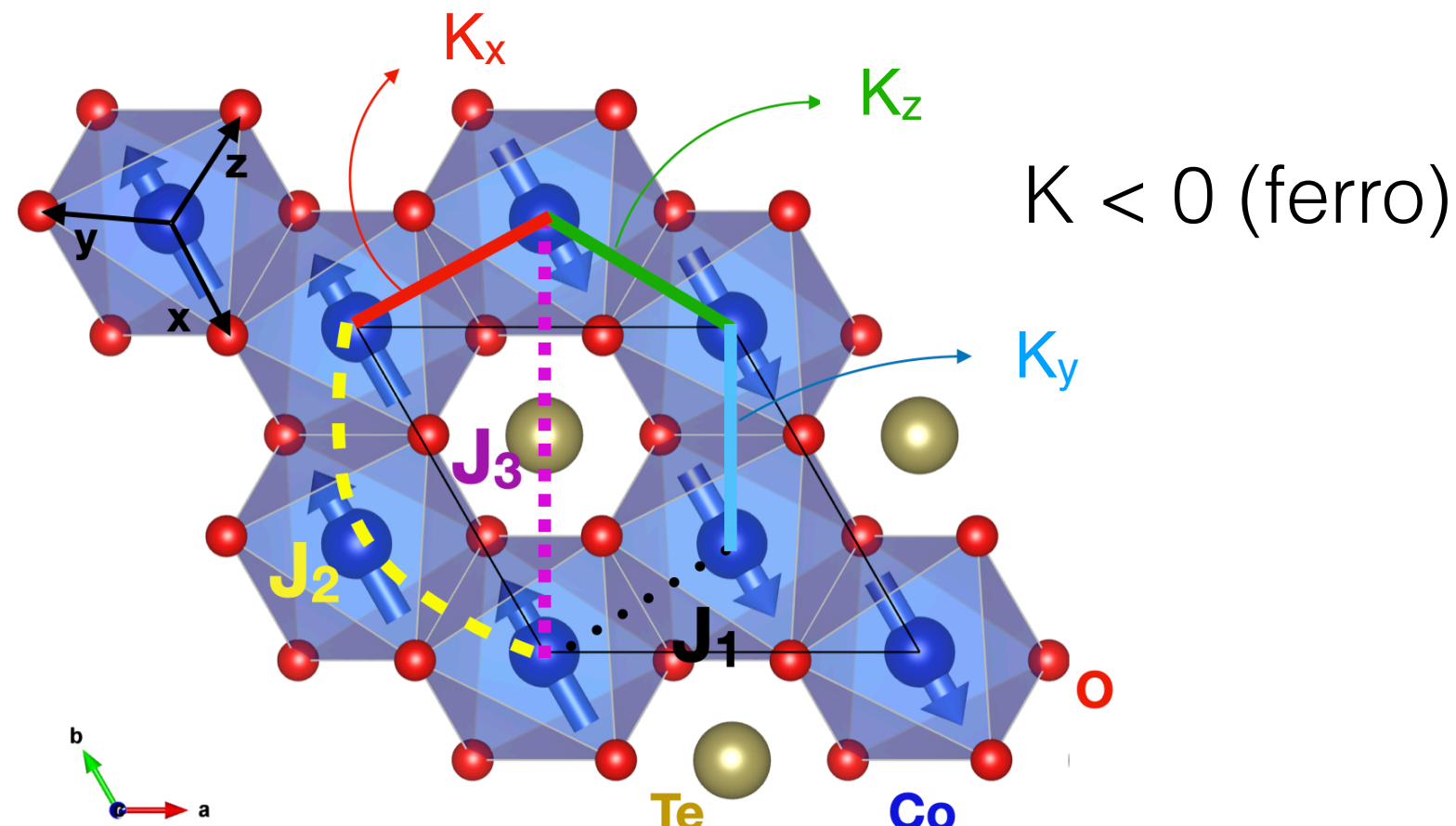
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Spin Hamiltonian : Kitaev-Heisenberg model

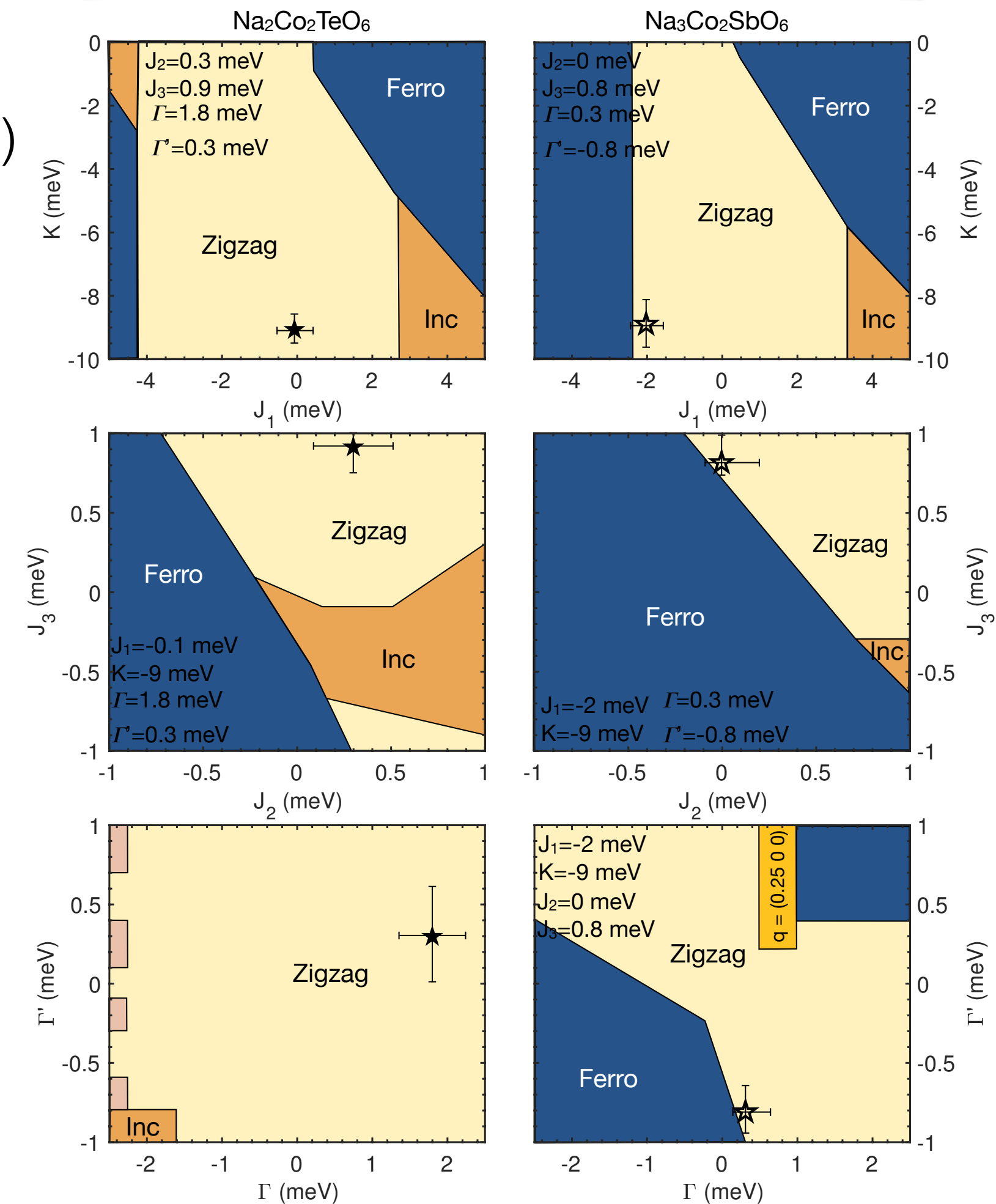


$$H_{K-H} = \sum_{n=1}^3 J_n \sum_{i,j} \mathbf{S}_i \cdot \mathbf{S}_j + \sum_{i,j} K S_i^\gamma S_j^\gamma + \sum_{i,j} \Gamma (S_i^\alpha S_j^\beta + S_i^\beta S_j^\alpha) + \sum_{i,j} \Gamma' (S_i^\alpha S_j^\gamma + S_i^\gamma S_j^\alpha + S_i^\beta S_j^\gamma + S_i^\gamma S_j^\beta),$$

$$\{\alpha, \beta, \gamma\} = \{y, z, x\}, \{z, x, y\}, \{x, y, z\}$$

H. Liu et al., Phys. Rev. Letters 125, 047201 (2020)

Phase diagram as function of exchange parameters



Testing the spin model : spin wave calculations

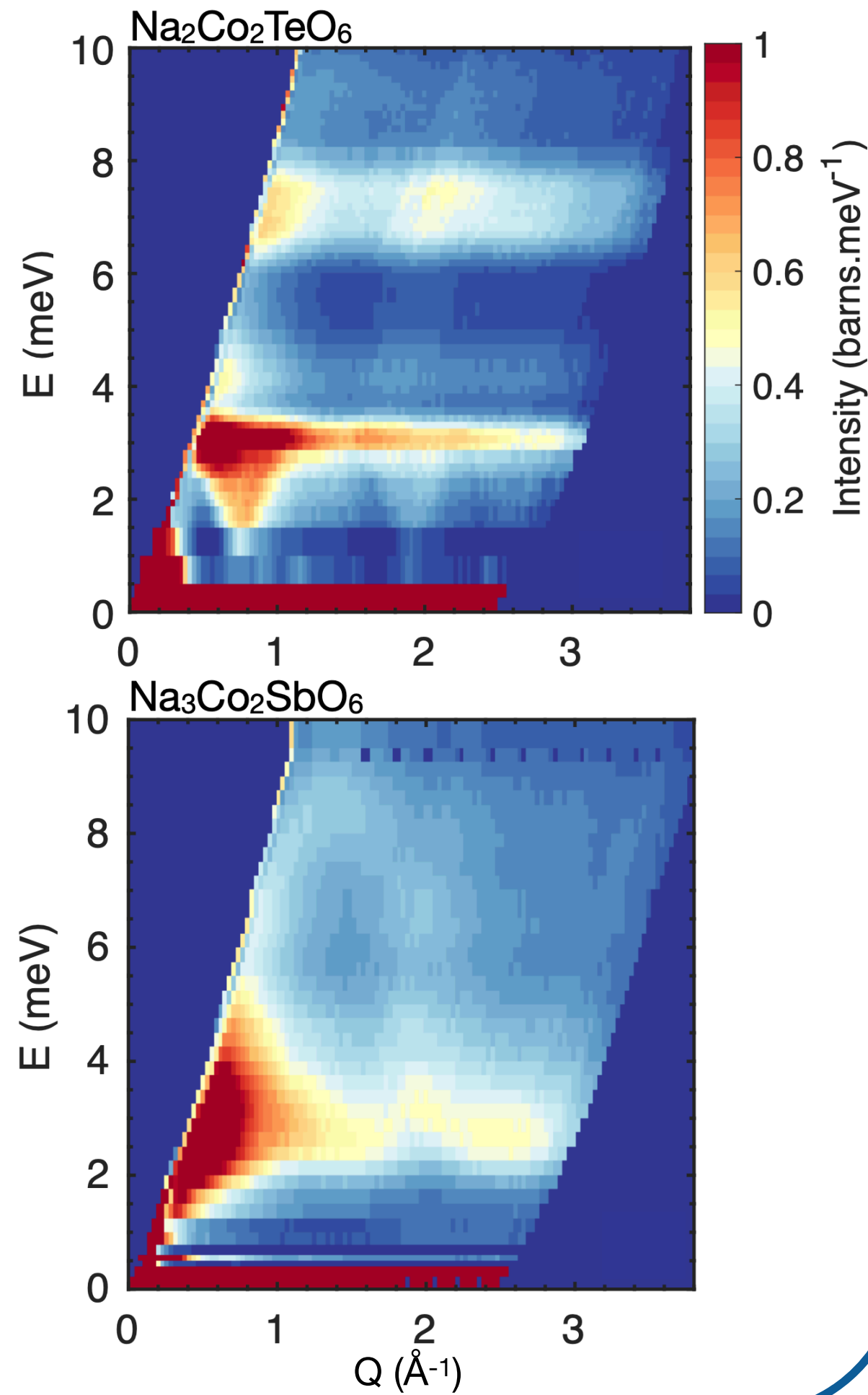


Low Energy:

Excitations within the $j_{\text{eff}} = 1/2$ manifolds : exchange interactions

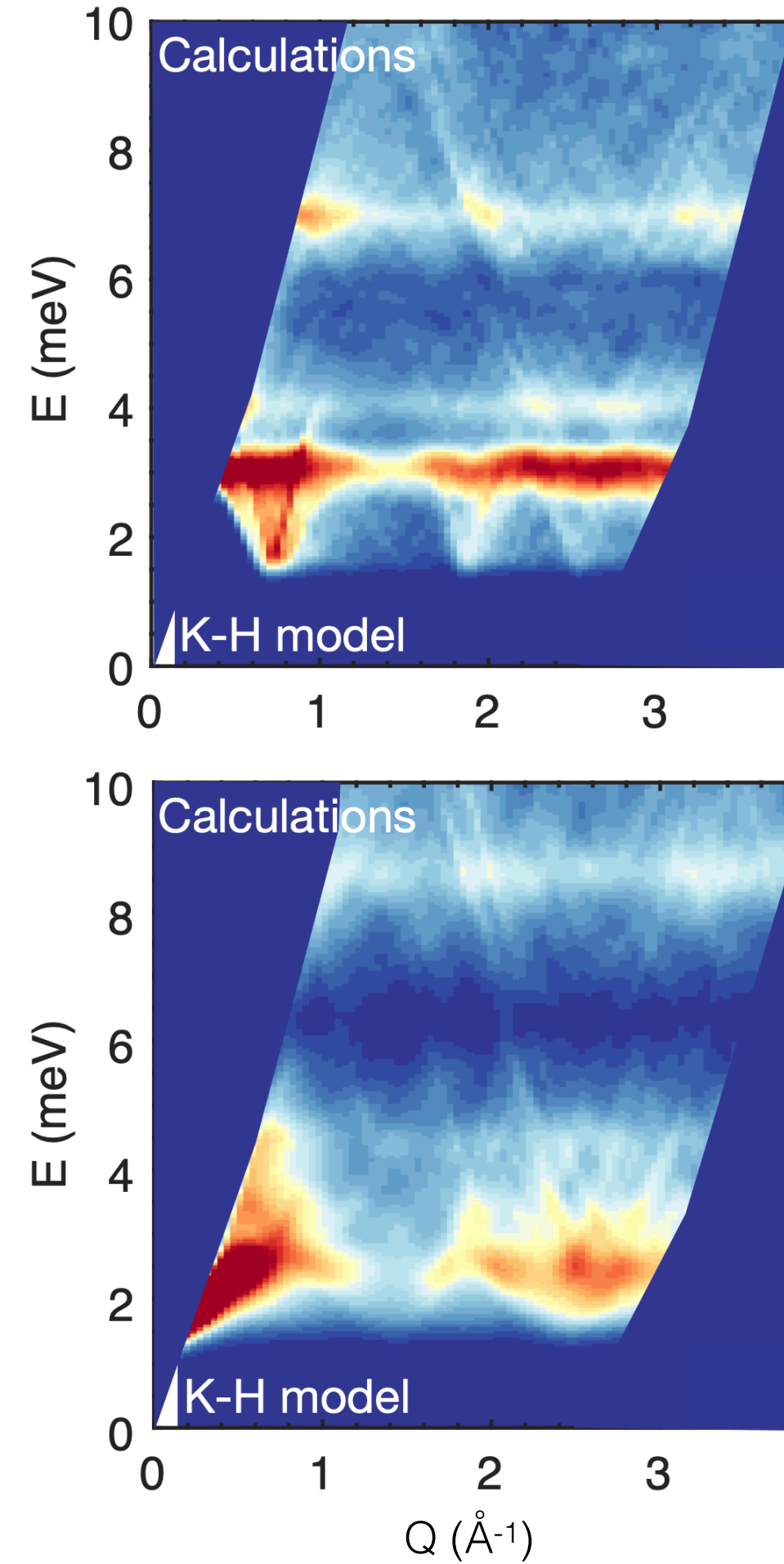
MACS, $E_f = 5 \text{ meV}$
 $T = 1.5 \text{ K}$

NIST
National Institute of
Standards and Technology

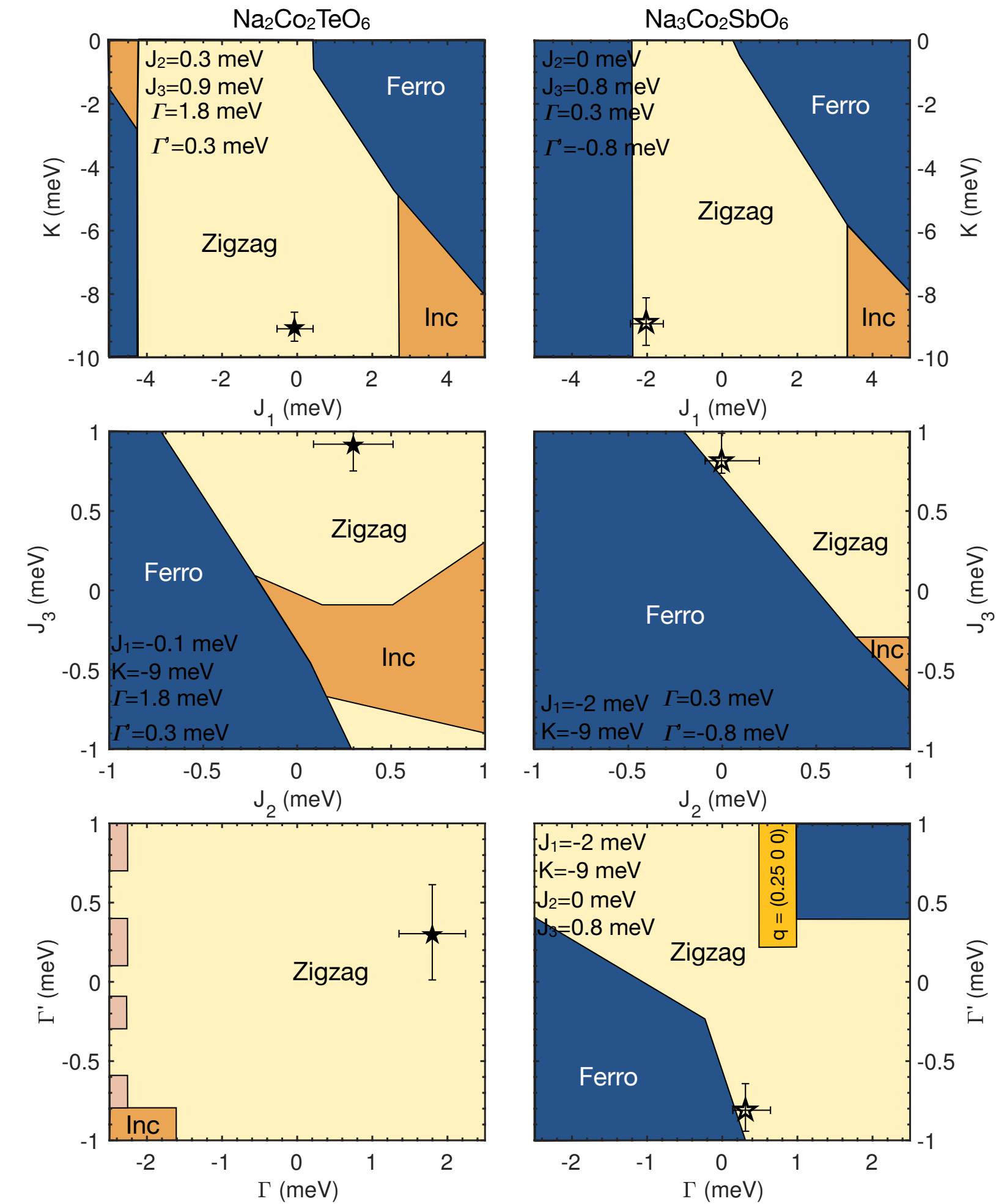


Spin wave calculations

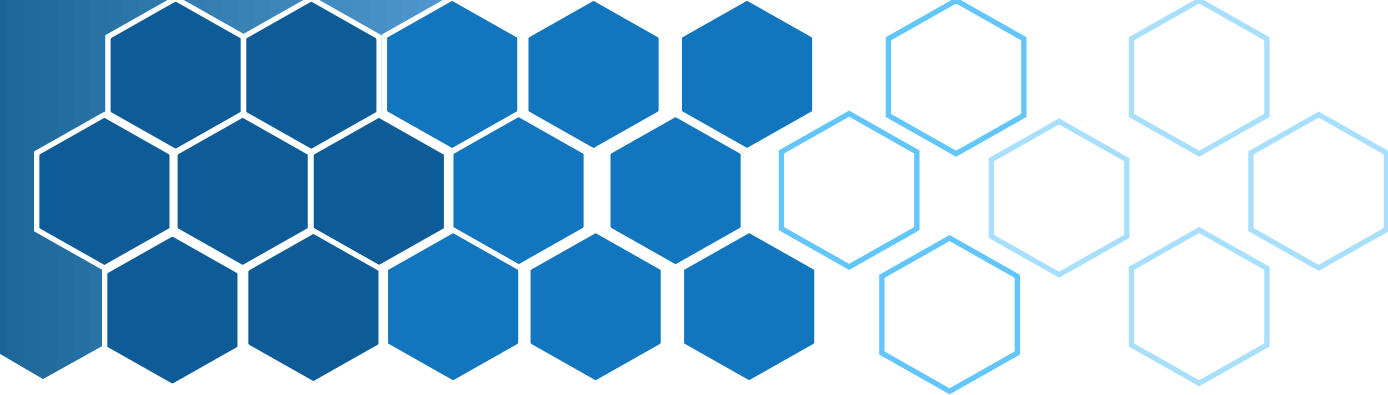
Spinwave software
S. Petit, Collection SFN 12, 105 (2011)



	J_1	J_2	J_3	K	Γ	Γ'
$\text{Na}_2\text{Co}_2\text{TeO}_6$	-0.1(5)	0.3(3)	0.9(3)	-9.0(5)	1.8(5)	0.3(3)
$\text{Na}_3\text{Co}_2\text{SbO}_6$	-2.0(5)	0.0(2)	0.8(2)	-9.0(10)	0.3(3)	-0.8(2)



Testing the spin model : spin wave calculations

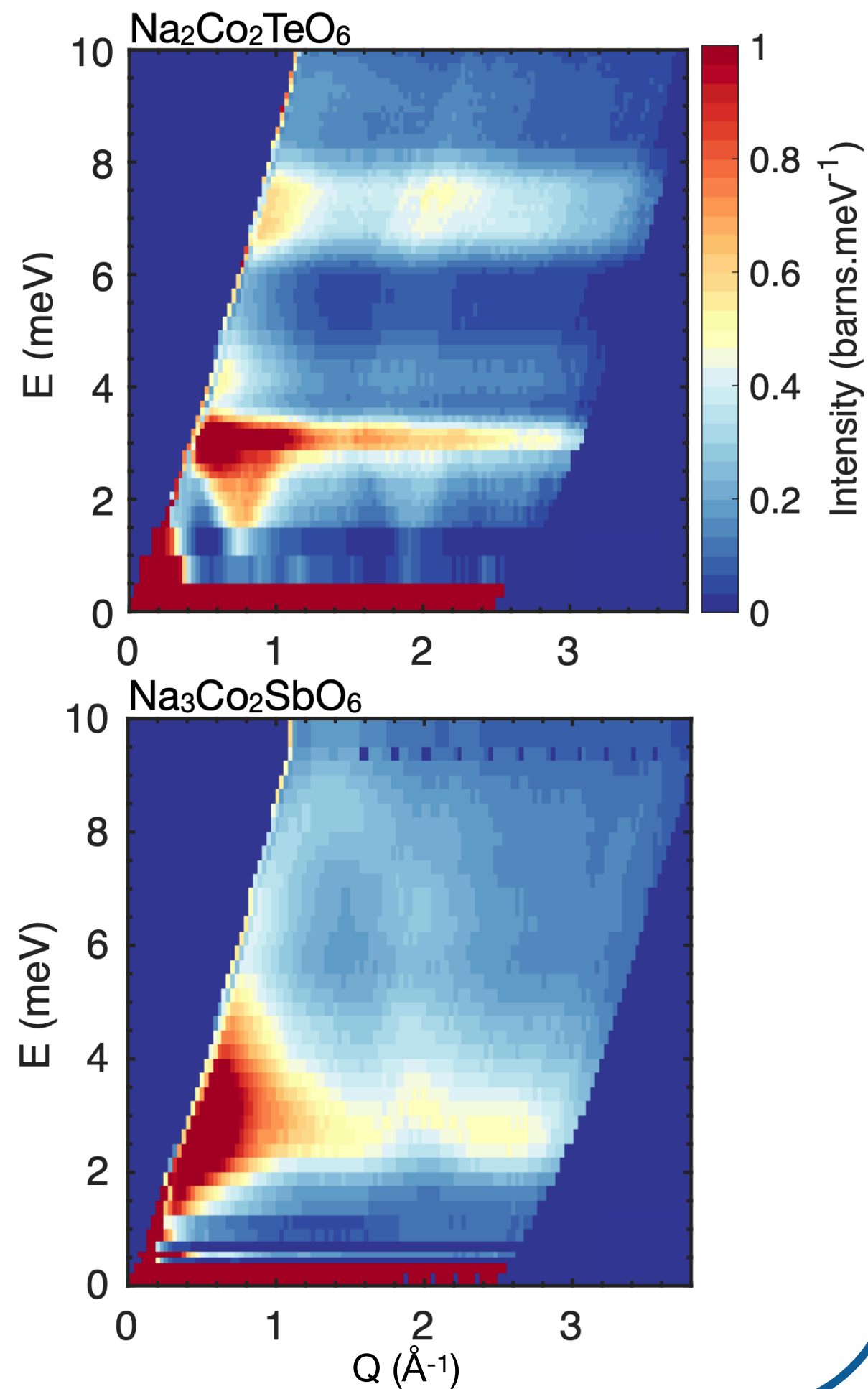


Low Energy:

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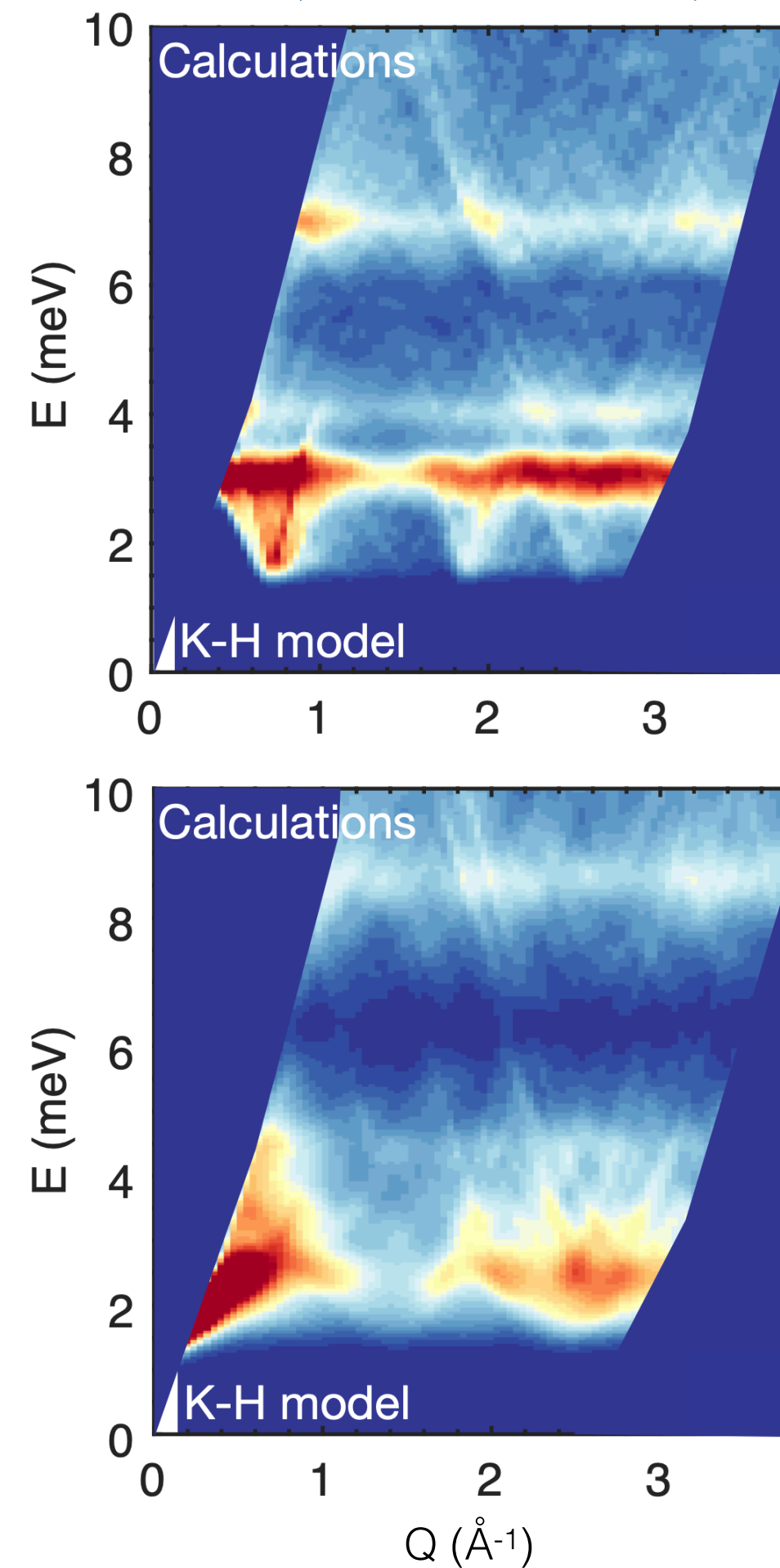
MACS, $E_f = 5 \text{ meV}$
 $T = 1.5 \text{ K}$

NIST
National Institute of
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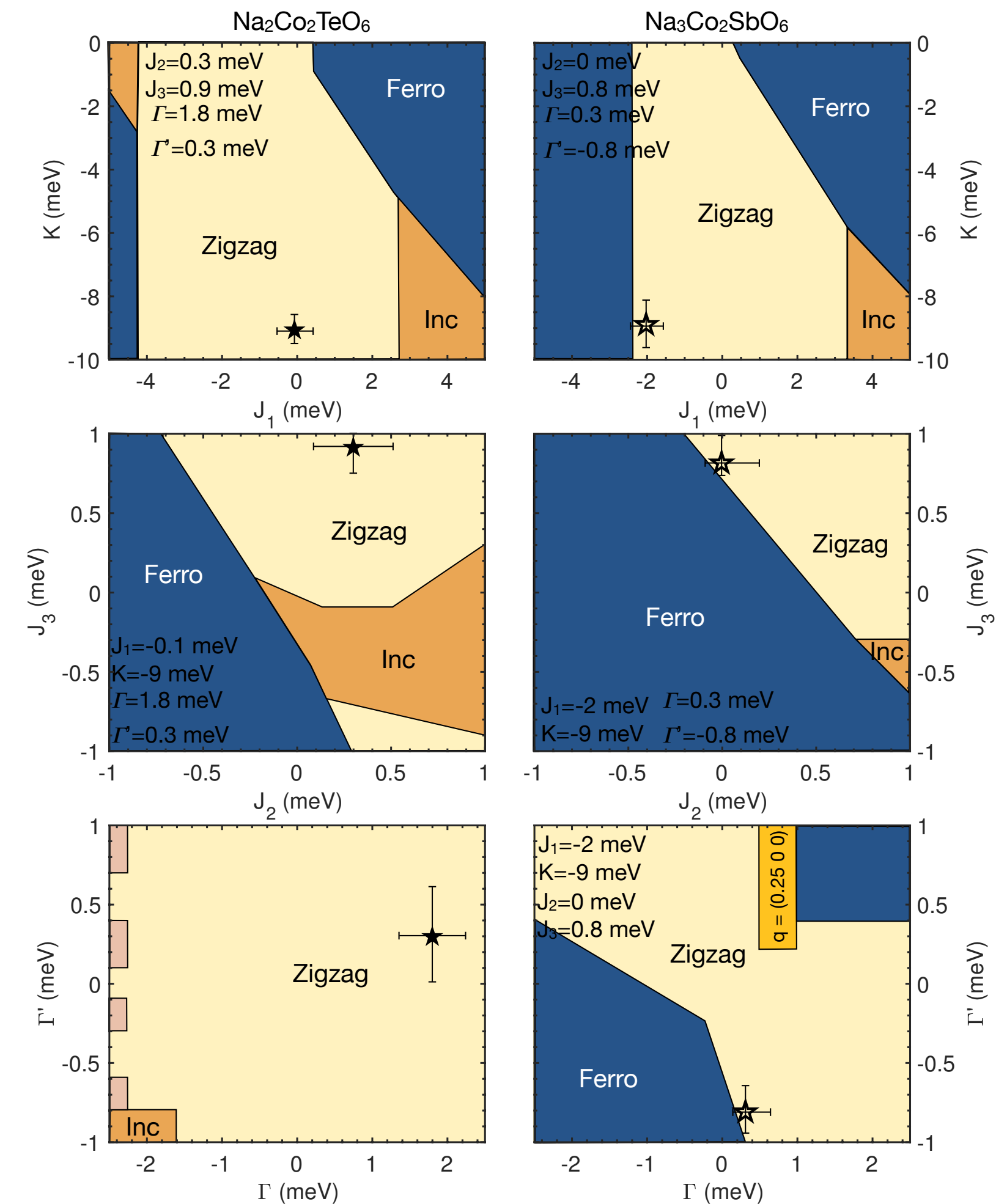


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Spinwave software
S. Petit, Collection SFN 12, 105 (2011)



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Comparison with theory: $\text{Na}_3\text{Co}_2\text{SbO}_6$

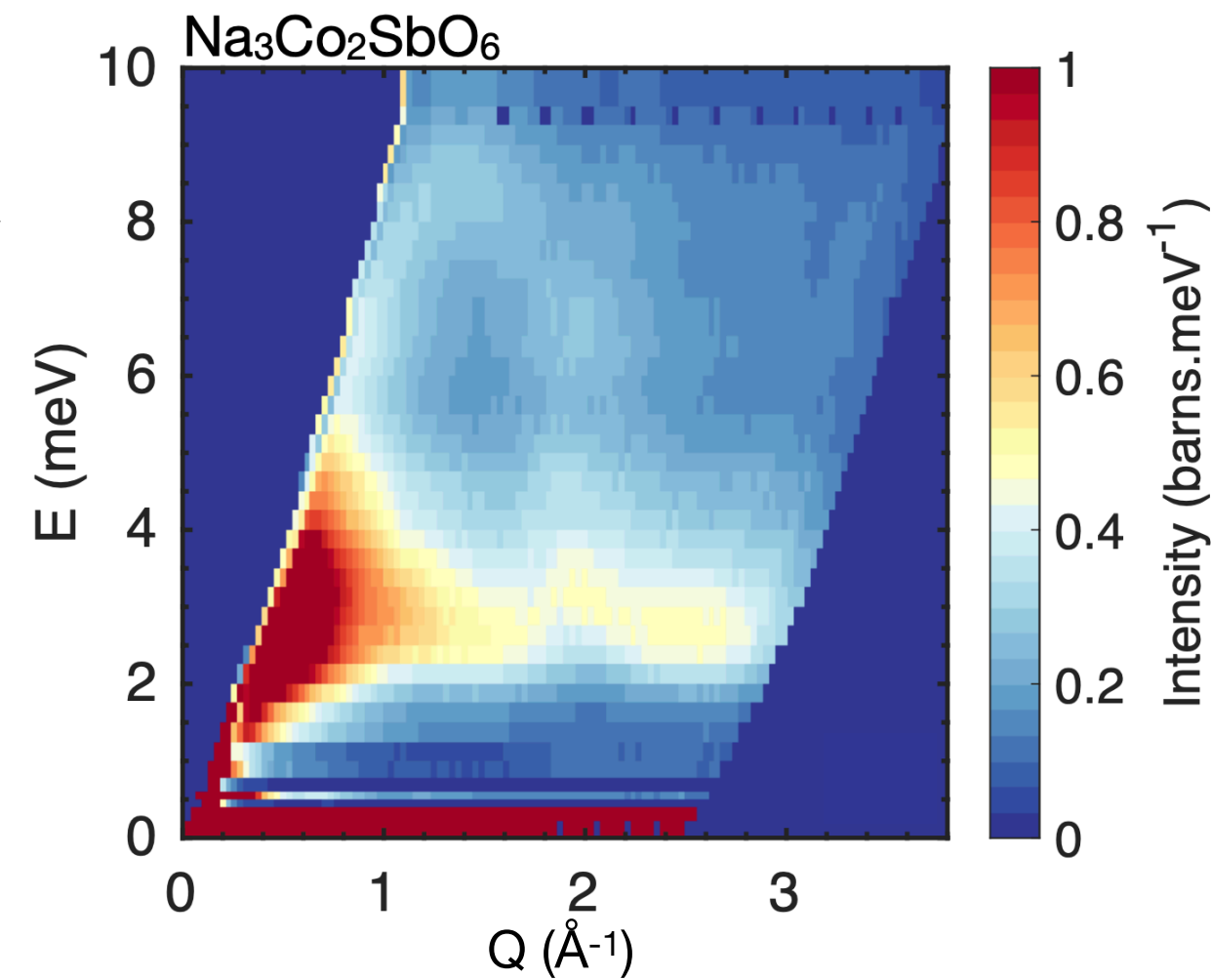


Low Energy:

Excitations within the $j_{\text{eff}} = 1/2$ manifolds : exchange interactions

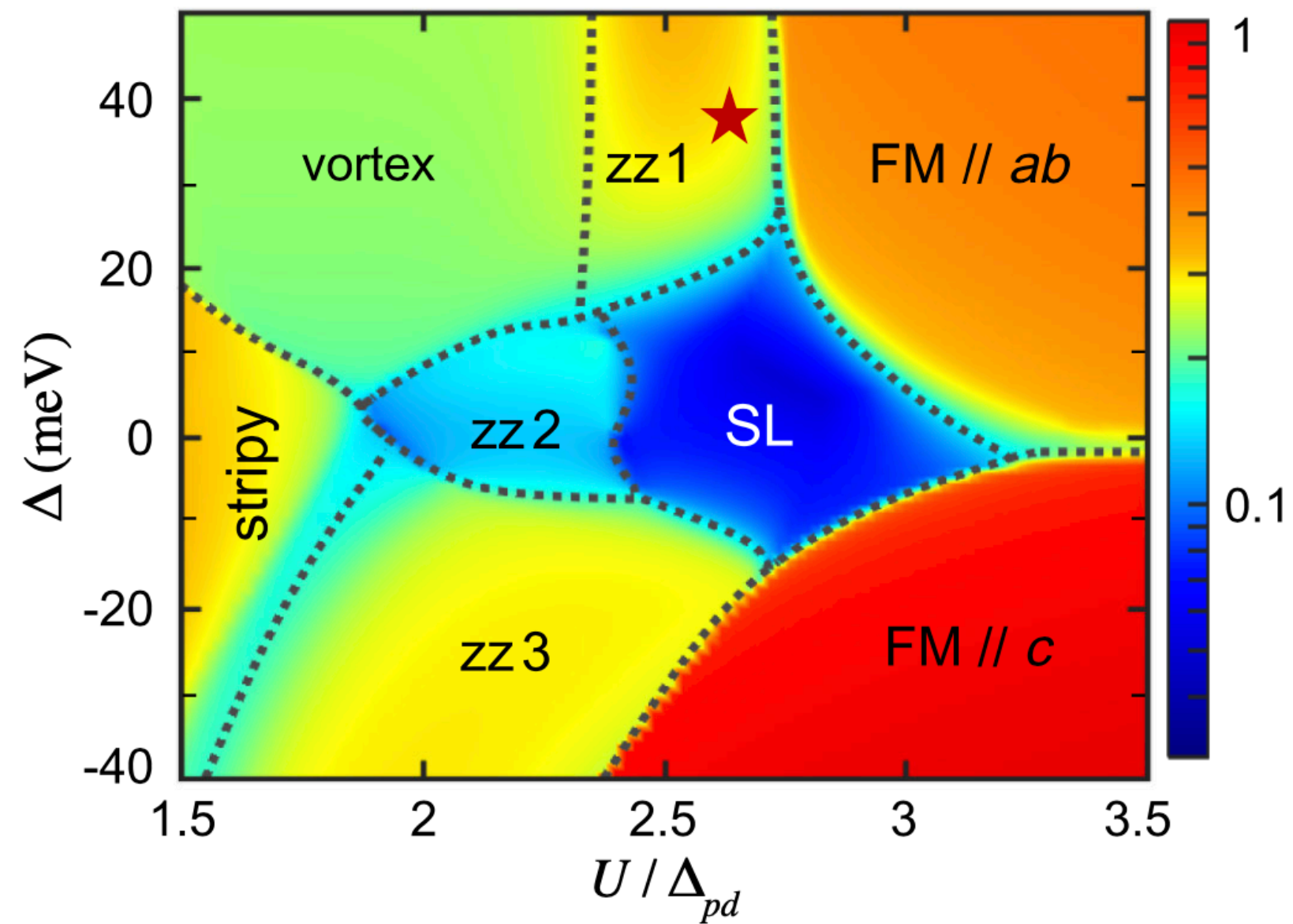
MACS, $E_f = 5 \text{ meV}$
 $T = 1.5 \text{ K}$

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Standards and Technology



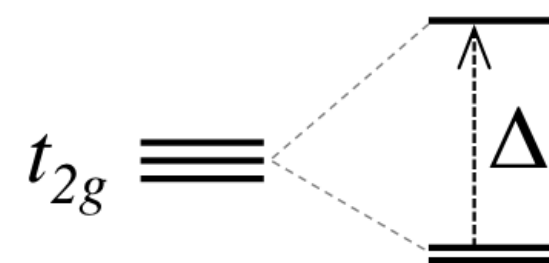
Comparison with theory : $\text{Na}_3\text{Co}_2\text{SbO}_6$

H. Liu et al., Phys. Rev. Letters 125, 047201 (2020)

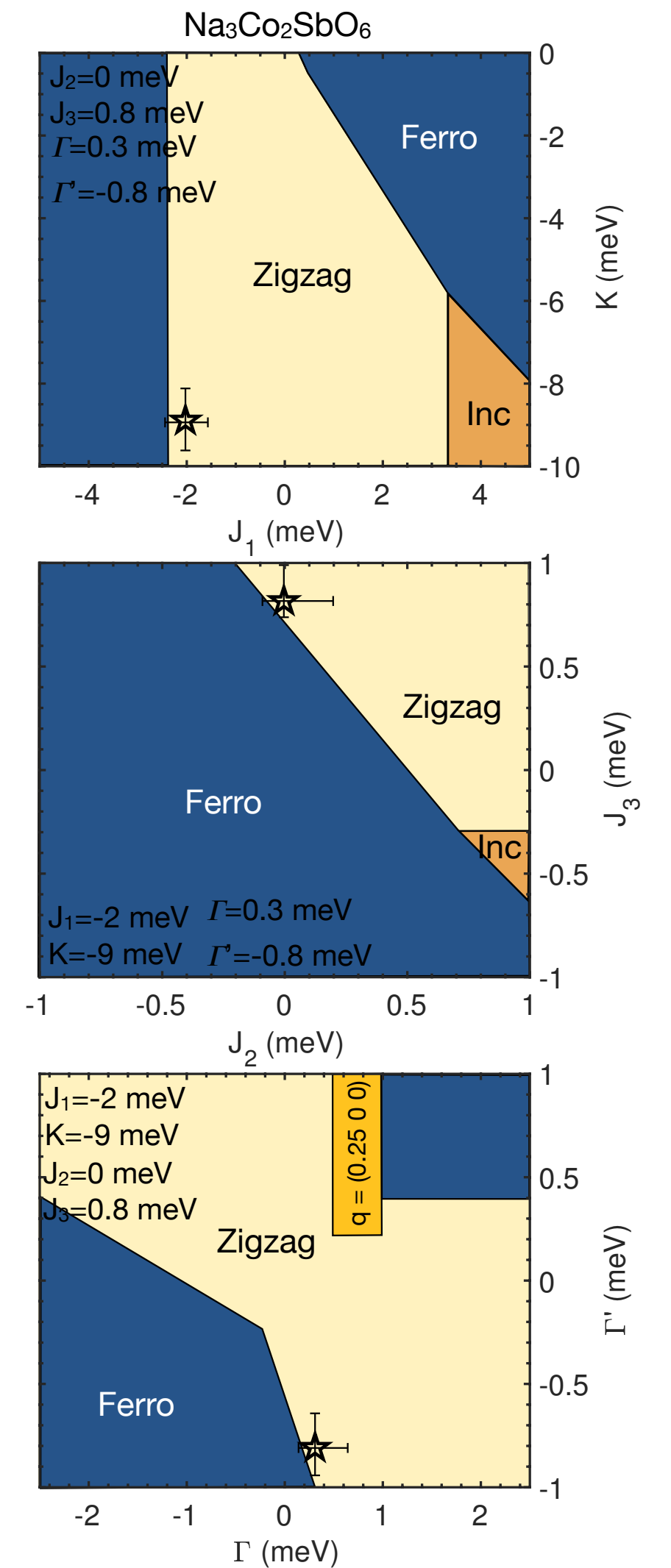


Trigonal field
(octahedral distortion)

cubic trigonal



Our work



Comparison with theory: $\text{Na}_3\text{Co}_2\text{SbO}_6$

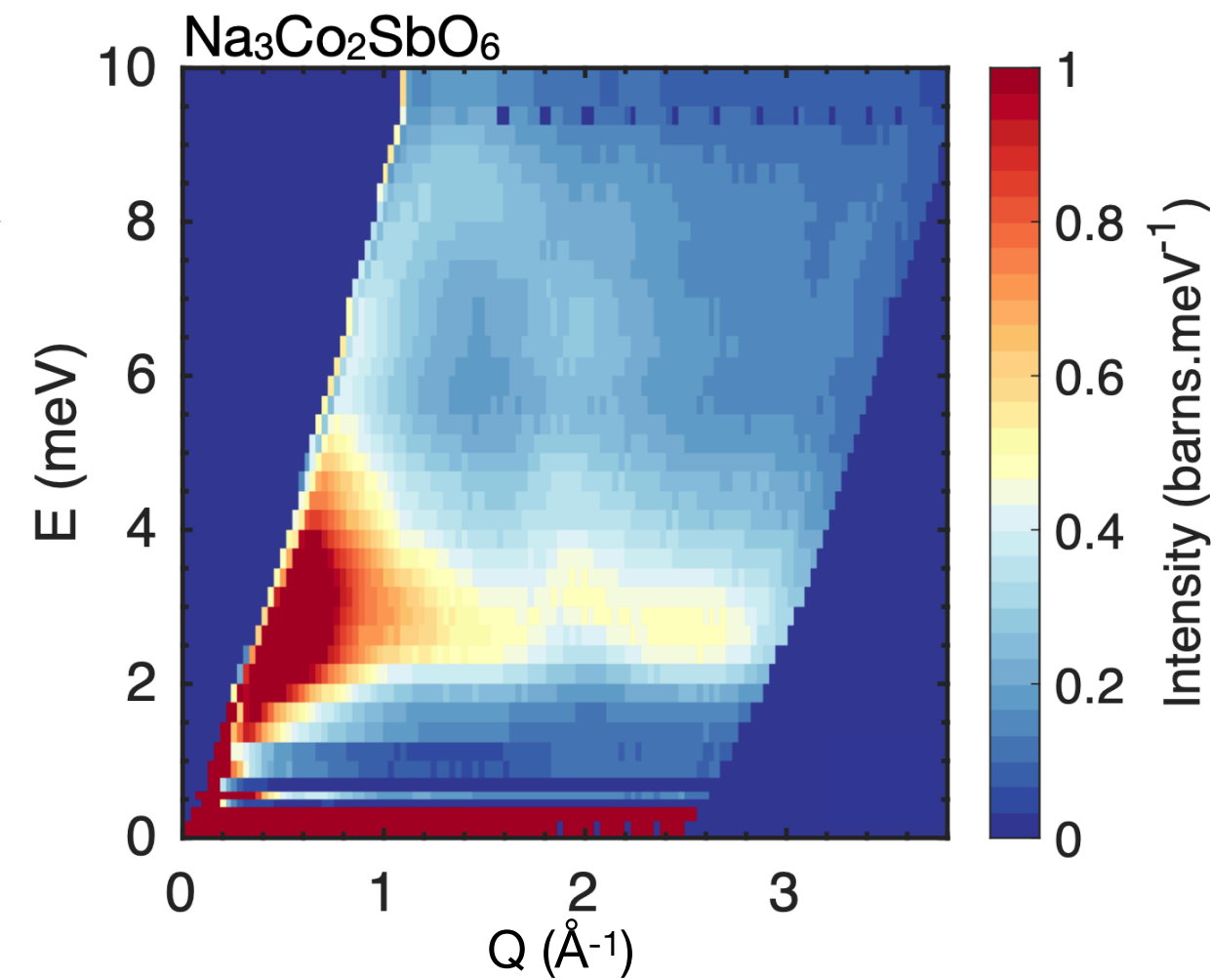


Low Energy:

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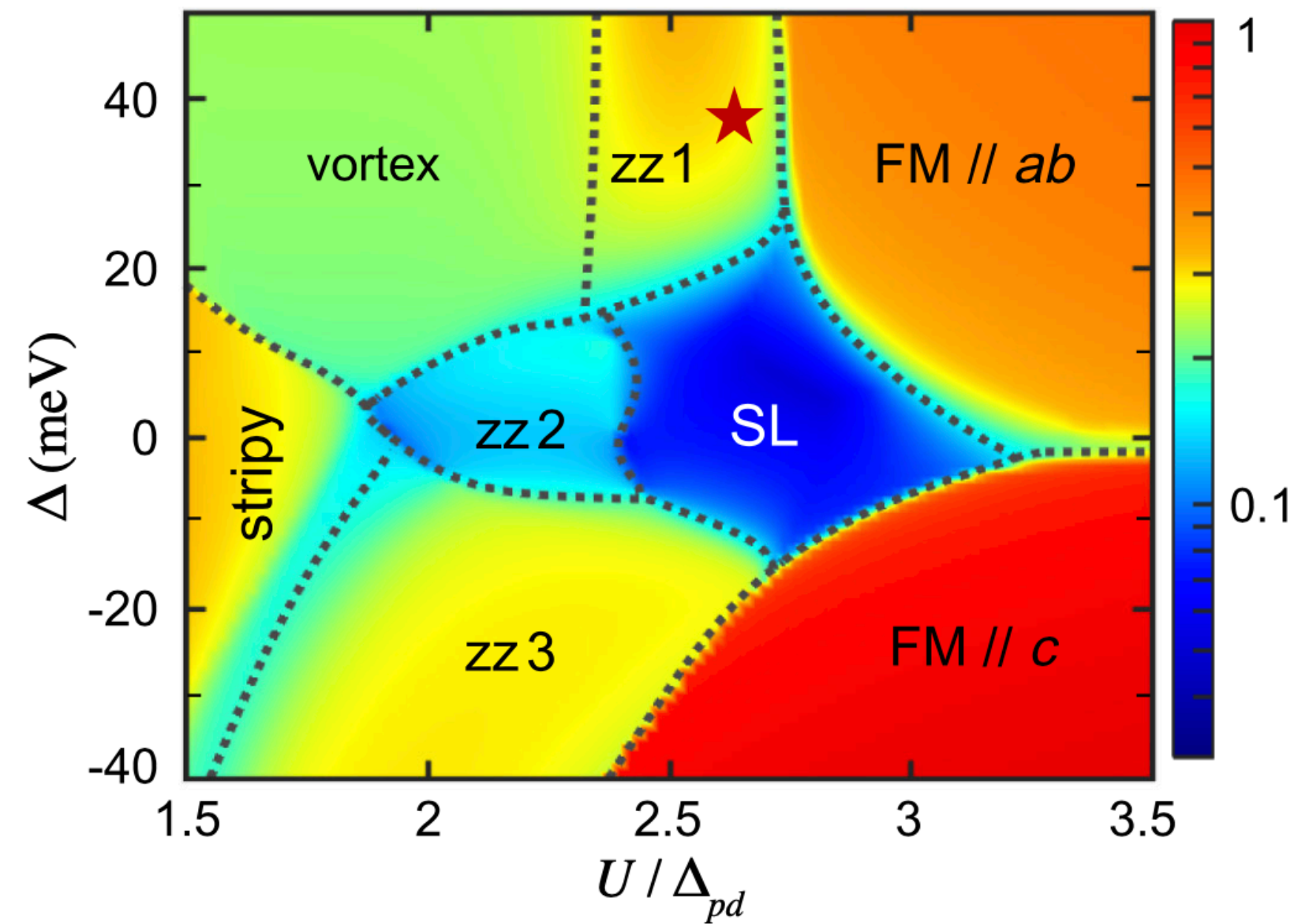
MACS, $E_f = 5 \text{ meV}$
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NIST
National Institute of
Standards and Technology



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H. Liu et al., Phys. Rev. Letters 125, 047201 (2020)

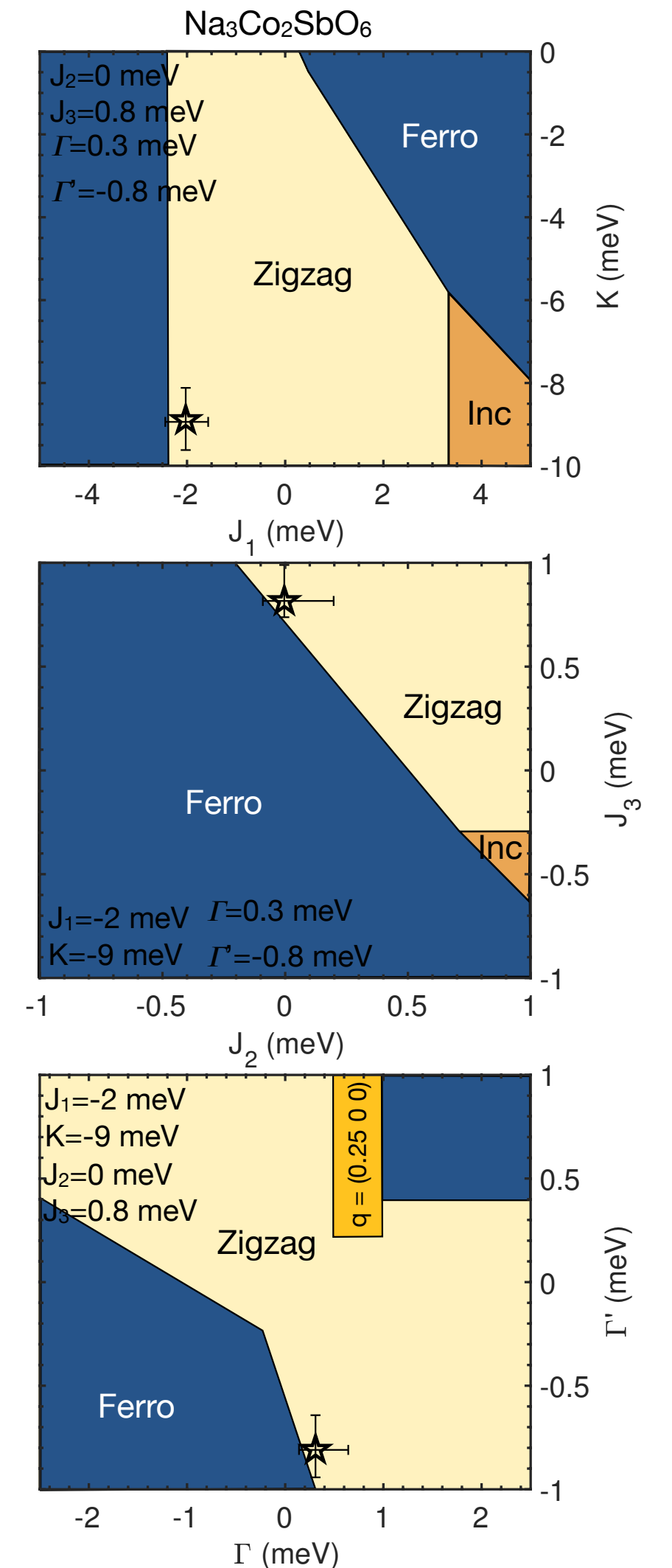


Trigonal field
(octahedral distortion)

Confirmation in single crystal materials is essential !!

Theory	$J/ K \sim -0.14$	$\Gamma/ K \sim -0.03$	$\Gamma'/ K \sim -0.16$
Experiment (our work)	$1/2 \cdot (J_1/J_3)/ K \sim -0.15$	$\Gamma/ K \sim -0.03$	$\Gamma'/ K \sim -0.08$

Our work

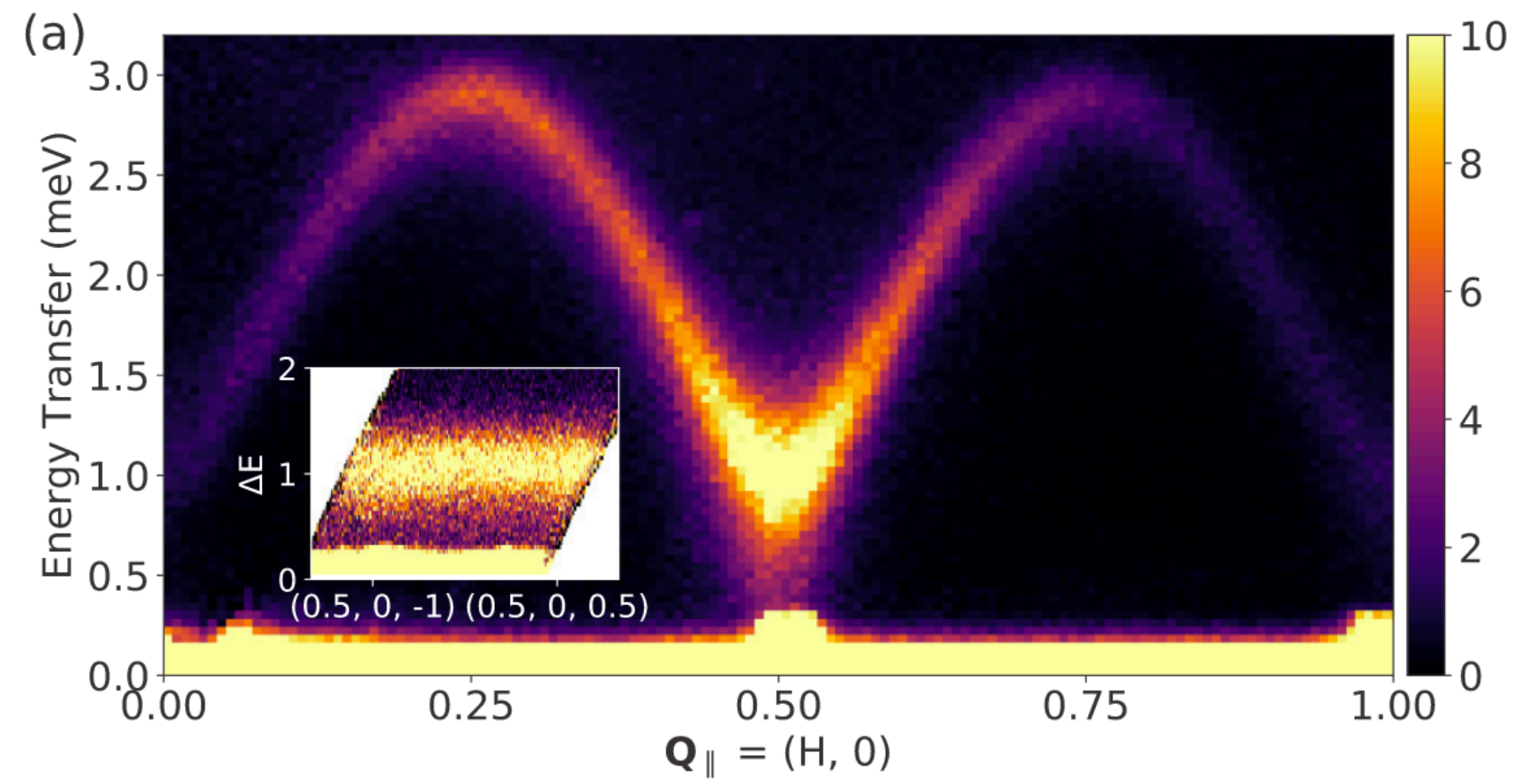


Recent single crystal data : $\text{Na}_2\text{Co}_2\text{TeO}_6$

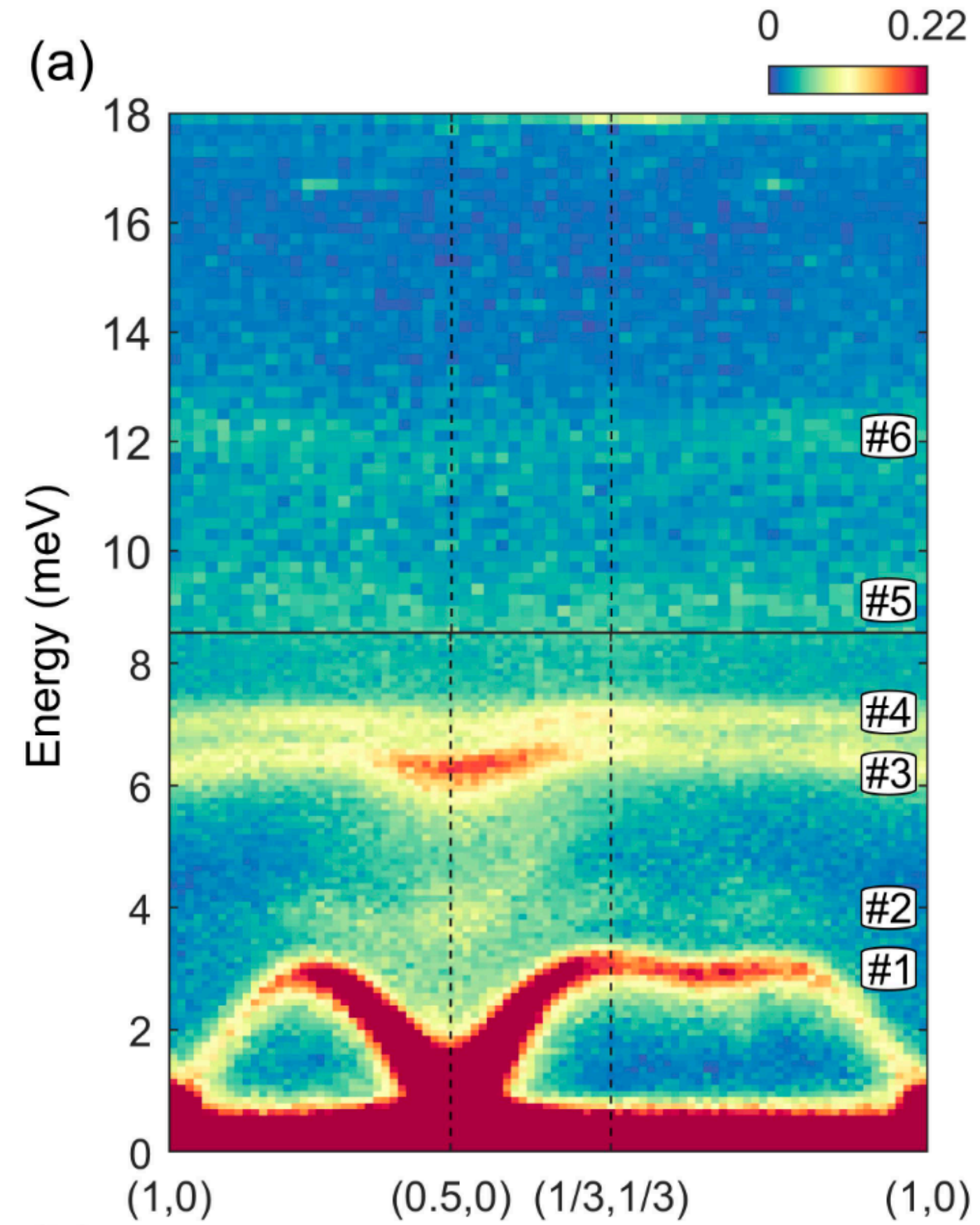


Neutron inelastic data

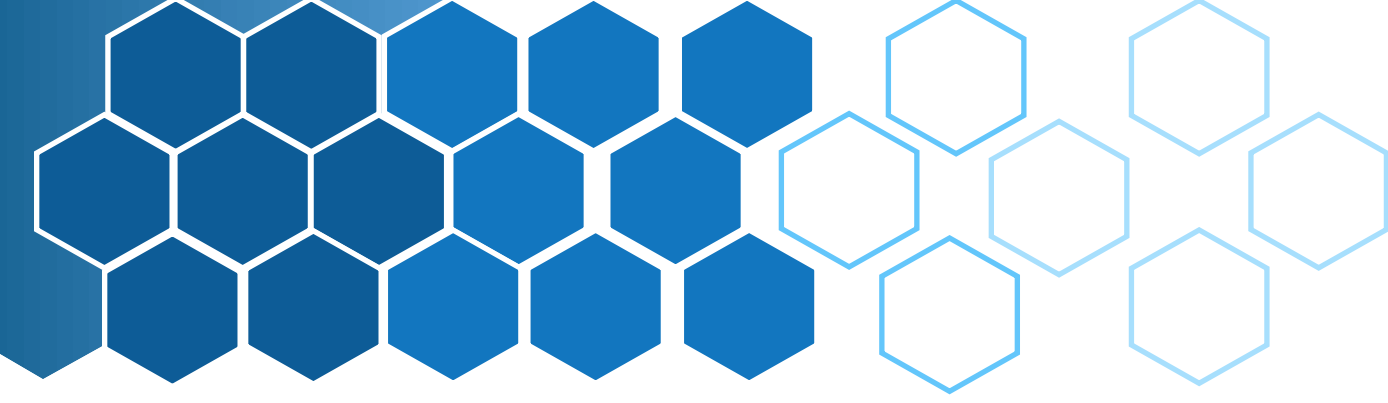
W. Chen et al., *Phys. Rev. B* 103, L180404 (2021)
W. Yao et al., *arXiv* 2203.00282v1 (2022)



► Flat band perpendicularly to the planes : quasi 2D-materials (J_{int} very weak)



Recent single crystal data : $\text{Na}_2\text{Co}_2\text{TeO}_6$



Neutron inelastic data

W. Chen et al., *Phys. Rev. B* 103, L180404 (2021) *Phys. Rev. B* 102, 224429 (2020)
W. Yao et al., *arXiv* 2203.00282v1 (2022)

Our model

J_1	J_2	J_3	K	Γ	Γ'
-0.1(5)	0.3(3)	0.9(3)	-9.0(5)	1.8(5)	0.3(3)

Lin et al.

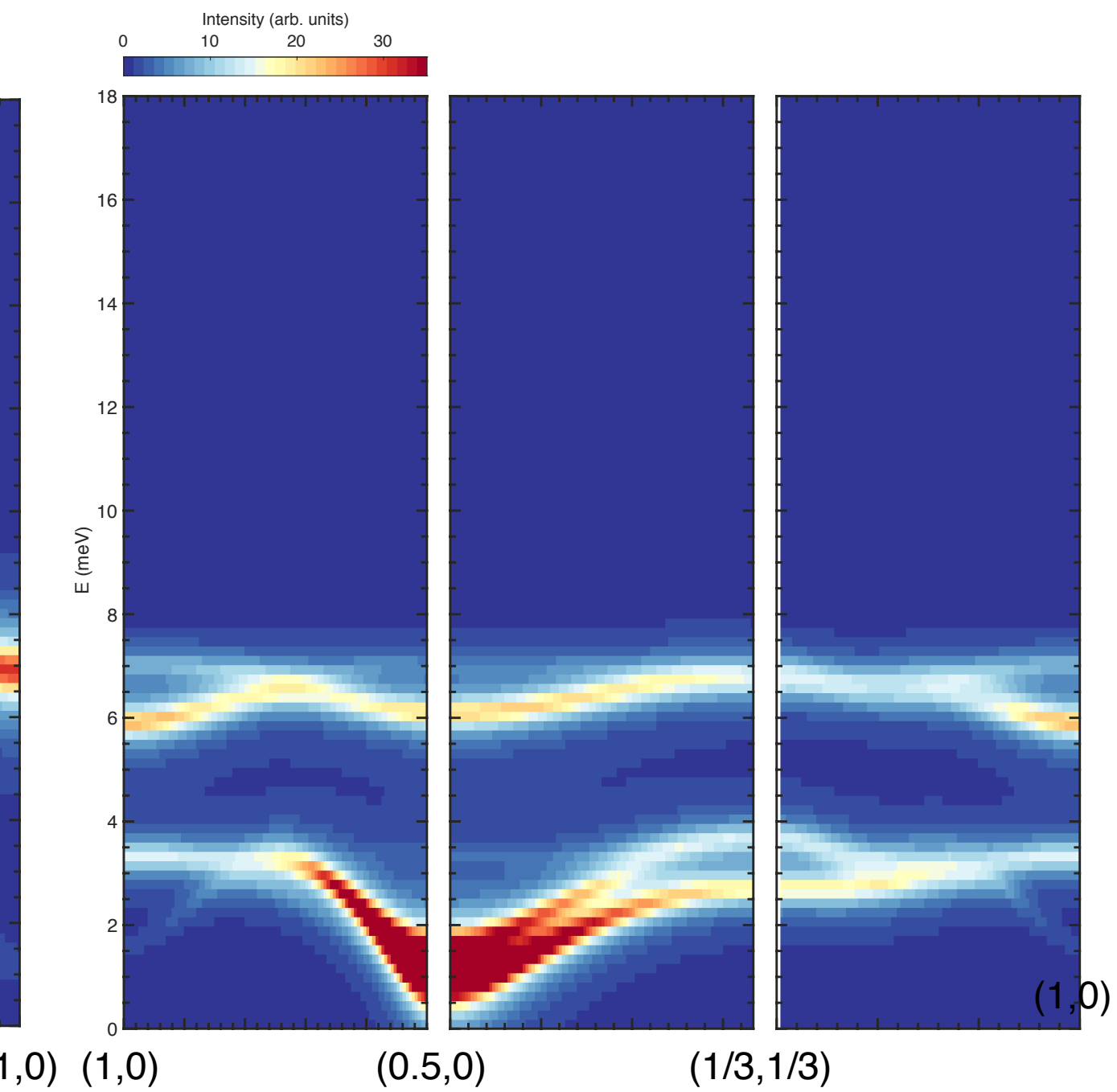
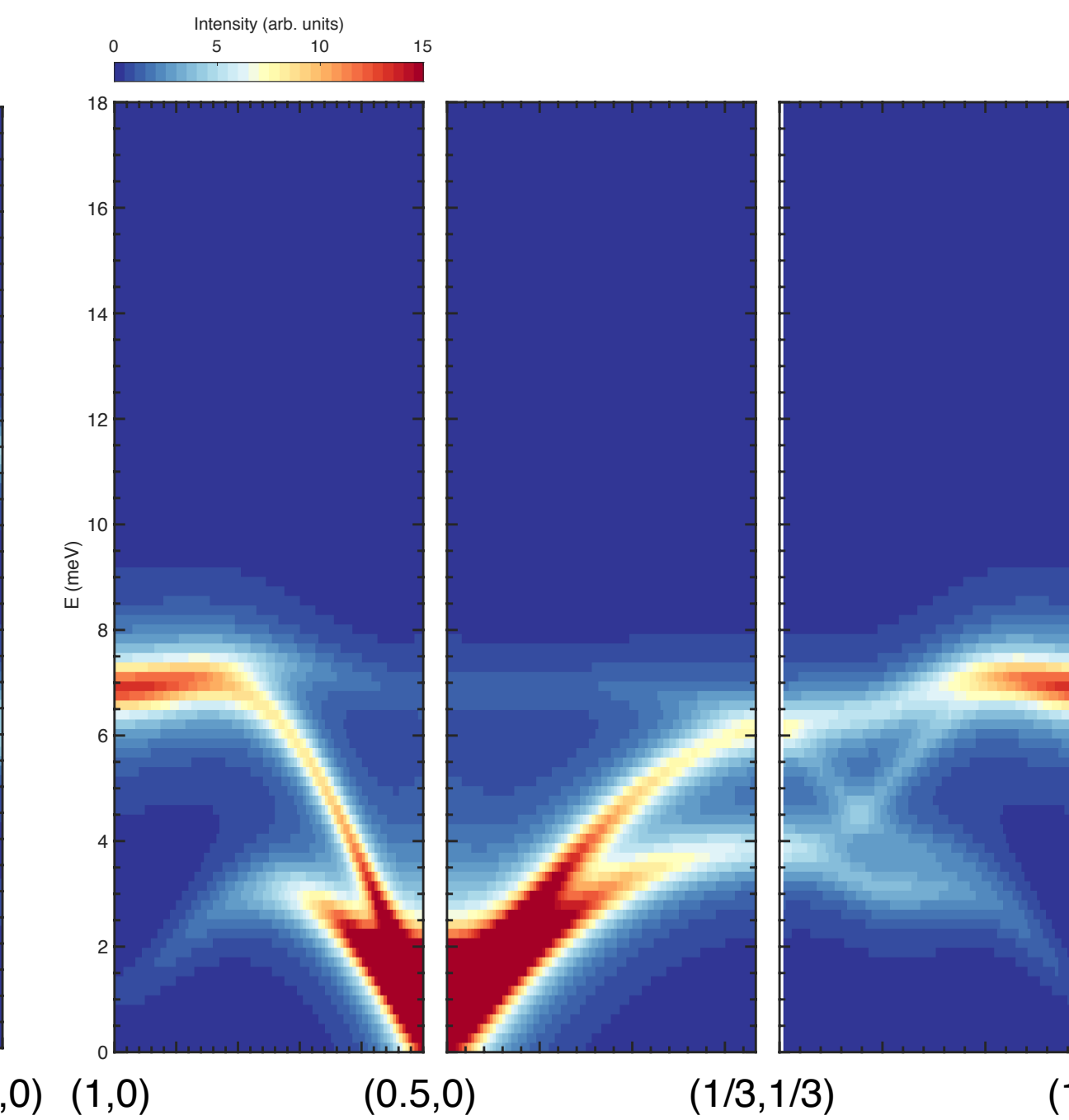
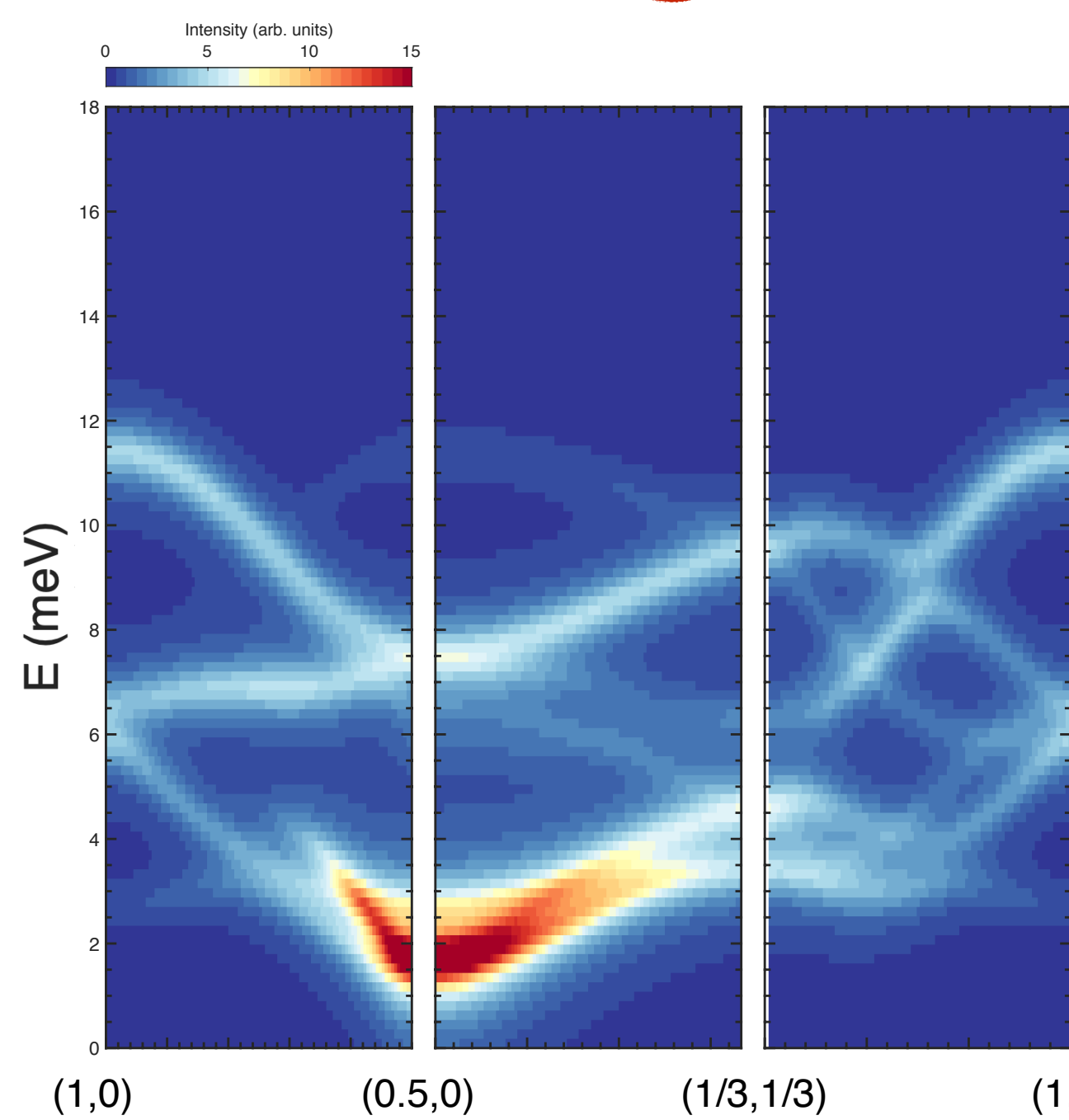
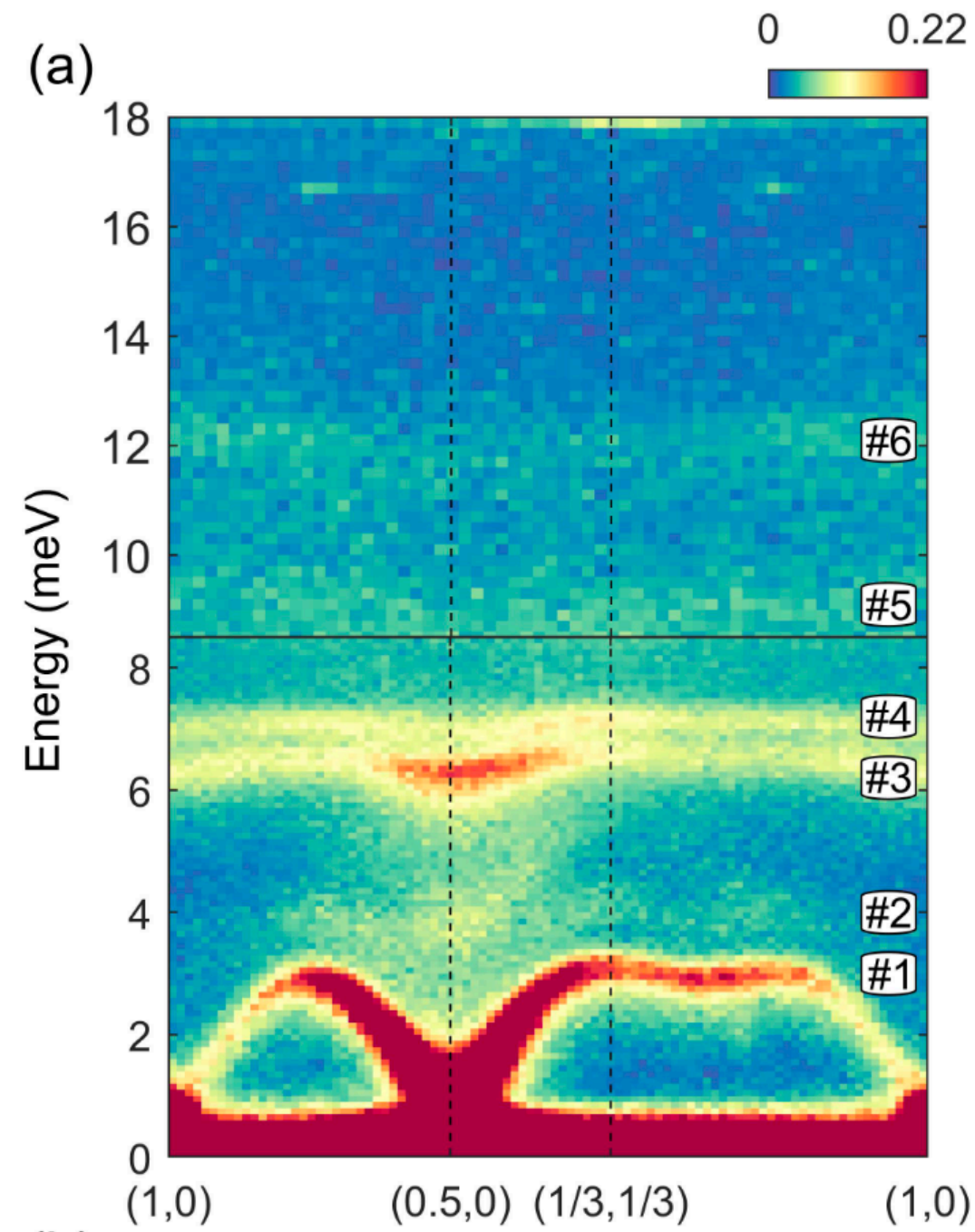
Nat. Comm. 12, 5559 (2021)

J_1	J_2	J_3	K	Γ	Γ'
2.35	0.0	-2.5	-0.125	-0.125	0.0

Kim et al.

J. Phys.: Condens. Matt. 34, 045802 (2021)

J_1	J_2	J_3	K	Γ	Γ'
-1.50(5)	0.0	1.50(2)	3.30(10)	-2.80(5)	2.10(7)



From powder studies

Recent single crystal data : $\text{Na}_2\text{Co}_2\text{TeO}_6$



Neutron inelastic data

W. Chen et al., Phys. Rev. B 103, L180404 (2021) Phys. Rev. B 102, 224429 (2020)
W. Yao et al., arXiv 2203.00282v1 (2022)

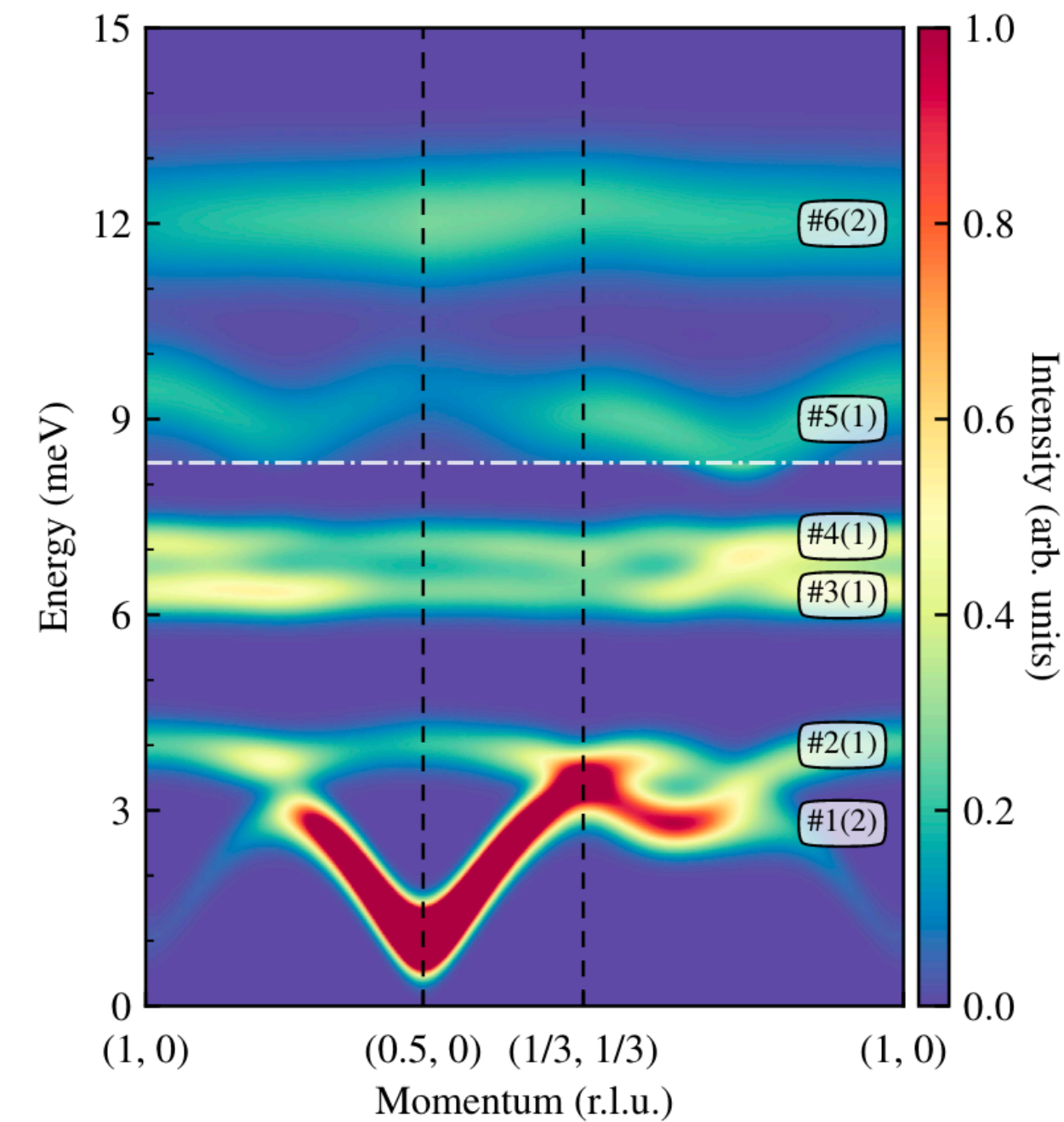
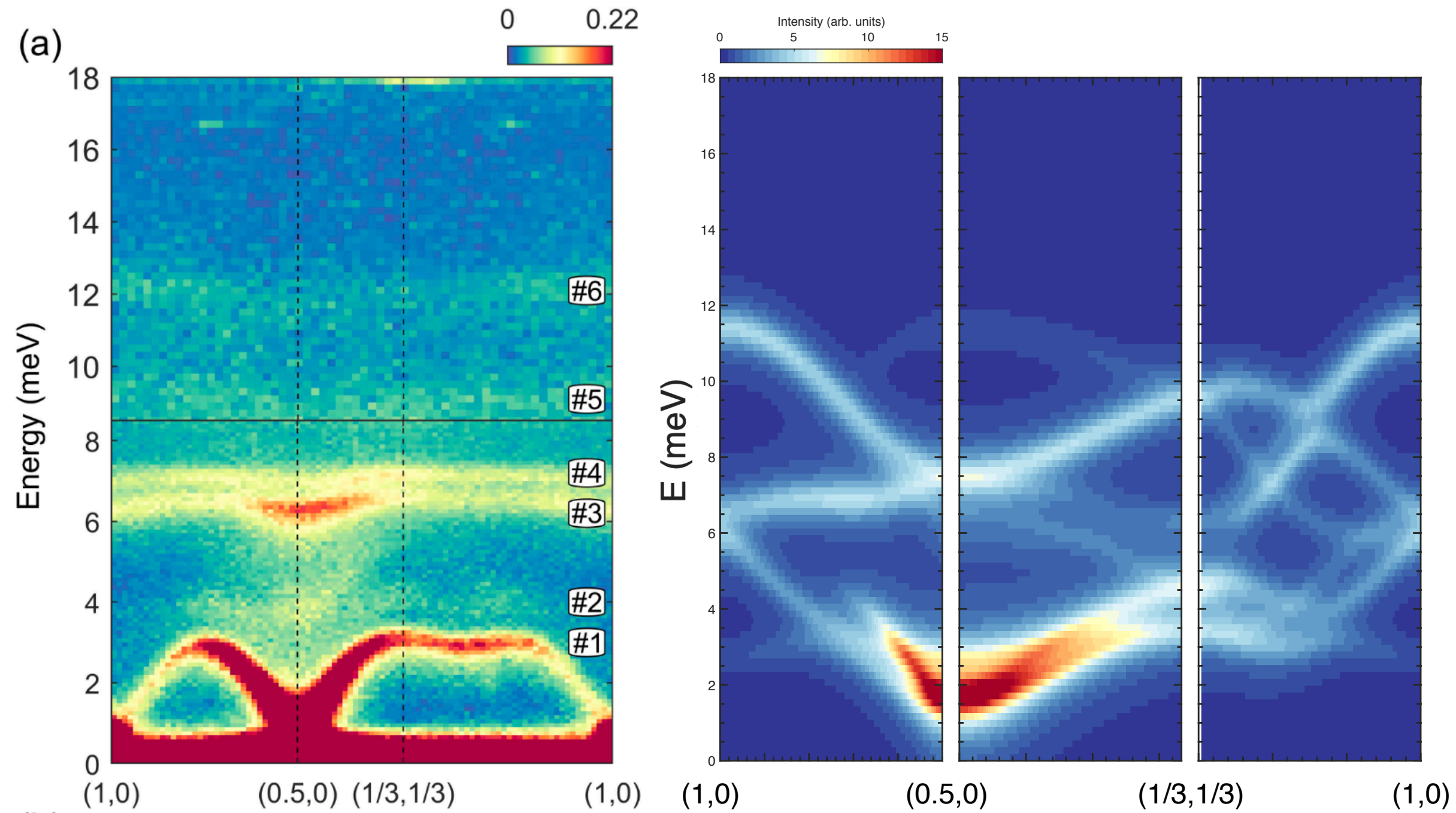
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Krüger et al.

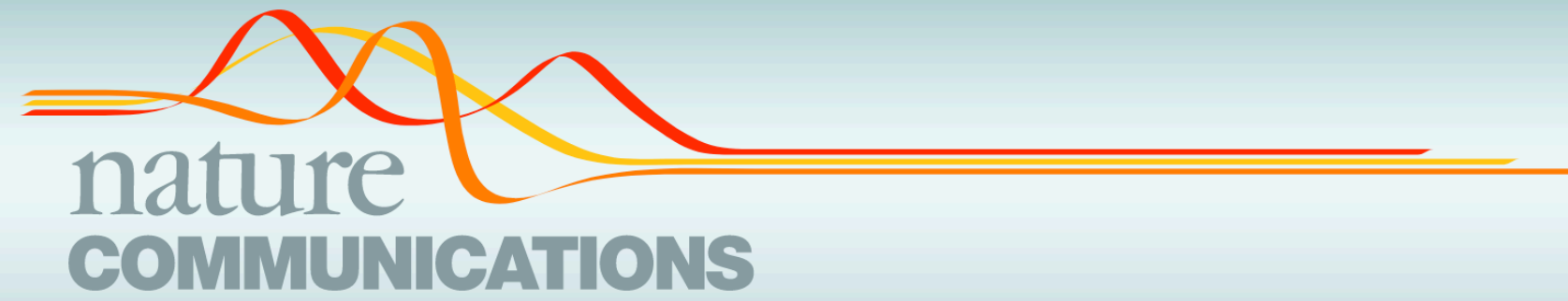
arXiv 2211.16957v1 (2022)

J_1	J_2^A	J_2^B	J_3	K	Γ	Γ'
1.23	0.32	-0.24	0.47	-8.29	1.86	-2.27



From powder study

- ▶ Proximity to a hidden-SU(2)-symmetric point
- ▶ Possible complex triple-Q magnetic ground state



ARTICLE



<https://doi.org/10.1038/s41467-021-23851-0>

OPEN

Order-by-disorder from bond-dependent exchange and intensity signature of nodal quasiparticles in a honeycomb cobaltate

M. Elliot ¹, P. A. McClarty², D. Prabhakaran ¹, R. D. Johnson³, H. C. Walker ⁴, P. Manuel ⁴ & R. Coldea ¹✉

M. Elliot et al., Nature Comm. 12, 3936 (2021)

B. Yuan et al., PRX 10, 011062 (2020), PRB 102, 134404 (2020)



- * Rich playground for material research/design: interplay between spin-orbit coupling, crystal field, Hund's coupling and lattice (3d/4d/5d transition metals, rare-earth, other geometries)
- * Recent motivation re-visit Co materials: versatile materials with rich and complex magnetic states, beyond Kitaev physics (complex magnetic order, multi-q state, hidden order, topological magnons...)

$BaCo_2(AsO_4)_2$, $BaCo_2(PO_4)_2$, $CoPS_3$, $CoTiO_3...$

L. -P. Regnault et al., Heliyon 4 (2018)
H. Nair et al., PRB 97, 134409 (2018)
T. Halloran et al., arXiv:2205.15262 (2022)
S. Das et al., PRB 104, 134425 (2021)
B. Yuan et al., PRX 10, 011062 (2020), PRB 102, 134404 (2020)
M. Elliot et al., Nature Comm. 12, 3936 (2021)
S. Winter, arXiv:2204.09856 (2022)
A.R. Wildes et al., J. Phys.: Condens. Matter 29, 455801 (2017)
B.C. Kim et al., PRB 102, 184426 (2020)
and many others...

Other geometries (triangular, 1D chains, hyper-honeycomb...)

$Ba_3CoSb_2O_9$: PRB 102, 064421 (2020), PRL 108, 057205 (2012)
 $Na_2BaCo(PO_4)_2$, $Na_2SrCo(PO_4)_2$ PNAS 116, 14505 (2019)



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B. Yuan et al., *PRX* 10, 011062 (2020), *PRB* 102, 134404 (2020)
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Thank you !

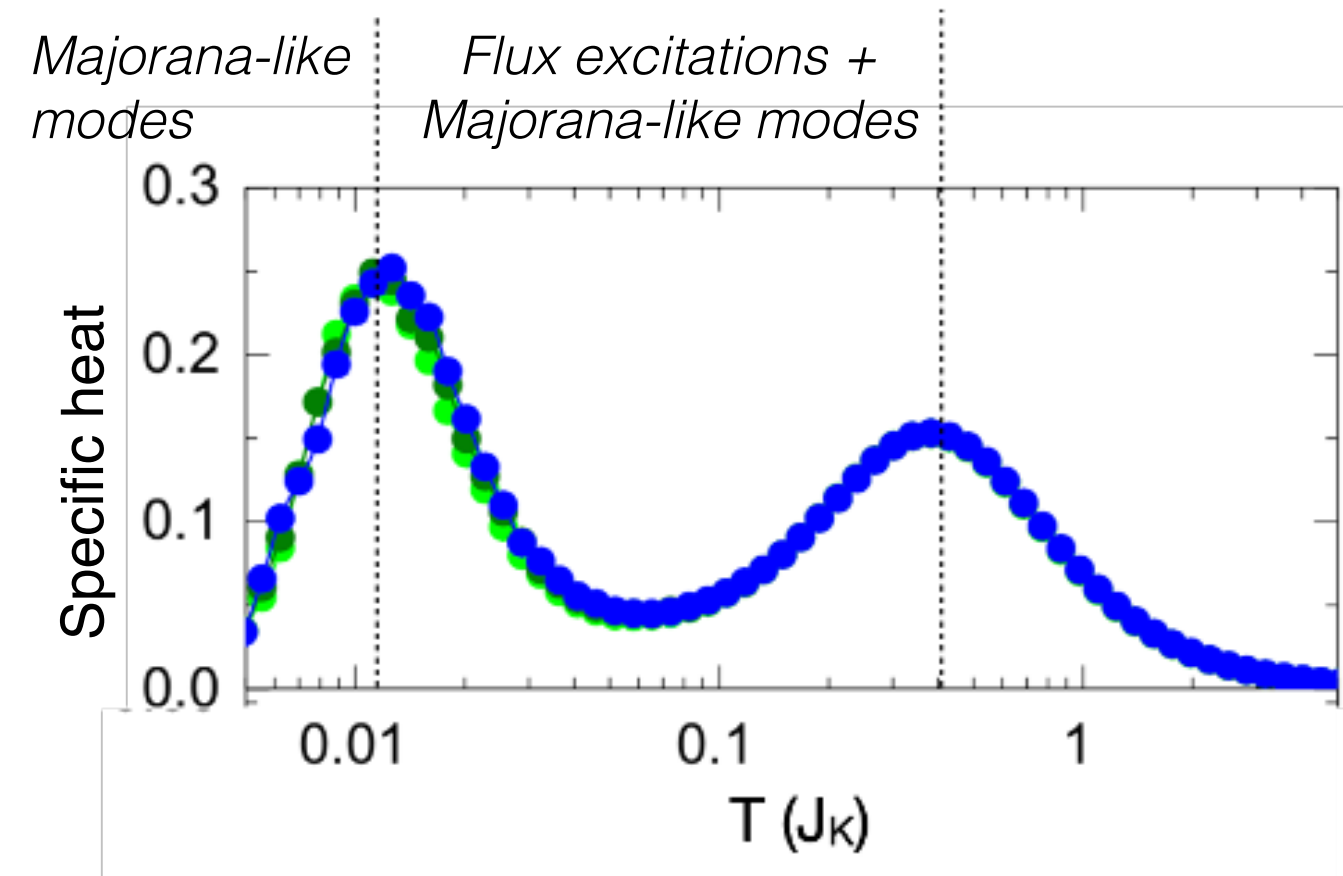


What experimental signatures?

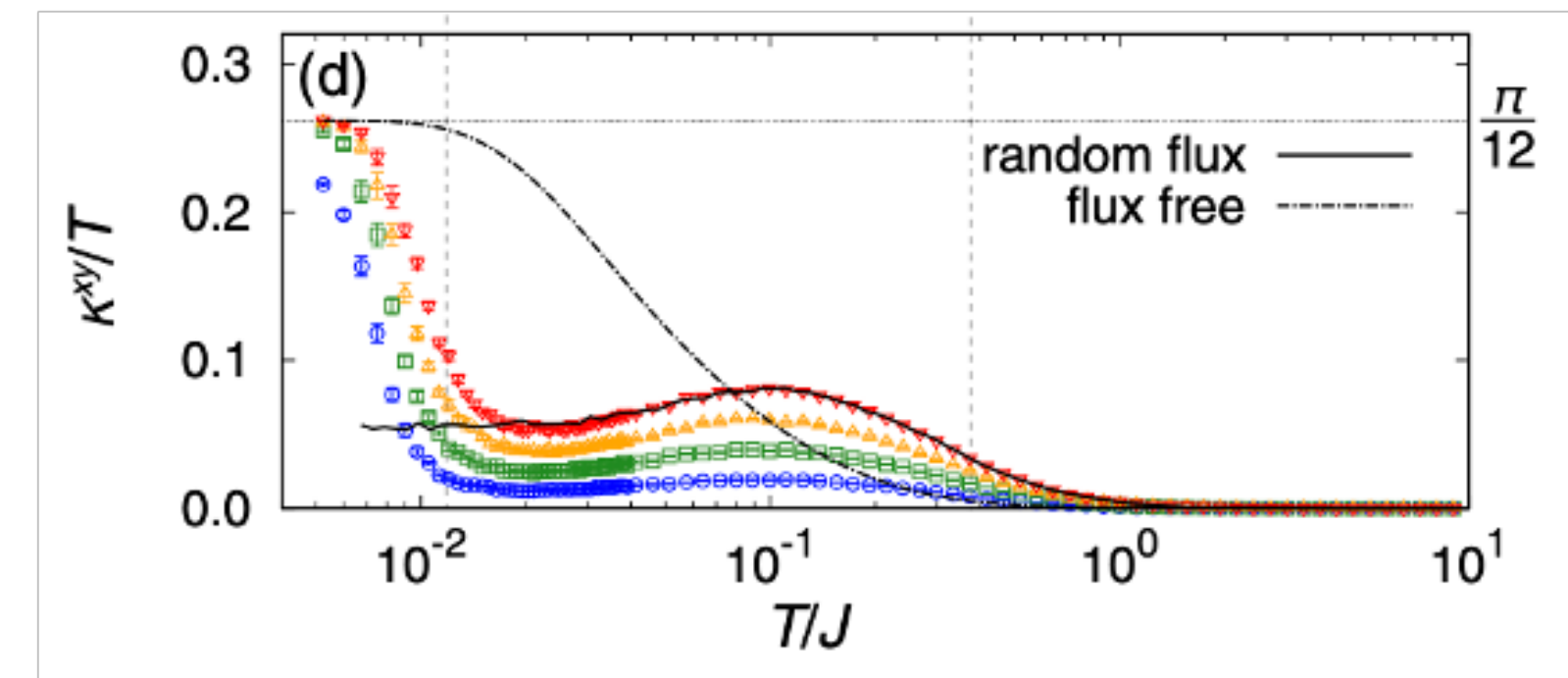


An exact model: predictions for experimental signatures

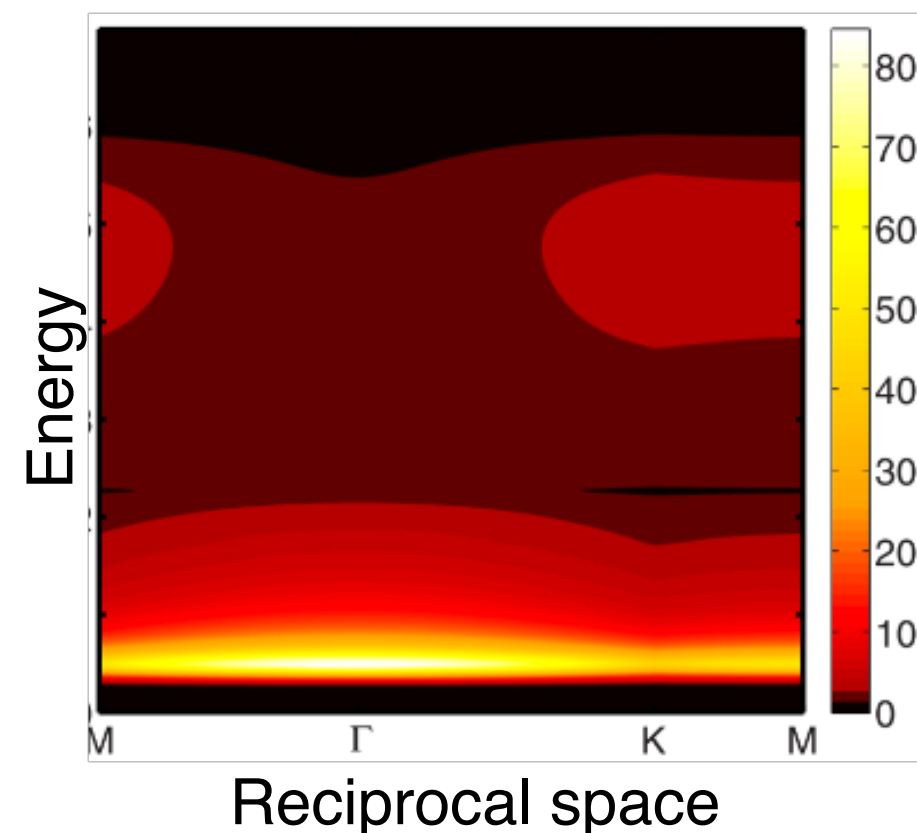
Magnetization, specific heat
Thermodynamic signatures of fractional excitations



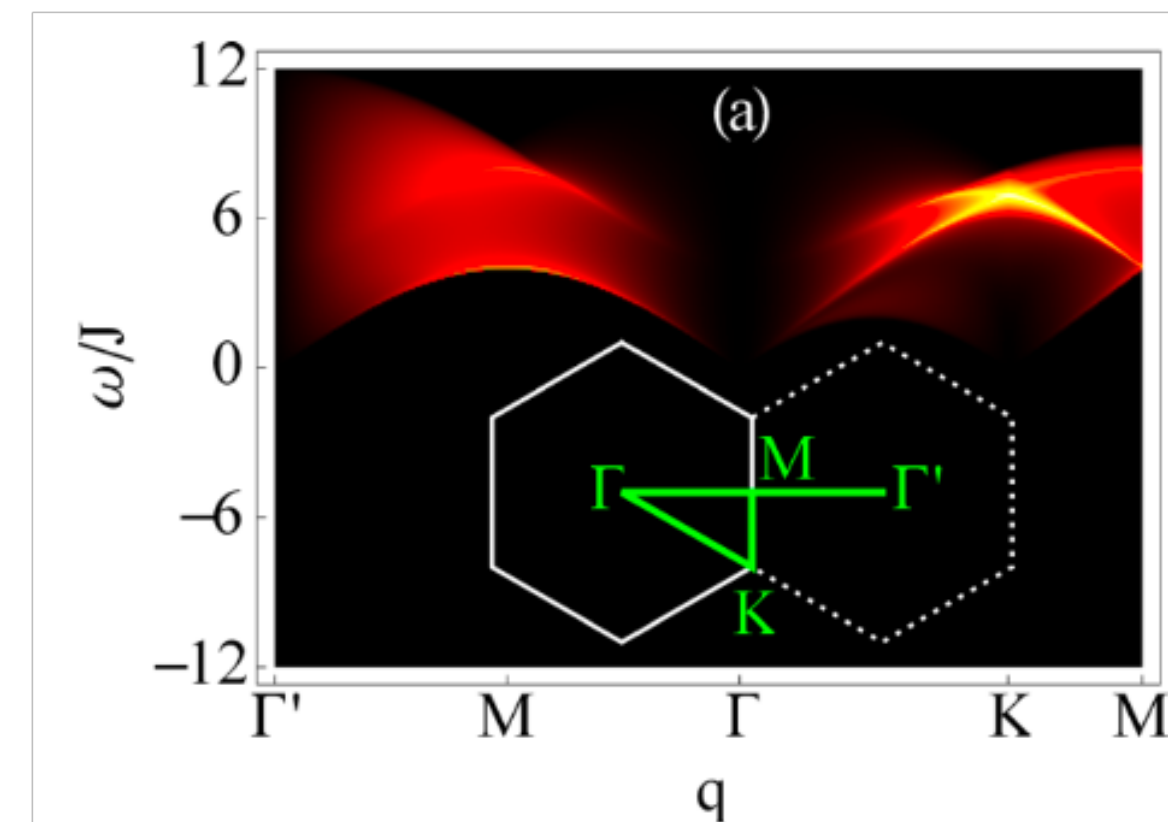
Thermal Hall effect
Signature for topological phase: chiral edge modes



Neutron scattering
Continuum of fractional excitations



Resonant X-ray scattering
Continuum of fractional excitations



J. Yoshitake et al., Phys. Rev. Letters (2016)
G. Halasz et al., Phys. Rev. B (2019)
J. Knolle et al., Phys. Rev. B (2015)

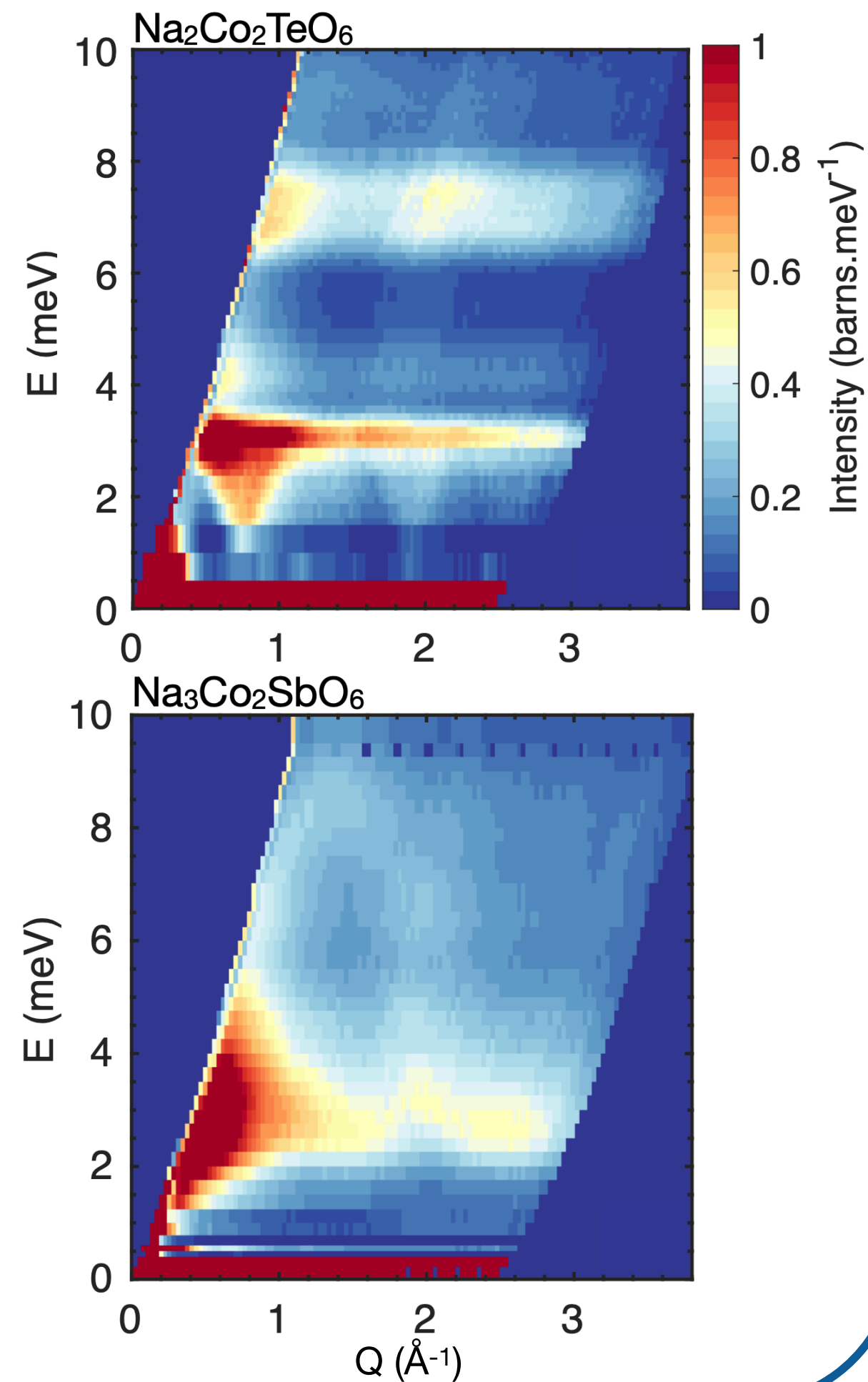
Neutron inelastic study (powders)



Low Energy:

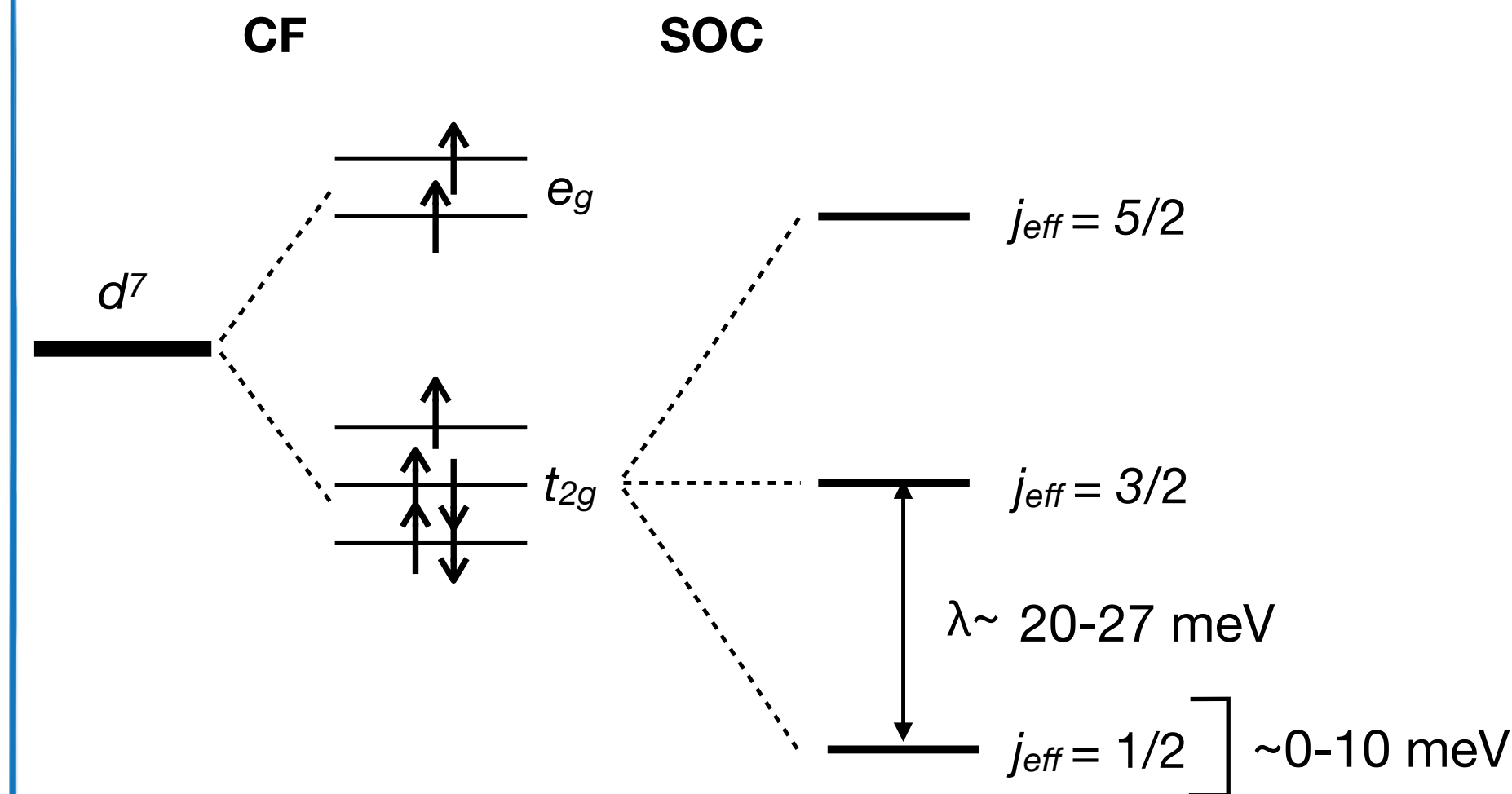
- Excitations within the $j_{\text{eff}} = 1/2$ manifolds : exchange interactions

MACS (NIST), $E_f = 5 \text{ meV}$
 $T = 1.5 \text{ K}$

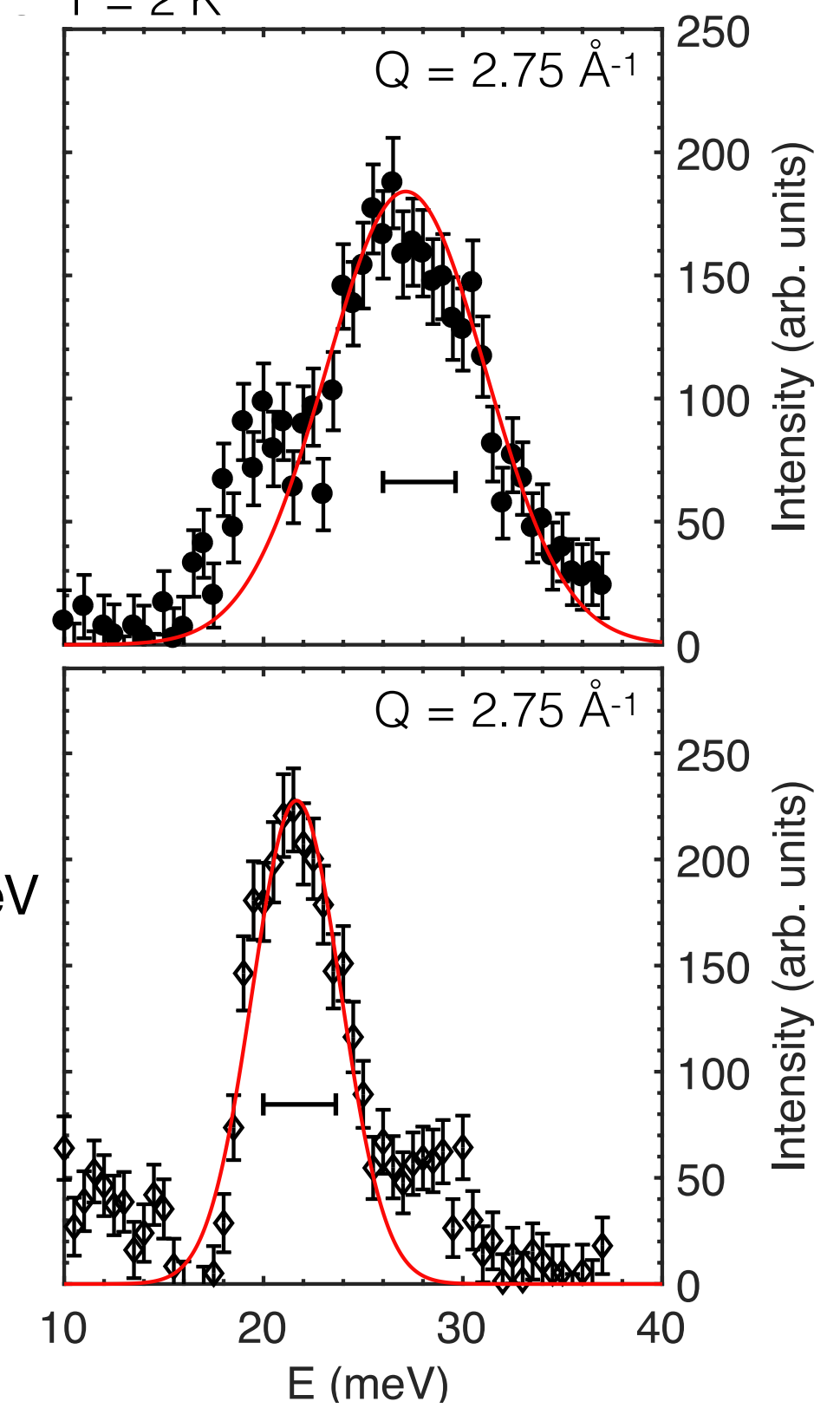


Higher Energy:

- Excitations between the $j_{\text{eff}} = 1/2$ and $j_{\text{eff}} = 3/2$ manifolds : spin-orbit coupling



BT4 (NIST, US)
 $E_f = 14.7 \text{ meV}$
 $T = 2 \text{ K}$



Testing the spin model : spin wave calculations

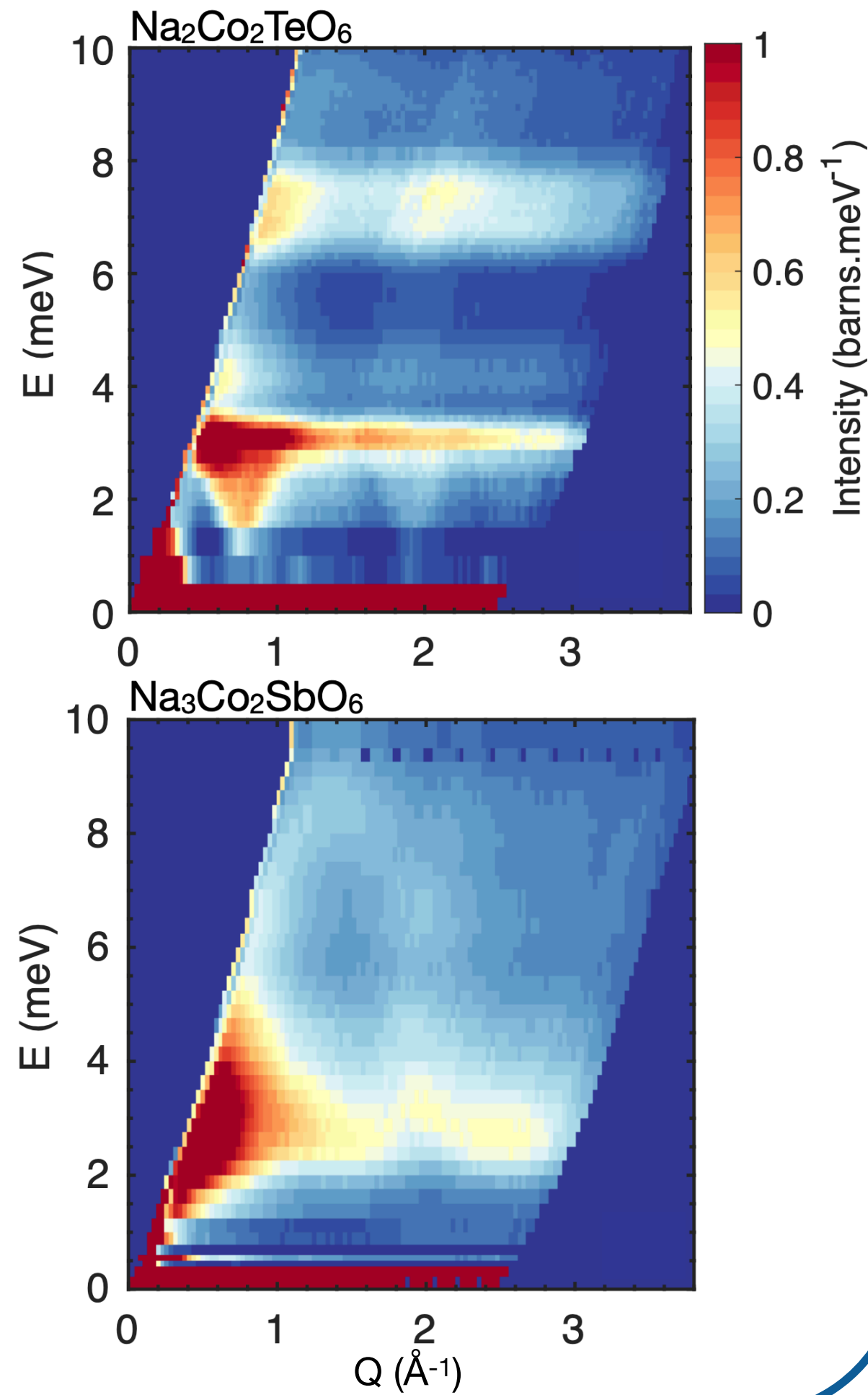


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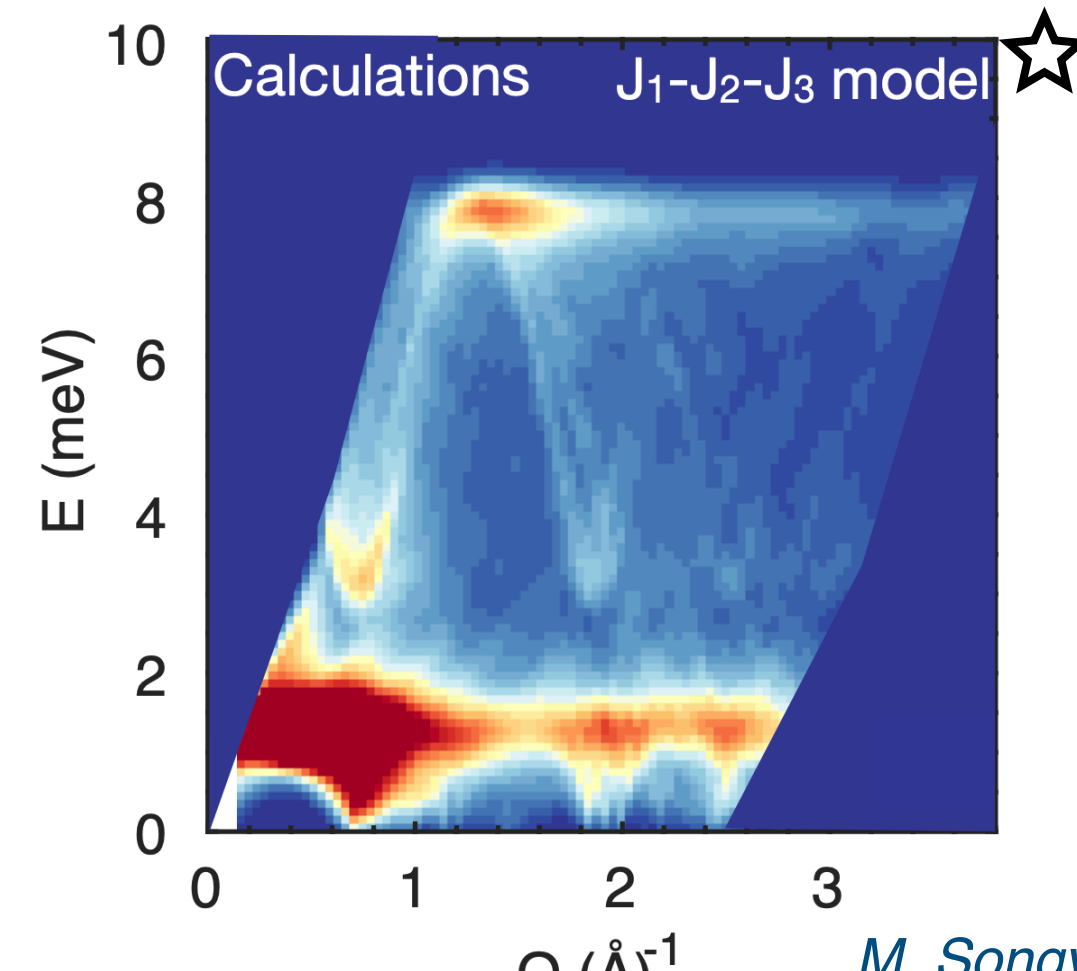
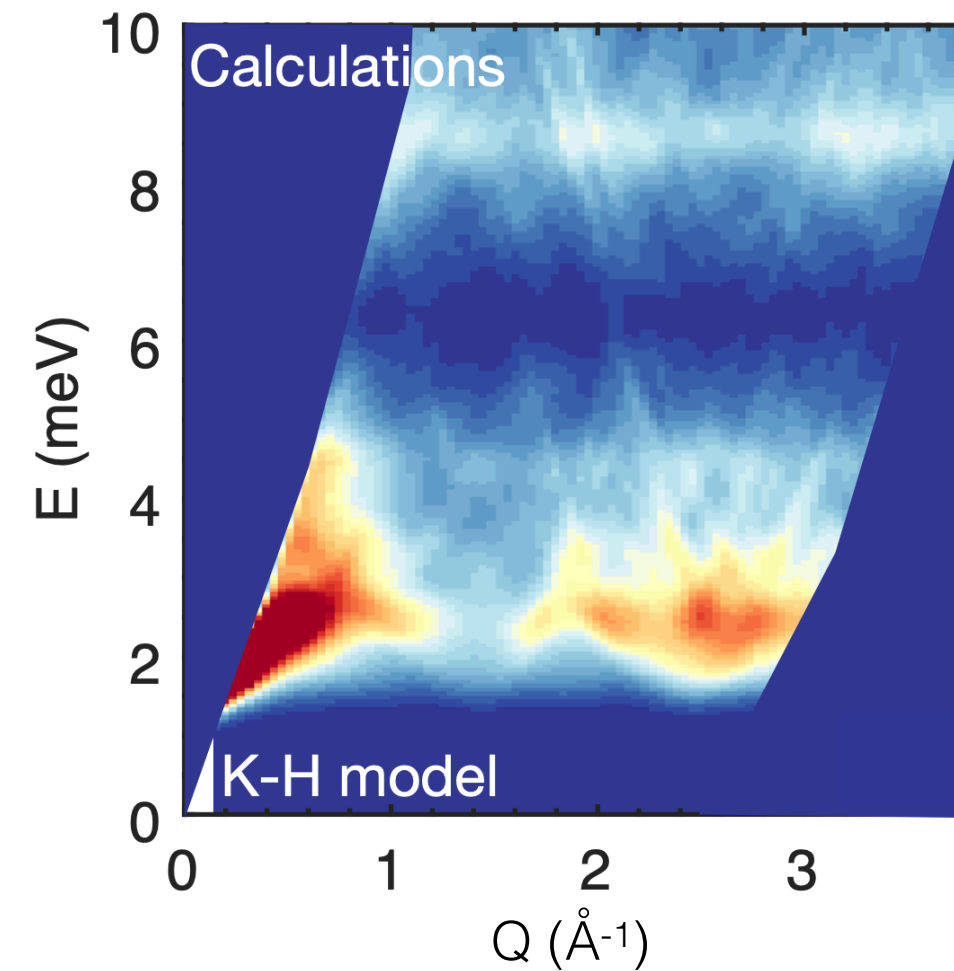
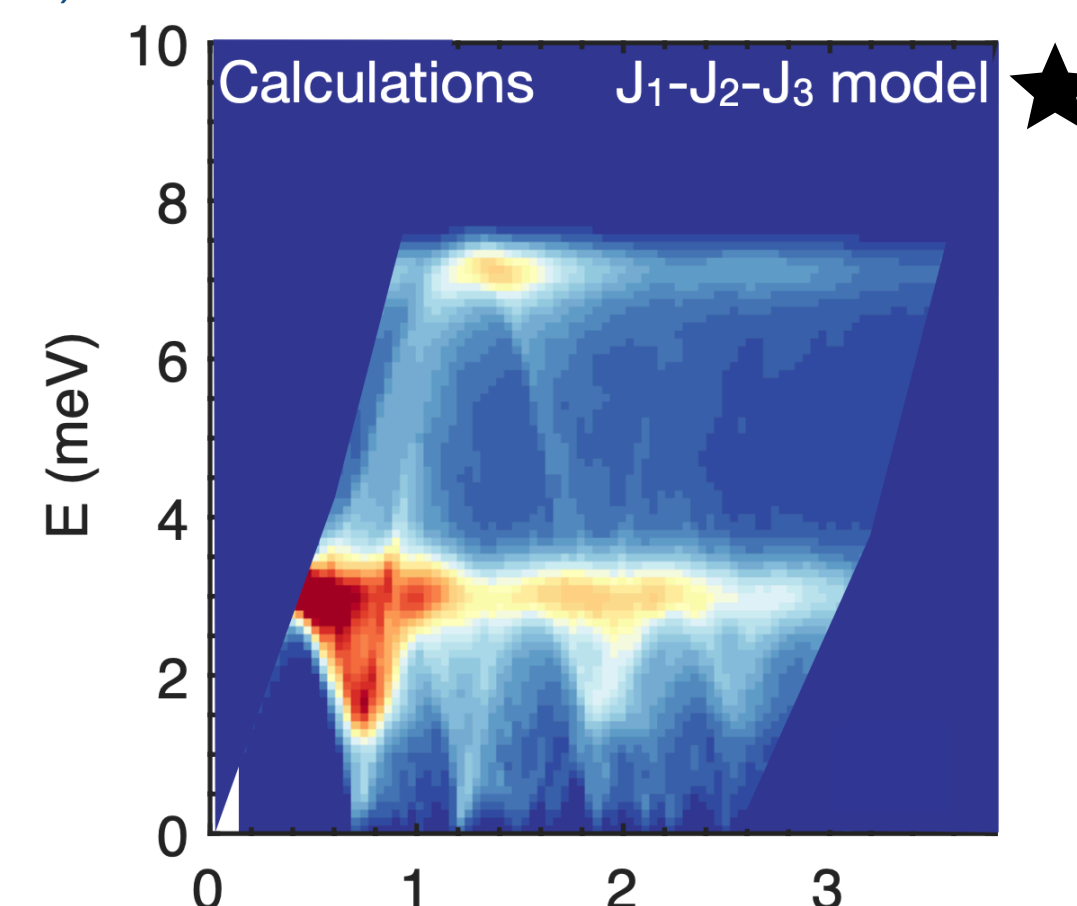
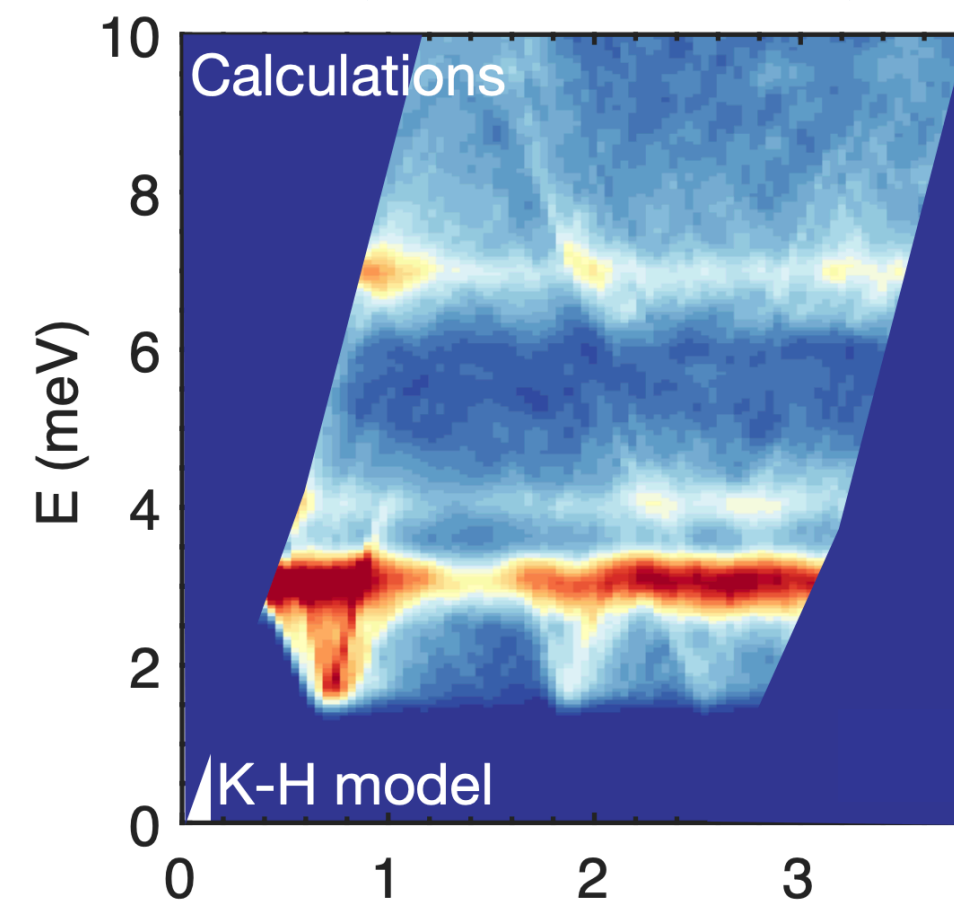
NIST
 National Institute of
 Standards and Technology



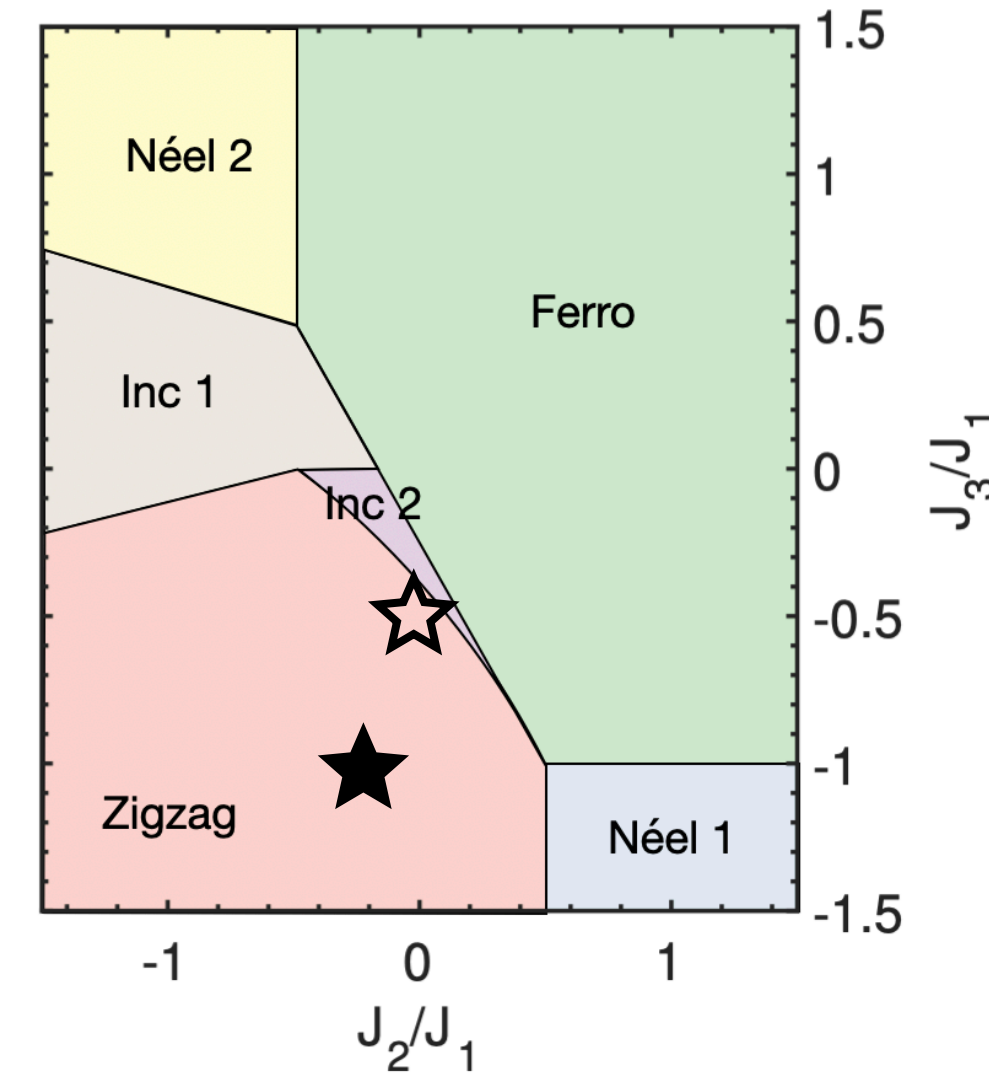
Spin wave calculations : Kitaev-Heisenberg vs. Heisenberg XXZ models

Spinwave software
 S. Petit, Collection SFN 12, 105 (2011)

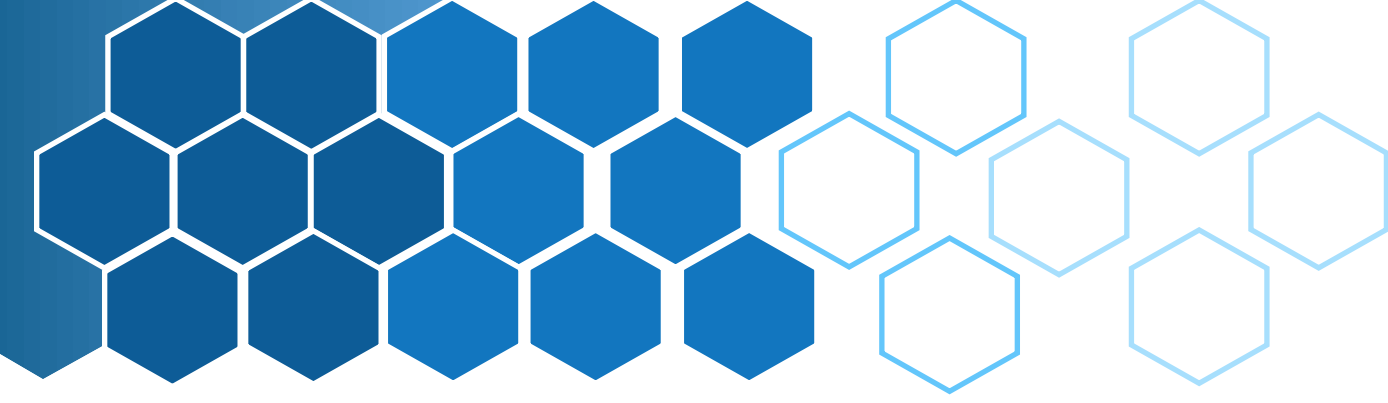
$$H_{\text{XXZ}} = \sum_{n=1}^3 J_n \sum_{i,j} (S_i^x S_j^x + S_i^y S_j^y + \Delta S_i^z S_j^z)$$



$J_1 < 0 ; \Delta = 0.95$



$Na_2Co_2TeO_6$: relevance of Kitaev interactions?

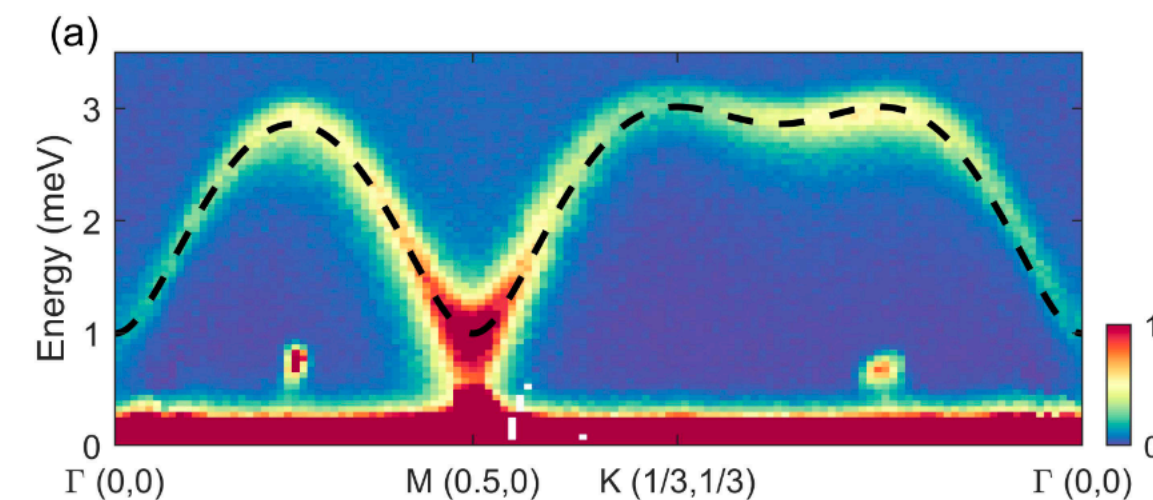
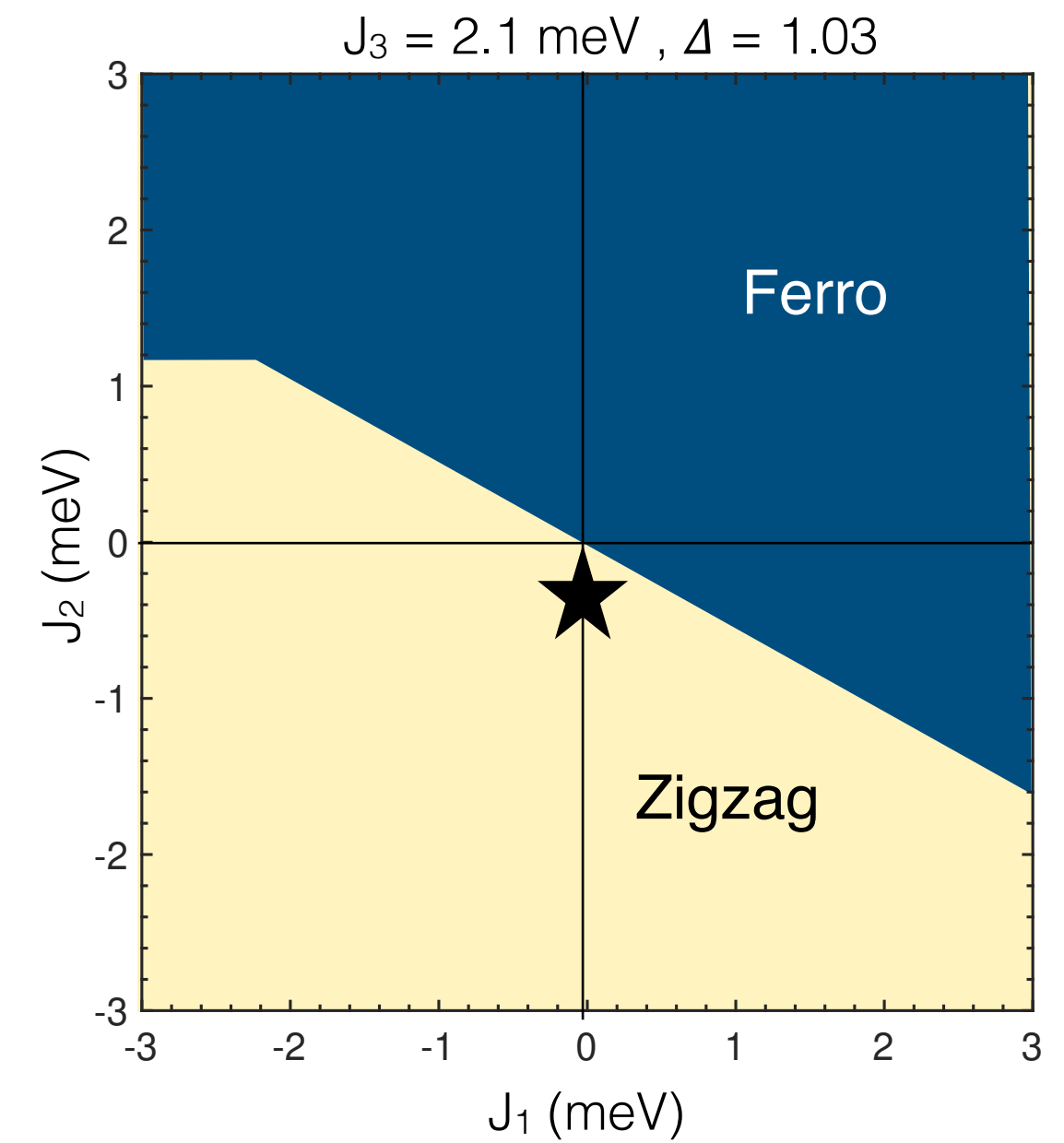
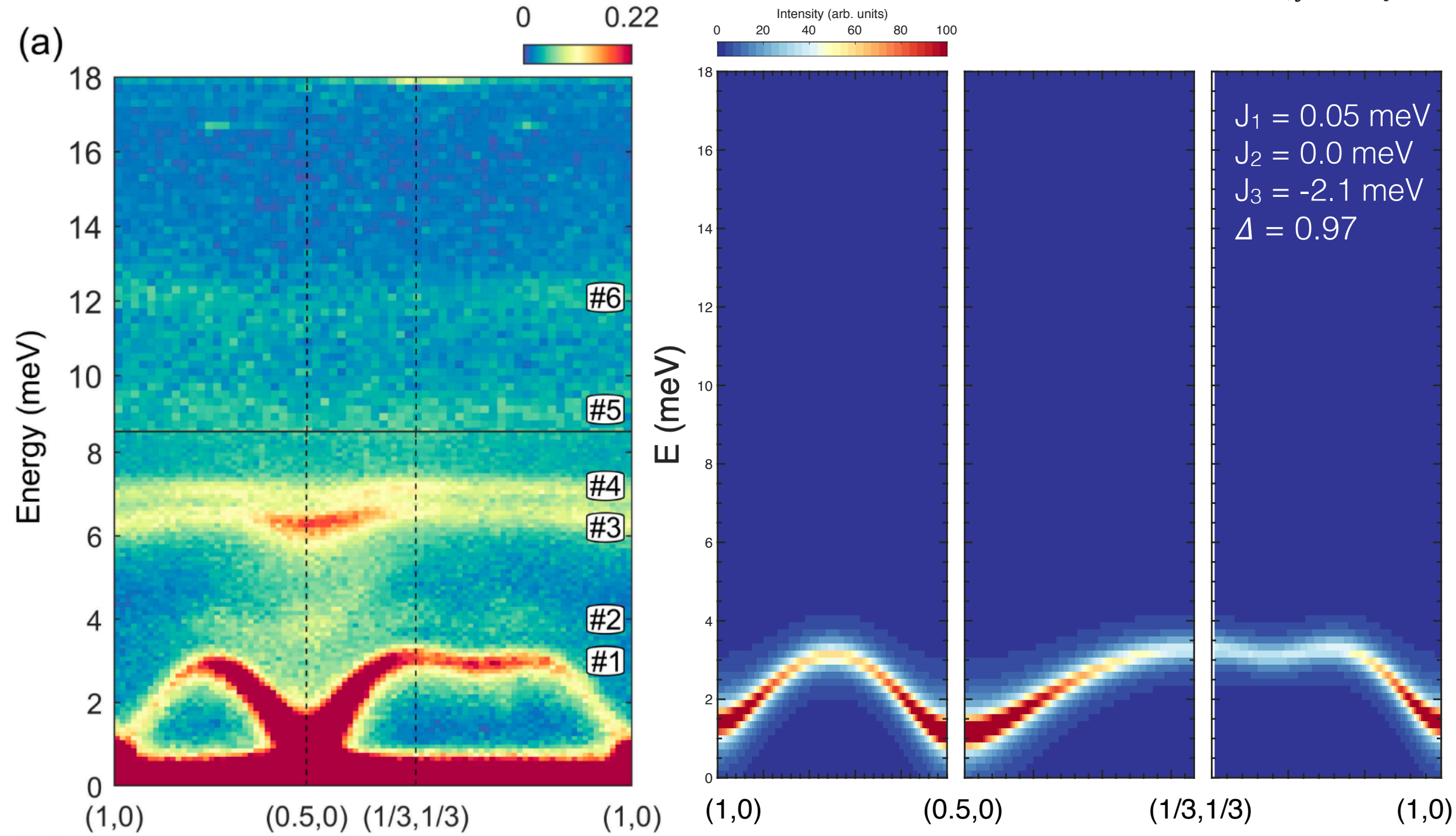


J_1 - J_2 - J_3 model with weak Ising anisotropy

$$H = \sum_{n=1}^3 J_n \sum_{i,j} (S_i^x S_j^x + S_i^y S_j^y + \Delta S_i^z S_j^z)$$

W. Chen et al., Phys. Rev. B 103, L180404 (2021)

W. Yao et al., arXiv 2203.00282v1 (2022)



► A weak J_1 interaction necessary to stabilise the $\mathbf{k} = (1/2 \ 0 \ 0)$ phase

$Na_2Co_2TeO_6$: relevance of Kitaev interactions?

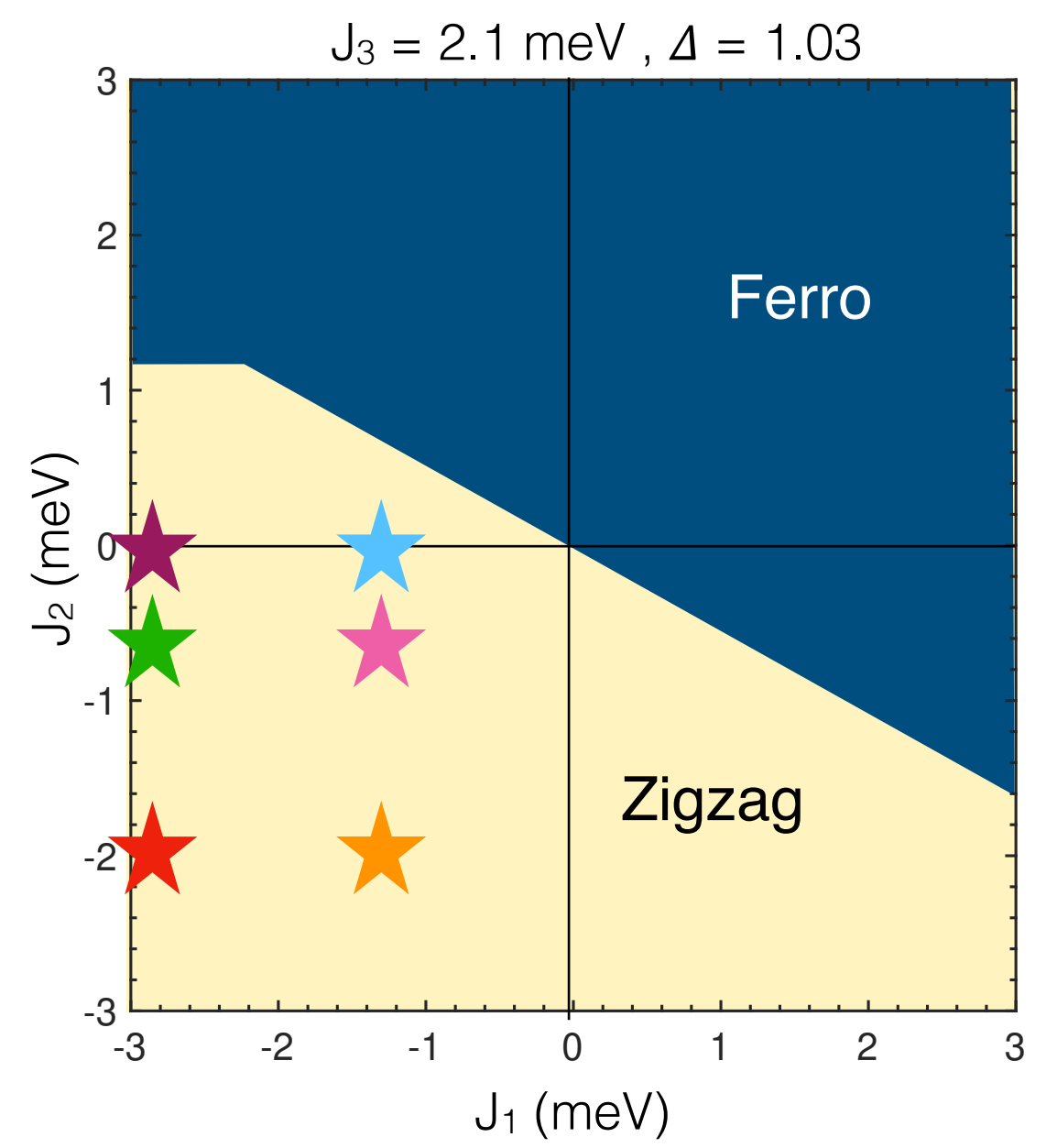
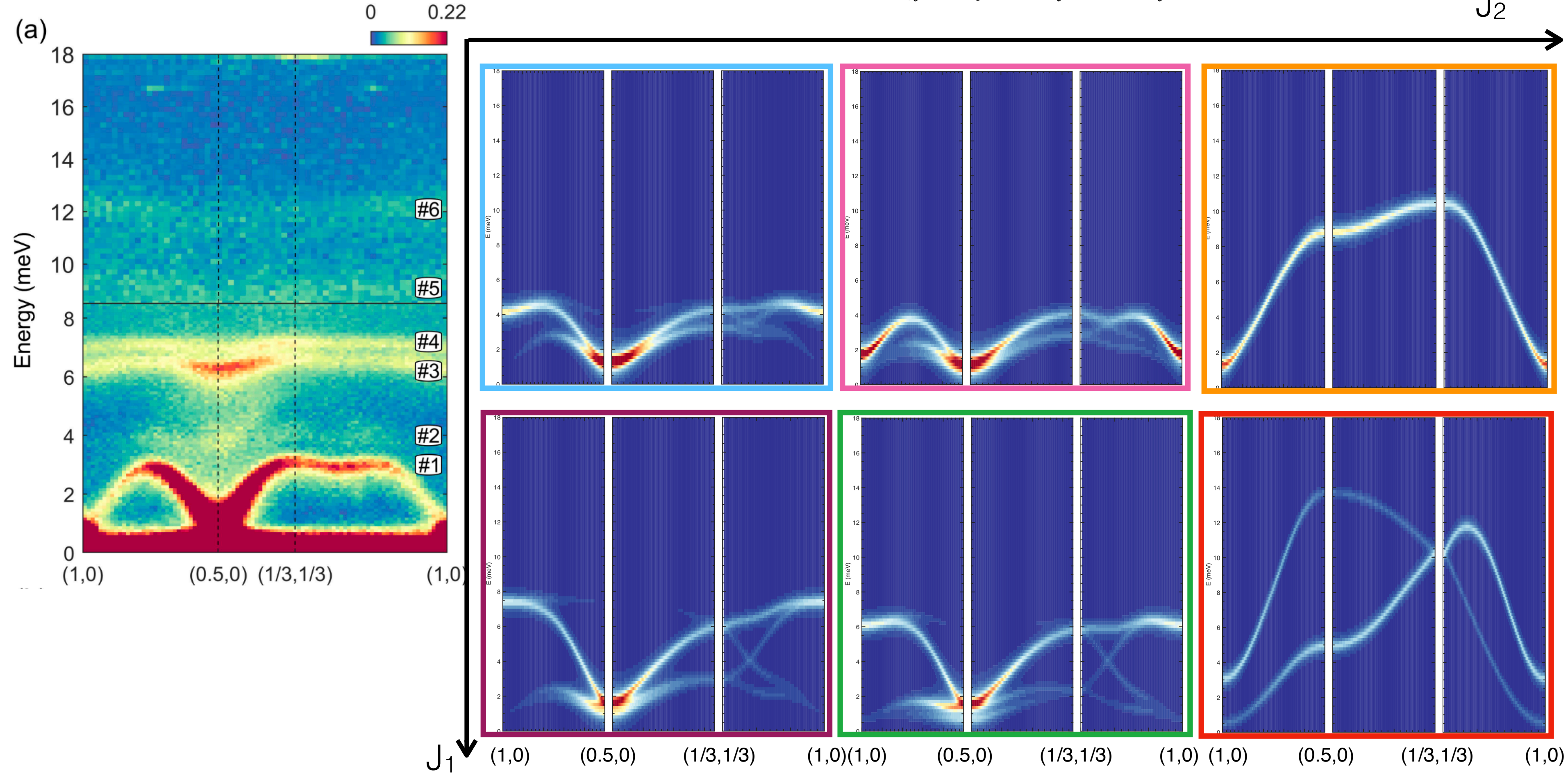


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► Another ingredient is necessary: bond dependent interactions? ... to be continued