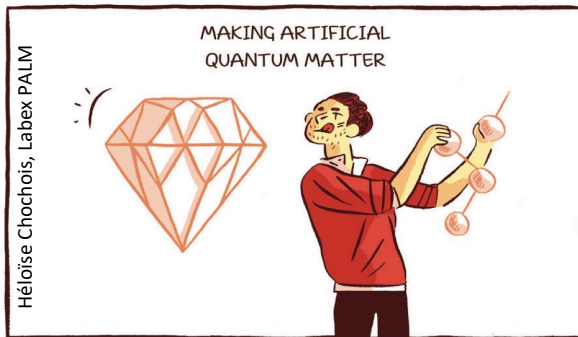


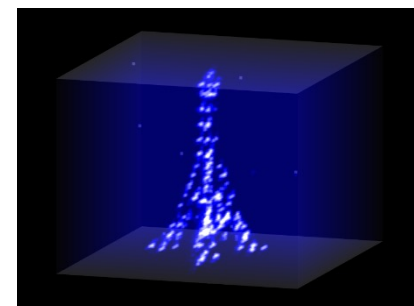
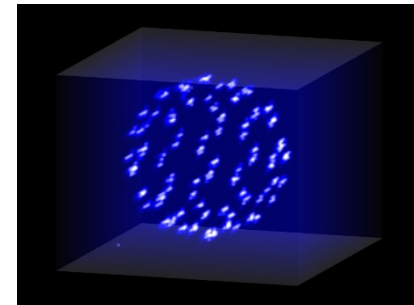
Magnetism and spin squeezing with arrays of Rydberg atoms



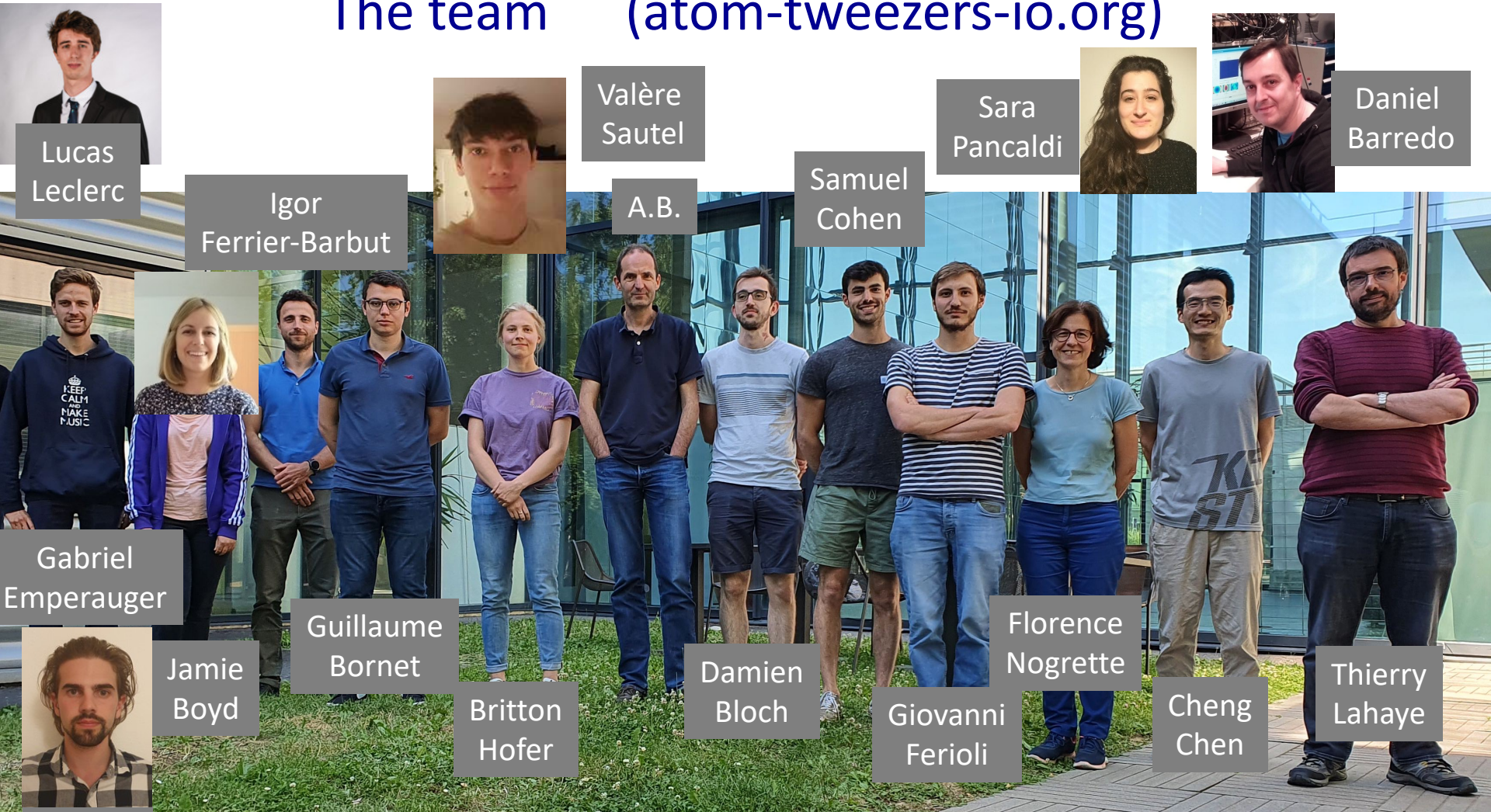
Antoine Browaeys

*Laboratoire Charles Fabry,
Institut d'Optique, CNRS, FRANCE*

Congrès SFP, july 6th 2023

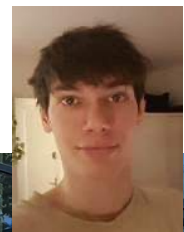


The team (atom-tweezers-io.org)



Lucas Leclerc

Igor Ferrier-Barbut

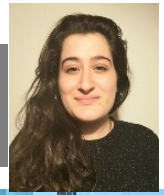


Valère Sautel

A.B.

Samuel Cohen

Sara Pancaldi



Daniel Barredo



Gabriel Emperauger



Bastien Gély



Jamie Boyd



Guillaume Bornet



Britton Hofer



Damien Bloch



Giovanni Ferioli



Florence Nogrette



Cheng Chen



Thierry Lahaye

Theory: N. Yao (Harvard), A. Läuchli (Lausanne), T. Roscilde (Lyon), H-P Büchler (Stuttgart), D. Chang (ICFO), F. Robicheaux (Perdew)



The team (atom-tweezers-io.org)



Lucas Leclerc



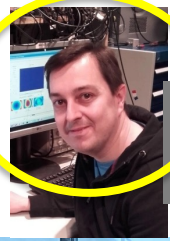
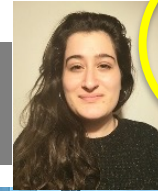
Igor Ferrier-Barbut

Valère Sautel

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The team (atom-tweezers-io.org)



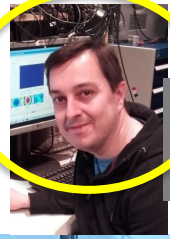
Lucas
Leclerc



Valère
Sautel



Sara
Pancaldi



Daniel
Barredo

Igor
Ferrier-Barbut

A.B.

Samuel
Cohen



Gabriel
Emperauger



Guillaume
Bo



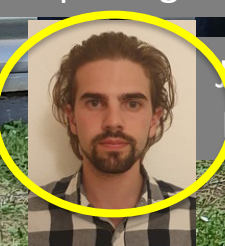
Florencia



Cheng
Chen



Thierry
Lahaye



Bastien
Gély

Jamie
Boyd

Looking for PhDs
& postdocs !!



Many-body physics with synthetic matter

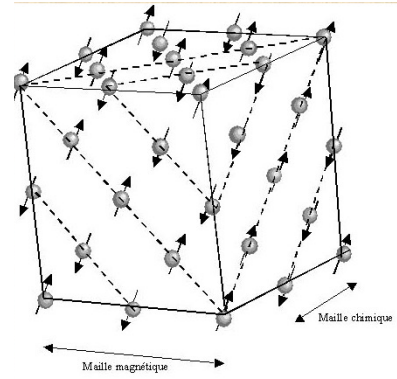
Goal: Understand ensembles of **interacting quantum particles**



superfluidity



superconductivity



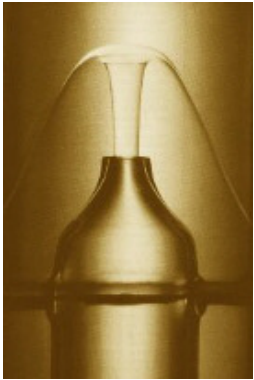
magnetism



neutron star

Many-body physics with synthetic matter

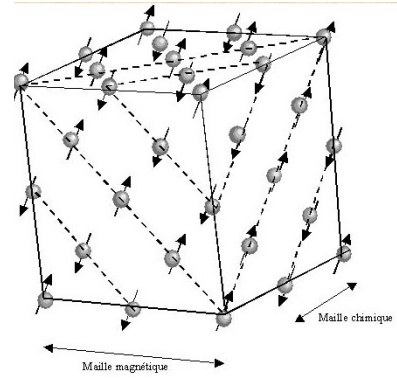
Goal: Understand ensembles of **interacting quantum particles**



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magnetism



neutron star

Open questions: Phase diagram, **dynamics** (hard for $N > 40$...)
Topology, disorder, **entanglement**,...

Many-body physics with synthetic matter

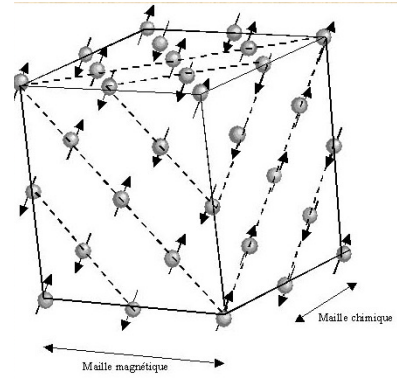
Goal: Understand ensembles of **interacting quantum particles**



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superconductivity

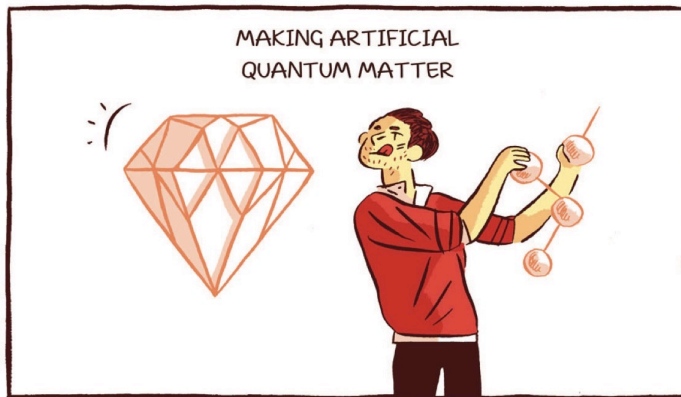


magnetism



neutron star

Open questions: Phase diagram, **dynamics** (hard for $N > 40 \dots$)
Topology, disorder, **entanglement**,...



R.P. Feynman

Use experimental control to

Implement **many-body Hamiltonians**
(including “mathematical” ones...)

Larger **tunability** than « real » systems

Many-body physics with synthetic matter

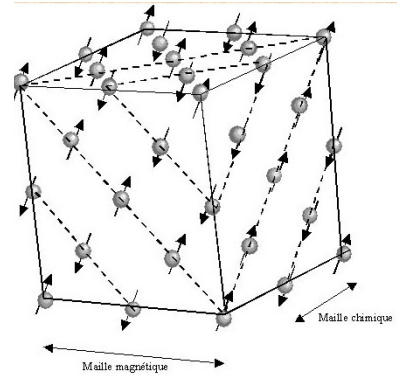
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superfluidity



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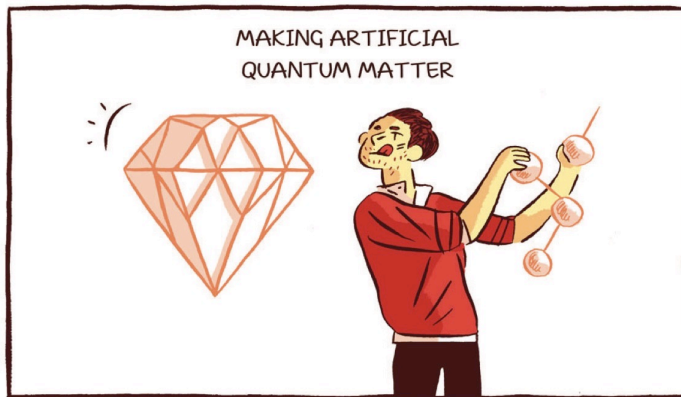


magnetism



neutron star

Open questions: Phase diagram, **dynamics** (hard for $N > 40$...)
Topology, disorder, **entanglement**,...



R.P. Feynman

Use experimental control to

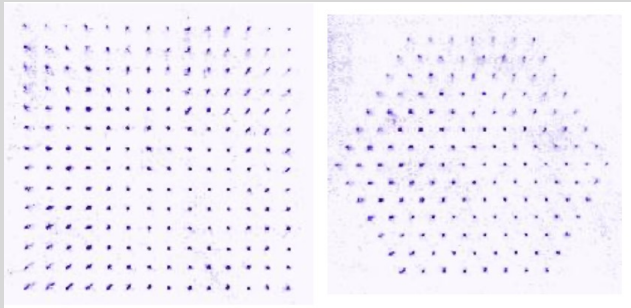
Implement **many-body Hamiltonians**
(including “mathematical” ones...)

Larger **tunability** than « real » systems

Quantum Simulation

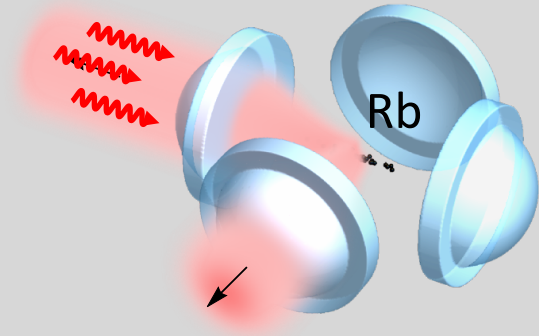
Many-body physics with synthetic quantum systems

Tunable arrays of individual Rydberg atoms



$$r \sim 10 \mu\text{m}$$

Light-induced interactions in atomic ensembles



$$r \sim \lambda \quad \text{arXiv:2207.10361} \\ \text{(Nat. Phys. 2023)}$$

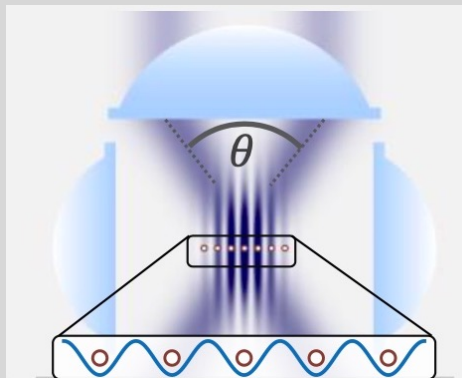
INSTITUT
d'OPTIQUE
GRADUATE SCHOOL



I. Ferrier-Barbut

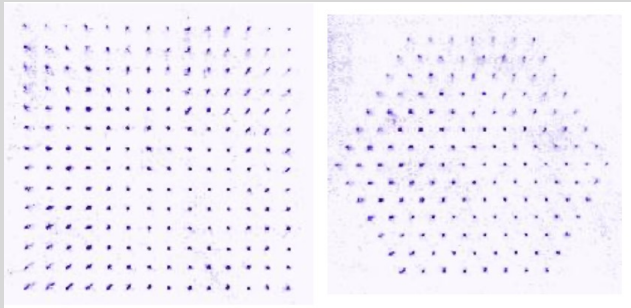
$$r \sim \lambda$$

Light-induced interactions in arrays of Dy atoms



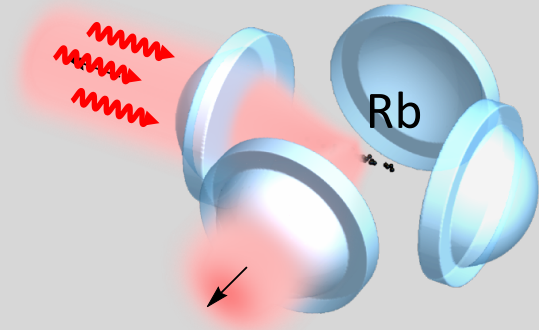
Many-body physics with synthetic quantum systems

Tunable arrays of individual Rydberg atoms



$$r \sim 10 \mu\text{m}$$

Light-induced interactions in atomic ensembles



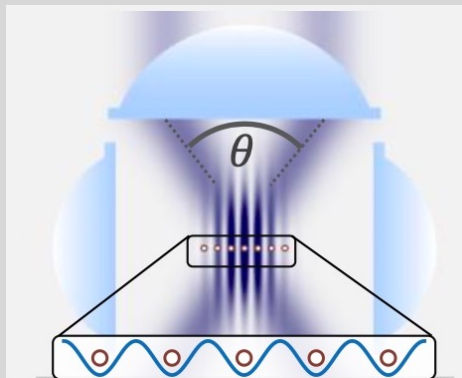
$$r \sim \lambda \quad \text{arXiv:2207.10361} \\ \text{(Nat. Phys. 2023)}$$



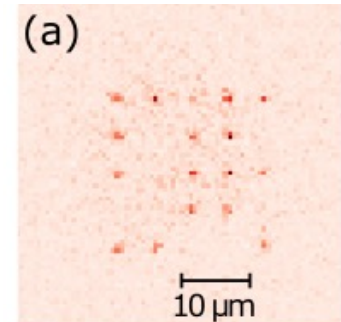
I. Ferrier-Barbut

$$r \sim \lambda$$

Light-induced interactions in arrays of Dy atoms



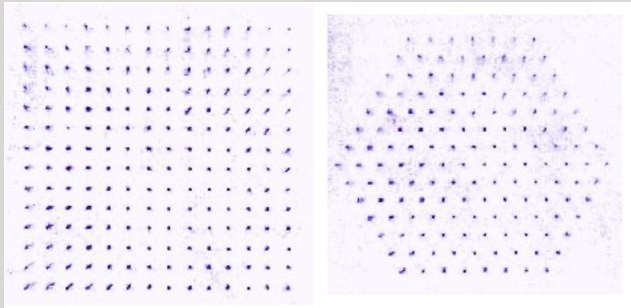
Spring 2023!!



Single Dy atoms
in tweezers

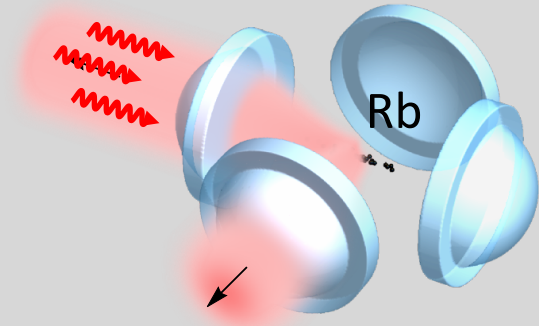
Many-body physics with synthetic quantum systems

Tunable arrays of individual Rydberg atoms



$$r \sim 10 \mu\text{m}$$

Light-induced interactions in atomic ensembles



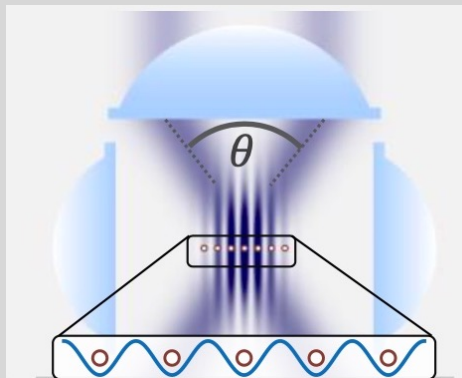
$$r \sim \lambda \quad \text{arXiv:2207.10361} \\ \text{(Nat. Phys. 2023)}$$



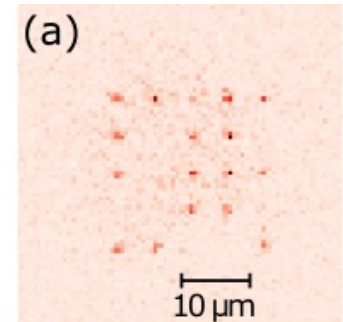
I. Ferrier-Barbut

$$r \sim \lambda$$

Light-induced interactions in arrays of Dy atoms



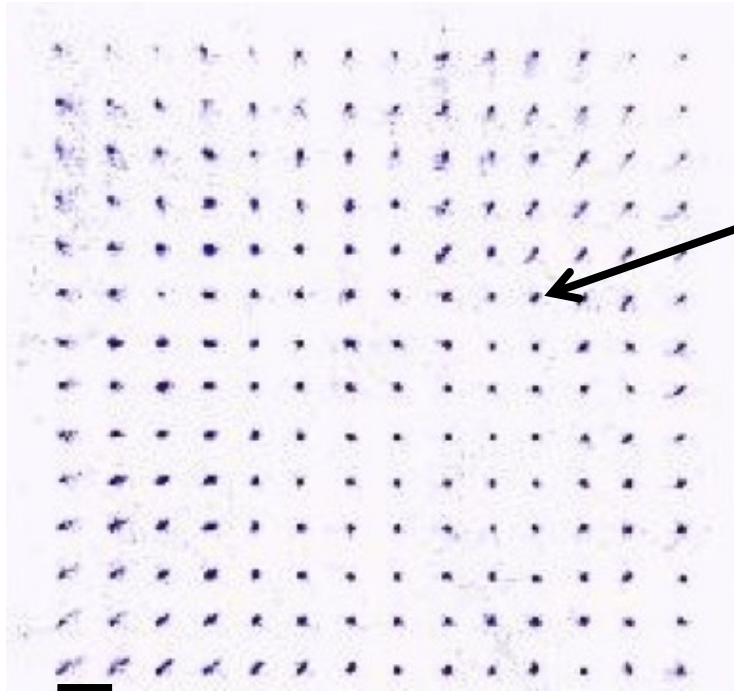
Spring 2023!!



Single Dy atoms
in tweezers

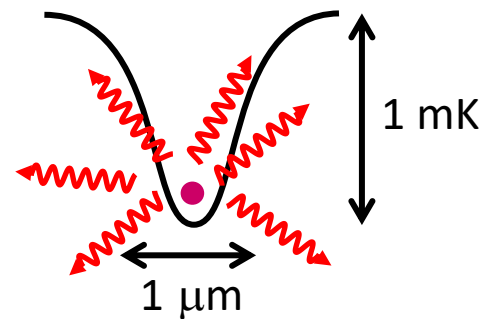
Arrays of interacting Rydberg atoms

Assembled arrays of tweezers
(~200 at.)



5 μm

1 ⁸⁷Rb atom
(fluorescence)

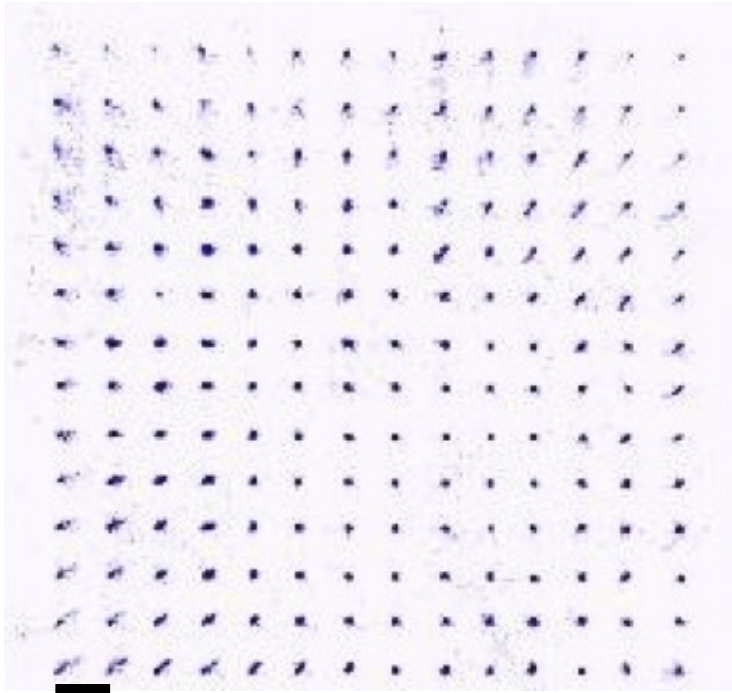


Grangier (2001)
Sortais (2007)

Fluorescence: single shot!!

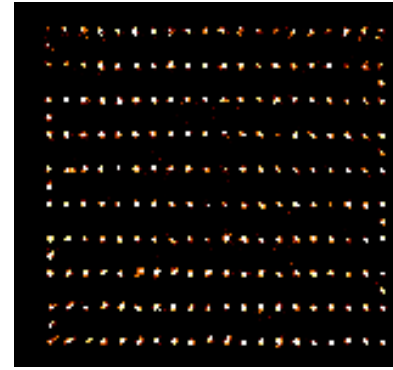
Arrays of interacting Rydberg atoms

Assembled arrays of tweezers
(~200 at.)



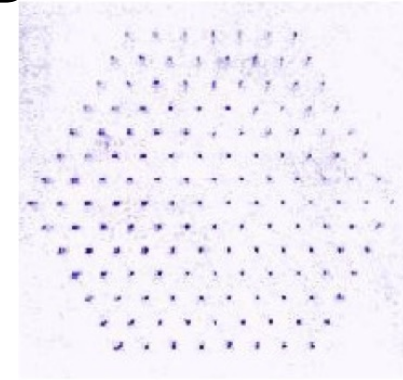
5 μm

1D



$\sim 100 \mu\text{m}$

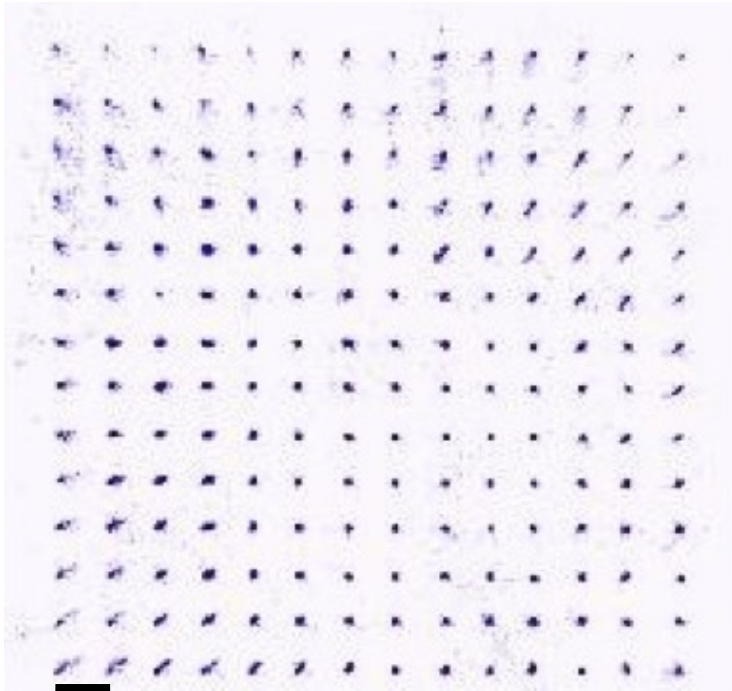
2D



Fluorescence: single shot!!

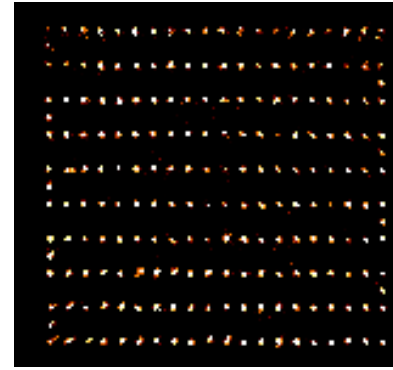
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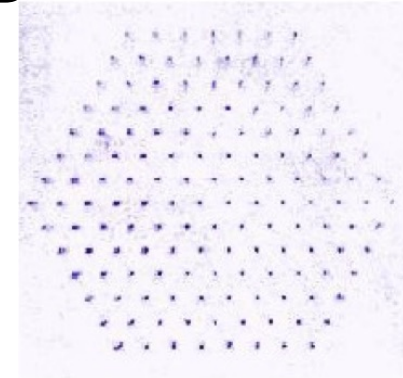
5 μm

1D

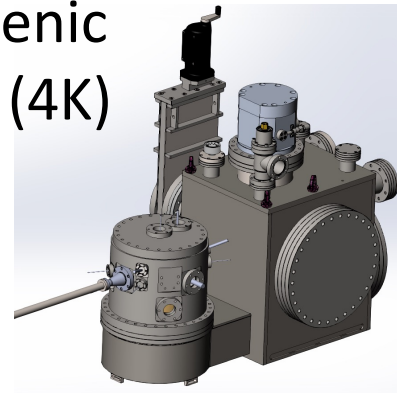


$\sim 100 \mu\text{m}$

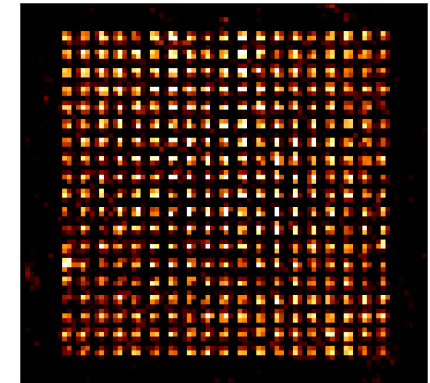
2D



Cryogenic
setup (4K)



Schymik, PRApplied 2021



Schymik, PRA 2022

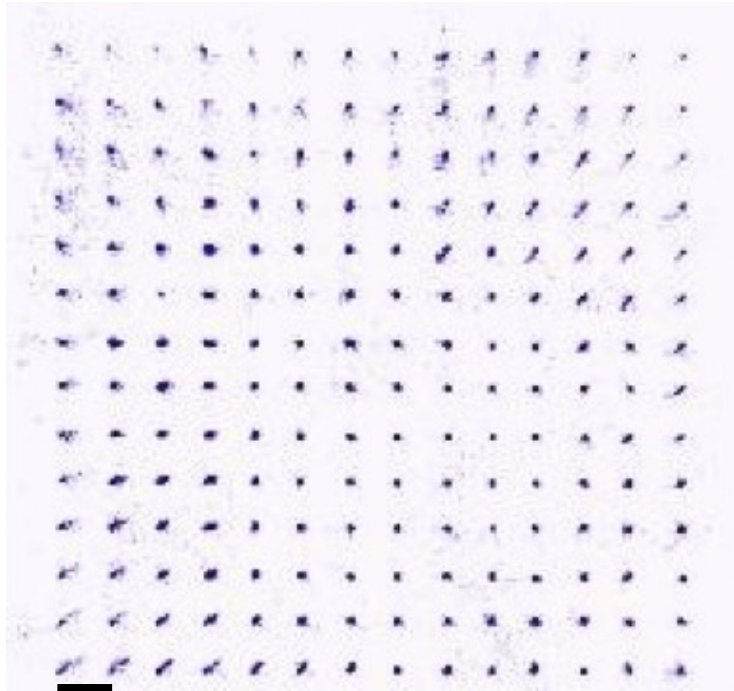
Fluorescence: single shot!!

> 320 atoms assembled

> 35% probability

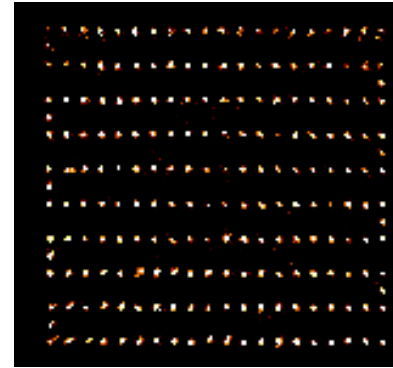
Arrays of interacting Rydberg atoms

Assembled arrays of tweezers (~200 at.)



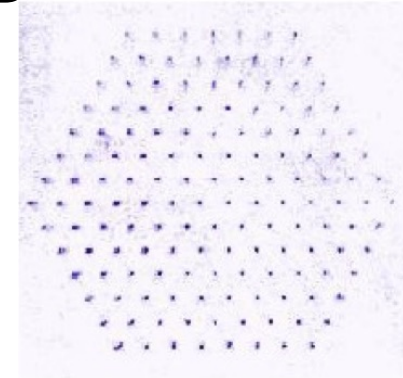
5 μm

1D

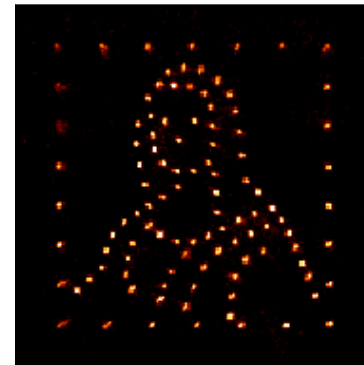


$\sim 100 \mu\text{m}$

2D



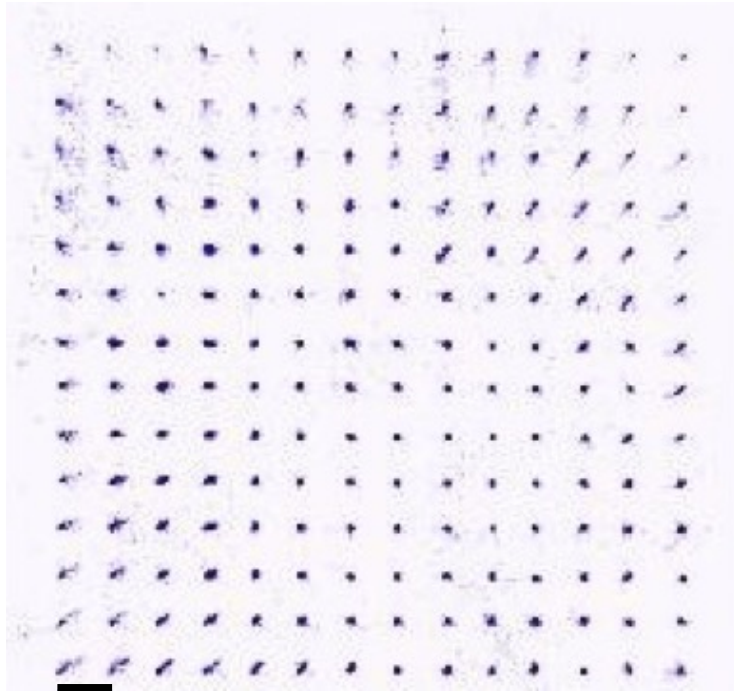
Schymik,
PRA 2021



Fluorescence: single shot!!

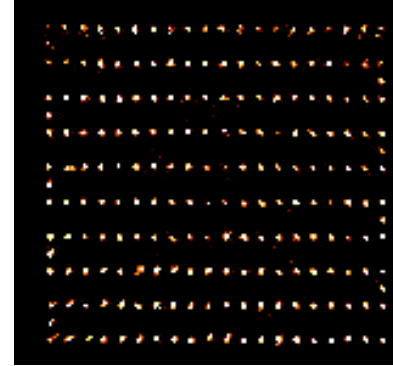
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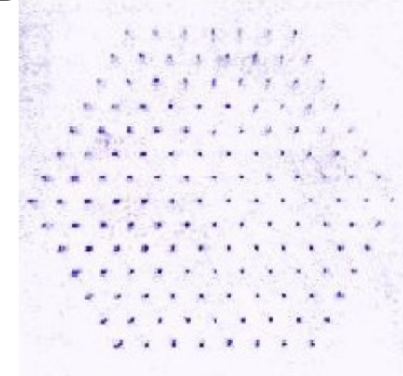
5 μm

1D

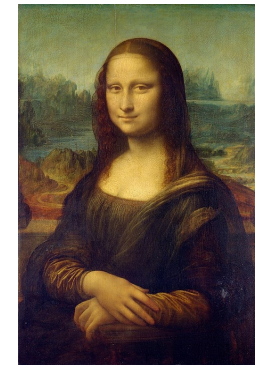
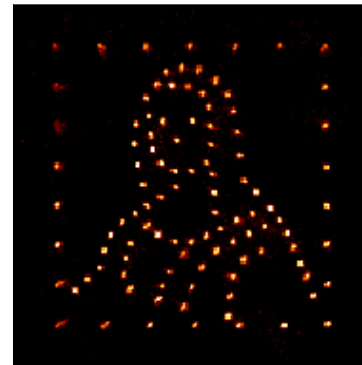


$\sim 100 \mu\text{m}$

2D



Schymik,
PRA 2021

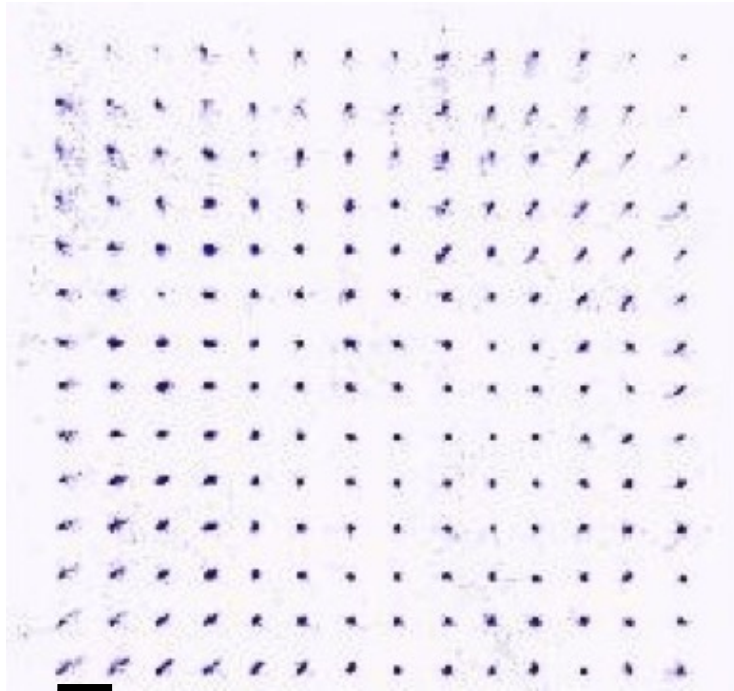


L. da Vinci

Fluorescence: single shot!!

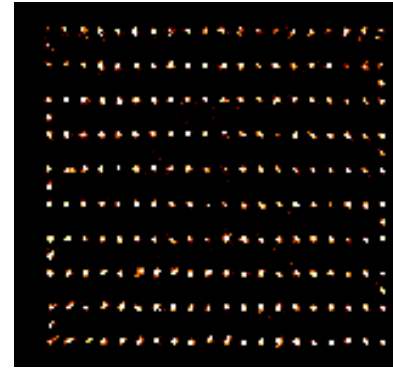
Arrays of interacting Rydberg atoms

Assembled arrays of tweezers (~200 at.)



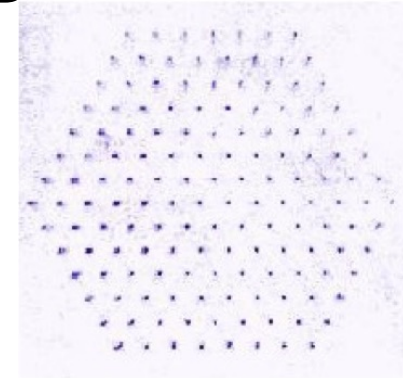
5 μm

1D

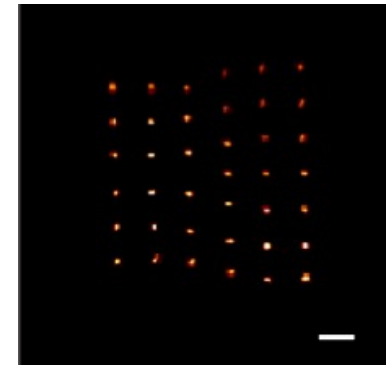
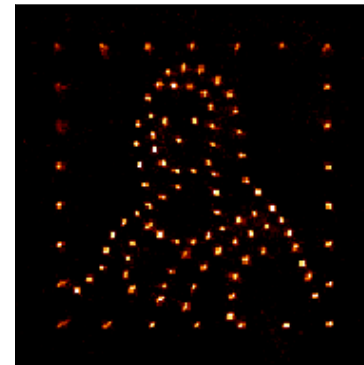


$\sim 100 \mu\text{m}$

2D



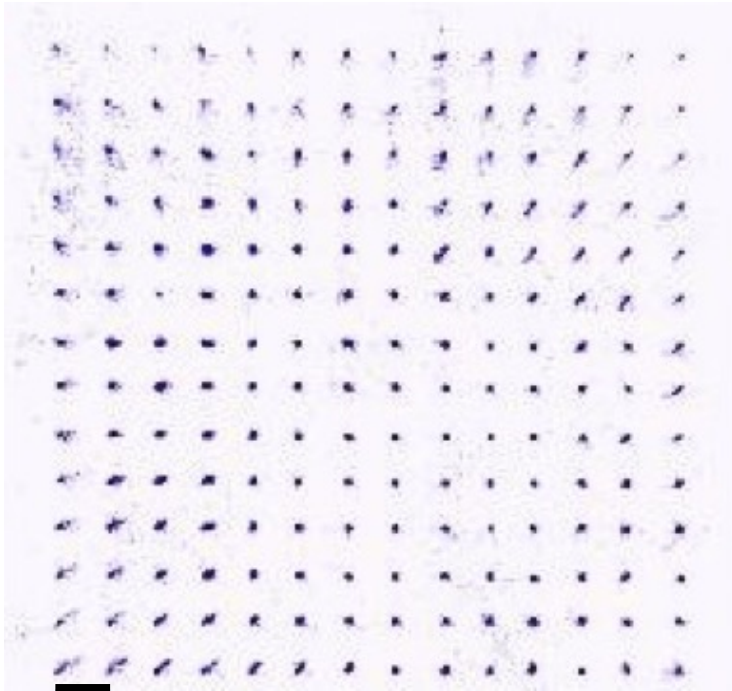
Schymik,
PRA 2021



Fluorescence: single shot!!

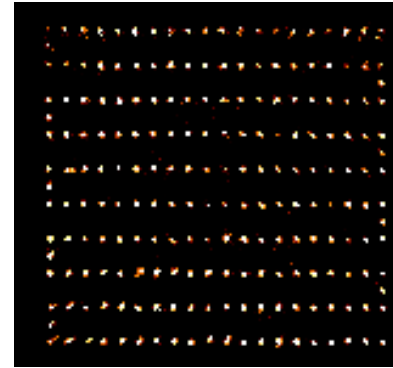
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Assembled arrays of tweezers
(~200 at.)



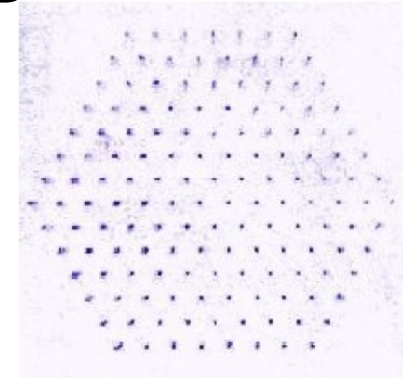
5 μm

1D

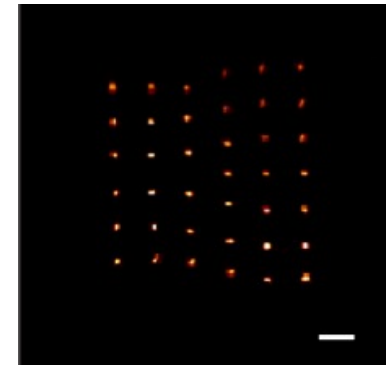
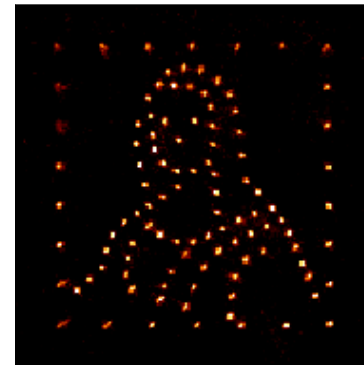


$\sim 100 \mu\text{m}$

2D

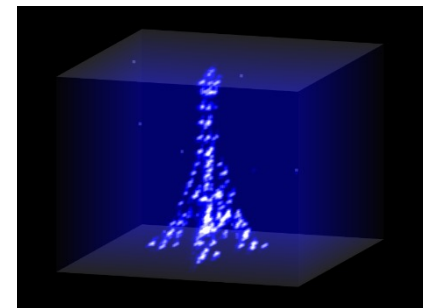
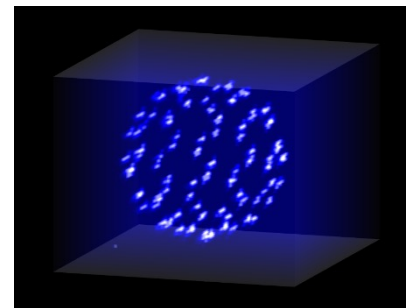


Schymik,
PRA 2021



Fluorescence: single shot!!

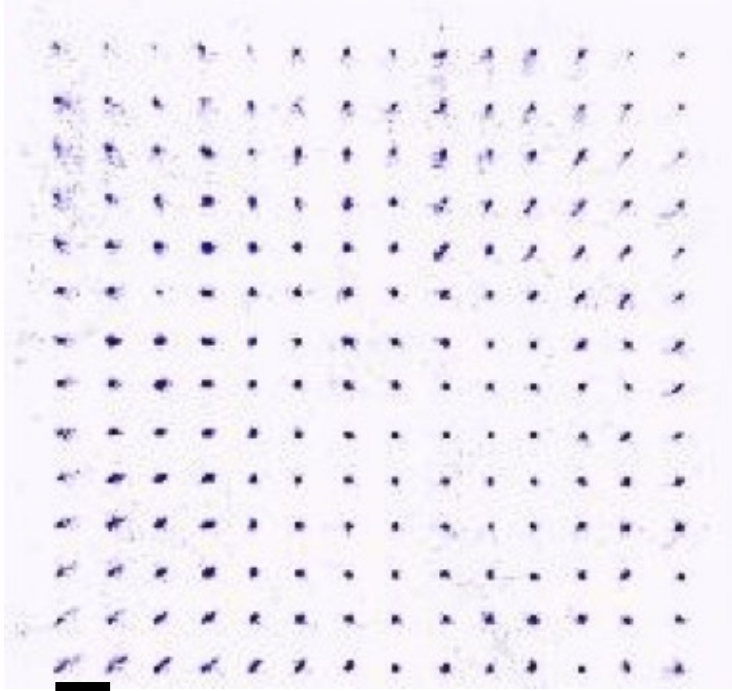
3D



(Averaged)

Arrays of interacting Rydberg atoms

**Assembled arrays of tweezers
(~200 at.)**

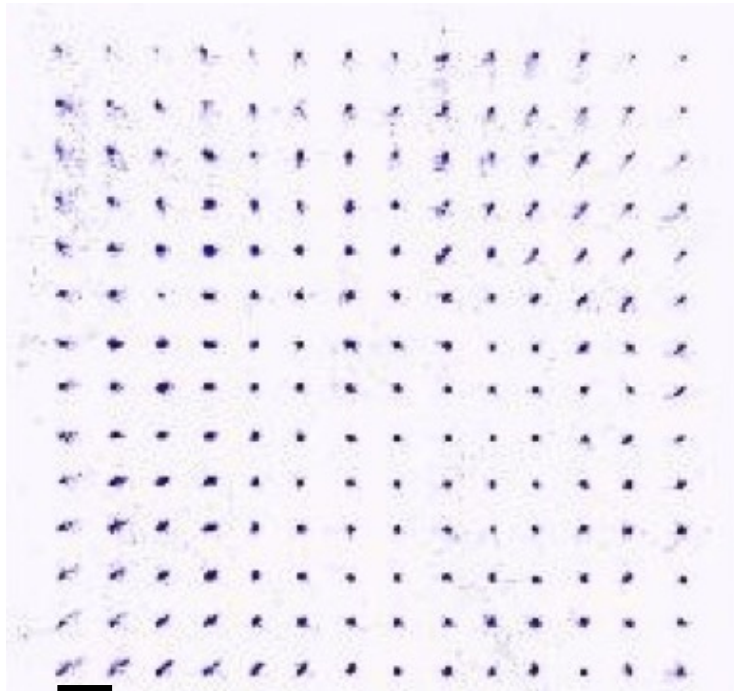


5 μm

Addressable!!

Arrays of interacting Rydberg atoms

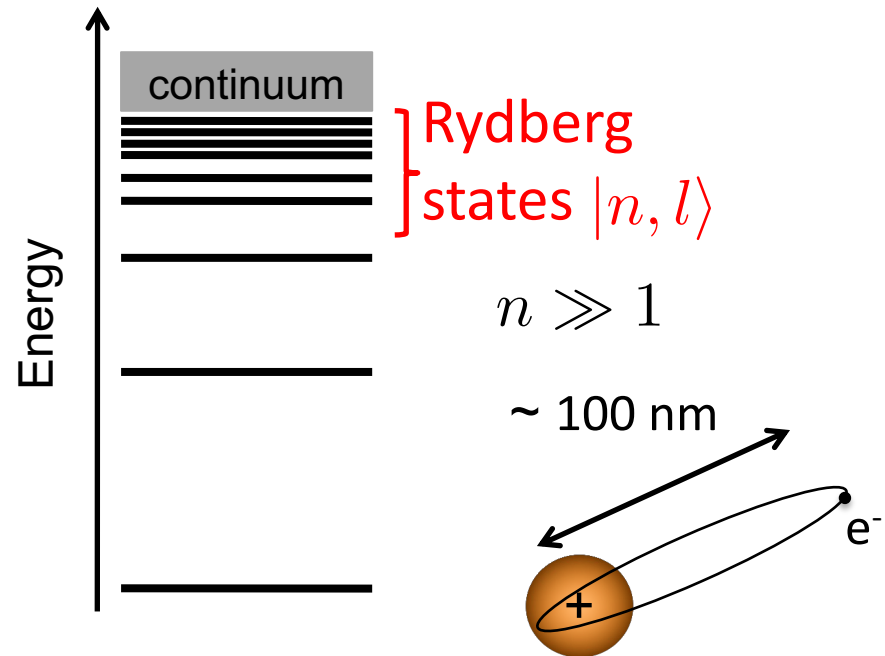
Assembled arrays of tweezers
(~200 at.)



5 μm

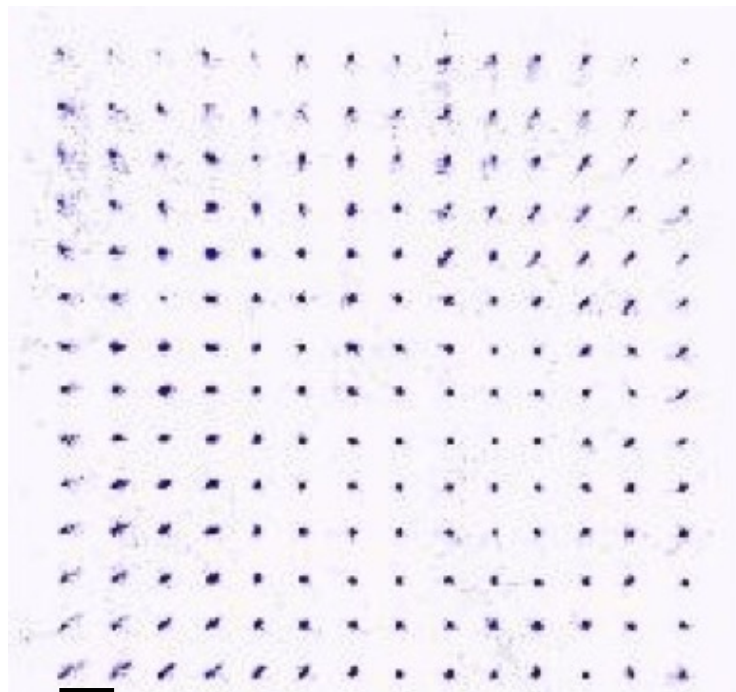
Addressable!!

Rydberg atoms



Arrays of interacting Rydberg atoms

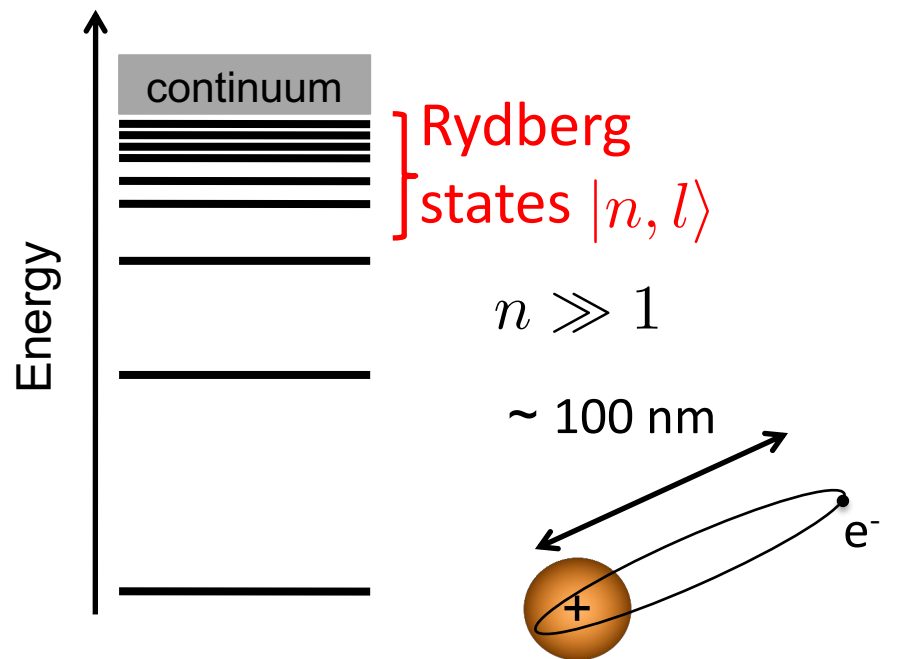
Assembled arrays of tweezers
(~200 at.)



5 μm

Addressable!!

Rydberg atoms

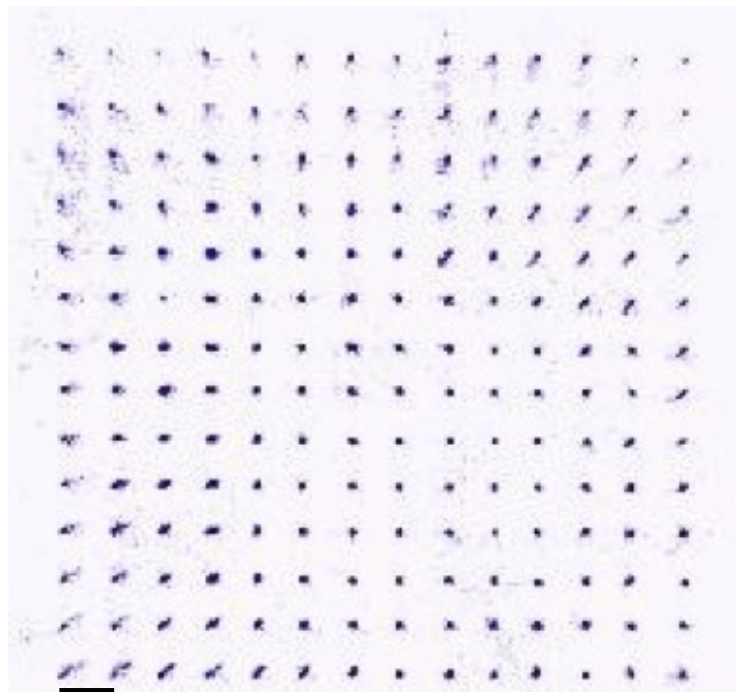


Lifetime $> 100 \mu\text{s}$

Transition dipole: $d_{n, n\pm 1} \sim n^2 e a_0$

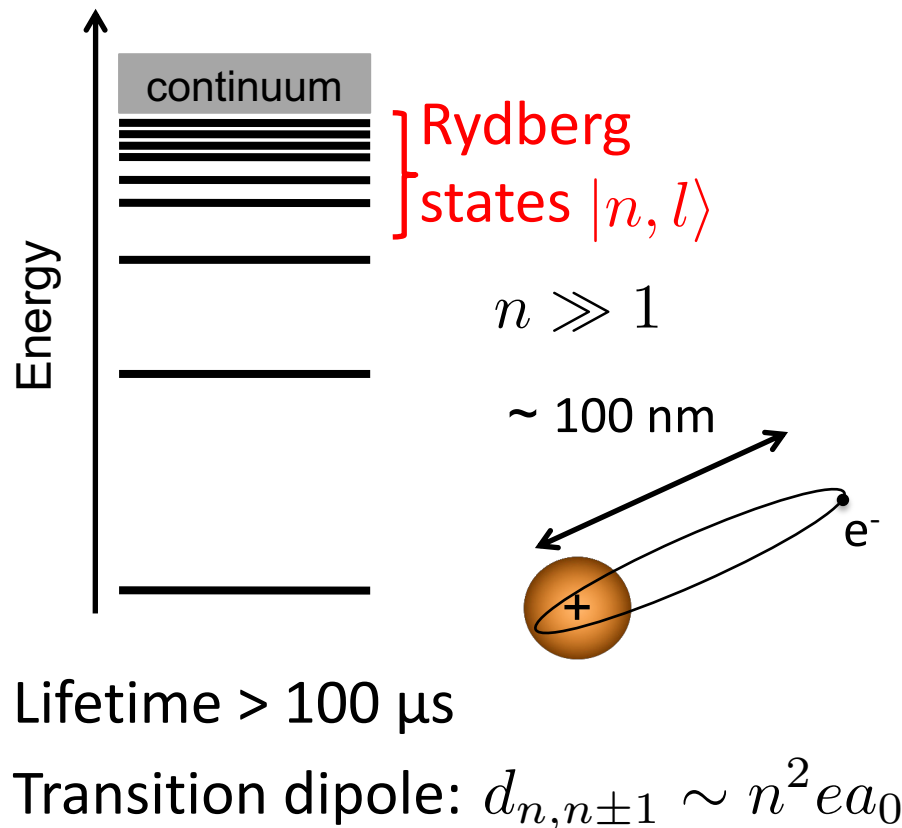
Arrays of interacting Rydberg atoms

Assembled arrays of tweezers
(~200 at.)



5 μm

Rydberg atoms

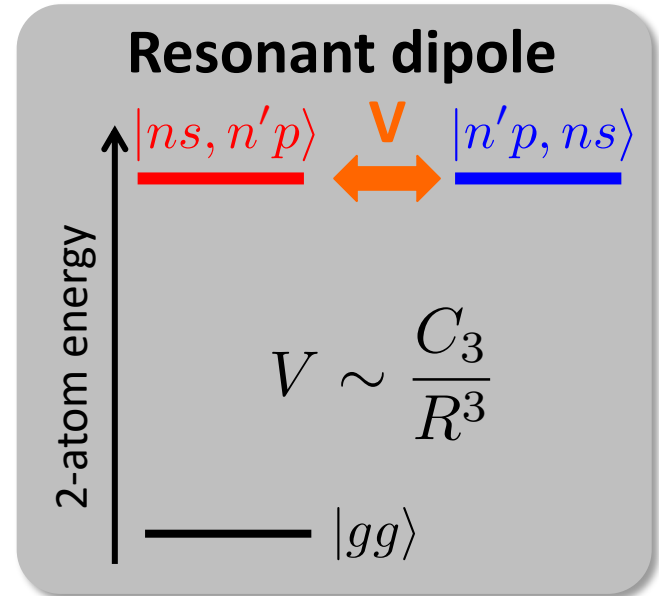
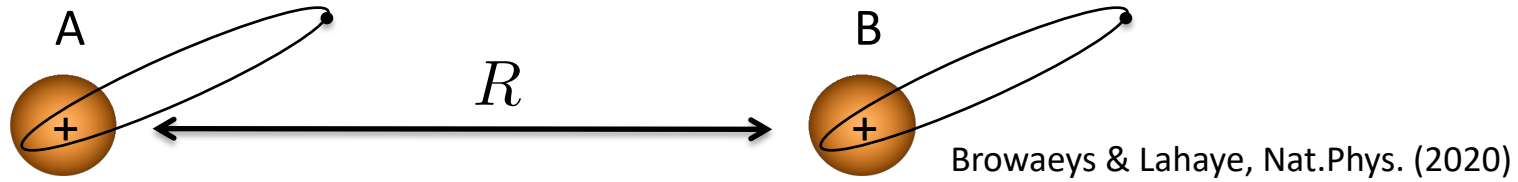


\Rightarrow Large dipole-dipole interactions

$$R = 10 \mu\text{m} \Rightarrow V_{\text{int}}/h \sim 1 - 10 \text{ MHz}$$

\Rightarrow timescales $< \mu\text{sec}$

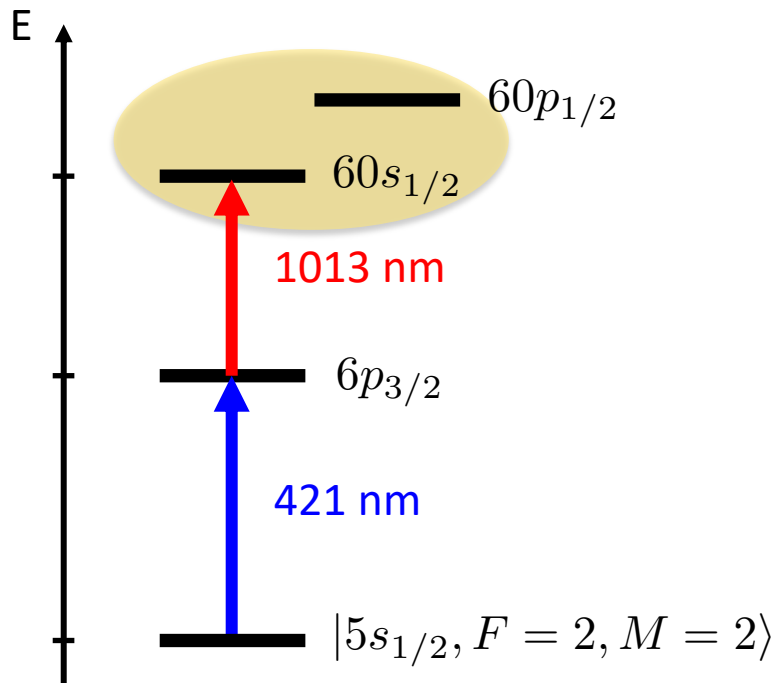
Interactions between Rydberg atoms and spin models



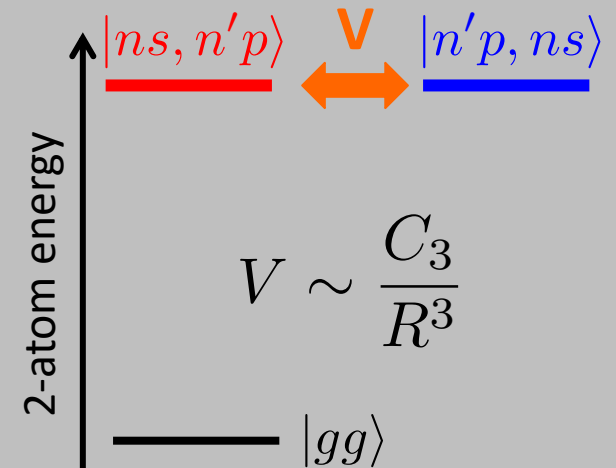
Interactions between Rydberg atoms and spin models



Browaeys & Lahaye, Nat.Phys. (2020)



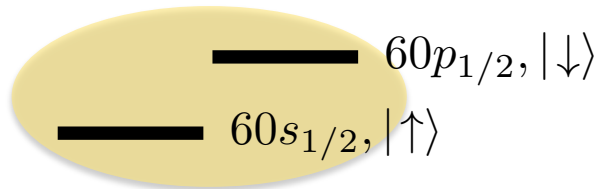
Resonant dipole



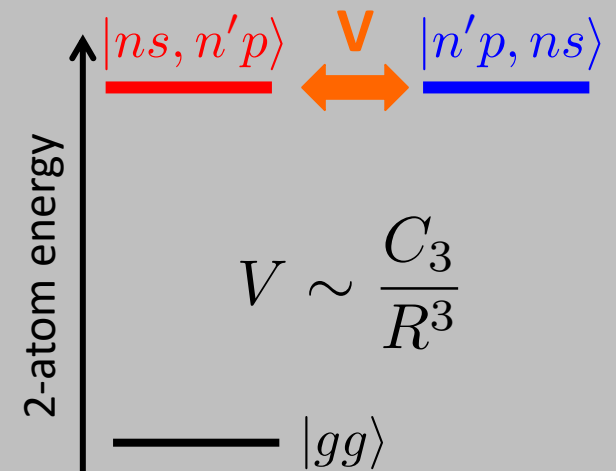
Interactions between Rydberg atoms and spin models



Browaeys & Lahaye, Nat.Phys. (2020)



Resonant dipole



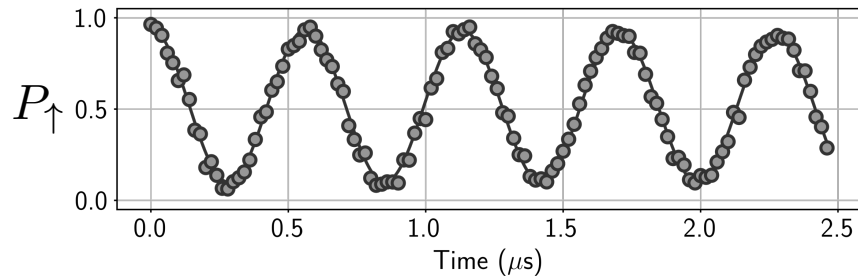
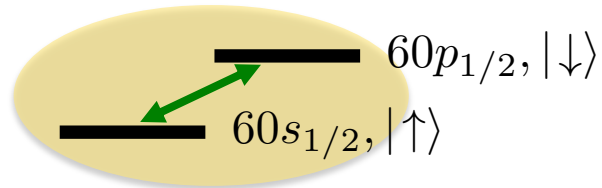
Interactions between Rydberg atoms and spin models



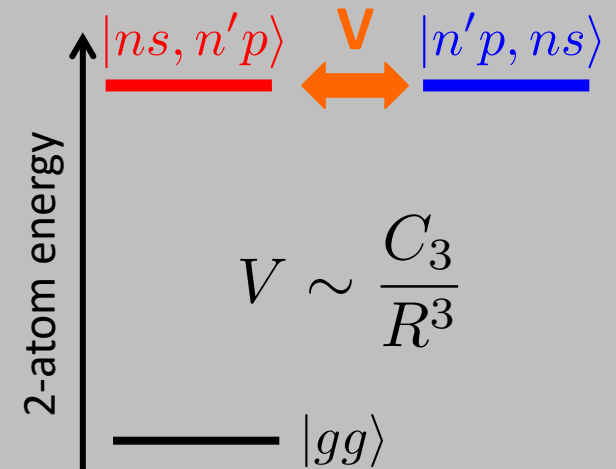
Browaeys & Lahaye, Nat.Phys. (2020)



16.7 GHz



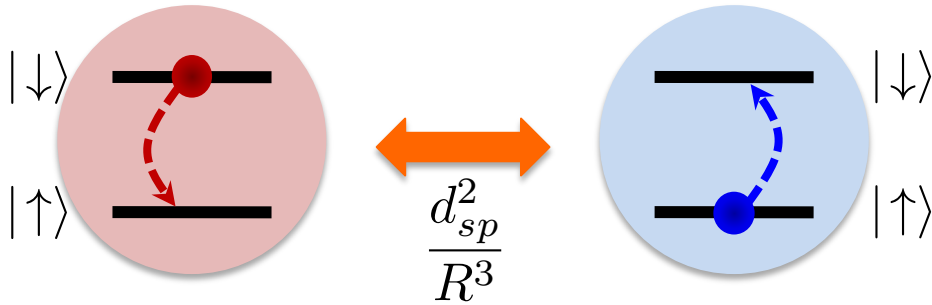
Resonant dipole



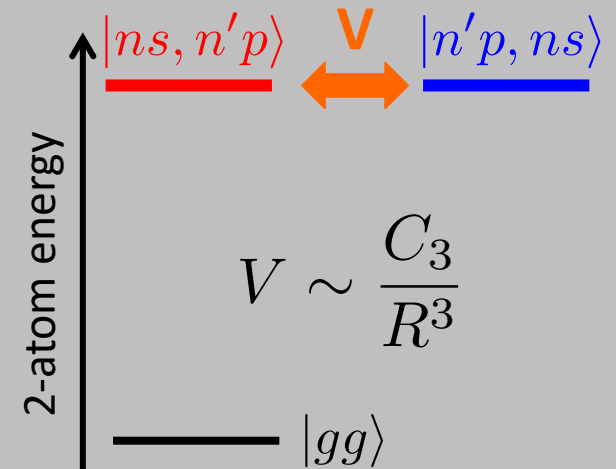
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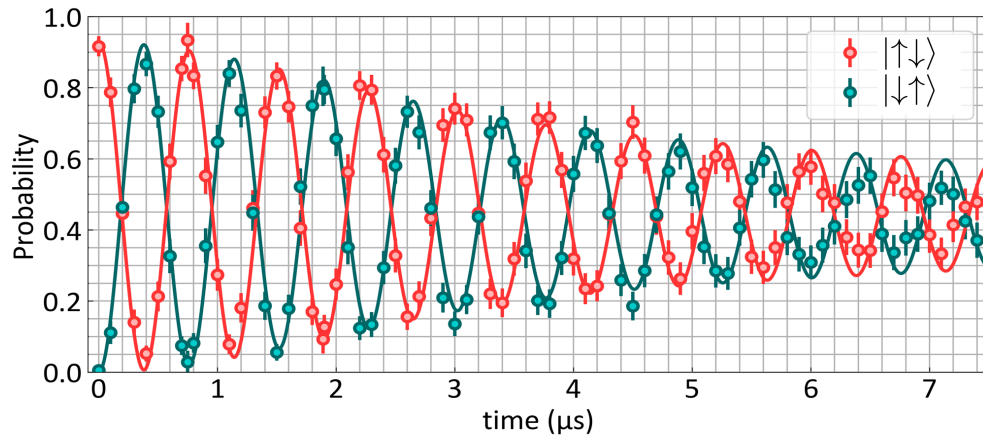
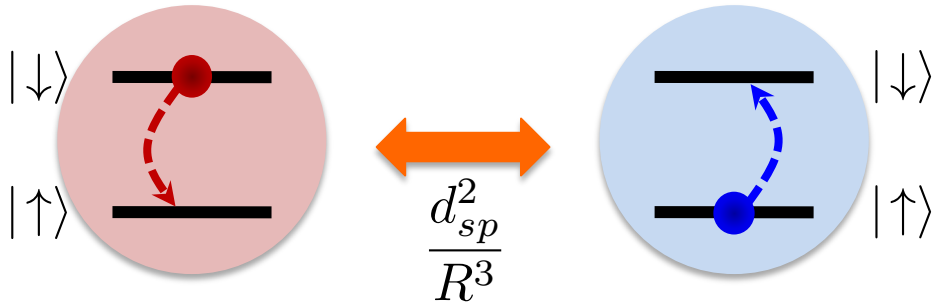
Resonant dipole



Interactions between Rydberg atoms and spin models

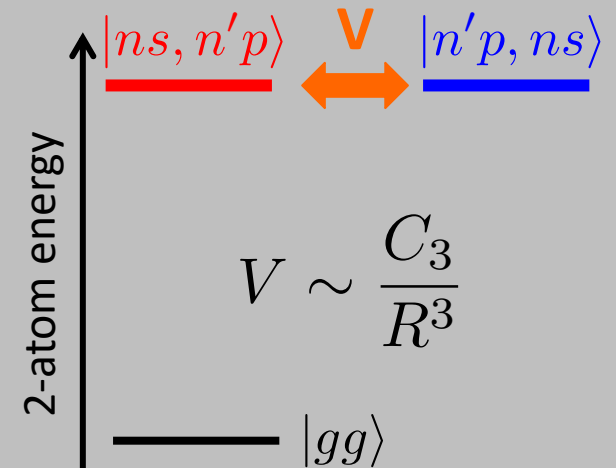


Browaeys & Lahaye, Nat.Phys. (2020)



Barredo PRL (2015), de Léséleuc, PRL (2017)

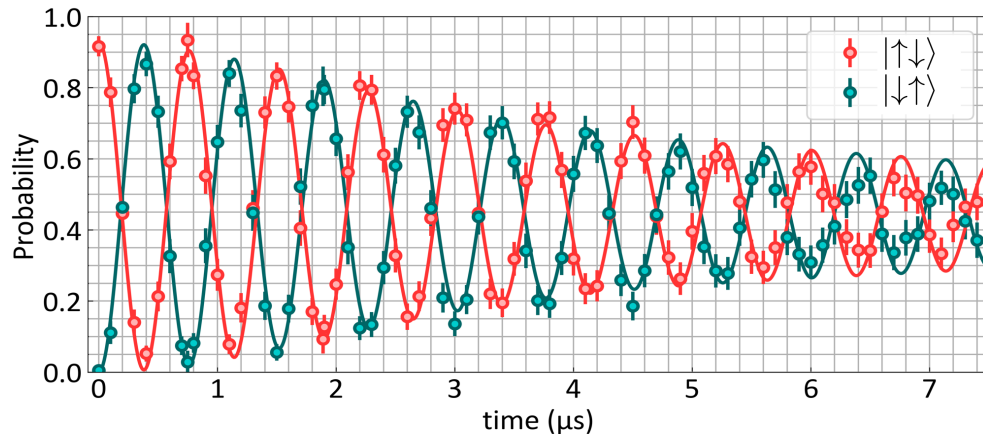
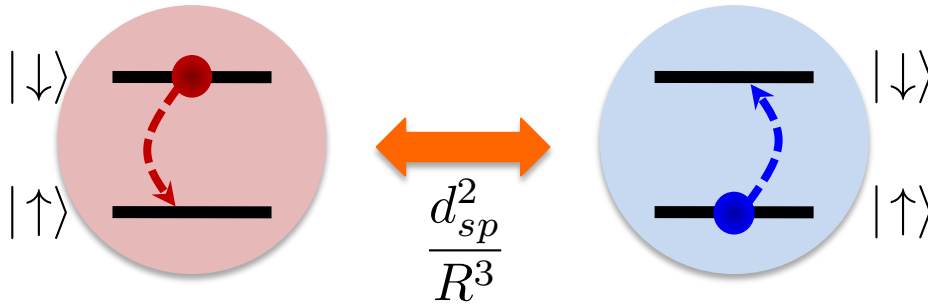
Resonant dipole



Interactions between Rydberg atoms and spin models



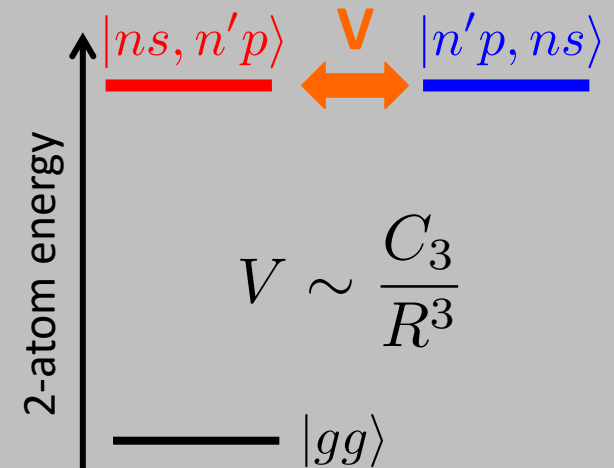
Browaeys & Lahaye, Nat.Phys. (2020)



Barredo PRL (2015), de Léséleuc, PRL (2017)

$$J_{ij} = C_3 / R_{ij}^3$$

Resonant dipole



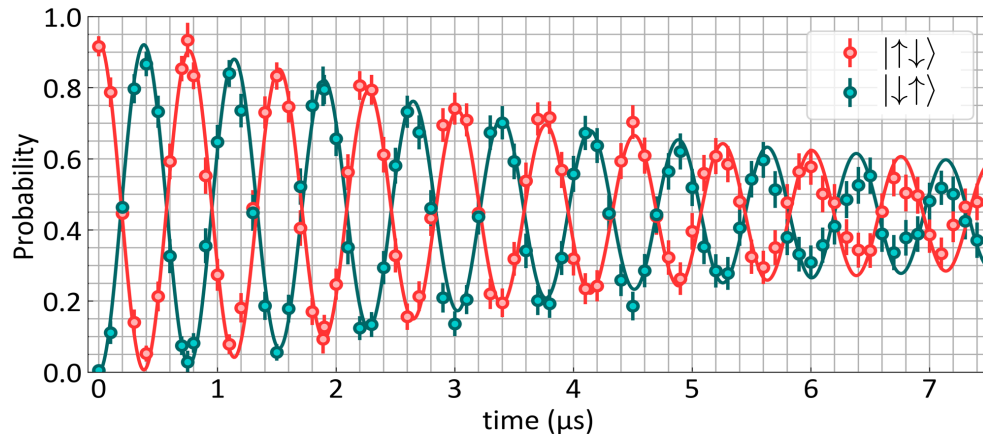
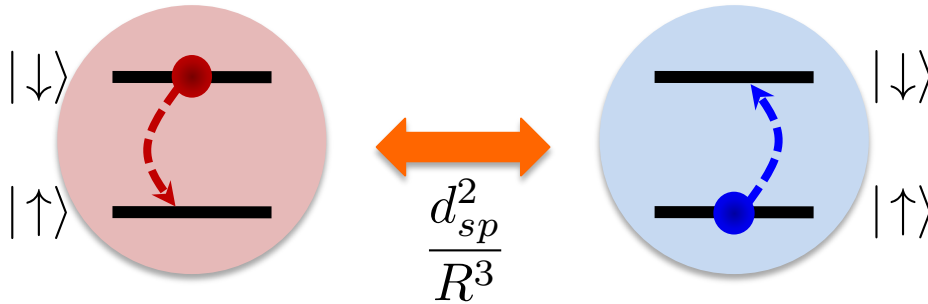
XY model

$$\hat{H} = \sum_{i \neq j} J_{ij} (\hat{\sigma}_i^+ \hat{\sigma}_j^- + \hat{\sigma}_i^- \hat{\sigma}_j^+)$$

Interactions between Rydberg atoms and spin models



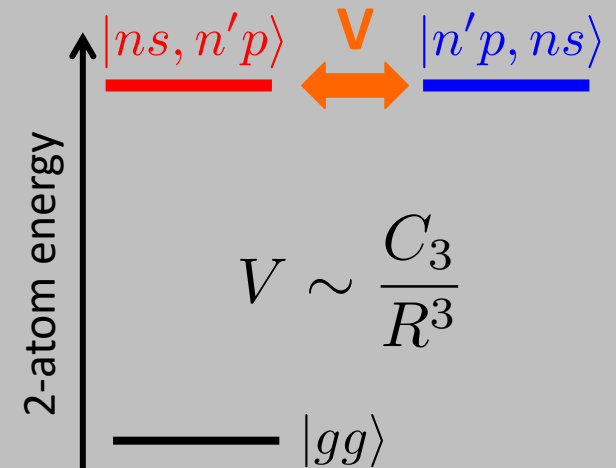
Browaeys & Lahaye, Nat.Phys. (2020)



Barredo PRL (2015), de Léséleuc, PRL (2017)

$$J_{ij} = C_3 / R_{ij}^3$$

Resonant dipole



XY model

$$\begin{aligned} \hat{H} &= \sum_{i \neq j} J_{ij} (\hat{\sigma}_i^+ \hat{\sigma}_j^- + \hat{\sigma}_i^- \hat{\sigma}_j^+) \\ &= \sum_{i \neq j} 2J_{ij} (\hat{\sigma}_i^x \hat{\sigma}_j^x + \hat{\sigma}_i^y \hat{\sigma}_j^y) \end{aligned}$$

Outline

1. Dipolar XY magnet with resonant dipole interactions
2. Spin squeezing using dipolar interaction

Outline

1. Dipolar XY magnet with resonant dipole interactions

C. Chen *et al.*, Nature 2023

2. Spin squeezing using dipolar interaction

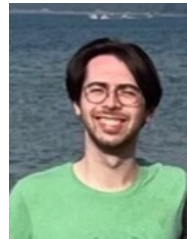


N. Yao

+



M. Zaletel



M. Bintz

V. Liu
J. Hauschild
S. Chatterjee
(Berkeley)



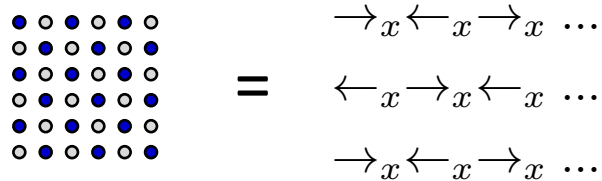
A. Läuchli + M. Schuler
(Innsbruck)

Ising versus XY model = classical versus quantum...

Ising model

$$\hat{H} = \sum_{\langle i,j \rangle} J_{ij} \hat{\sigma}_i^x \hat{\sigma}_j^x$$

Antiferro $J_{ij} < 0$



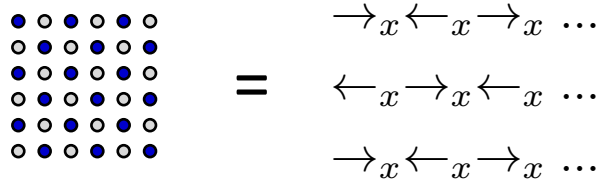
Ground state $(1/2, 1/3\dots) =$
classical Néel configurations

Ising versus XY model = classical versus quantum...

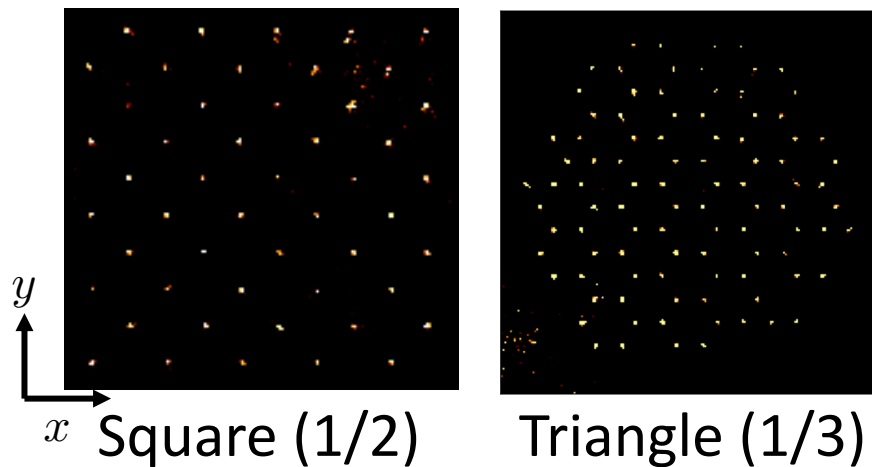
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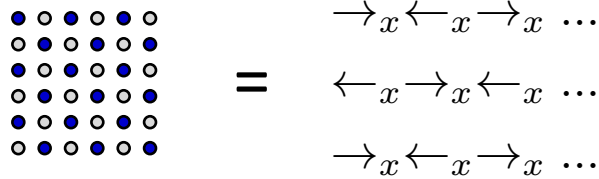
Schauss *et al.*, Nature 2013
Scholl *et al.*, Nature 2021
Ebadi *et al.*, Nature 2021
Choi *et al.*, Nature 2023...

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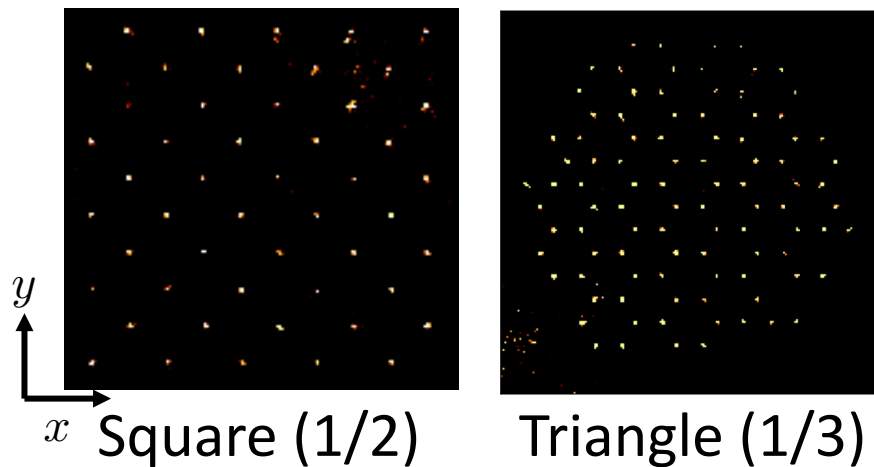
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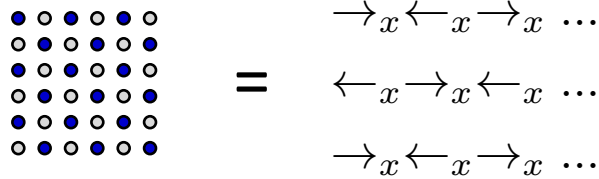


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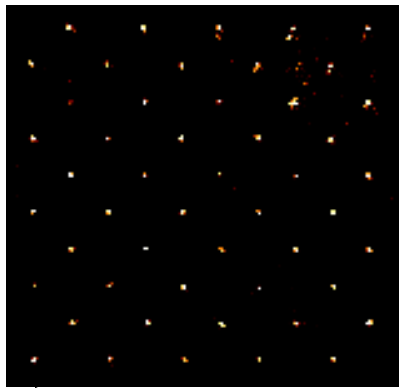
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Competing order along x / along y

$$\left| \begin{array}{c} \rightarrow x \leftarrow x \\ \leftarrow x \rightarrow x \end{array} \right\rangle + \left| \begin{array}{c} \uparrow y \downarrow y \\ \downarrow y \uparrow y \end{array} \right\rangle$$



x y
Square (1/2)

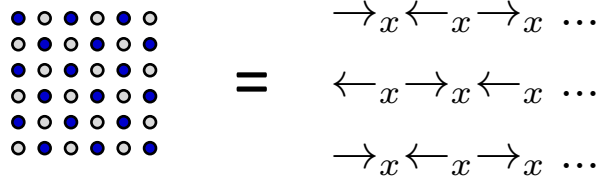
Triangle (1/3)

Ising versus XY model = classical versus quantum...

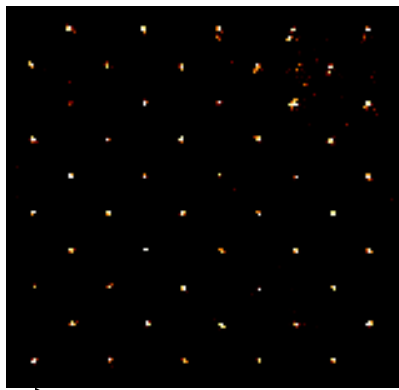
Ising model

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classical Néel configurations



Square $(1/2)$



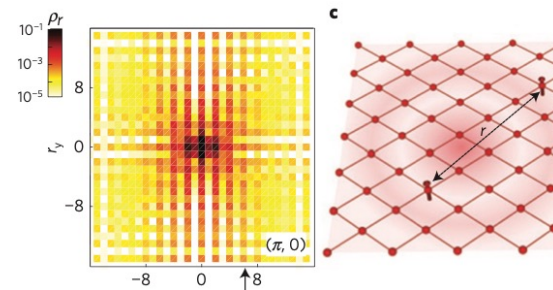
Triangle $(1/3)$

XY model

$$\hat{H} = \sum_{\langle i,j \rangle} J_{ij} (\hat{\sigma}_i^x \hat{\sigma}_j^x + \hat{\sigma}_i^y \hat{\sigma}_j^y)$$

Metal organic compound

Cu(DCOO)2 \cdot 4D2O



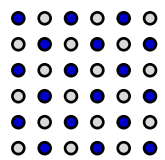
Dalla Piazza, Nat. Phys. 2017

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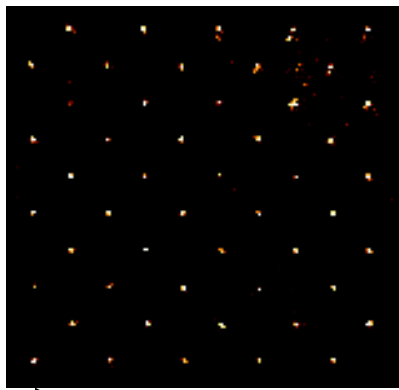
Antiferro $J_{ij} < 0$



=

$\rightarrow x \leftarrow x \rightarrow x \dots$
 $\leftarrow x \rightarrow x \leftarrow x \dots$
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Ground state $(1/2, 1/3\dots) =$
classical Néel configurations



Square $(1/2)$

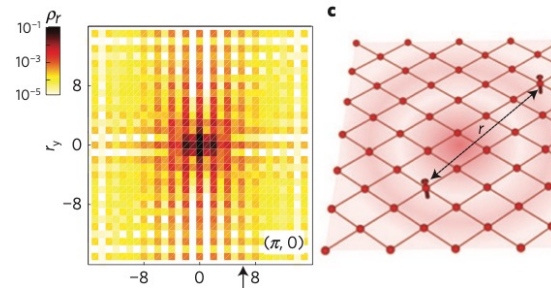


Triangle $(1/3)$

XY model

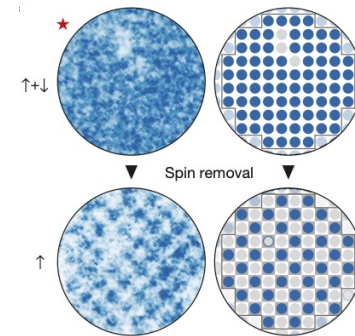
$$\hat{H} = \sum_{\langle i,j \rangle} J_{ij} (\hat{\sigma}_i^x \hat{\sigma}_j^x + \hat{\sigma}_i^y \hat{\sigma}_j^y)$$

Metal organic compound



Dalla Piazza, Nat. Phys. 2017

Atoms in lattices



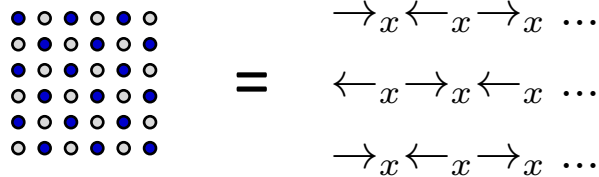
Greiner, Bloch,
Esslinger, Kuhr...

Ising versus XY model = classical versus quantum...

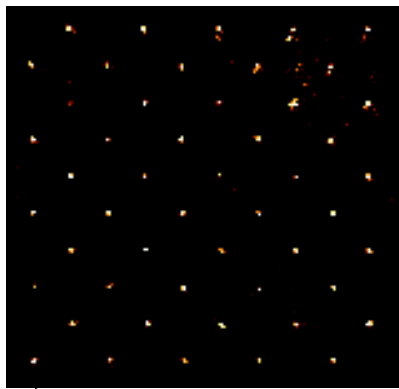
Ising model

$$\hat{H} = \sum_{\langle i,j \rangle} J_{ij} \hat{\sigma}_i^x \hat{\sigma}_j^x$$

Antiferro $J_{ij} < 0$



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classical Néel configurations



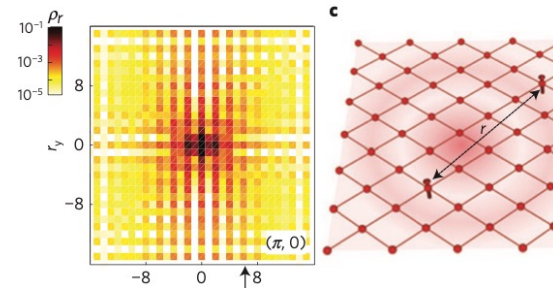
Square $(1/2)$

Triangle $(1/3)$

XY model

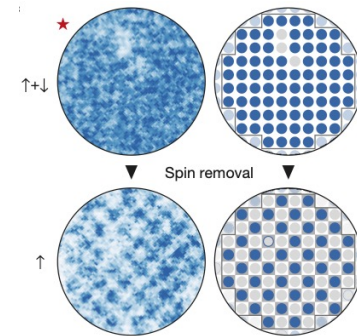
$$\hat{H} = \sum_{\langle i,j \rangle} J_{ij} (\hat{\sigma}_i^x \hat{\sigma}_j^x + \hat{\sigma}_i^y \hat{\sigma}_j^y)$$

Metal organic compound



Dalla Piazza, Nat. Phys. 2017

Atoms in lattices



Greiner, Bloch, Esslinger, Kuhr...

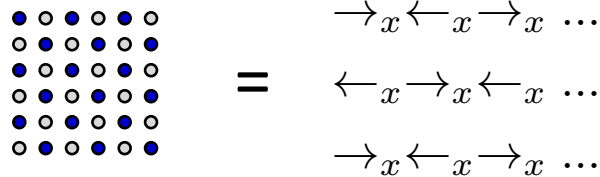
Heisenberg: $\hat{H} = \sum_{i \neq j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$

Ising versus XY model = classical versus quantum...

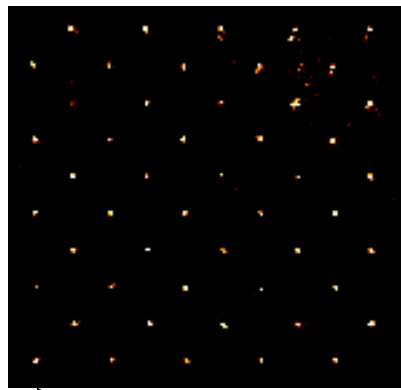
Ising model

$$\hat{H} = \sum_{\langle i,j \rangle} J_{ij} \hat{\sigma}_i^x \hat{\sigma}_j^x$$

Antiferro $J_{ij} < 0$



Ground state (1/2, 1/3...) = **classical** Néel configurations



Square (1/2)

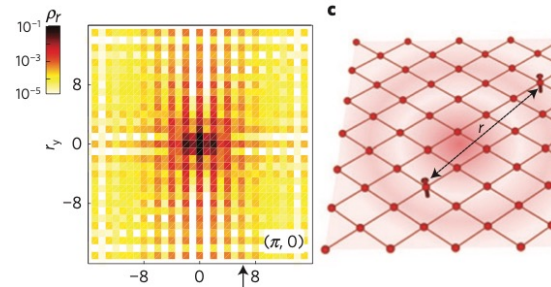


Triangle (1/3)

XY model

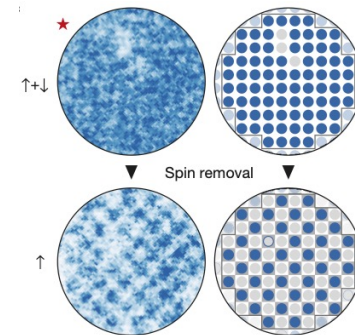
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Metal organic compound



Dalla Piazza, Nat. Phys. 2017

Atoms in lattices



Greiner, Bloch, Esslinger, Kuhr...

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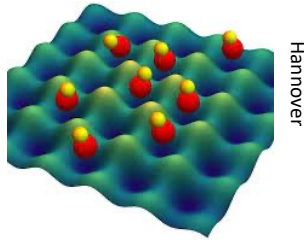
Short-range interactions

Dipolar XY magnets: possibility of Long-Range Order

Dipolar interactions $\Rightarrow 1/R^3$

Polar molecules

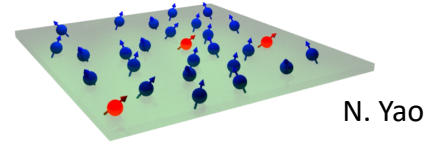
KRb, NaRb Bakr, Ye, Ni...



Magnetic atoms

Cr, Er, Dy
Laburthe, Ferlino, Pfau,
Ketterle, Modugno...

Defects in solid

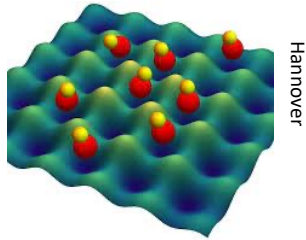


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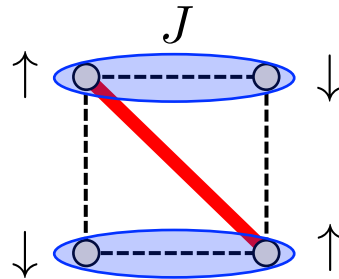
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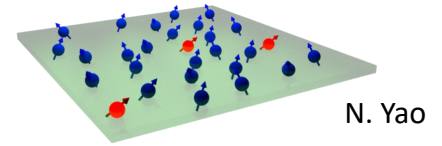


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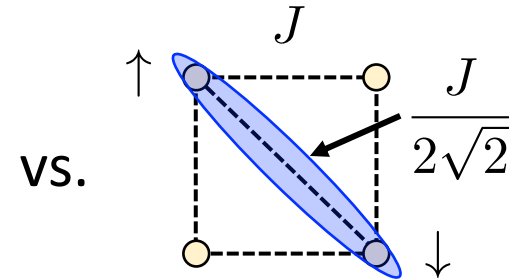


Defects in solid



Introduces **frustration!!**

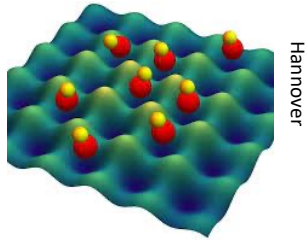
AFM: $J < 0$



Dipolar XY magnets: possibility of Long-Range Order

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Polar molecules

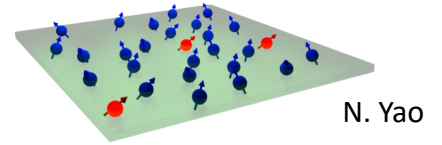


KRb, NaRb Bakr, Ye, Ni...

Magnetic atoms

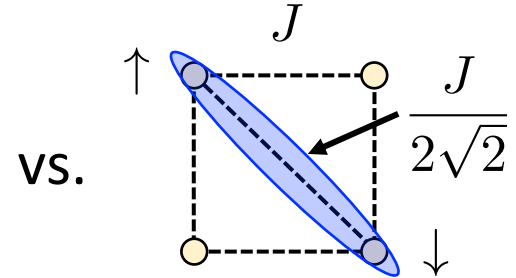
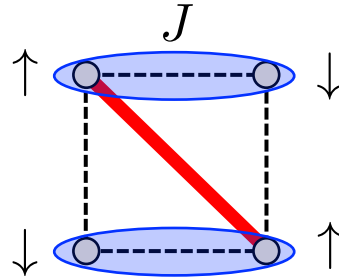
Cr, Er, Dy
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Defects in solid



Introduces **frustration!!**

AFM: $J < 0$



Expectations for ground state:

$T = 0 \Rightarrow$ Long Range order for FM & AFM

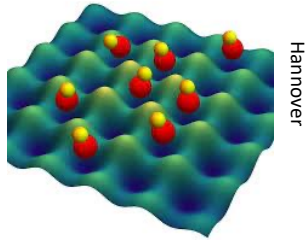
Bruno, PRL 2001

$$\langle \sigma_i^x \sigma_j^x \rangle \neq 0, |i - j| \rightarrow \infty$$

Dipolar XY magnets: possibility of Long-Range Order

Dipolar interactions $\Rightarrow 1/R^3$

Polar molecules

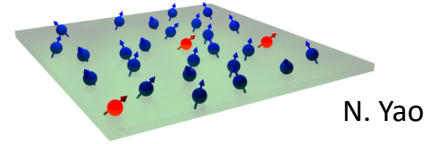


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Magnetic atoms

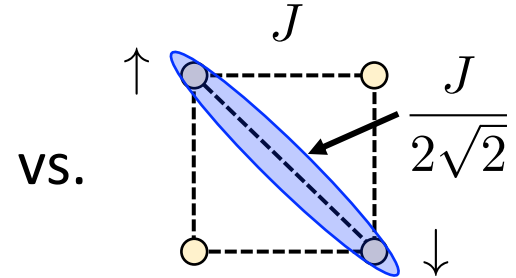
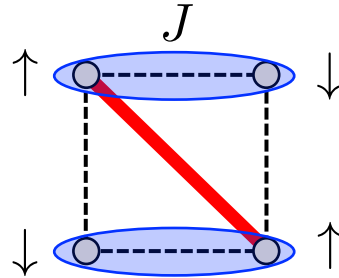
Cr, Er, Dy
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Defects in solid



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AFM: $J < 0$



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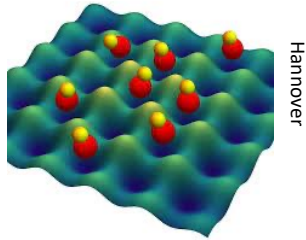
$T \neq 0 \Rightarrow$ LRO for FM $\langle \sigma_i^x \sigma_j^x \rangle \neq 0, |i - j| \rightarrow \infty$

No LRO for AFM (frustration destabilizes)

Dipolar XY magnets: possibility of Long-Range Order

Dipolar interactions $\Rightarrow 1/R^3$

Polar molecules



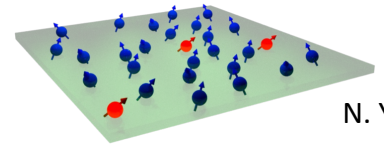
Hanover

KRb, NaRb Bakr, Ye, Ni...

Magnetic atoms

Cr, Er, Dy
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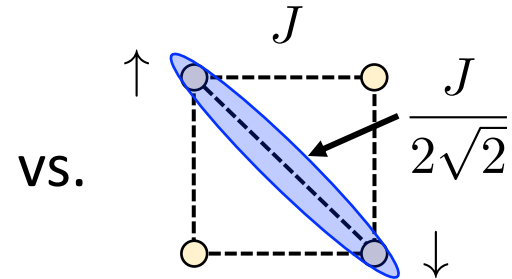
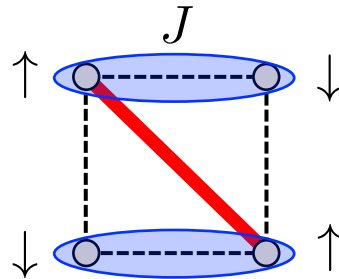
Defects in solid



N. Yao

Introduces **frustration!!**

AFM: $J < 0$



Expectations for ground state:


$T = 0 \Rightarrow$ Long Range order for FM & AFM Bruno, PRL 2001

$T \neq 0 \Rightarrow$ LRO for FM $\langle \sigma_i^x \sigma_j^x \rangle \neq 0, |i - j| \rightarrow \infty$

No LRO for AFM (frustration destabilizes)

Long-range order in 2D - XY magnets never observed...

Experimental preparation of XY ferro- & anti-ferromagnets

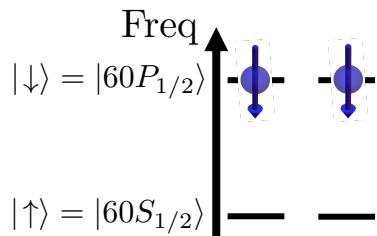
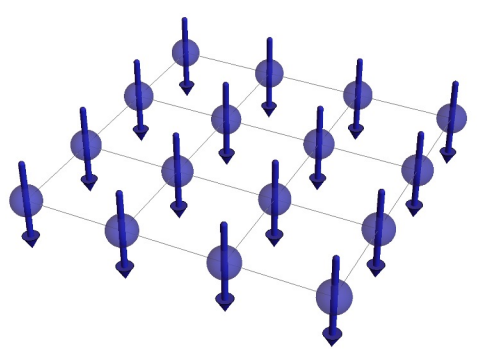
Start from: $H_{XY} = -J \sum_{i < j} \frac{a^3}{r_{ij}^3} (\sigma_i^x \sigma_j^x + \sigma_i^y \sigma_j^y) + \hbar \sum_i \delta_i \sigma_i^z$
($J/h \approx 0.8$ MHz)  staggered

Experimental preparation of XY ferro- & anti-ferromagnets

Start from:
$$H_{XY} = -J \sum_{i < j} \frac{a^3}{r_{ij}^3} (\sigma_i^x \sigma_j^x + \sigma_i^y \sigma_j^y) + \hbar \sum_i \delta_i \sigma_i^z$$

($J/h \approx 0.8$ MHz) ↖ **staggered**

1. Prepare a **classical Néel state** along z: checkerboard pattern

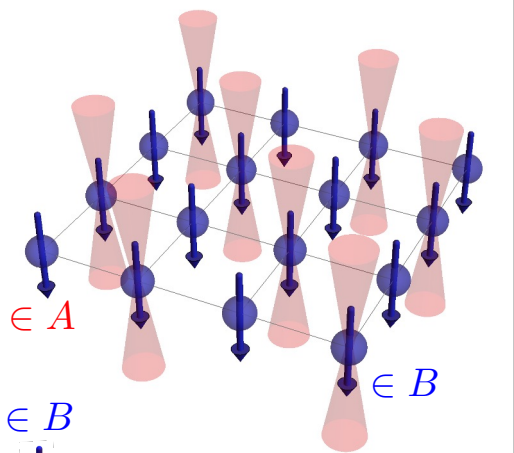


Experimental preparation of XY ferro- & anti-ferromagnets

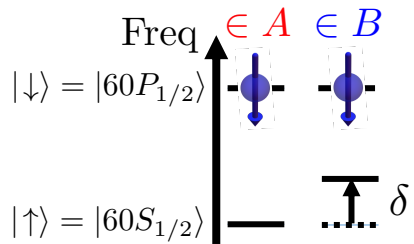
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apply local light-shifts

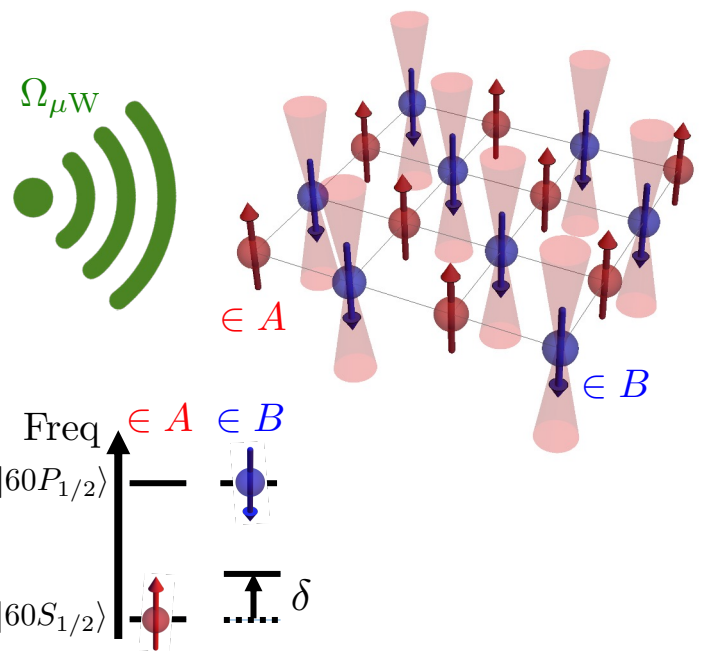


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1. Prepare a **classical Néel state** along z: checkerboard pattern



$M_z = 0$

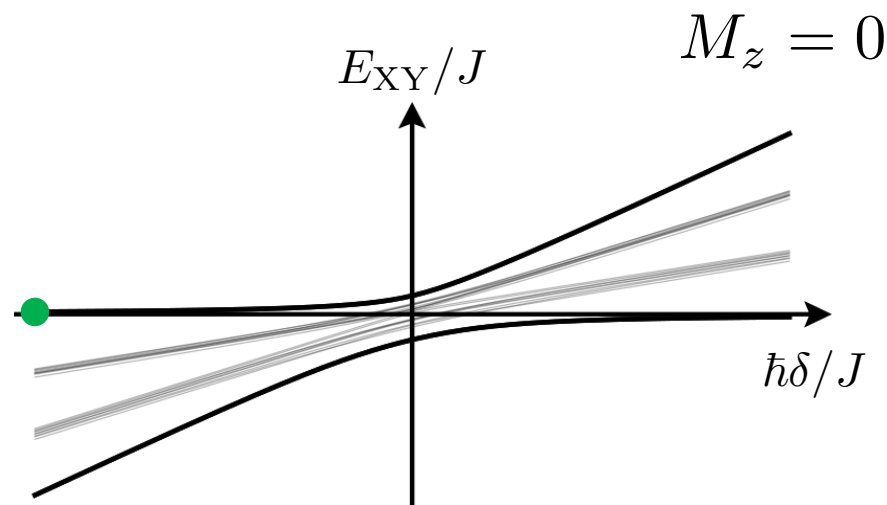
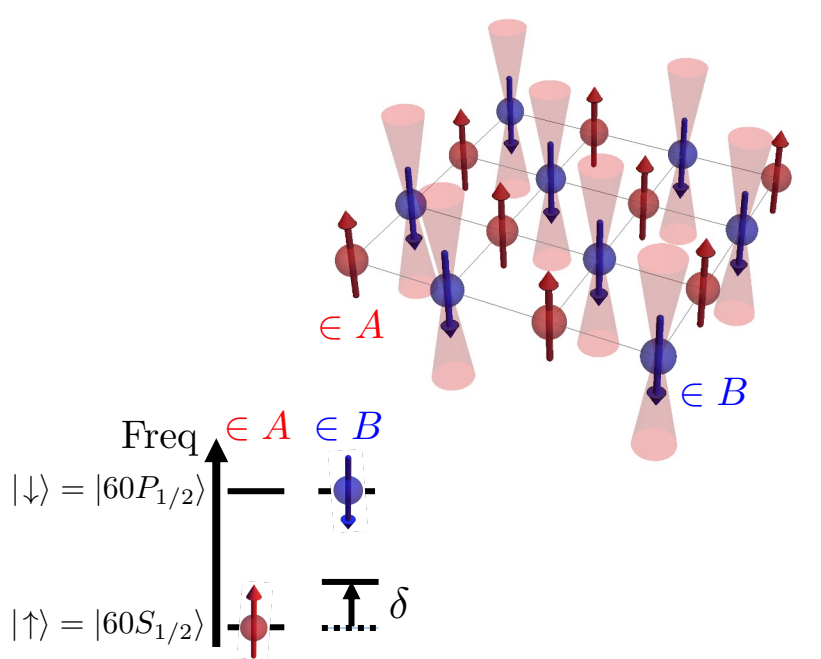
apply local light-shifts
+
microwaves

Experimental preparation of XY ferro- & anti-ferromagnets

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2. Adiabatically decrease δ to “melt” into XY **AFM**

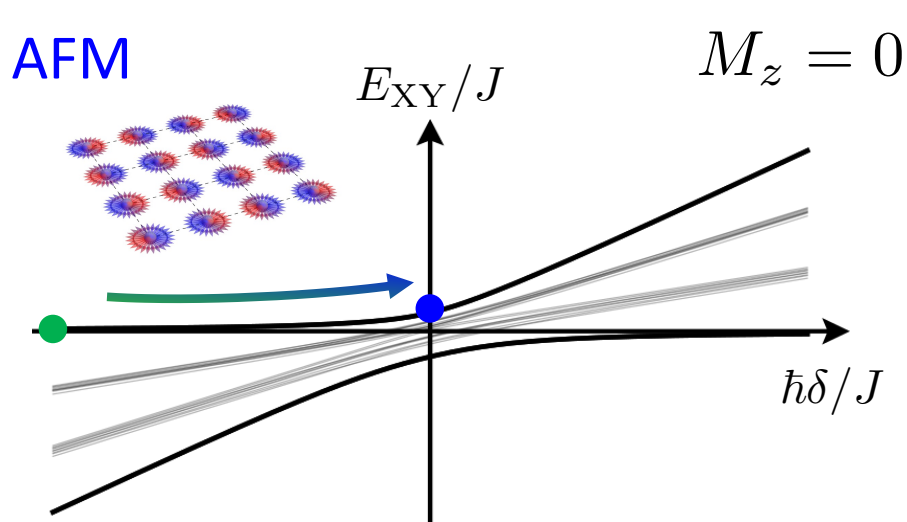
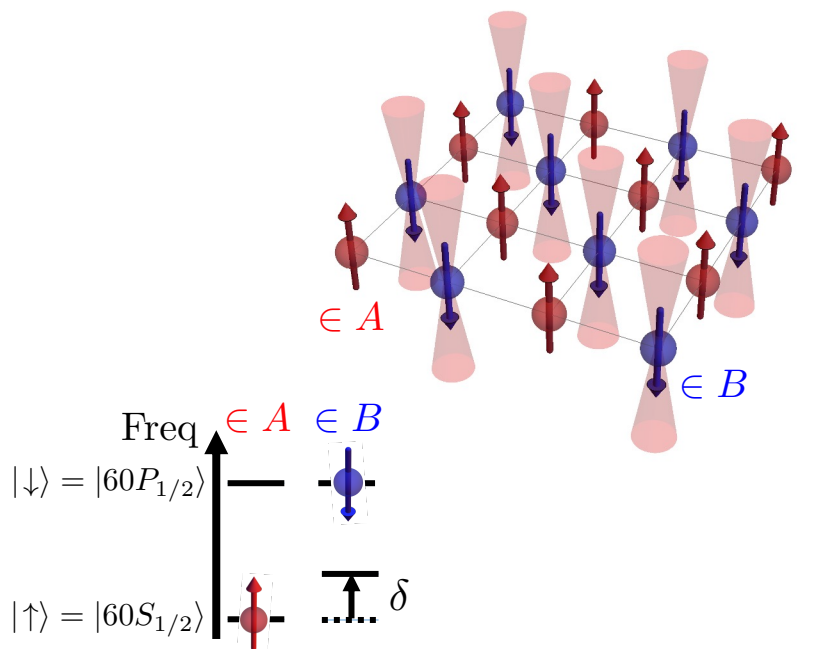


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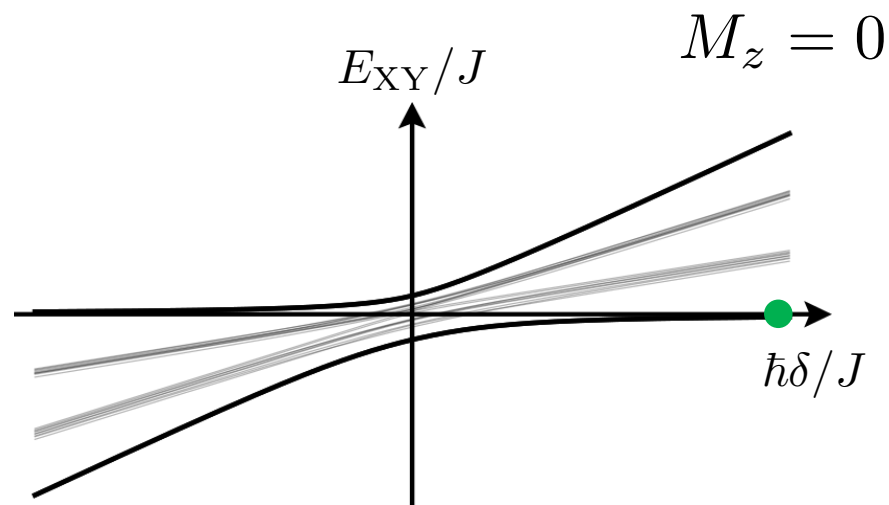
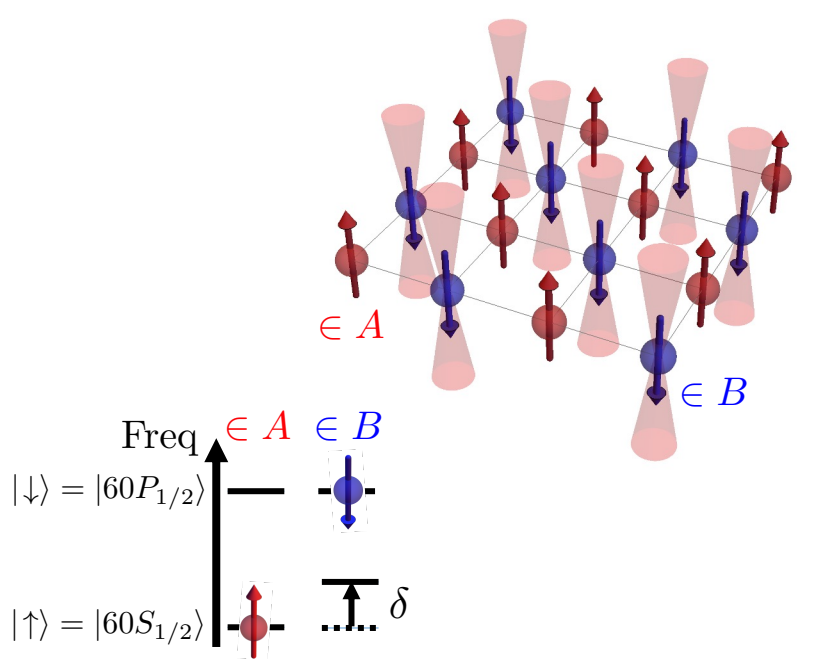


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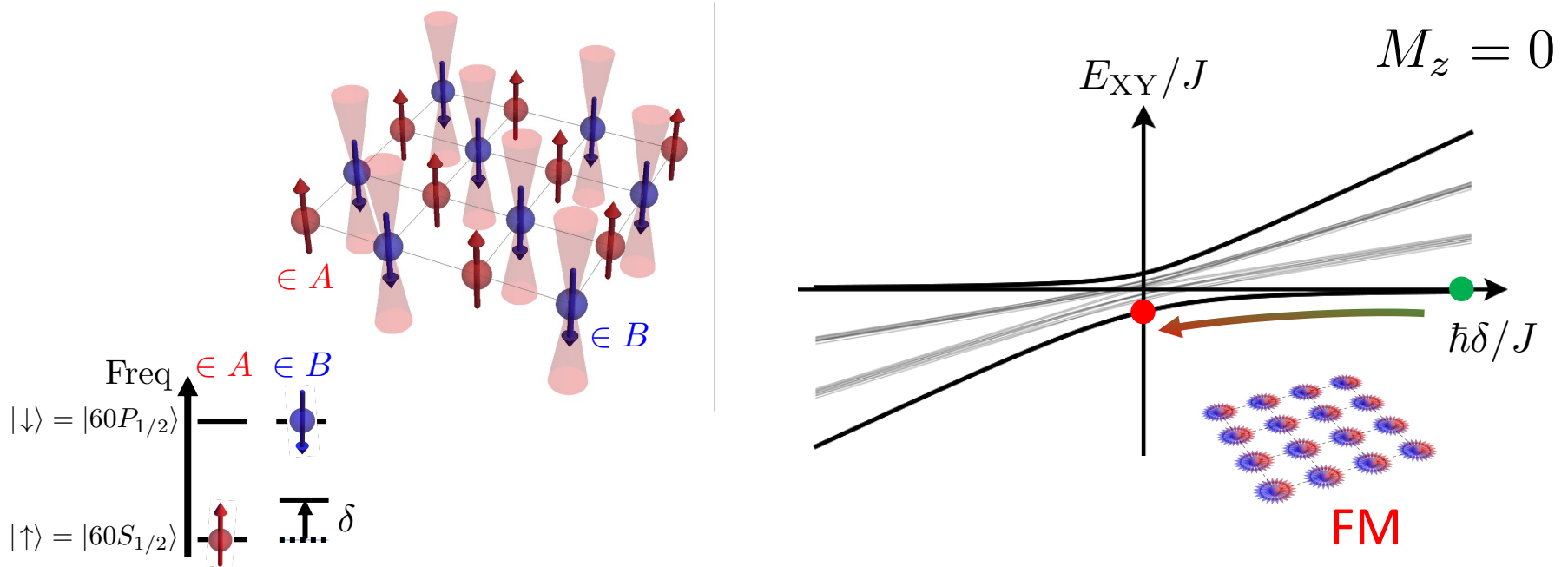


Experimental preparation of XY ferro- & anti-ferromagnets

Start from:
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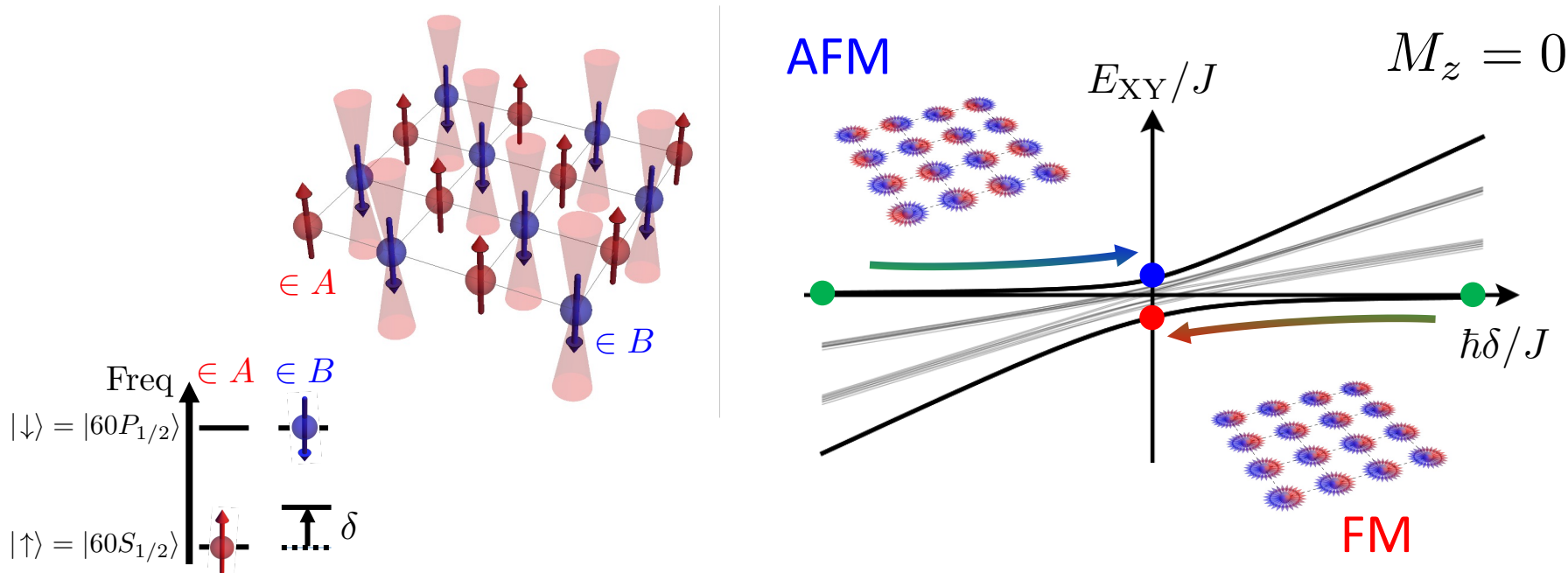


Experimental preparation of XY ferro- & anti-ferromagnets

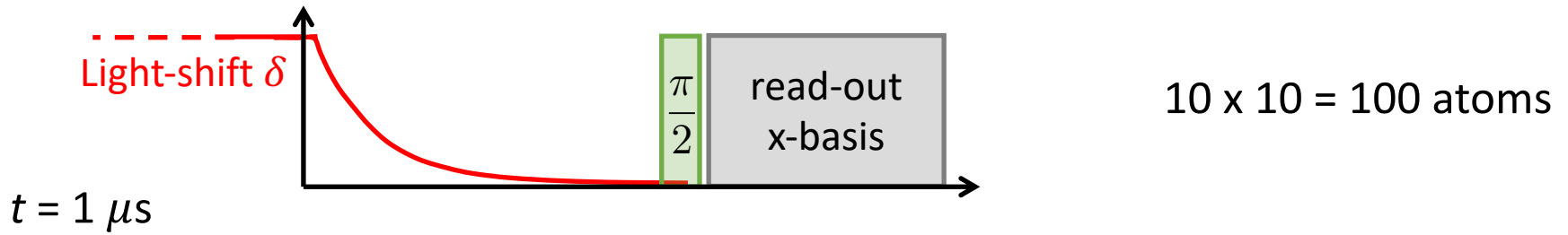
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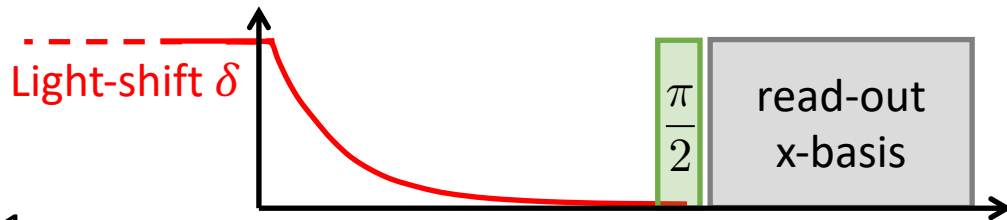
2. Adiabatically decrease δ to “melt” into XY **AFM** / **FM**



Observation of Long-Range FM order

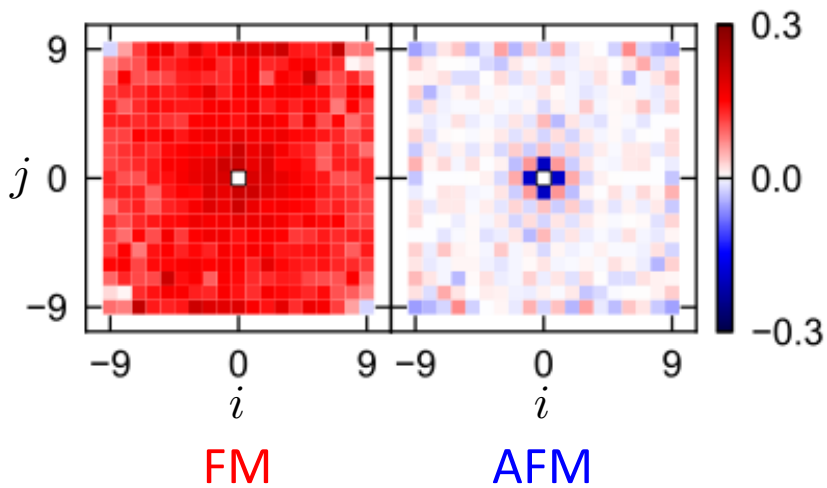


Observation of Long-Range FM order

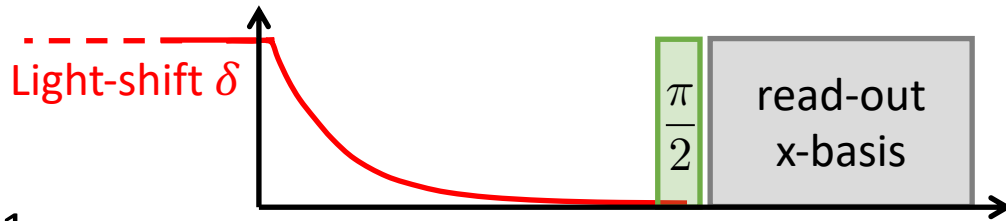


10 x 10 = 100 atoms

$$C_{ij}^x = \langle \sigma_i^x \sigma_j^x \rangle - \langle \sigma_i^x \rangle \langle \sigma_j^x \rangle$$

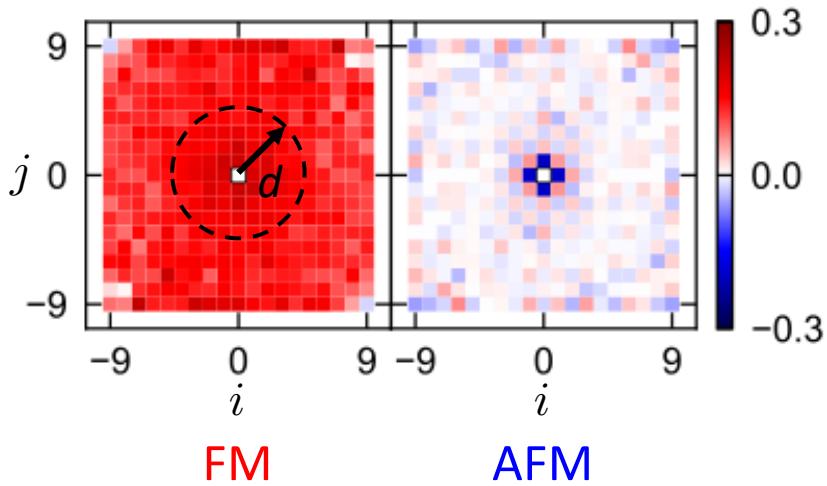


Observation of Long-Range FM order

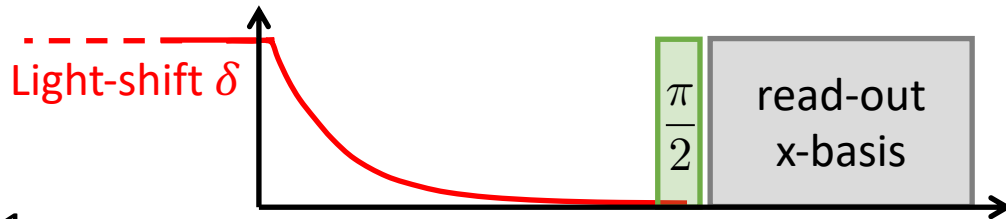


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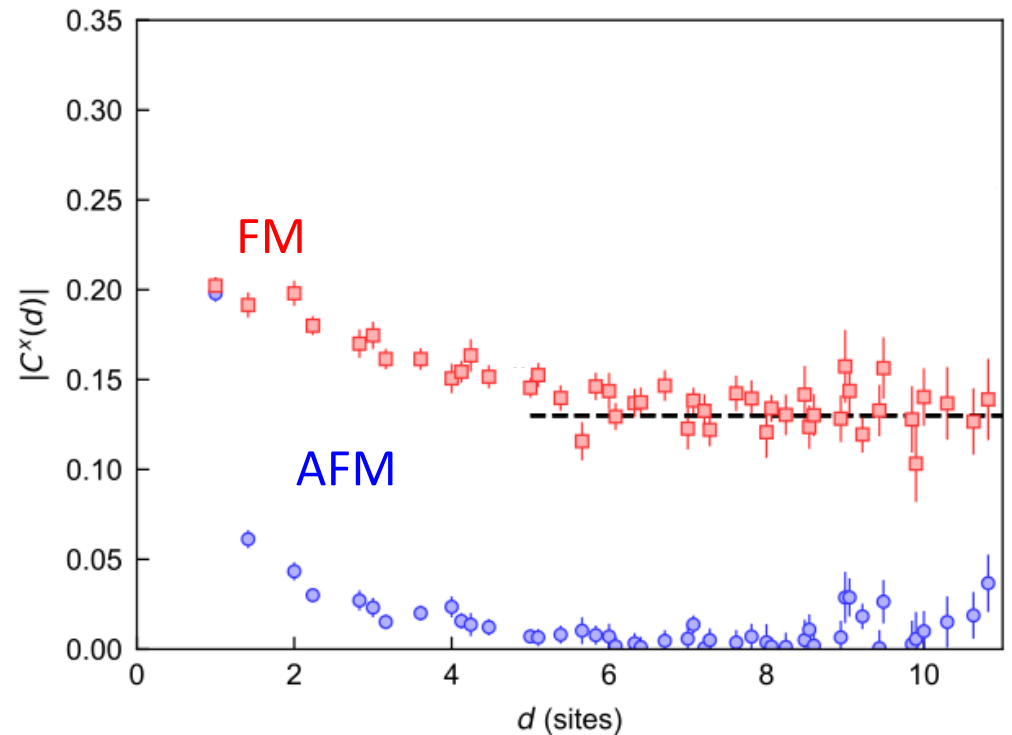
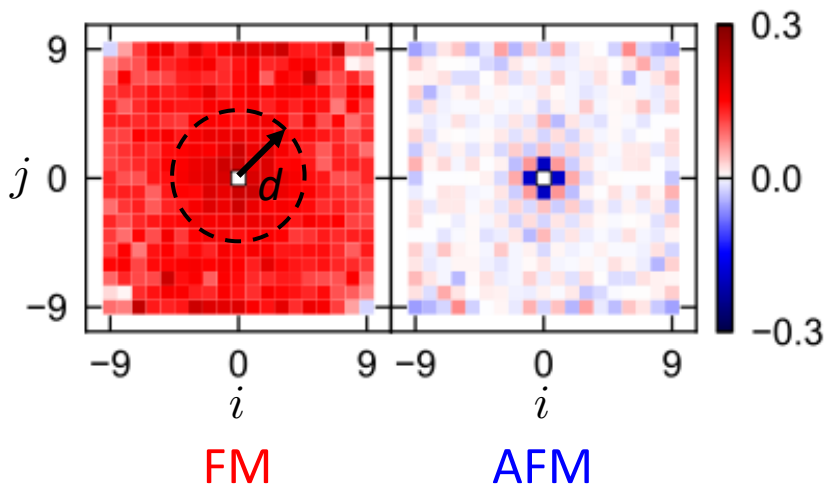
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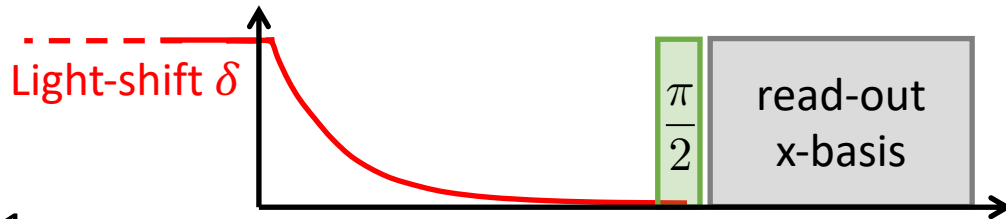
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$t = 1 \mu s$

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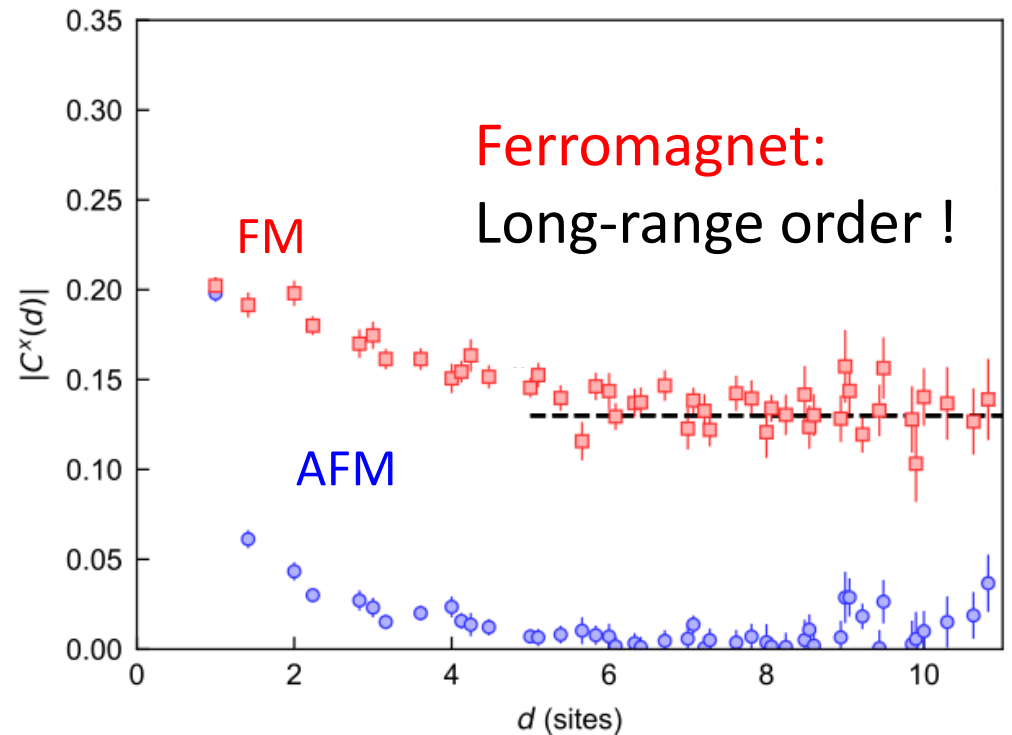
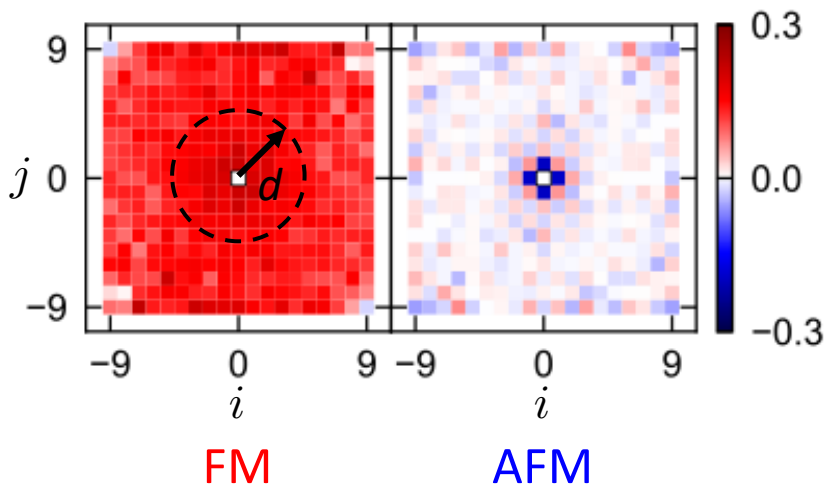
Observation of Long-Range FM order



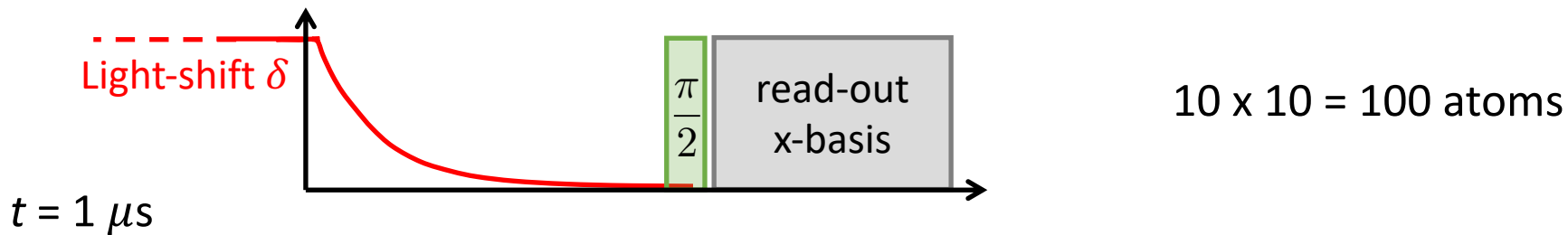
10 x 10 = 100 atoms

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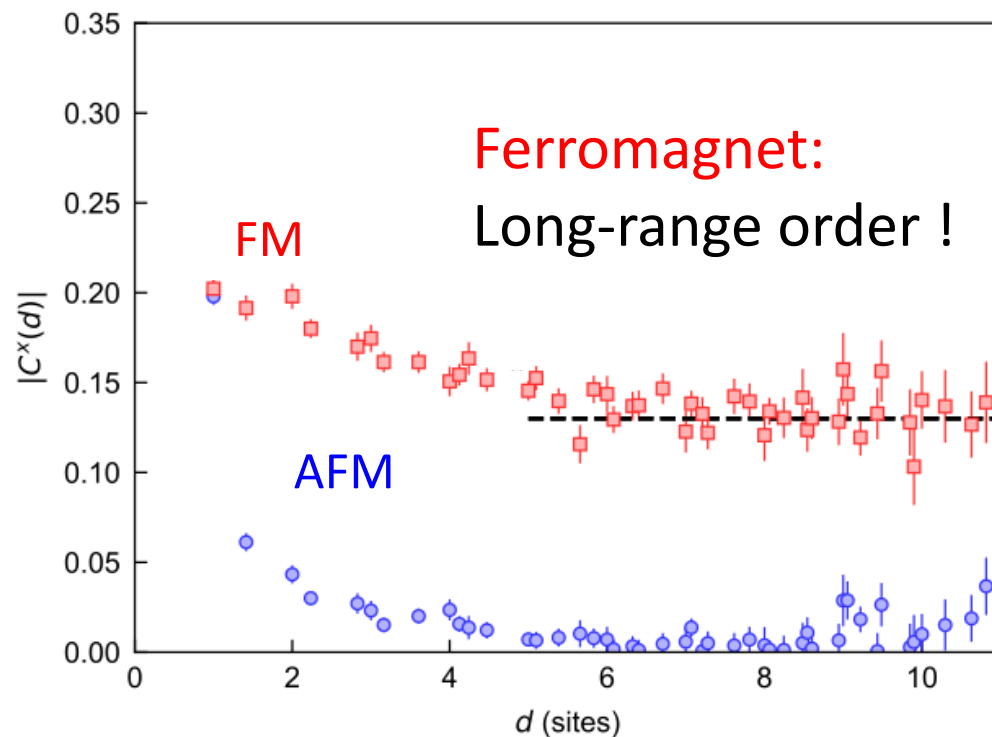
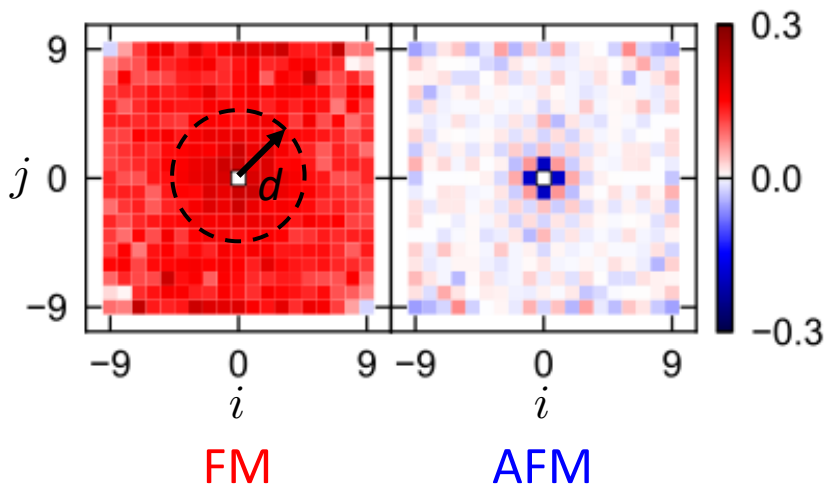
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Observation of Long-Range FM order

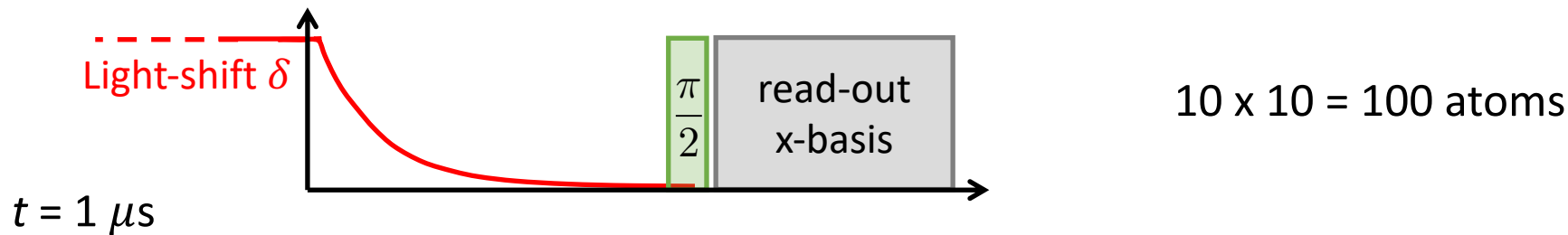


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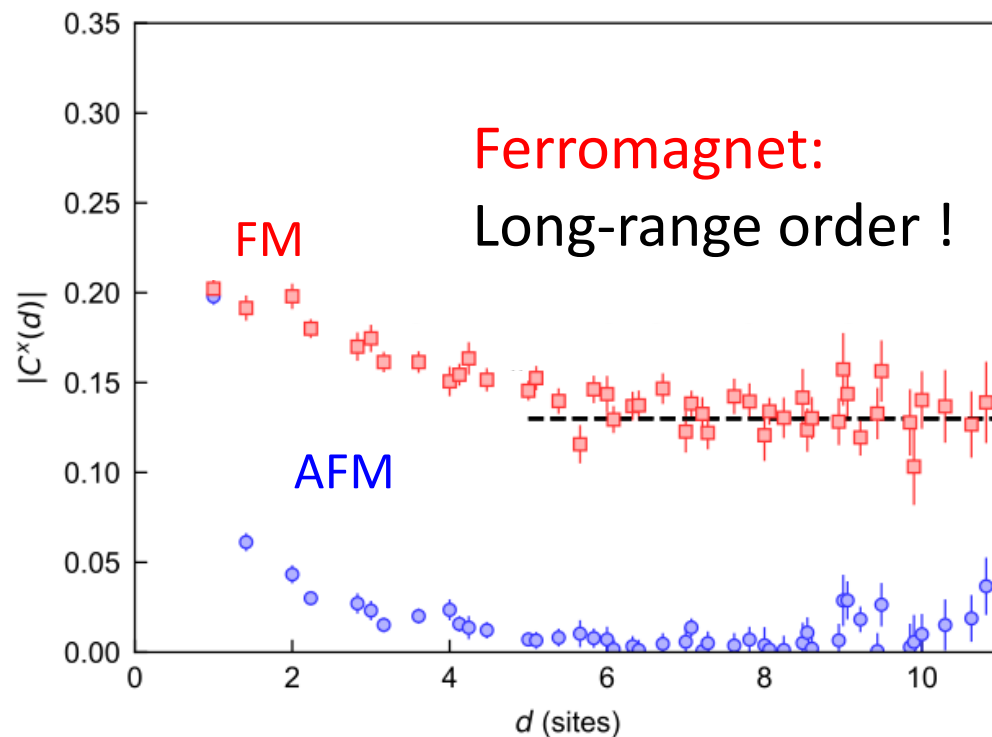
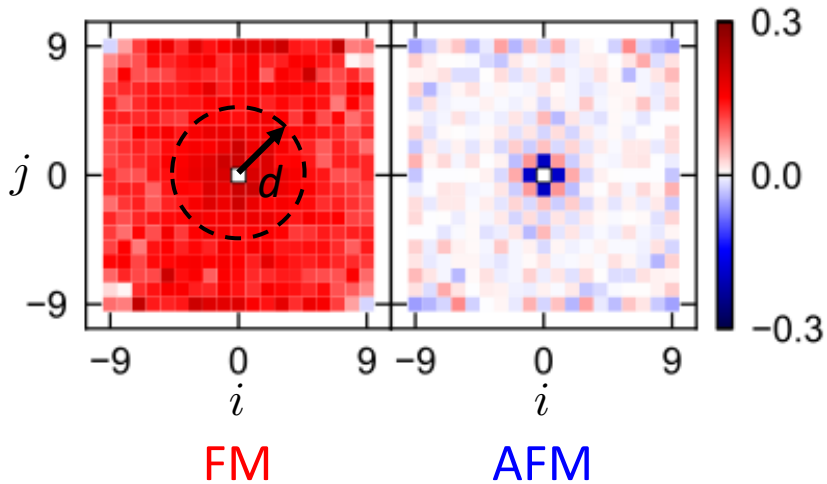


Antiferromagnet: LRO destabilized by imperfections

Observation of Long-Range FM order



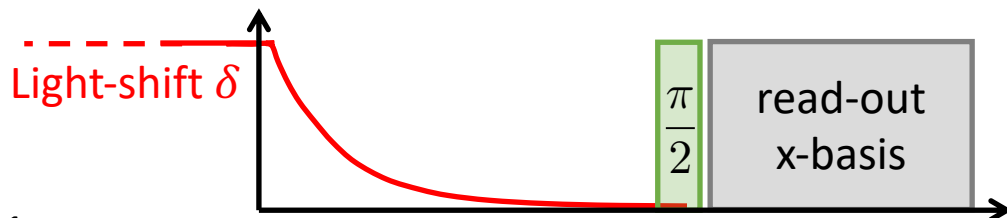
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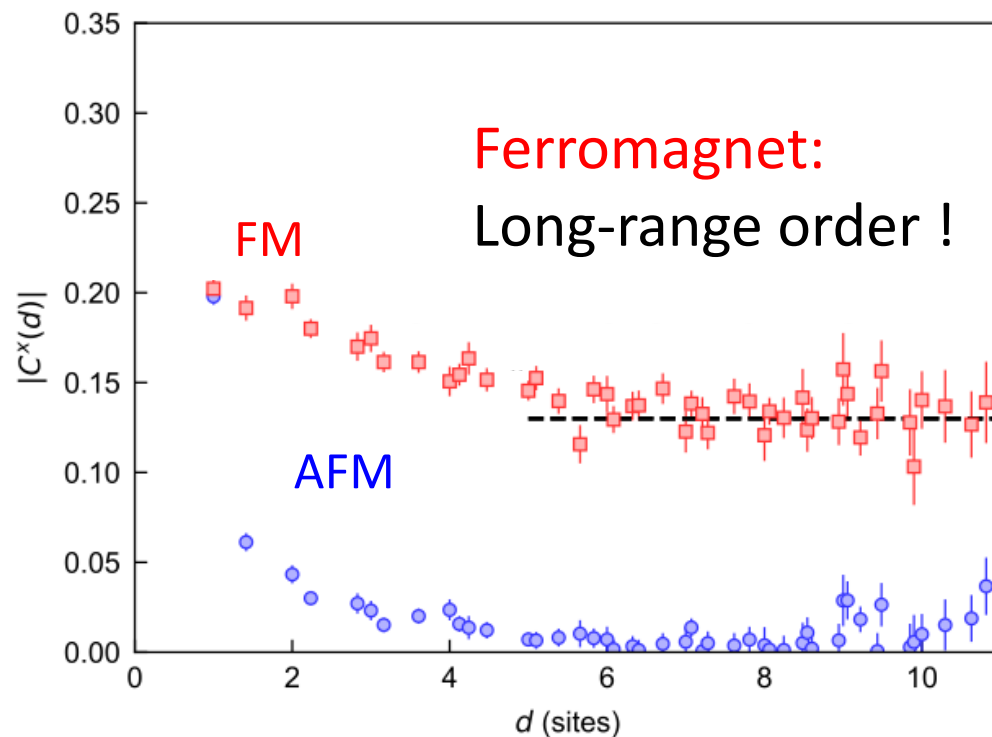
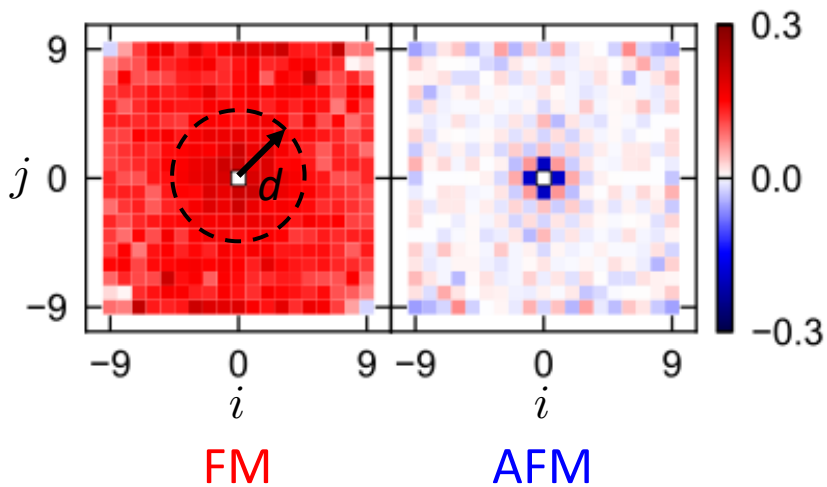
Important role $1/r^3$ of interaction

Observation of Long-Range FM order



10 x 10 = 100 atoms

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Antiferromagnet: LRO destabilized by imperfections

Outline

1. Dipolar XY magnet with resonant dipole interactions
2. Spin squeezing using dipolar interaction

G. Bornet *et al.*, arXiv:2303.08053



N. Yao
M. Block
B. Ye
(Harvard)

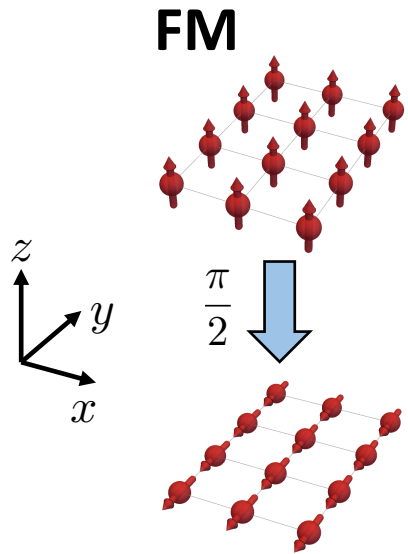


T. Roscilde



F. Mezzacapo
(Lyon)

Dynamics under XY Hamiltonian

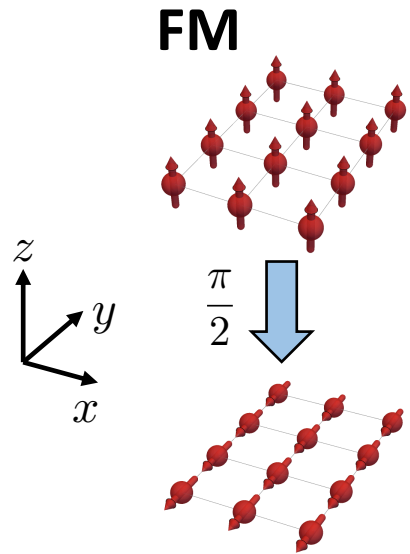


MW-pulse

$\frac{\pi}{2}$

Initialize: $|\rightarrow, \rightarrow \dots\rangle_y = (|\uparrow\rangle + i|\downarrow\rangle)^{\otimes N}$
“Coherent spin state”

Dynamics under XY Hamiltonian



MW-pulse

$\frac{\pi}{2}$

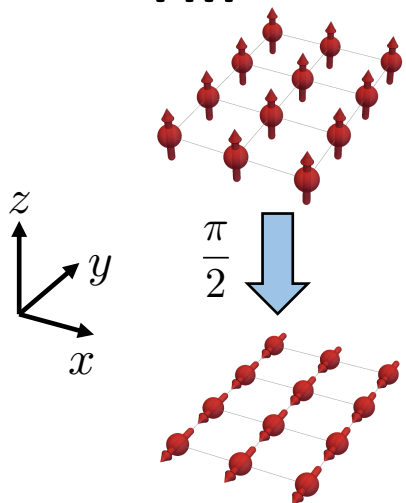
Initialize: $|\rightarrow, \rightarrow \dots\rangle_y = (|\uparrow\rangle + i|\downarrow\rangle)^{\otimes N}$
“Coherent spin state”

Evolve:

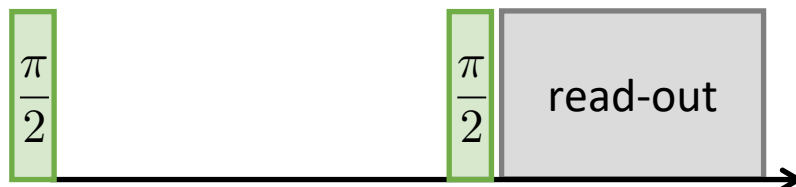
$$|\psi(t)\rangle = e^{-iH_{XY}t/\hbar} |\psi(0)\rangle$$

Dynamics under XY Hamiltonian

FM



MW-pulse



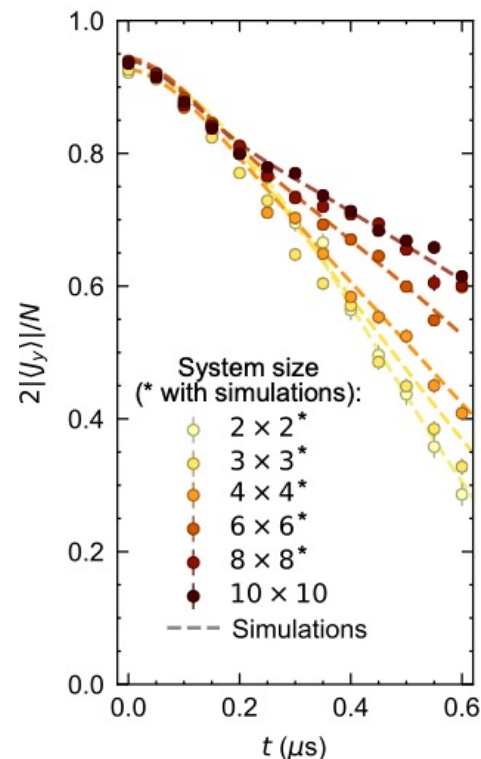
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Evolve:

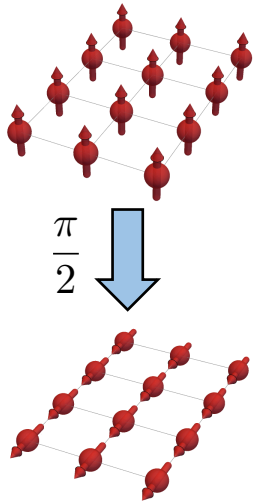
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Interactions depolarize...

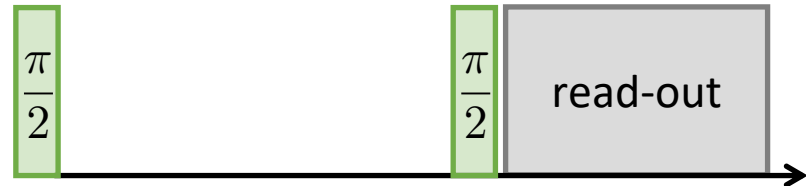


Dynamics under XY Hamiltonian

FM



MW-pulse



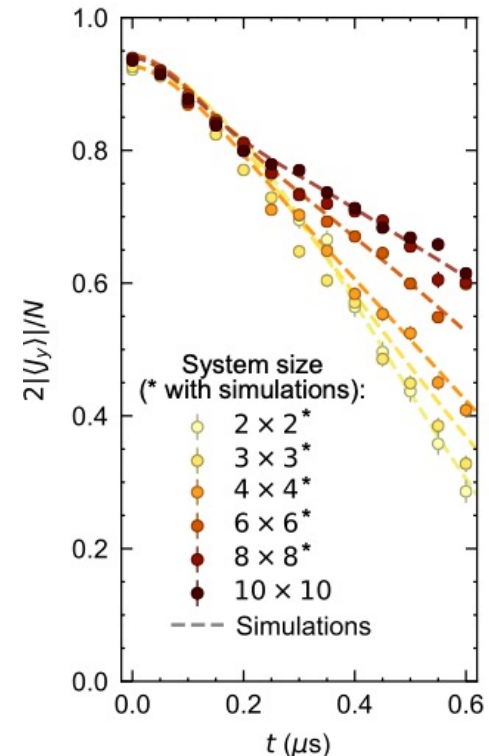
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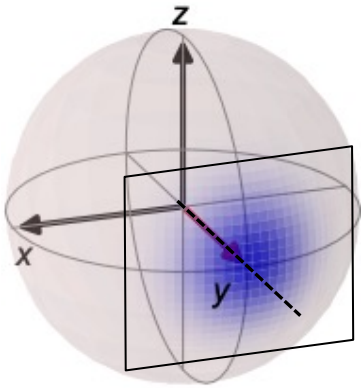
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Interactions depolarize...
Generation entanglement?

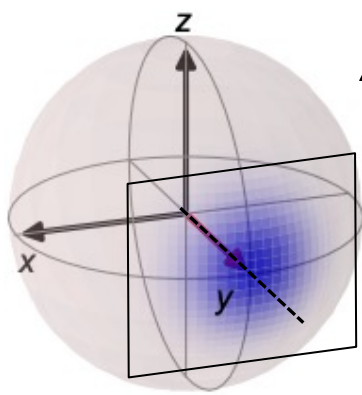


A detour: spin squeezing in OAT versus dipolar model

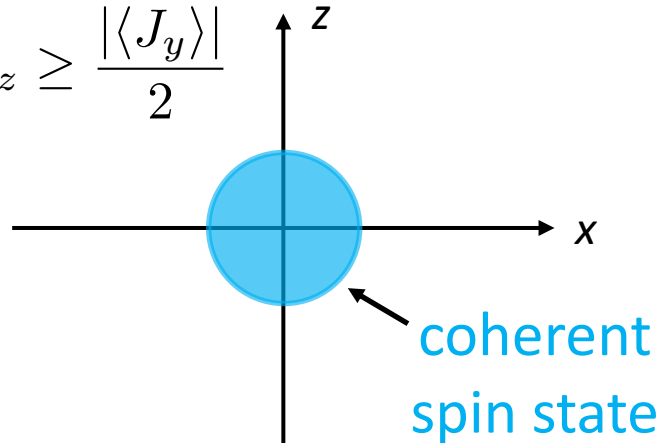


Collective spin:
$$\hat{J}_\alpha = \sum_{i=1}^N \hat{\sigma}_i^\alpha$$

A detour: spin squeezing in OAT versus dipolar model

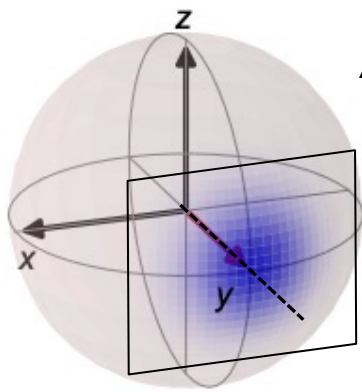


$$\Delta J_x \Delta J_z \geq \frac{|\langle J_y \rangle|}{2}$$

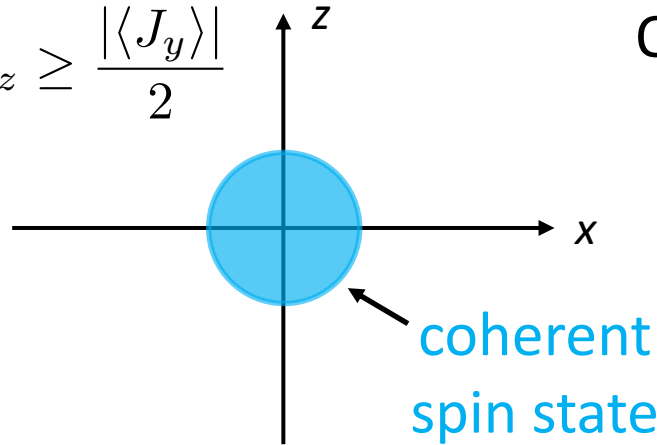


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A detour: spin squeezing in OAT versus dipolar model



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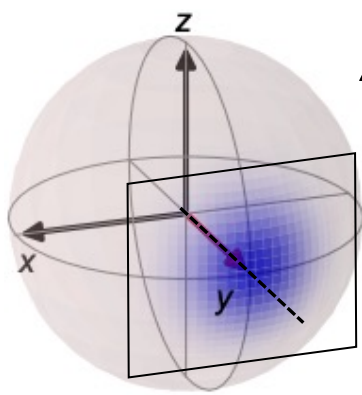


One-axis twisted model

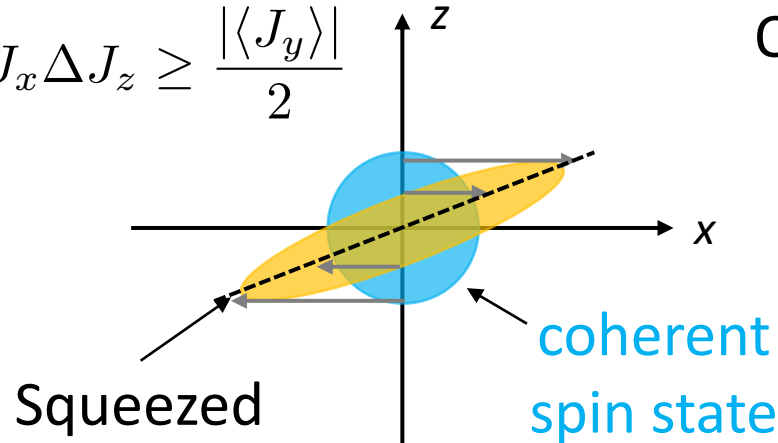
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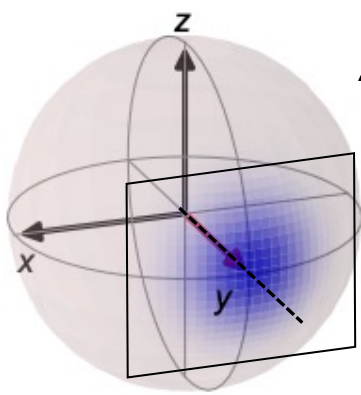


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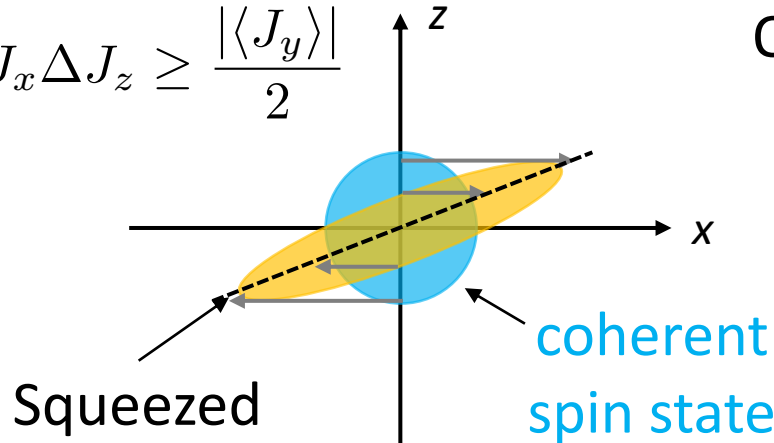
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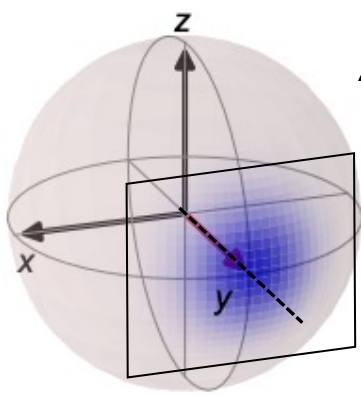
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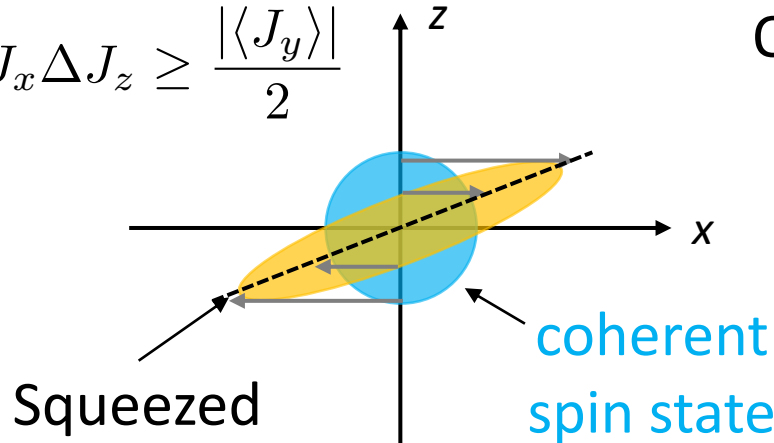
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Metrological gain in Ramsey interf.: $\delta\theta_{\text{sq}} = \xi_R^2 \delta\theta_{\text{SQL}}$ Wineland, PRA 1994

A detour: spin squeezing in OAT versus dipolar model



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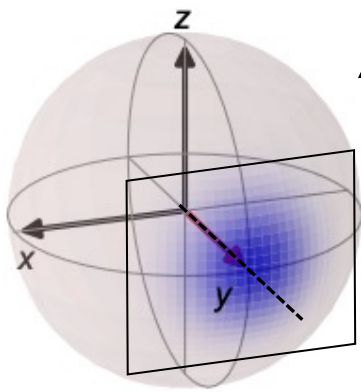
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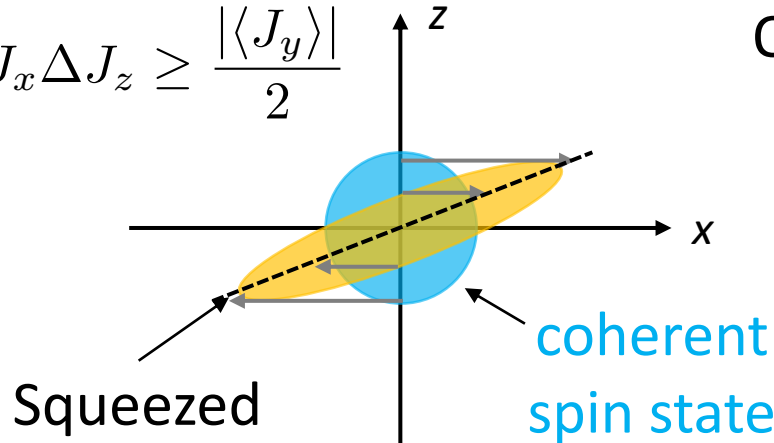
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A detour: spin squeezing in OAT versus dipolar model



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Is $1/r^3$ long-range enough to generate squeezing?
If yes, does it scale with N ?

From dipolar XY to one-axis twisting model...

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$$H_{XY} \sim \sum_{i < j} \frac{1}{r_{ij}^3} (\sigma_i^x \sigma_j^x + \sigma_i^y \sigma_j^y) \sim \hat{\mathbf{J}}^2 - \hat{J}_z^2$$

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Prediction: yes! M.P.A Jones & T. Pohl, PRL (2014)
A-M. Rey, PRL (2020)
T. Roscilde, PRL **129**, 150503 (2022)
N. Yao, arXiv:2301.09636

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M.P.A Jones & T. Pohl, PRL (2014)

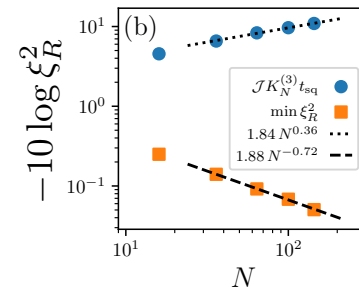
A-M. Rey, PRL (2020)

T. Roscilde, PRL **129**, 150503 (2022)

N. Yao, arXiv:2301.09636

And should scale:

Roscilde
PRL (2022)



From dipolar XY to one-axis twisting model...

Is $1/r^3$ long-range enough to generate squeezing?

$$H_{XY} \sim \sum_{i < j} \frac{1}{r_{ij}^3} (\sigma_i^x \sigma_j^x + \sigma_i^y \sigma_j^y) \sim \hat{\mathbf{J}}^2 - \hat{J}_z^2$$

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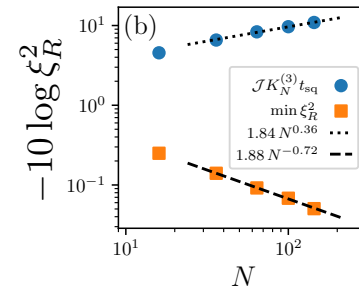
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Rotor / spin wave theory

Roscilde *et al.*, arXiv:2302.0927, 2303.00380

$$H_{XY} \approx E_0 + \frac{(\hat{J}_z)^2}{2I_N} + \sum_{\mathbf{q} \neq 0} \hbar \omega_{\mathbf{q}} a_{\mathbf{q}}^\dagger a_{\mathbf{q}}$$

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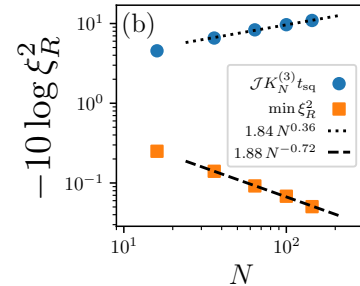
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“Rotor”, $\mathbf{q} = 0$

$$I_N \sim \frac{N}{J_0}$$

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$$J_0 = \frac{J a^\alpha}{N} \sum_{i \neq j} (\pm 1)^{|i-j|} \frac{1}{r_{ij}^\alpha}$$

↖ FM
↗ AFM

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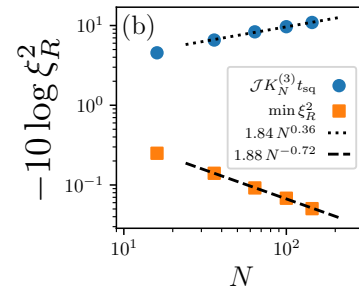
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Spin wave

“Rotor”, $\mathbf{q} = 0$

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FM

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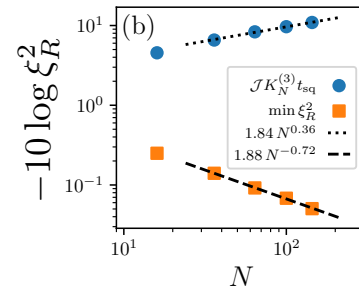
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PRL (2022)



Rotor / spin wave

arXiv:2302.0927, 2303.00380

N. Yao's conjecture:

H with LRO at $T \neq 0 \Rightarrow$ squeezing

arXiv:2301.09636

Here: dipolar FM has LRO

spin wave

Collective spin

$$\hat{J}_\alpha = \sum_{i=1}^N \hat{\sigma}_i^\alpha$$

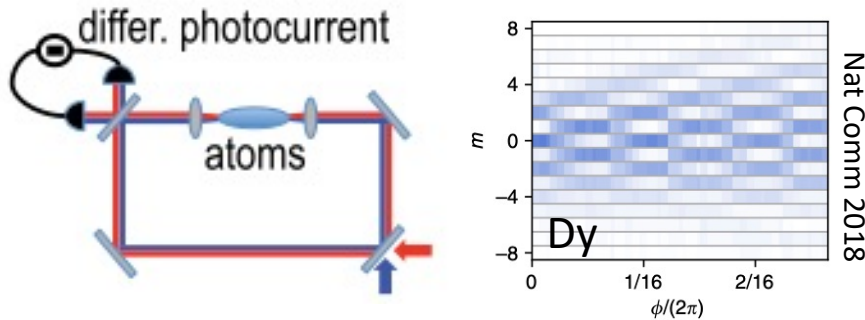
$$\sum_{i \neq j} (\pm 1)^{|i-j|} \frac{1}{r_{ij}^\alpha}$$

↖ FM
↙ AFM

Experimental observations of spin squeezing

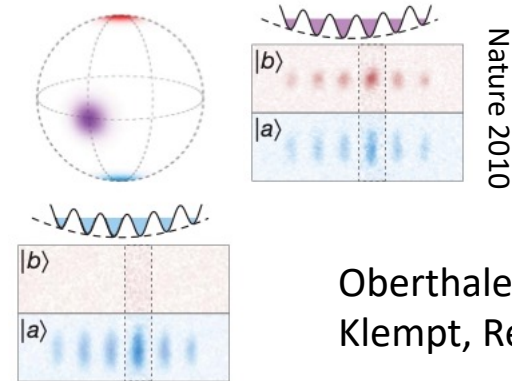
Pezzé *et al.*, RMP 2018

Hot / cold atomic vapors



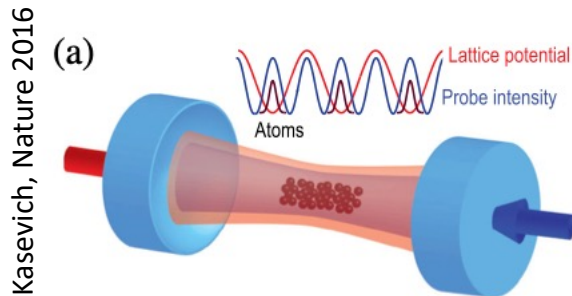
Polzik (1999), Giacobino, Mitchell, Nascimbene...

Bose-Einstein condensate (OAT)



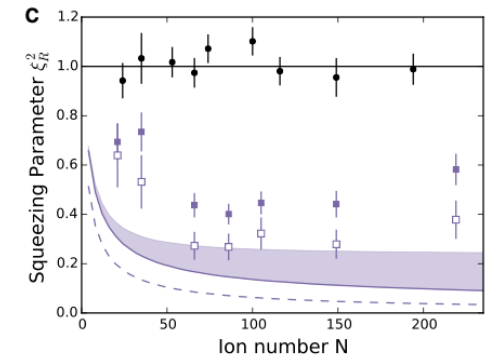
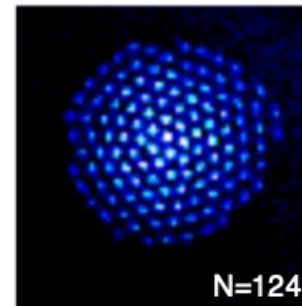
Oberthaler, Treutlein, Klempt, Reichel, You...

Cavity QED + cold atoms (OAT)



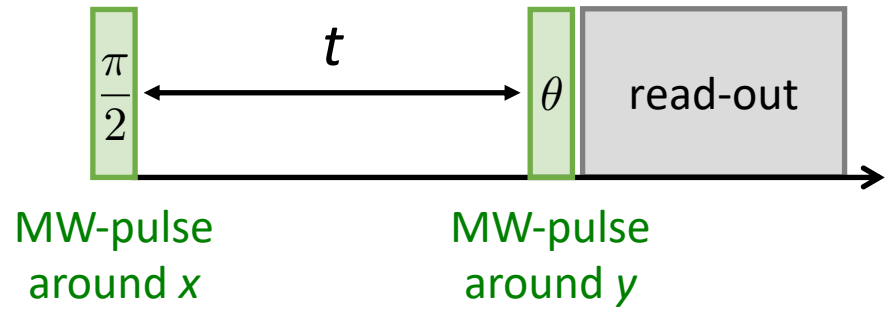
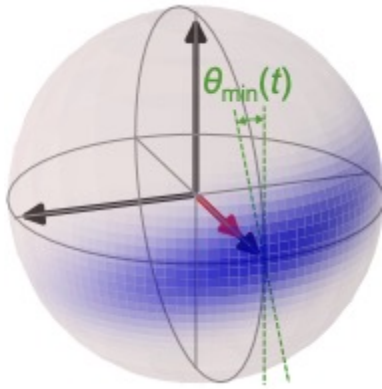
Vuletic, Kasevich, Thompson (JILA), Je, Schleier-Smith...

Ion crystal (~OAT)

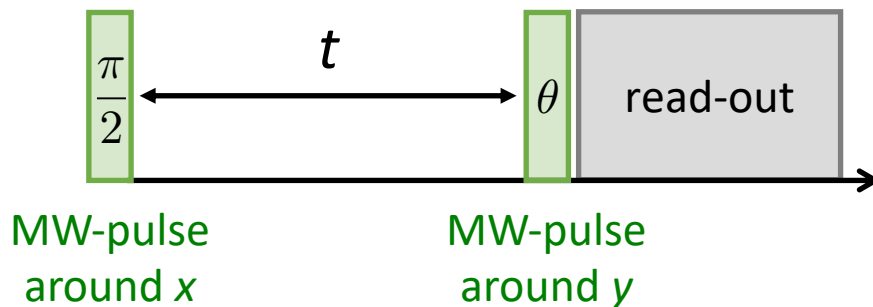
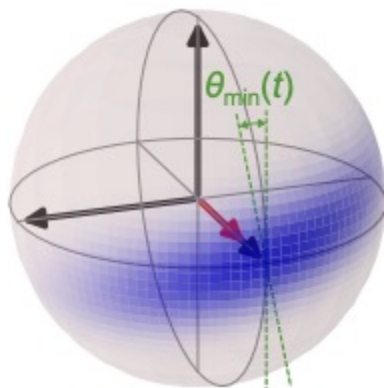


Bollinger, Science 2016

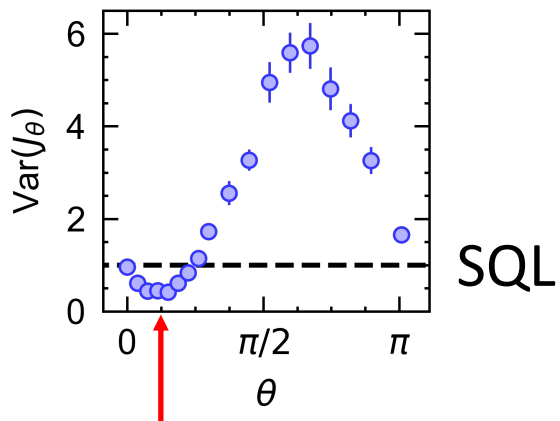
Dipolar squeezing with Rydberg atoms: the recipe



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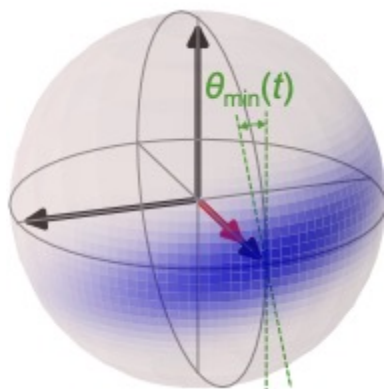


6 x 6 atoms
 $t = 300$ ns

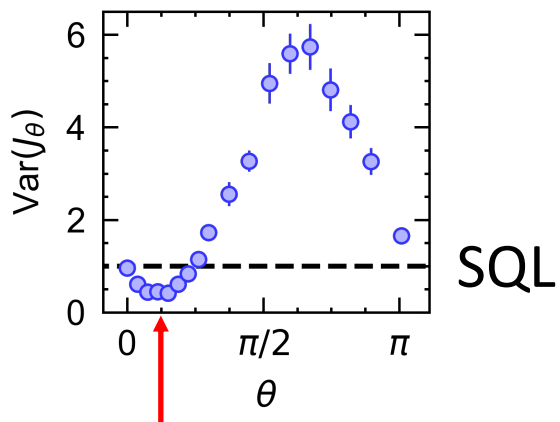


Squeezing !

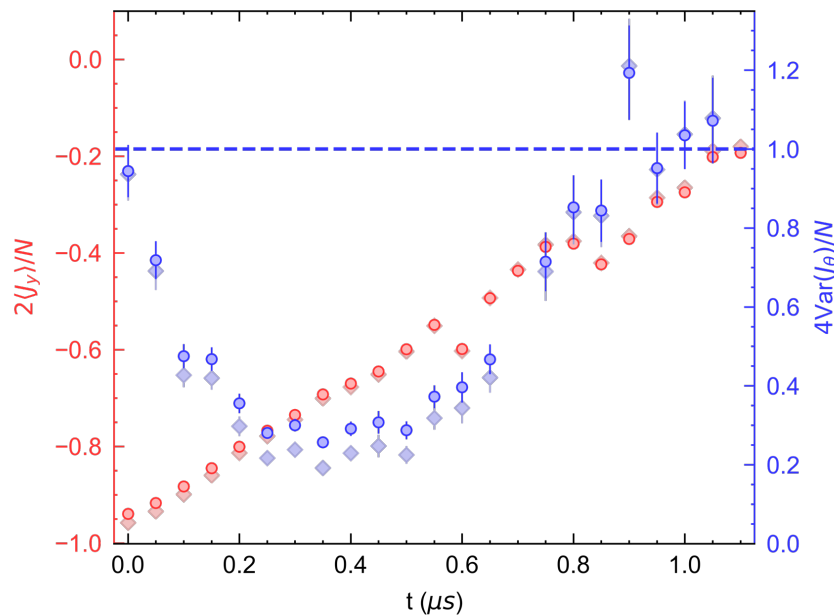
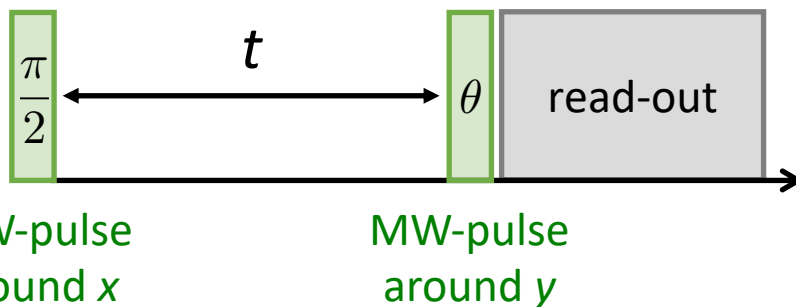
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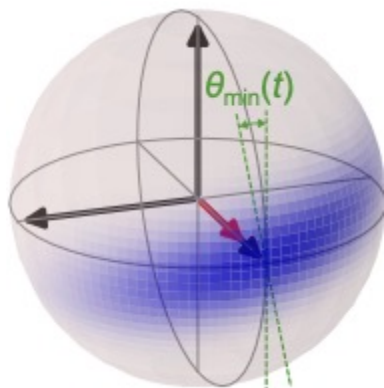
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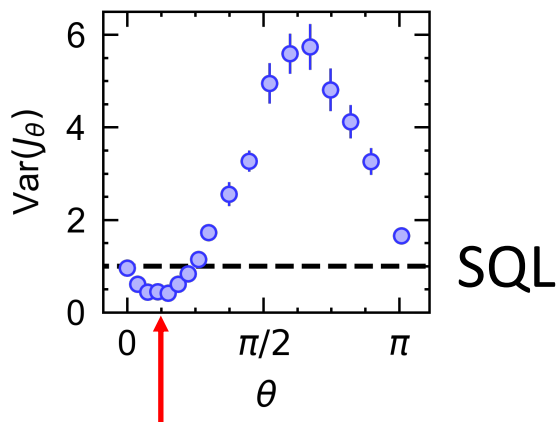
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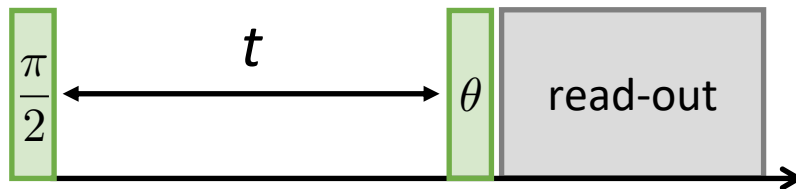
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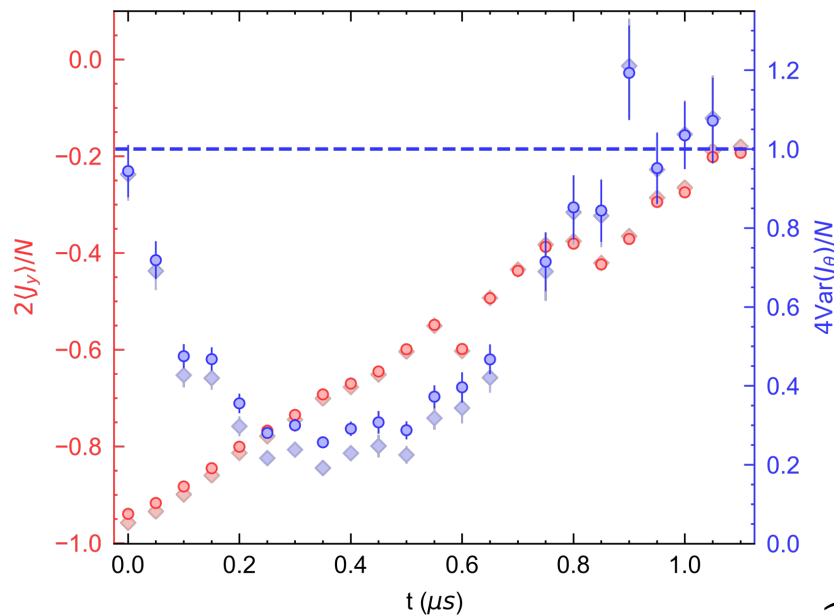


Squeezing !

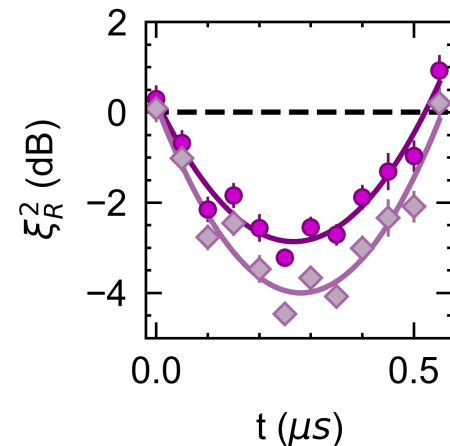


MW-pulse
 around x

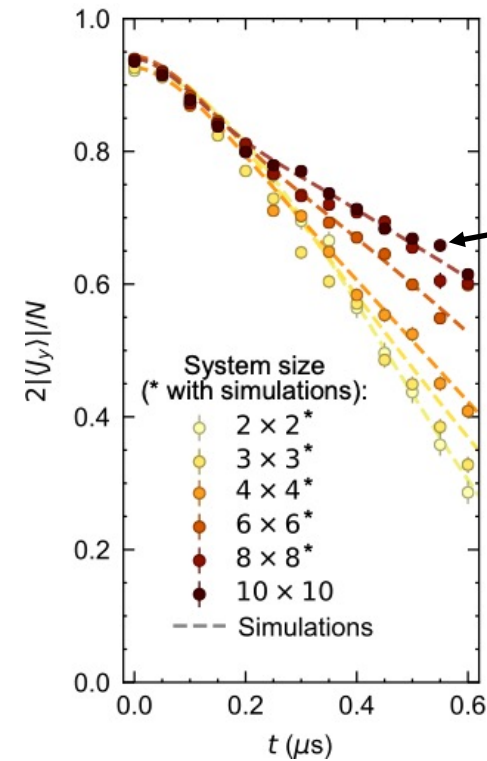
MW-pulse
 around y



$$\xi_R^2 = N \frac{\min_{\perp} (\Delta J_{\perp}^2)}{\langle \mathbf{J} \rangle^2}$$



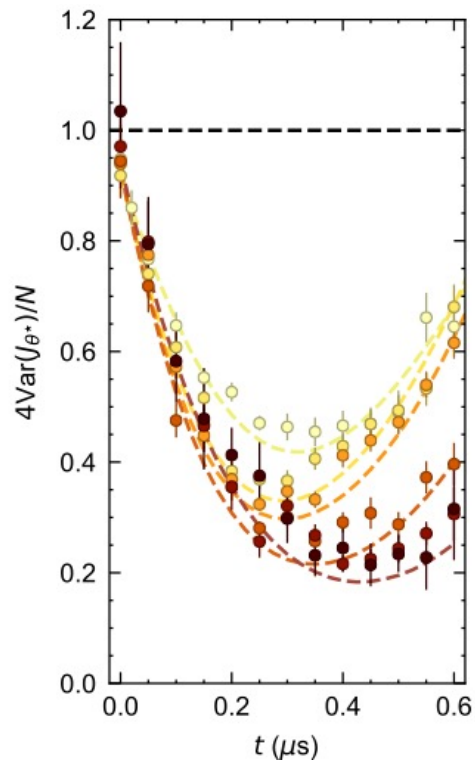
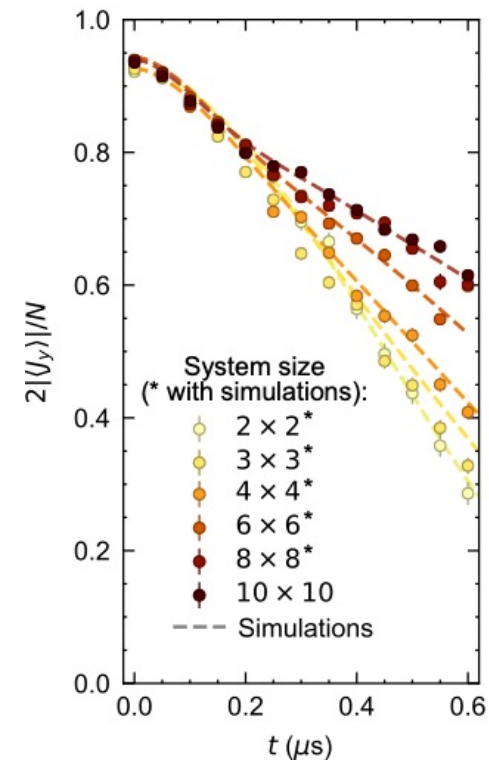
Scaling of squeezing with atom number



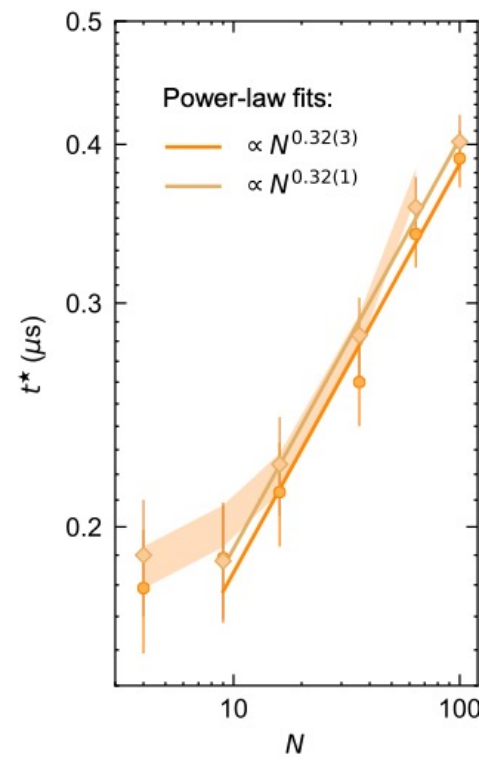
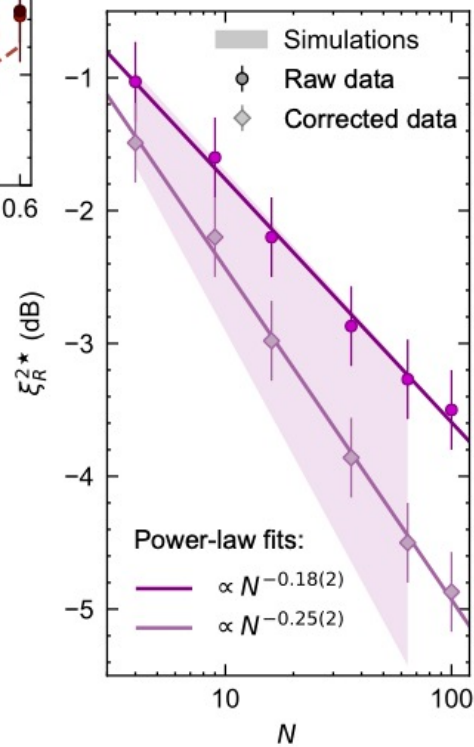
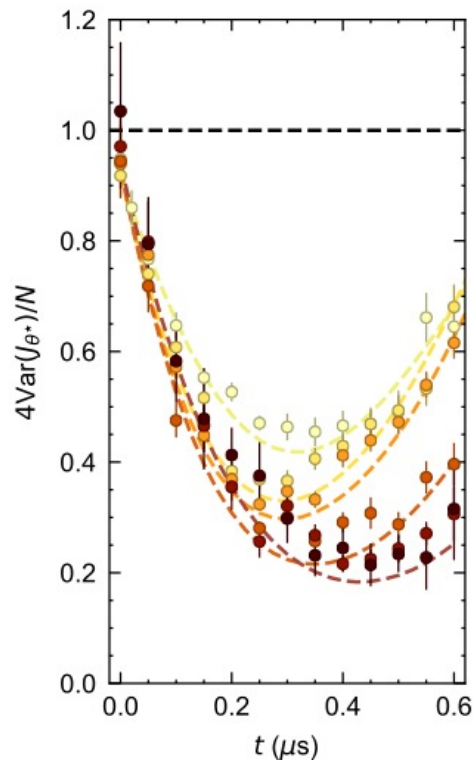
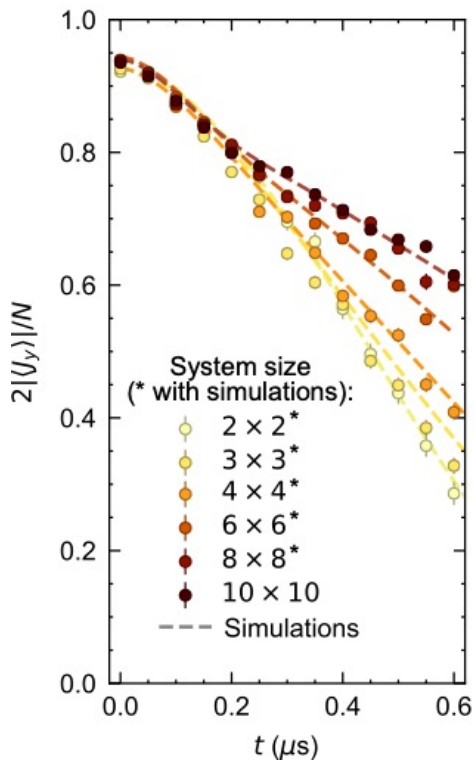
Dynamics of the Rotor

$$H \sim \frac{(J_z)^2}{2I_N} \quad \text{with} \quad I_N \sim \frac{N}{J_0}$$

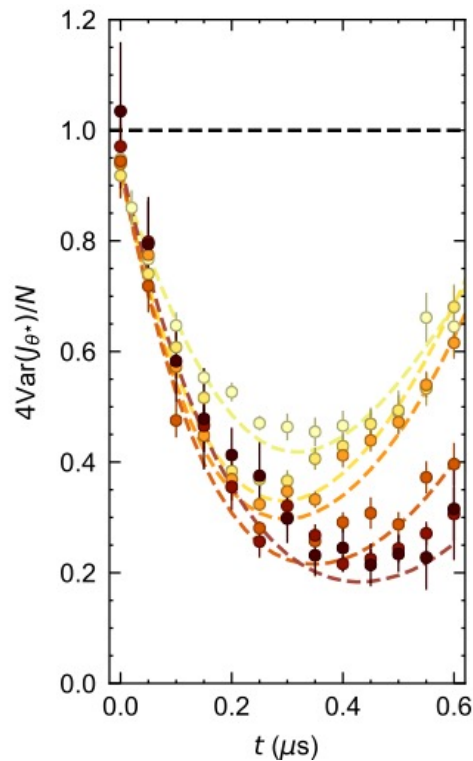
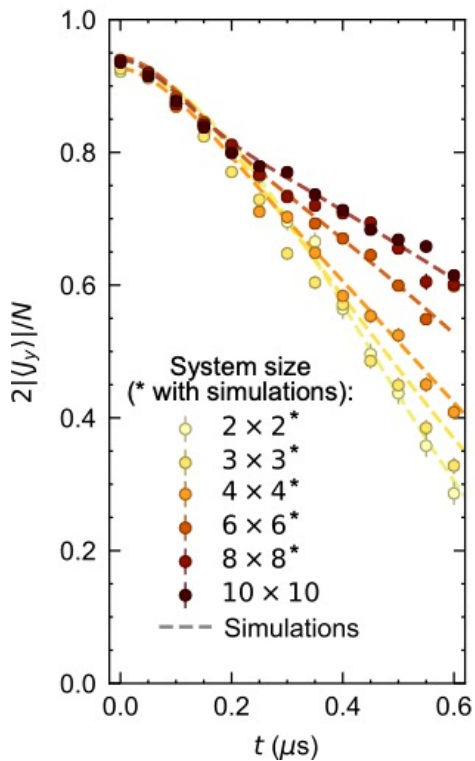
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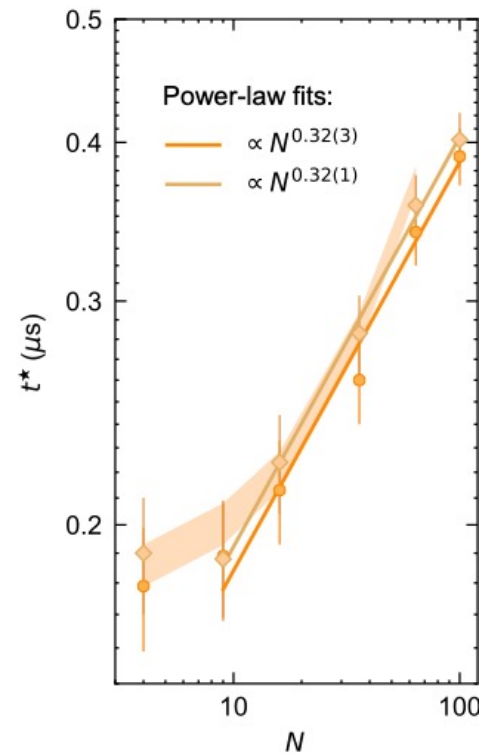
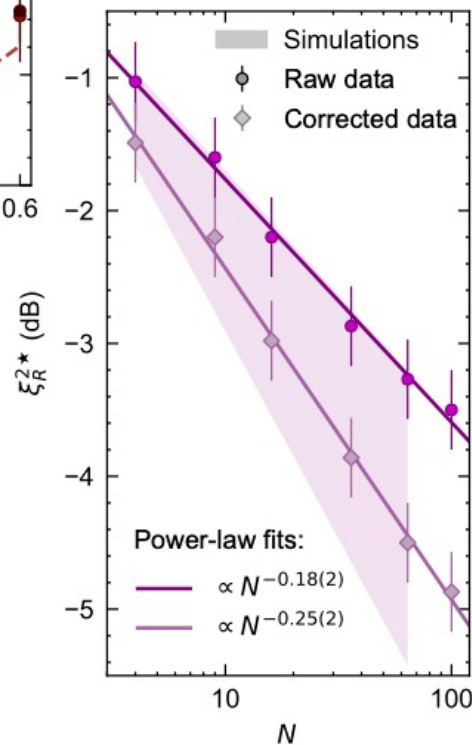
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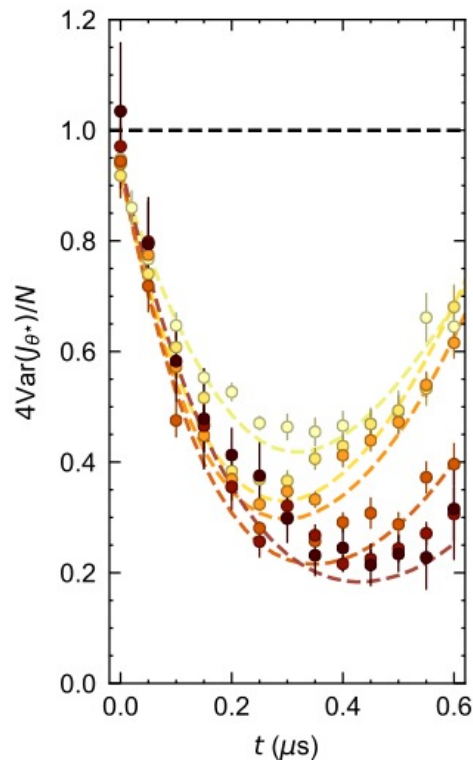
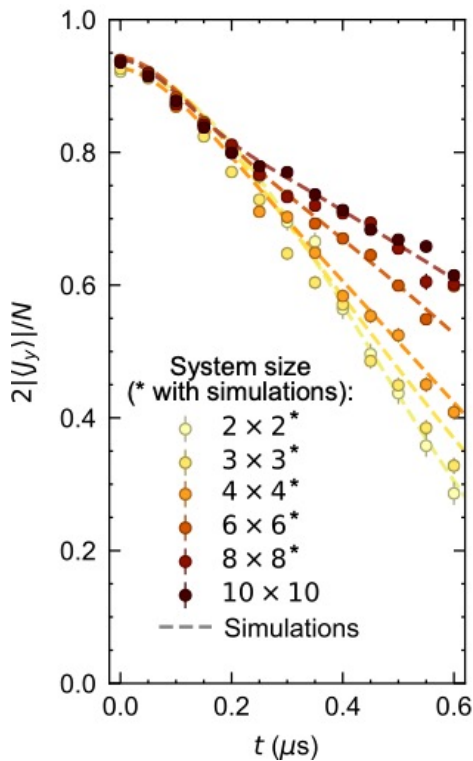
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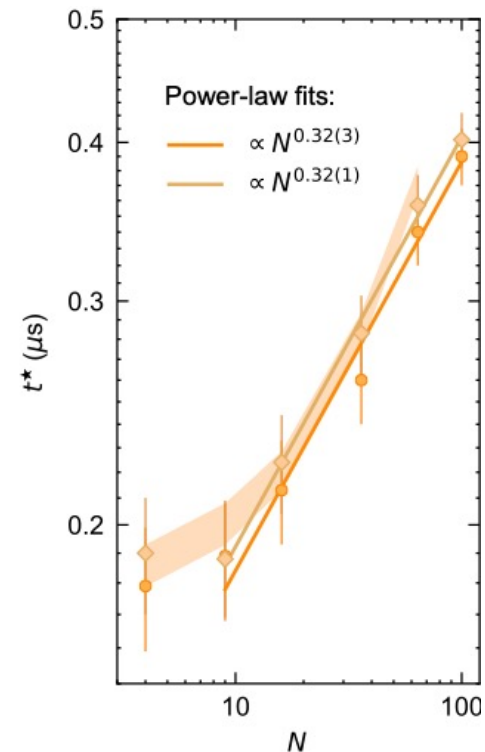
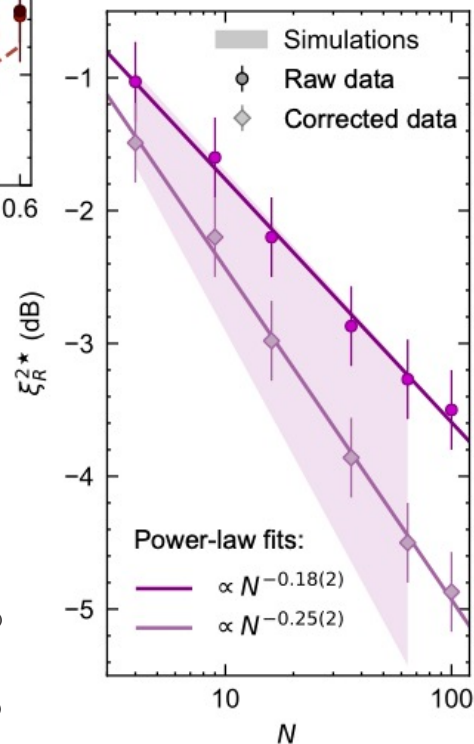
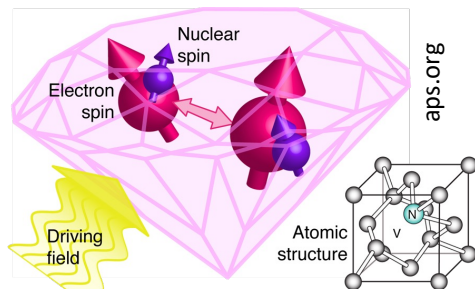
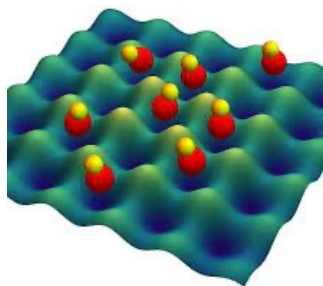
Conclusion: dipolar squeezing
is scalable!!



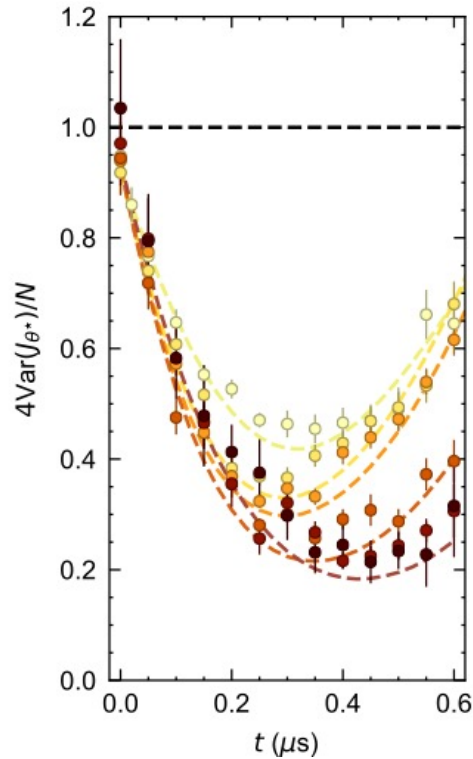
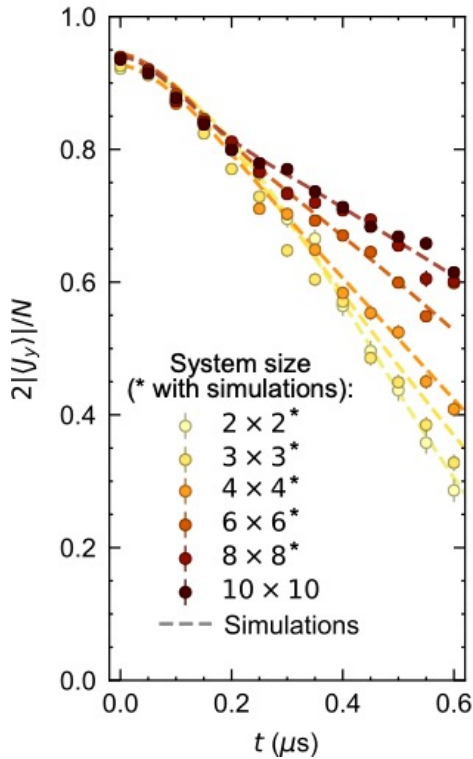
Scaling of squeezing with atom number



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Scaling of squeezing with atom number



Trapped ions: C. Roos

[arXiv:2303.10668](https://arxiv.org/abs/2303.10668)

Dressed Rydberg atoms:

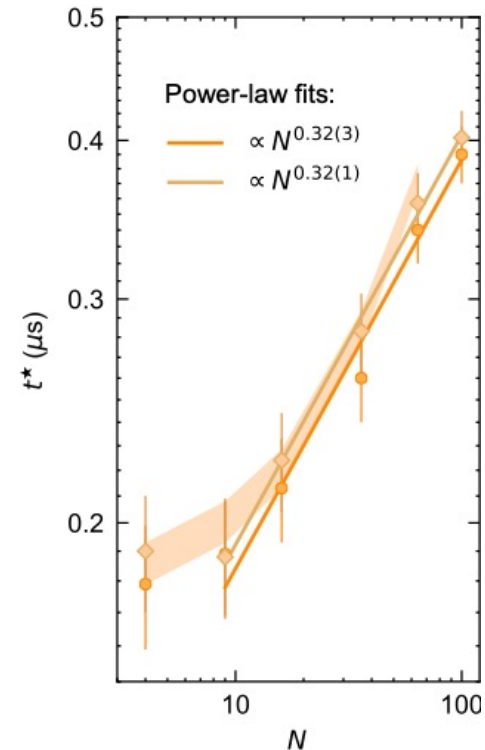
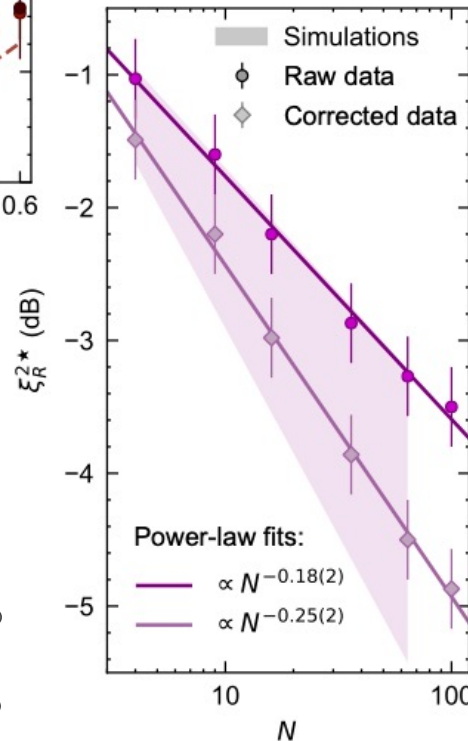
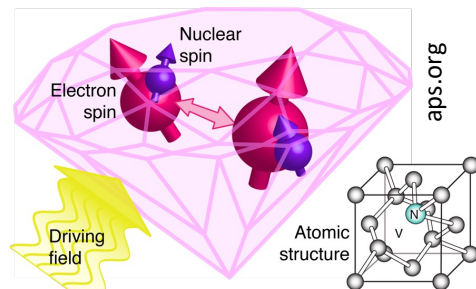
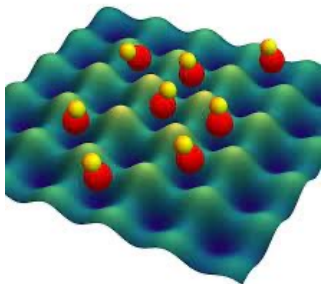
A. Kaufman

[arXiv:2303.10668](https://arxiv.org/abs/2303.10668)

M. Schleier-Smith

[arXiv:2303.08805](https://arxiv.org/abs/2303.08805)

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Conclusion and outlook: XY and beyond...

Measuring the dispersion relation

FM: $\omega(\mathbf{q}) \propto \sqrt{q}$

AFM: $\omega(\mathbf{q}) \propto q$

H. P. Büchler PRL 2012

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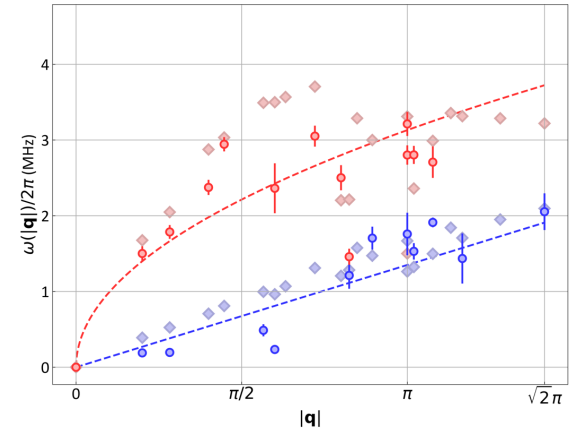
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Preliminary



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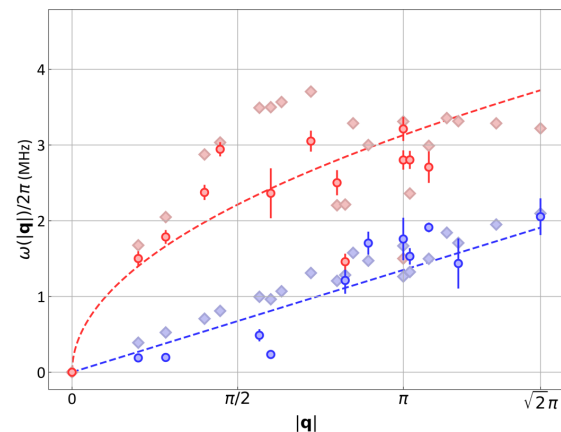
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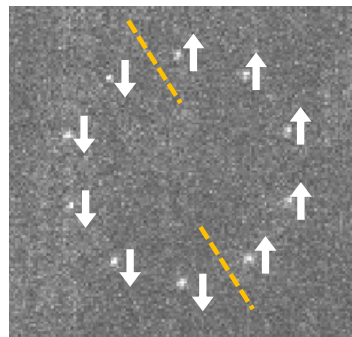
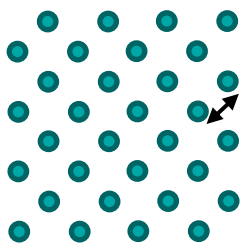
Preliminary



Floquet engineering

XYZ model: MW + XY

$$\hat{H}_{XYZ} = \sum_{i \neq j} J_{ij}^x \sigma_i^x \sigma_j^x + J_{ij}^y \sigma_i^y \sigma_j^y + J_{ij}^z \sigma_i^z \sigma_j^z$$



$$\hat{H}_{\text{Heis.}} = \sum_{i \neq j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$$

Scholl *et al.*, PRXQ (2022)

Conclusion and outlook: XY and beyond...

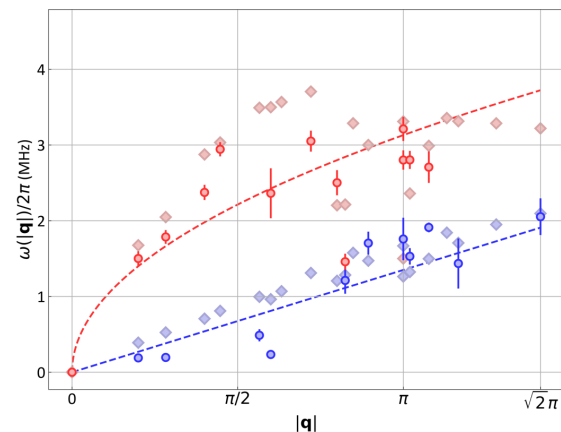
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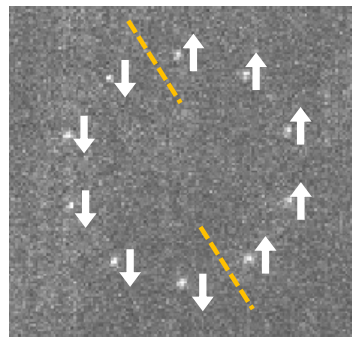
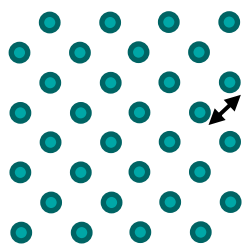
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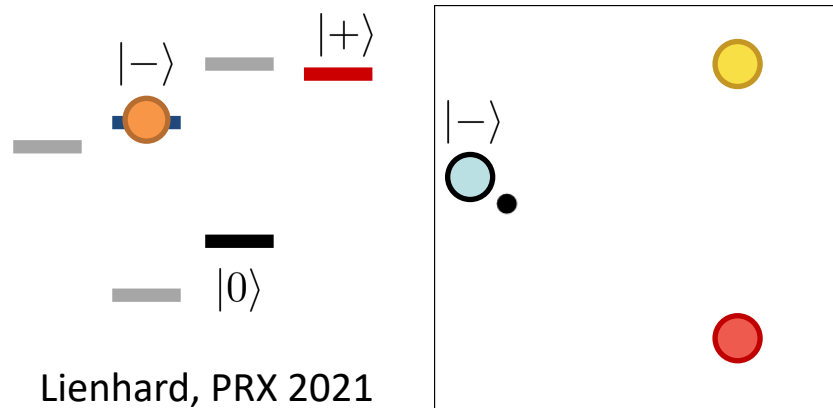
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Scholl *et al.*, PRXQ (2022)

$$\hat{H}_{\text{Heis.}} = \sum_{i \neq j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$$

Spin-orbit coupling



Lienhard, PRX 2021

Frac. Chern ins. Weber, *et al.* PRXQ 2022

