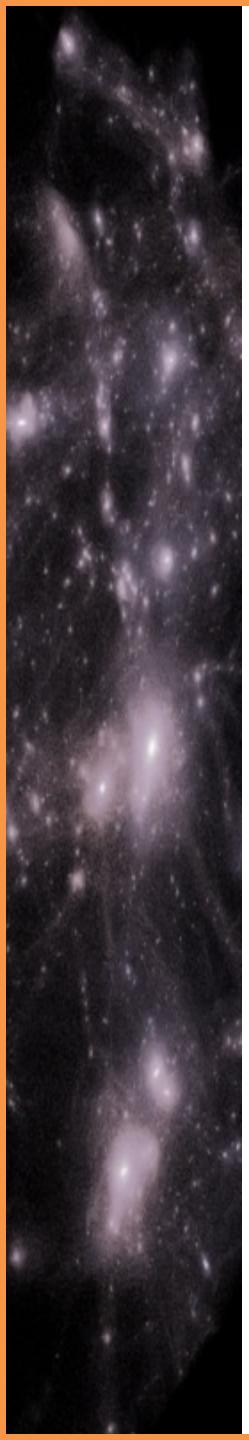


Cosmological Constraints from Galaxy Cluster Mass Profiles

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Why and How ?

Bibliography:

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- Corasaniti & Rasera, MNRAS, 487, 4382 (2019)
- Corasaniti, Giocoli, Baldi, PRD, 102, 043501 (2020)
- Corasaniti, Sereno, Ettori, ApJ, 911, 82 (2021)
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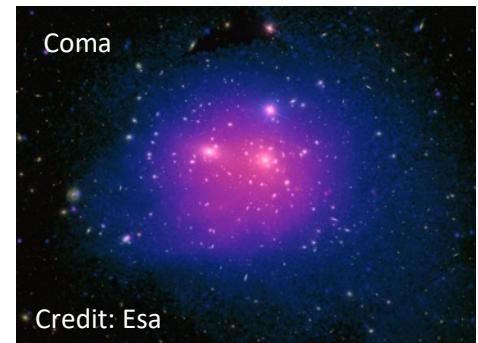
Collaborators:

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Galaxy Cluster Cosmology

Cosmic Probes

- Largest Most Massive Structures in the Universe
- Ultimate Result of Hierarchical Bottom-Up Structure Formation Process
- X-ray, SZ, Optical & Near-IR
- Cluster Abundance, Baryon Fraction, Spatial Clustering & Internal Mass Distribution



Cluster Number Counts

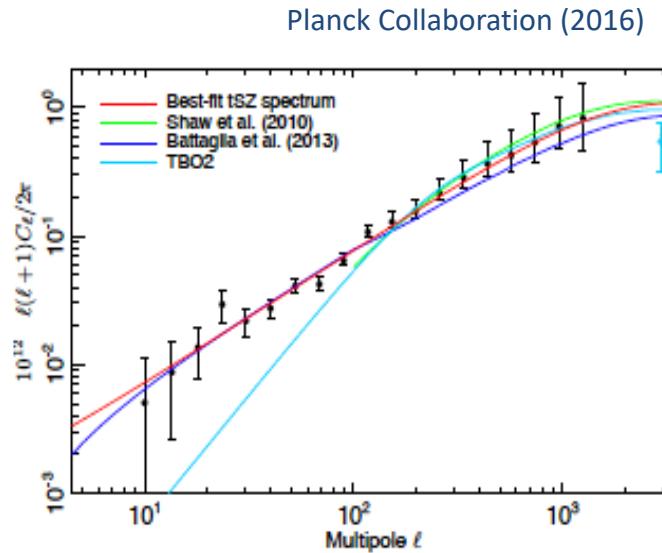
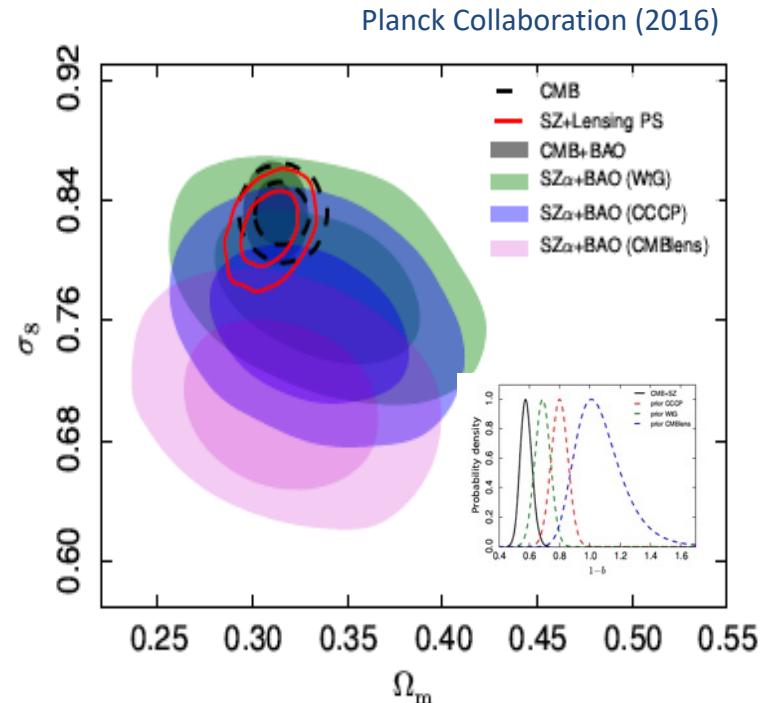
- Planck-SZ Catalog
- SPT-SZ, XXL, DES
- Low Ω_m & σ_8
- Primary Systematics: Mass Calibration Bias, Selection, Halo Mass Function Model

Baryon Fraction

- $f_{\text{gas}} = M_{\text{gas}}/M_{\text{tot}} \sim f_{\text{baryon}} = \Omega_b / \Omega_m$
- Primary Systematics: Mass Calibration Bias, Gas Depletion

Spatial Clustering

- 2-Point Correlation Function SZ Sources
- Primary Systematics: Selection Function, Halo Bias Model, Secondary Sources



NFW-Profile

Universal Profile

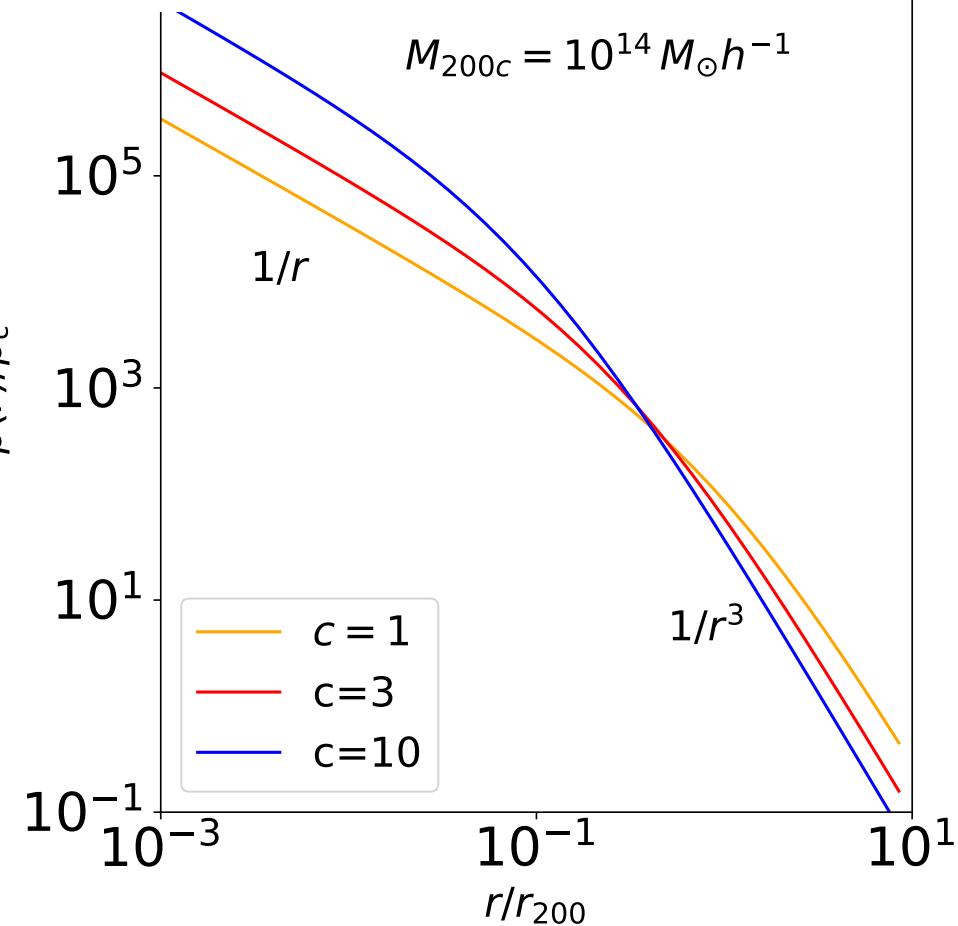
$$\rho_{\text{NFW}}(r) = \frac{M_{200}}{4\pi[\ln(1+c) - c/(1+c)]} \times \frac{1}{r \left(\frac{r_{200}}{c} + r\right)^2}$$

$$c = \frac{r_{200}}{r_s}$$

Navarro, Frenk & White (1997)

$$\rho_{\text{NFW}}(r) \propto \begin{cases} r^{-1} & r \ll r_s \\ r^{-3} & r \gg r_s, \end{cases}$$

- The smaller r_s the more compact the halo
- c is a proxy of halo concentration

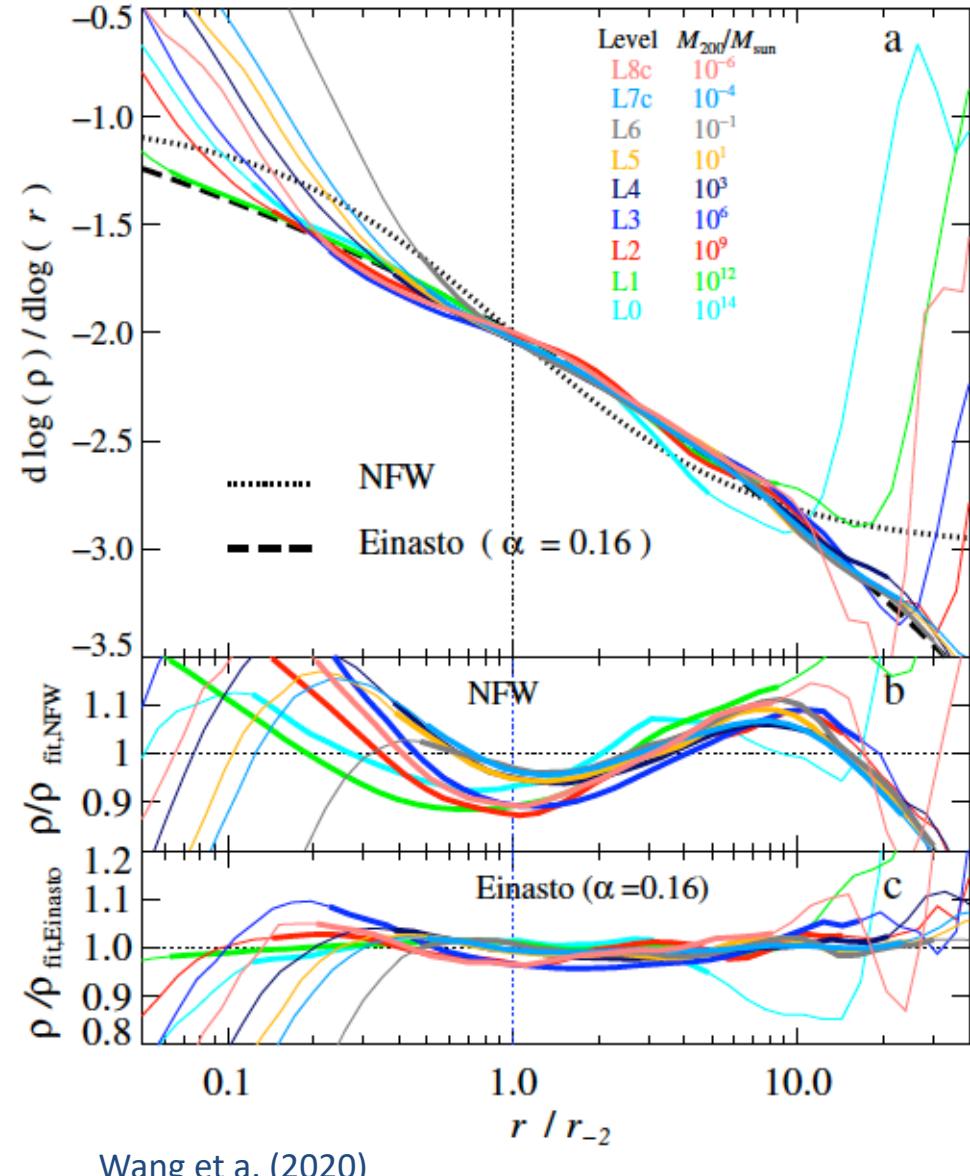


Universality of Halo Profile

- Successive N-body zoom simulations
- Average profile of dozen most massive halos at each refinement level
- Spans 20 order mass scales
 - NFW ($< 10\%$)
 - Einasto ($< 5\%$)

Origin of Universality?

- Gravity + Initial Scale Invariant Spectrum



Concentration-Mass Relation

Halo Density Profile

- c = random variate

- Median

$$c(M, z) = \frac{c_0}{1+z} \left(\frac{M}{10^{14} h^{-1} M_{\odot}} \right)^{\alpha}$$

- scatter

$$\sigma_{\ln c} \sim 0.3 \text{ (large)}$$

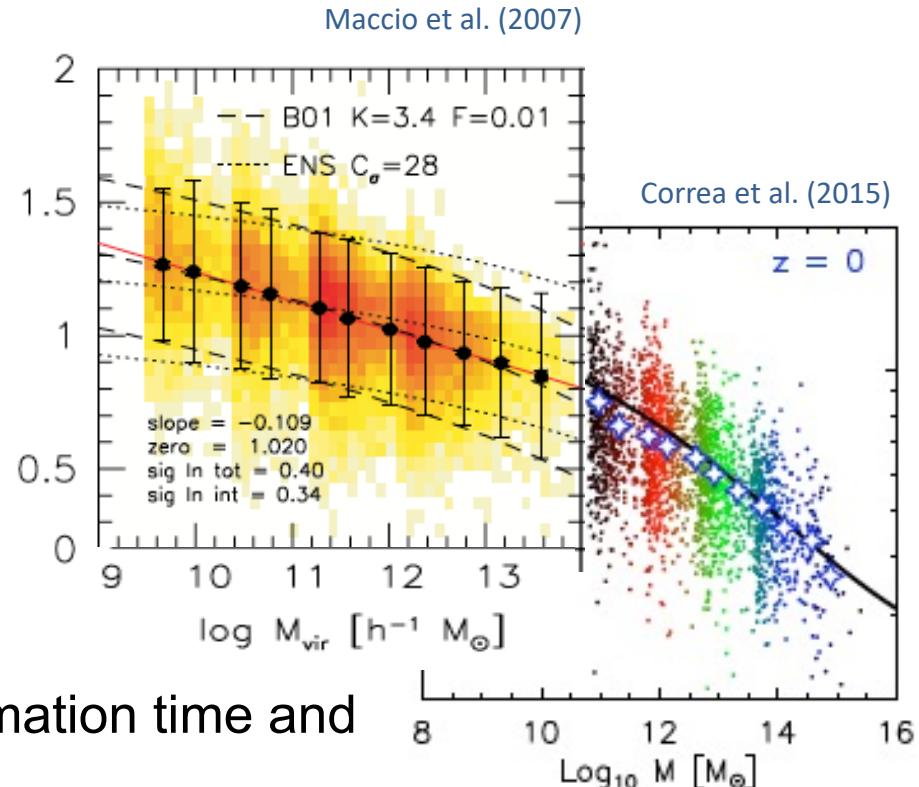
- Correlates with halo formation time and mass assembly history

see e.g. Zhao et al. (2003), Ludlow et al. (2012)

Cosmology

- $\alpha \sim -0.1$;
- c_0 : cosmology dependent;

Klypin et al. (2003); Dolag et al. (2004)



$$c_0 \rightarrow c_0^{\Lambda CDM} \cdot \frac{D_+(z_{coll})}{D_+^{\Lambda CDM}(z_{coll})}$$

Observational Challenges

Systematic Effects

- Impact of Cooling, Star Formation, SN & AGN feedback
- X-ray Observations: Deviations from HE

e.g. Gnedin et al. (2004); Duffy et al. (2010); De Boni et al. (2013);
Rasia et al. (2013)

- Lensing Observations: Shape & Orientation

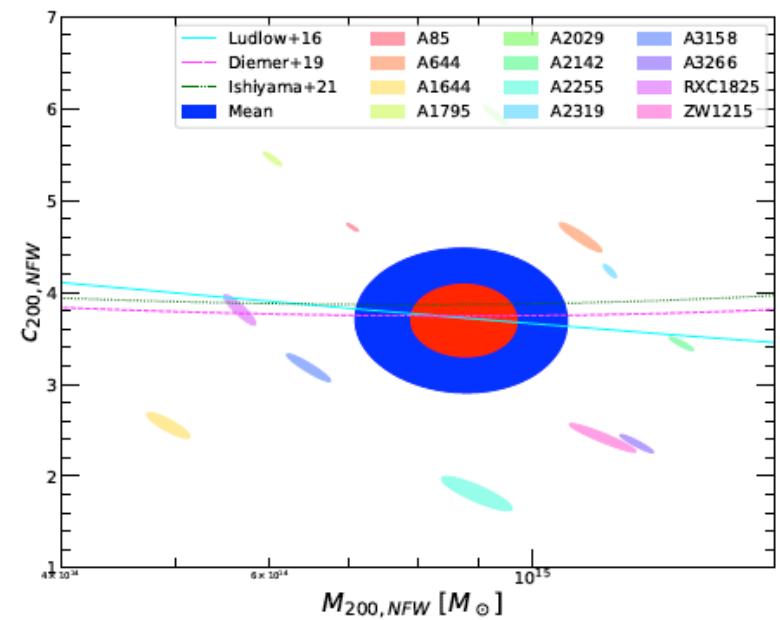
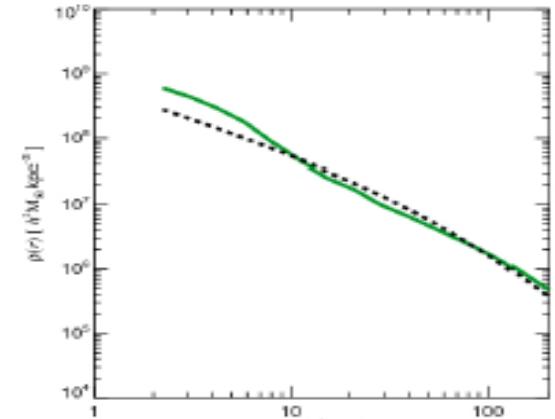
e.g. Oguri et al. (2005); Corless, King & Clowe (2009), Sereno et al. (2013)

- Selection Effects

Sereno et al. (2014)

X-COP Concentrations

- Large Scatter
- Consistent with c-M relations in literature
- No cosmological constraints out of it





Claim

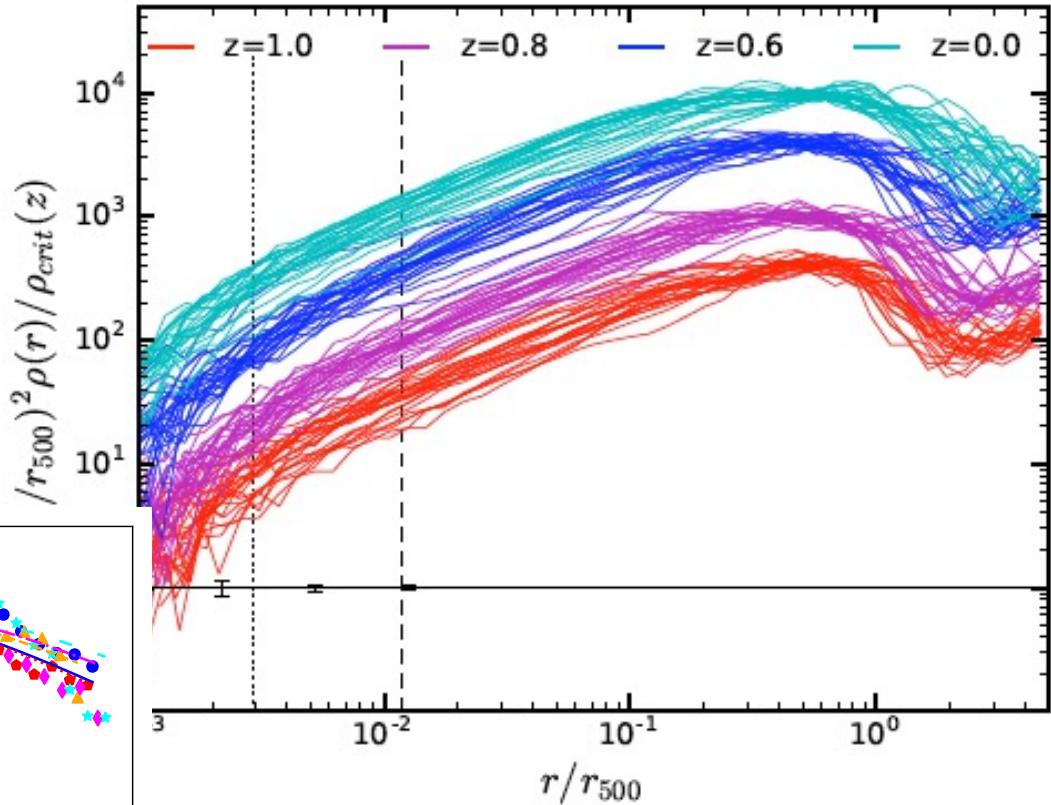
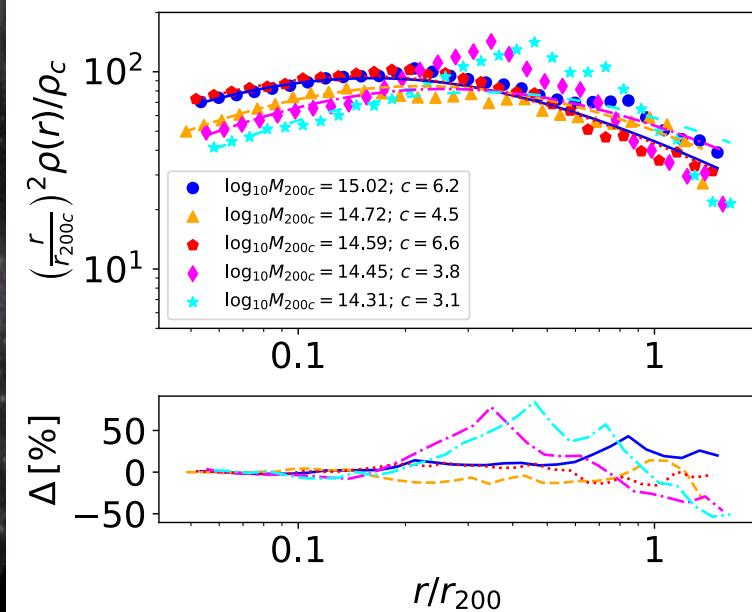
**There is cosmological and
astrophysical information encoded in
the mass profile of halos which goes
beyond what is parametrized by the
NFW profile!**

N-body Halo Profiles

Perturbed Profile

Le Brun et al. (2018)

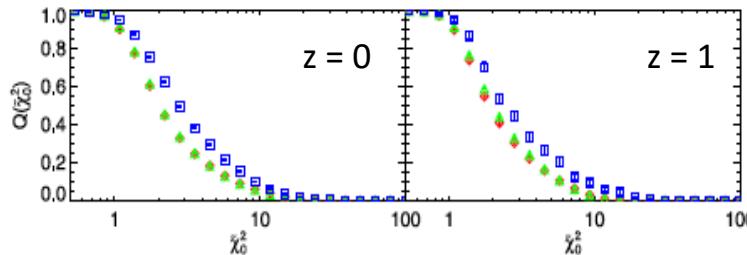
- Zooms of 25 massive halos $\sim 10^{15} M_{\text{sun}} h$
- Negligible Poisson Errors
- Scatter: sub-structures and perturbed state



- Five most massive Bolshoi halos
- Deviations $\sim 10\%$ relaxed halos
- Impact NFW goodness-of-fit

Perturbed Halo Profiles

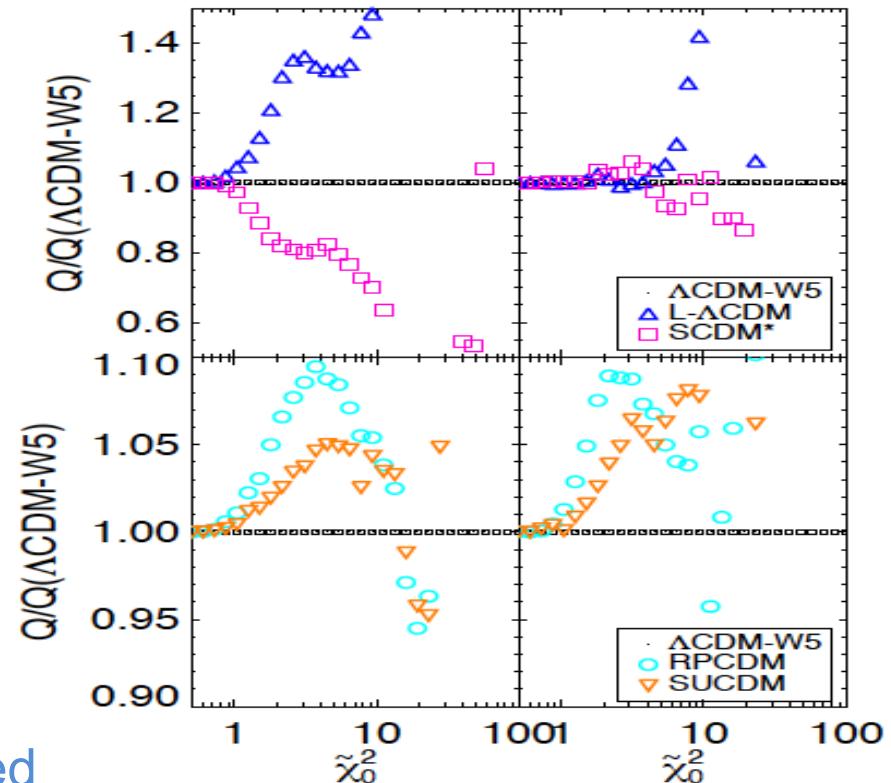
NFW Goodness-of-fit



- Cumulative Reduced χ^2 -distribution
- 10% of halos $>2\sigma$ deviation from NFW
- Deviations larger for massive halos

- Deviations strongly correlates with underlying model

- The less efficient the structure formation with respect to reference model the larger the fraction of halos deviating from NFW



Non-parametric proxy needed



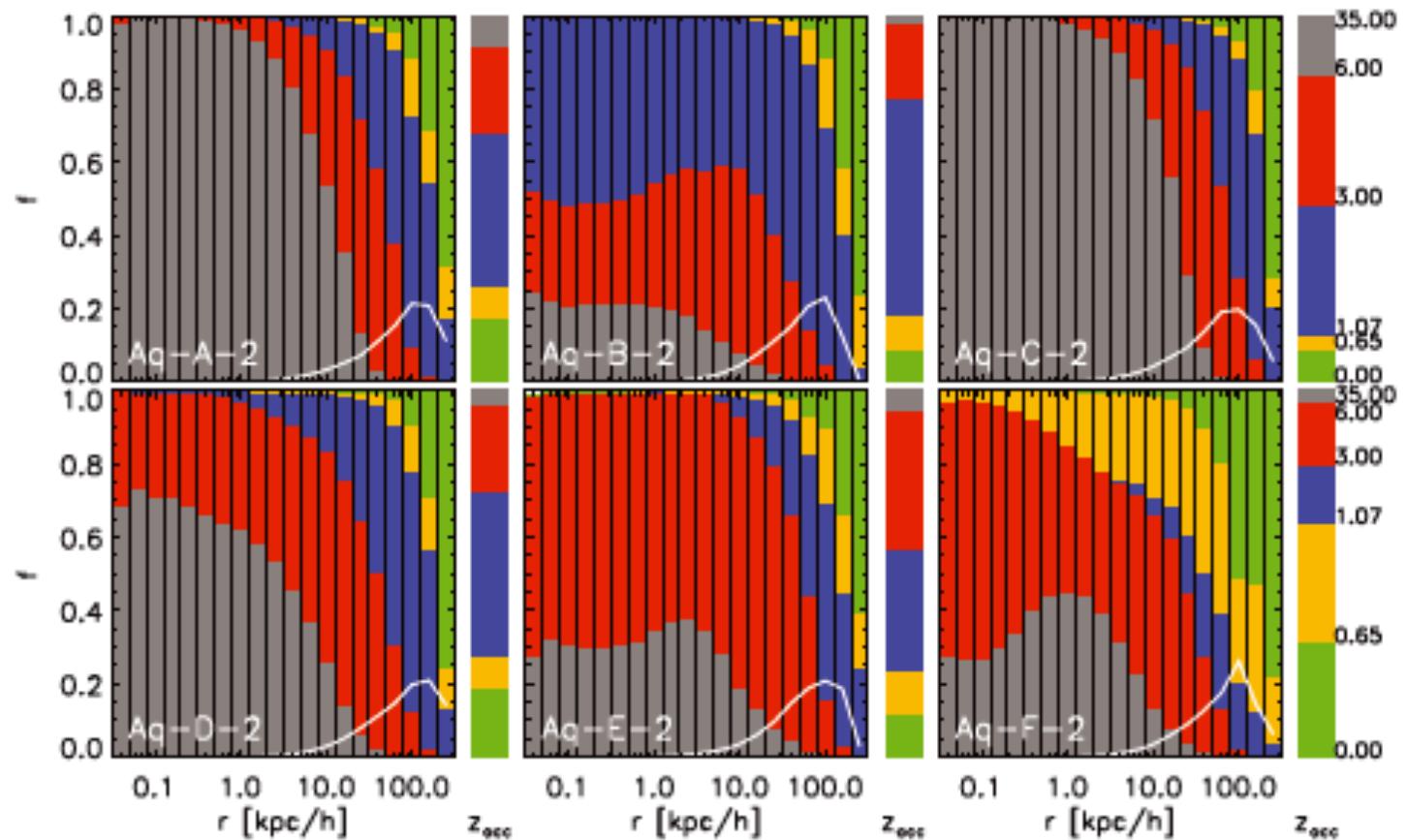
Proxy of Halo Mass Profile

- Non-parametric Observable Estimator
- Capture differences in radial halo mass distribution
- Probe region of choice
- Retrieve cosmological information
- Easily predictable

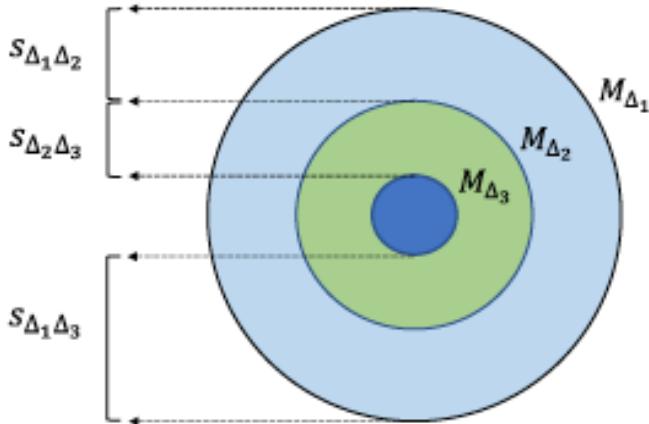
Halo Structure

Aquarius Halos

- Halo form inside-out (Onion-like structure)



Halo Sparsity



Mass Ratio:

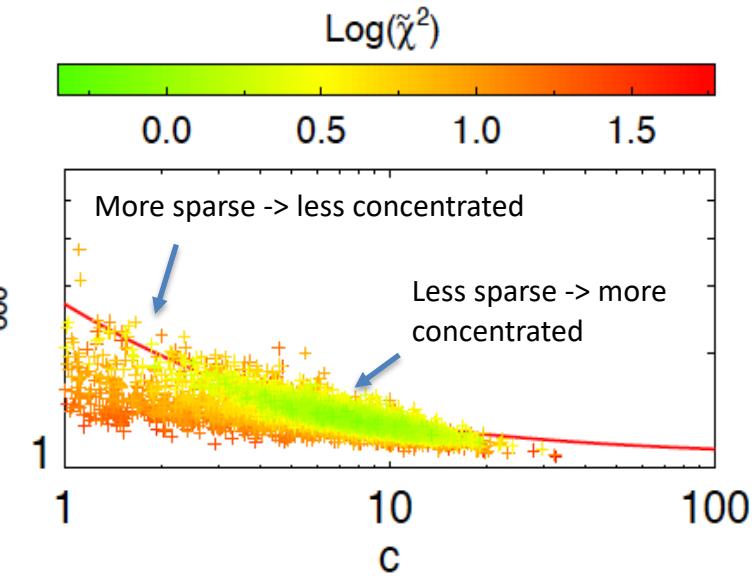
$$\bar{s}_{\Delta_i \Delta_j} = \frac{M_{\Delta_i}}{M_{\Delta_j}} \equiv \frac{\Delta M}{M_{\Delta_j}} + 1$$

- $\Delta_i < \Delta_j$
- $\Delta_i \geq 100$ (preserve halo individuality)
- $\Delta_j \leq 2000$ (avoid baryon dominated region)

Sparsity of NFW Halos

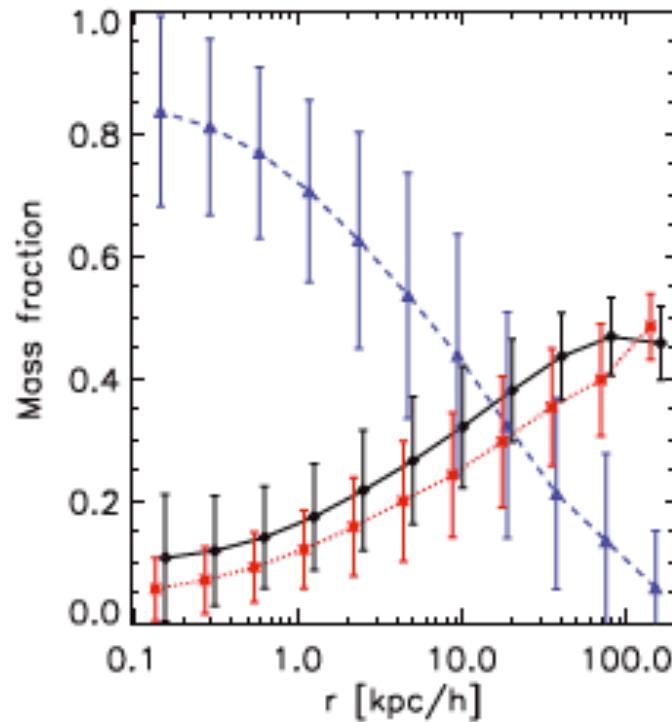
$$s_\Delta = \frac{200}{x^3 \Delta} \quad \& \quad x^3 \frac{\Delta}{200} = \frac{\ln(1 + cx) - \frac{cx}{1+cx}}{\ln(1 + c) - \frac{c}{1+c}}$$

- Halos with $<1\sigma$ NFW along the expected relation
- Distributed nearly constant value with small scatter



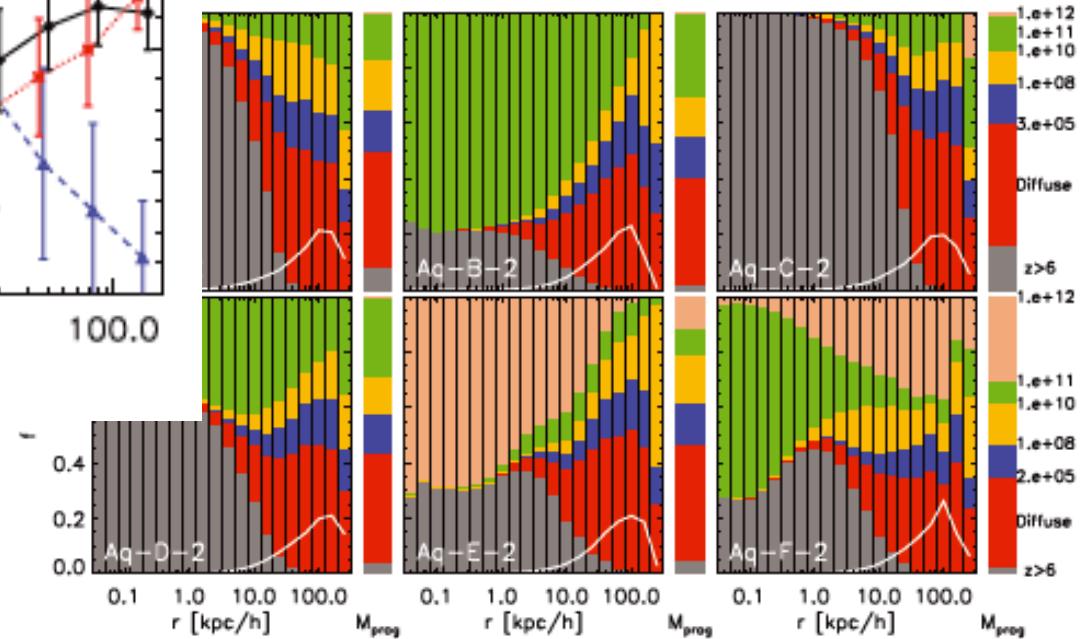
Halo Mass Distribution

Aquarius Halos



- Diffuse Matter contributes non-negligibly to final halo mass

- Major Mergers (~inner regions)
 - Diffuse Matter Accretion & Minor Mergers (~external regions)



Halo Assembly History

Halo Growth

- Fast Accretion (Major Mergers)
- Slow Smooth Accretion (Minor Mergers & Diffuse Matter)

see e.g. Zhao et al. (2003), Li et al. (2007)

Pseudo-Evolution

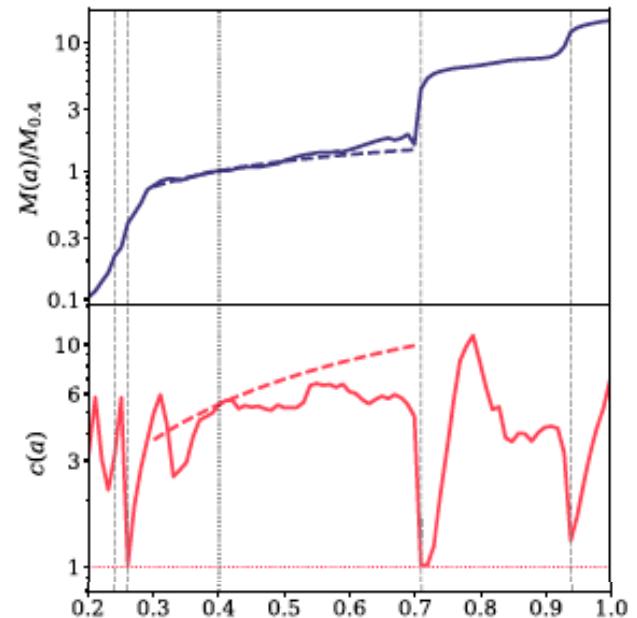
- Halo mass evolution due to reference density

$$M_\Delta(z) = \frac{4}{3}\pi R_\Delta^3(z)\Delta(z)\rho_{\text{ref}}(z)$$

Diemer, More, Kravtsov (2013)

Slow vs Fast Accretion

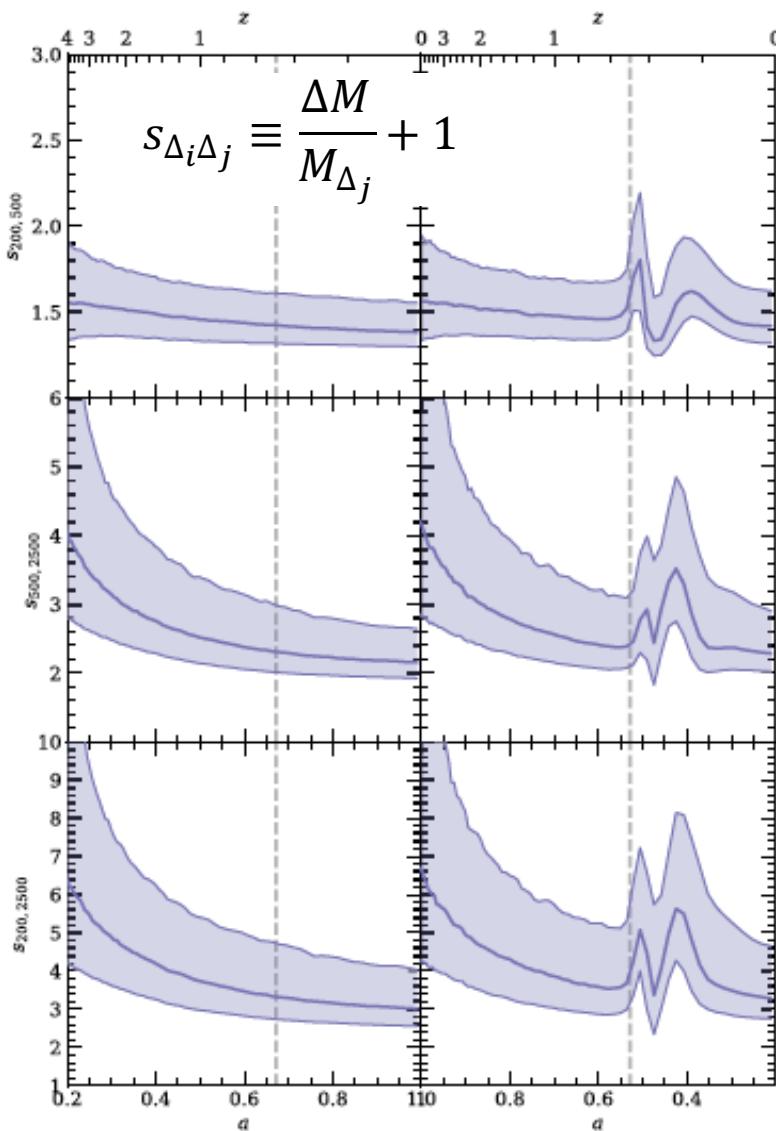
- Concentration deviates from pseudo-evolution
- Scatter due to stochastic minor mergers during slow accretion
- Universal response during major mergers with large excursion



K. Wang et al. (2020)

Halo Sparsity Evolution

Slow vs Pulse-like Evolution



Quiescent Halos Average Sparsities:

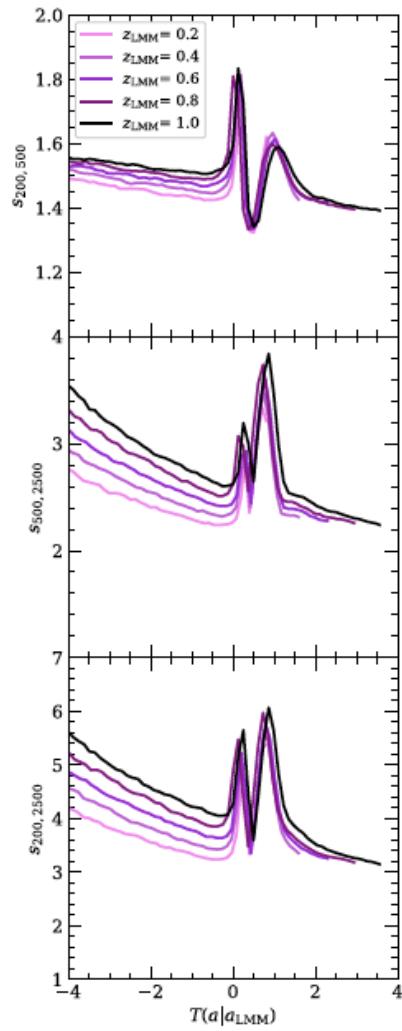
- Nearly Constant Evolution Outer Region
- Decreasing Trend Inner Region

Average Sparsities of Major Mergers
 $z = 0.5$:

- Quiescent Evolution Before Merger
- Pulse-like Shape:
 - First Peak = Merger Enters Outer Region
 - First Dip = Merger Arrives Cores
 - Second Peak = Merger within $< R_{500c}$

Major Merger Response

Universality



- Identical Behavior (in units of dynamical time)

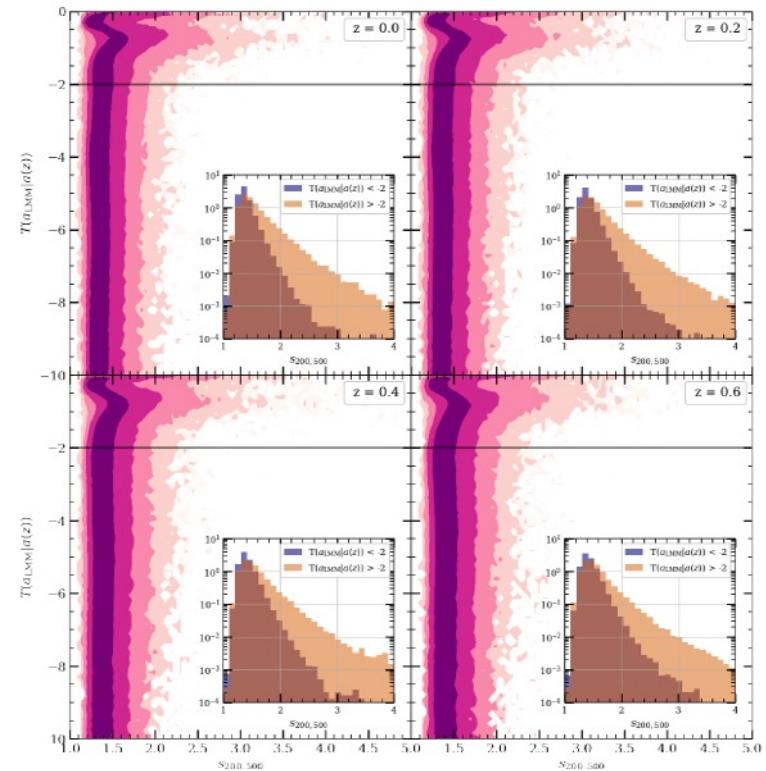
$$T(z; z_{\text{LMM}}) = \frac{\sqrt{2}}{\pi} \int_{z_{\text{LMM}}}^z \frac{\sqrt{\Delta_{\text{vir}}(z)}}{z+1} dz$$

see also Wang et al. (2020) for concentration

- Quiescent Evolution Recovered $t > 2T$

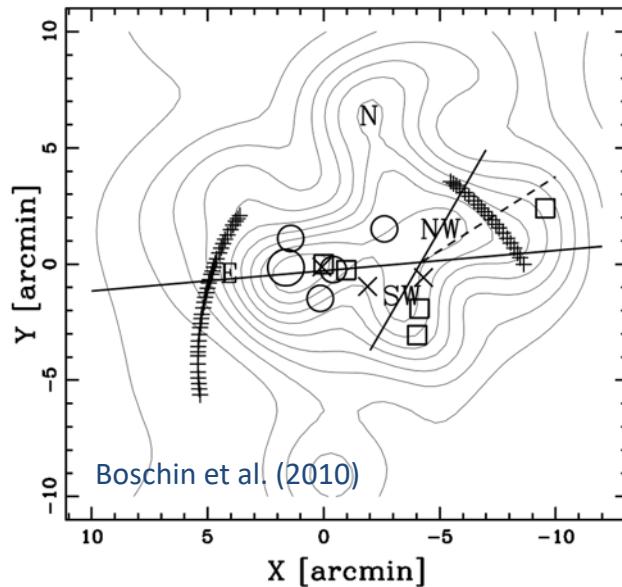
- Halo Population:

- Perturbed Halos ($< 2T$ from last major merger)
- Contribute to scatter in sparsity
- Quiescent Halos



ABELL 2345

Lensing & Radio Relics



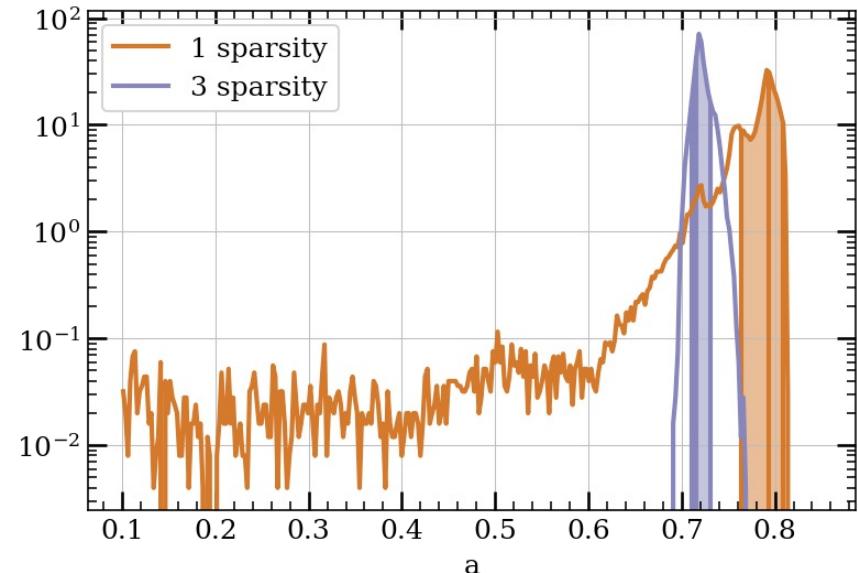
- Uchuu Simulations
Calibrated Distributions
- Timing the merger event:

$$z_{LMM} = 0.396 \pm^{0.01}_{0.03}$$

$$|T| = 0.86 \tau_{dyn}$$

$$\tilde{t}_{LMM} = 2.14 \pm^{0.08}_{0.2} \text{ Gyr (LCDM)}$$

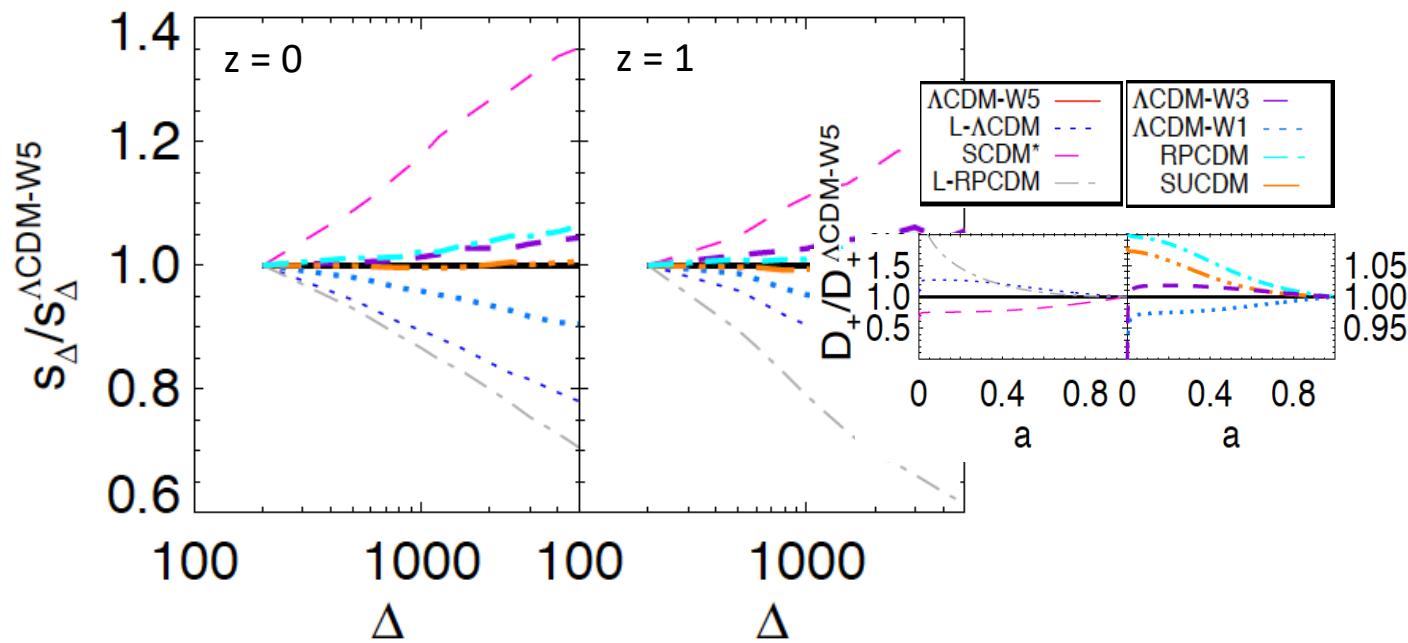
- Redshift $z = 0.176$
- Lensing Masses ($10^{13} M_{\text{sun}}/h$)
 - $M_{2500c} = 0.32 \pm 0.12$ Okabe et al. (2010)
 - $M_{500c} = 6.52 \pm 2.47$
 - $M_{200c} = 28.44 \pm 10.76$
- Sparsities:
 - $s_{200,500} = 4.26 \pm 2.33$
 - $s_{200,2500} = 87.50 \pm 46.83$
 - $s_{500,2500} = 20.06 \pm 10.93$



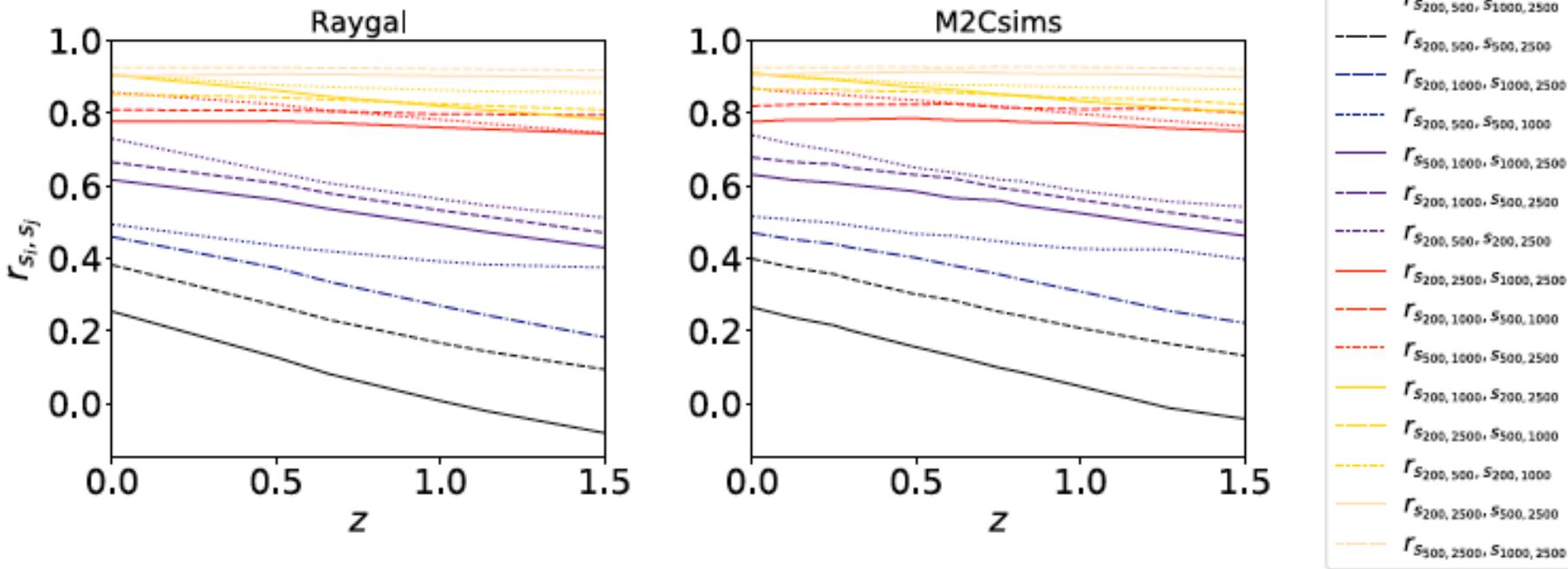
Cosmological Imprint

Average Sparsity

- Cosmological signal increases for $\Delta_2 \gg \Delta_1$
- Sparsity evolution correlates with linear growth history
- The earlier the formation of structures the smaller the sparsity

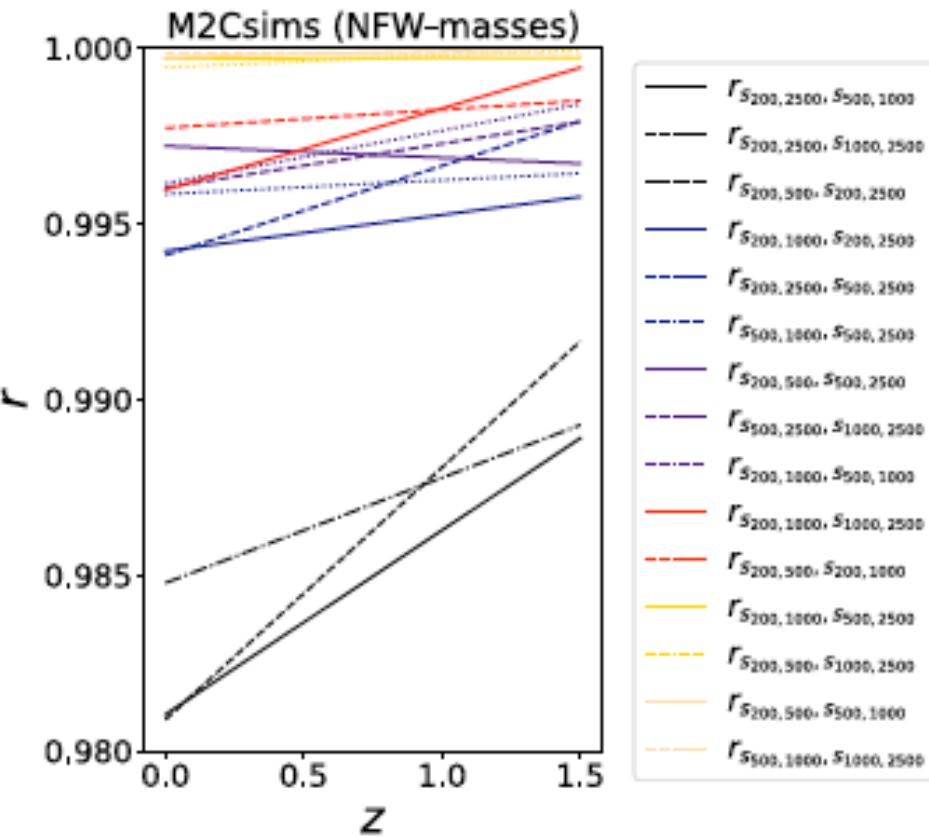


Sparsity Correlations



- Correlations increase at lower redshift (consistent with halo mass assembly process)
- Sparsities probing distant halo shells have low correlations (inner vs outer region)
- Expected from mass accretion history (inner region contains mass from major merger events, outer from minor and diffuse matter accretion)

NFW-induced Correlations



Corasaniti, Le Brun, Richardson et al. (2022)

- Best-fit M2Csims halos at given z with NFW
- Estimate corresponding sparsities halo by halo
- Compute correlations among NFW halo sparsities at given redshift

Results

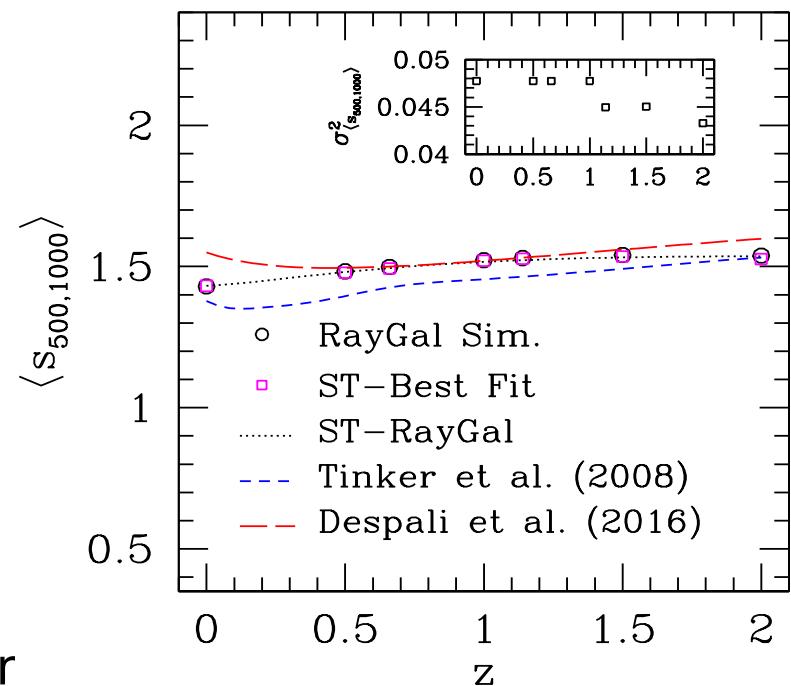
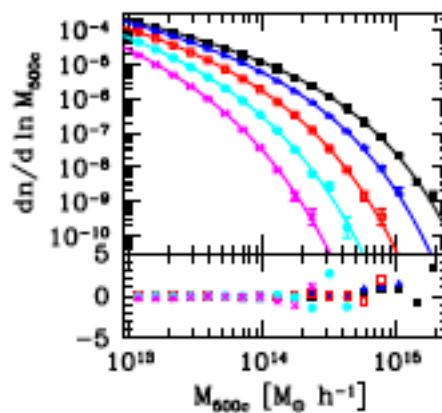
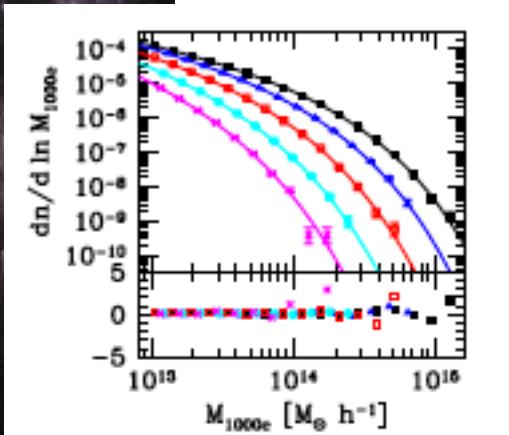
- Assuming NFW destroys all information encoded in different halo mass shells
- Impose Spurious Correlations: $r \sim 1$
- There is more information on the halo mass profile than encoded in the NFW profile

Average Halo Sparsity

Sparsity – Mass Function Relation

$$\frac{dn}{dM_{\Delta_2}} = s_{\Delta_1 \Delta_2} \frac{dn}{dM_1} \frac{d \log M_1}{d \log M_{\Delta_2}} \rightarrow \int_{M_{\Delta_2}^{\min}}^{M_{\Delta_2}^{\max}} \frac{dn}{dM_{\Delta_2}} d \ln M_{\Delta_2} = \langle s_{\Delta_1, \Delta_2} \rangle \int_{\langle s_{\Delta_1, \Delta_2} \rangle M_{\Delta_2}^{\min}}^{\langle s_{\Delta_1, \Delta_2} \rangle M_{\Delta_2}^{\max}} \frac{dn}{dM_{\Delta_1}} d \ln M_{\Delta_1}$$

- N-body Calibrated Halo Mass Functions at Δ_1 and Δ_2



- Accurate to sub-percent level
- Quantitative Framework for Cosmological Model Prediction

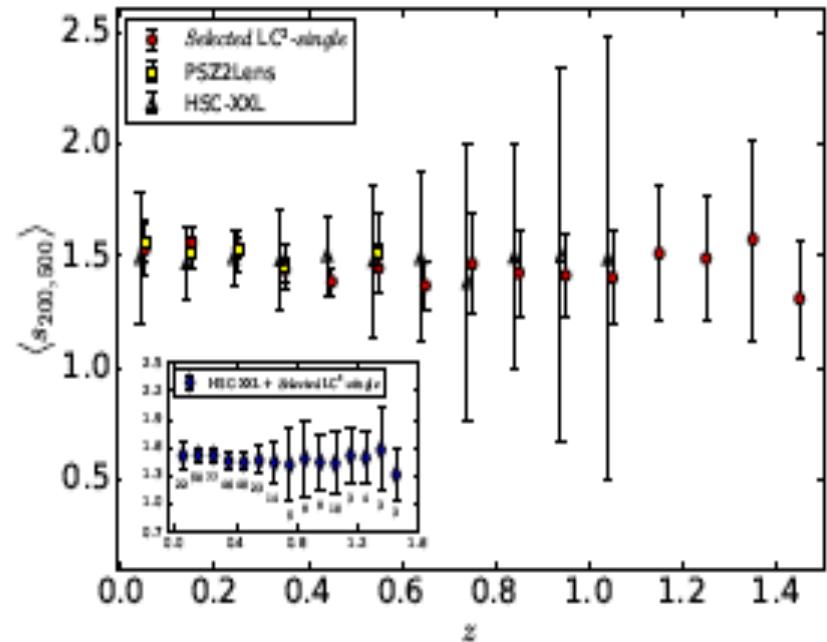
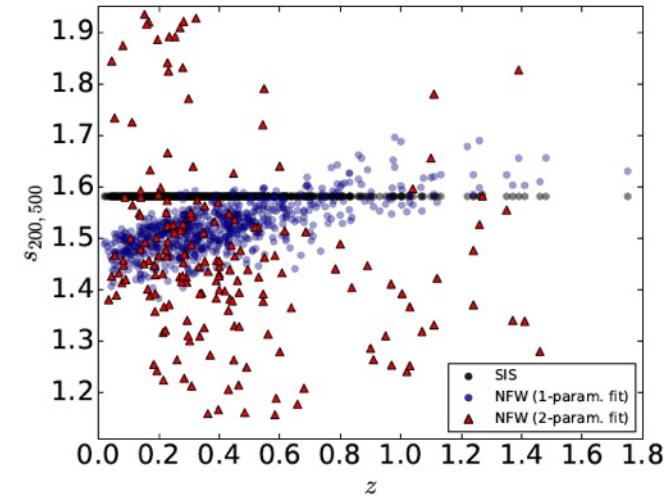
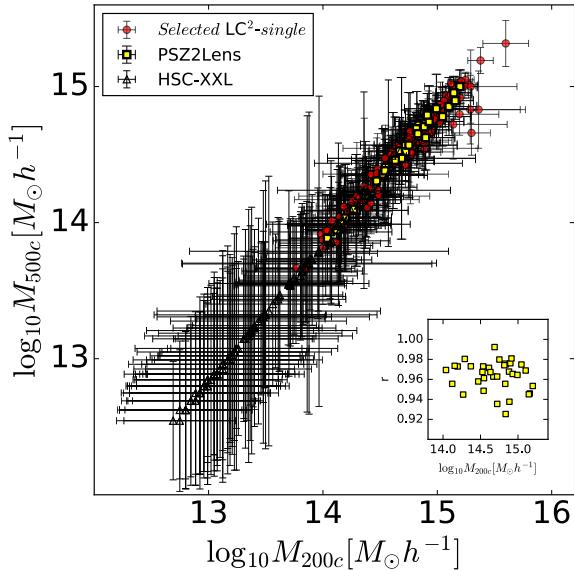
Cosmological Parameter Analysis

Weak Lensing Cluster Masses

- LC² catalog (672 clusters, $z < 1.7$)
[Sereno \(2015\)](#)
- Removing Biased Estimates

Sparsity Cosmological Sample

- Selected LC²-single (317 \supset PSZ2Lens) + HSC-XXL (136, $z < 1.03$)
- $0 < z < 1.5$; $M_{200c} > 10^{13} M_{\odot} h^{-1}$



MCMC - Sparsity + BAO

Model Parameters & Priors

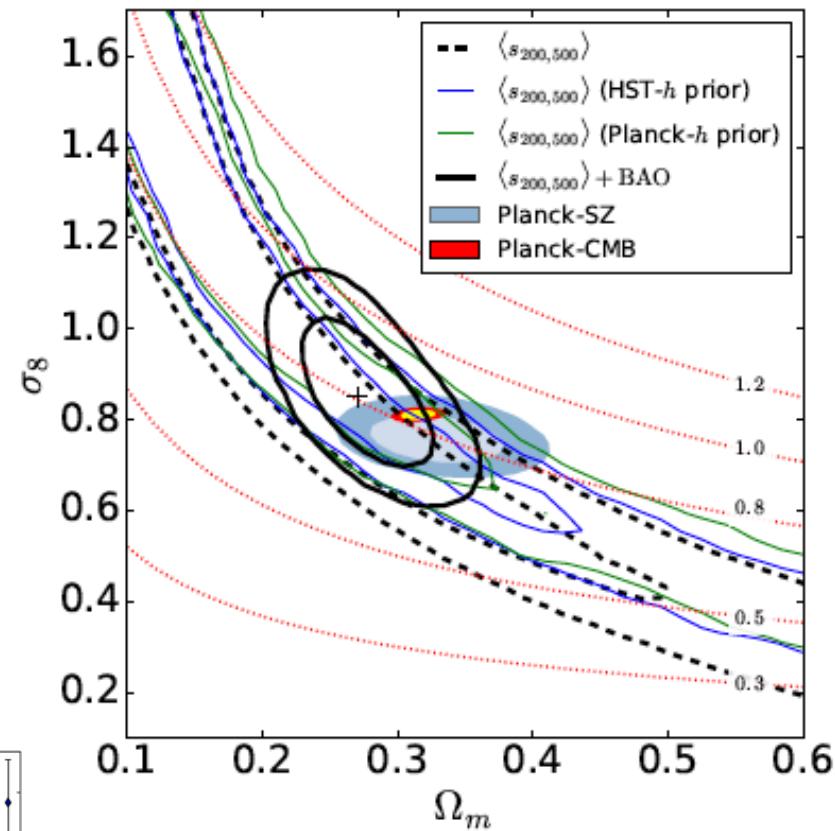
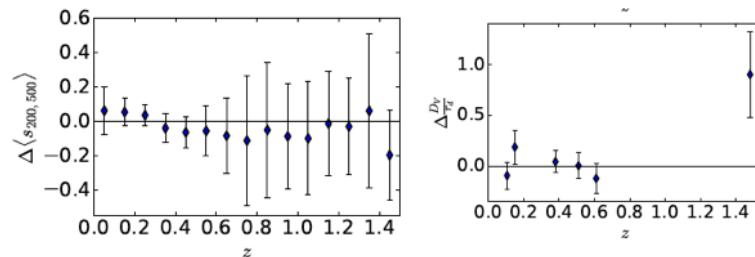
- Ω_m , σ_8 , h (+ n_s -Planck prior & $\Omega_b h^2$ -BBN prior)
- S_8 degeneracy
 - $S_8 = 0.75 \pm 0.20$
 - $S_8 = 0.80 \pm 0.18$ (HST-prior)
 - $S_8 = 0.82 \pm 0.16$ (Planck h-prior)

Pre-reconstruction BAO Data

- Marginal Stats:

$$\begin{aligned}\Omega_m &= 0.28 \pm 0.03 \\ \sigma_8 &= 0.86 \pm 0.10 \\ h &= 0.66 \pm 0.02\end{aligned}$$

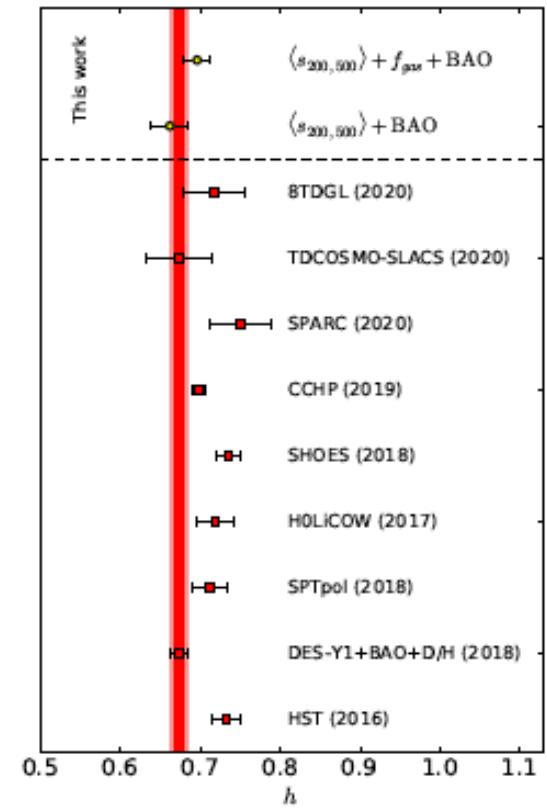
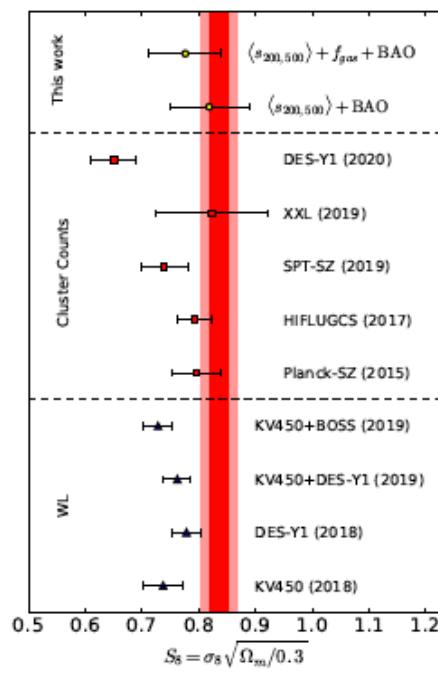
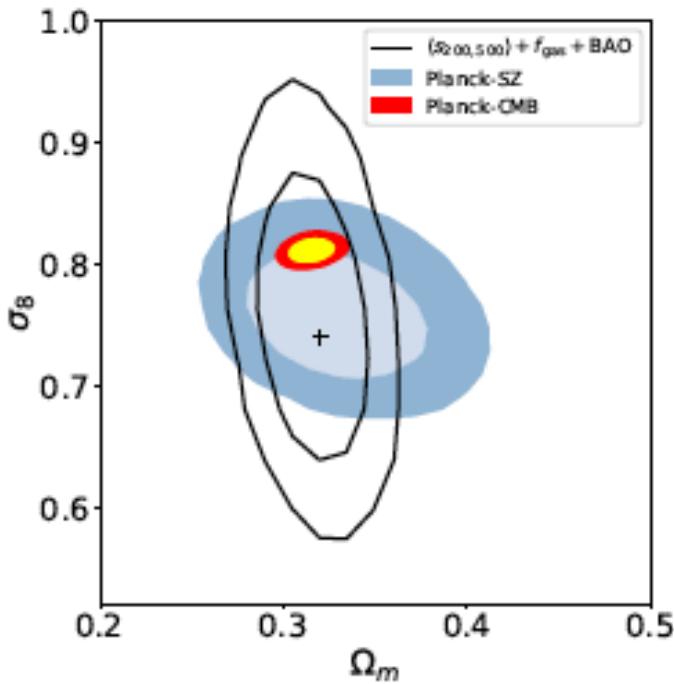
- Residuals



MCMC – Sparsity + f_{gas} + BAO

Joint Analysis

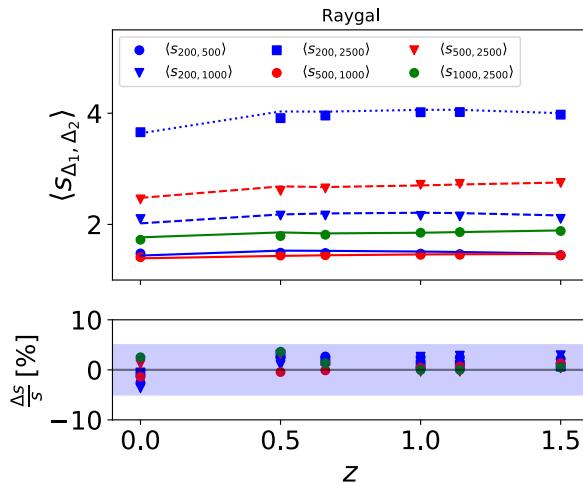
- Marginalized on f_{gas} parameters (K & Y_b)
- $\Omega_m = 0.32 \pm 0.02$; $\sigma_8 = 0.76 \pm 0.07$; $h = 0.70 \pm 0.02$



- Assuming $K_{\text{CLASH}} \sim G(0.79, 0.09)$ $\rightarrow Y_b > 0.89$

Multiple Sparsity Measurements

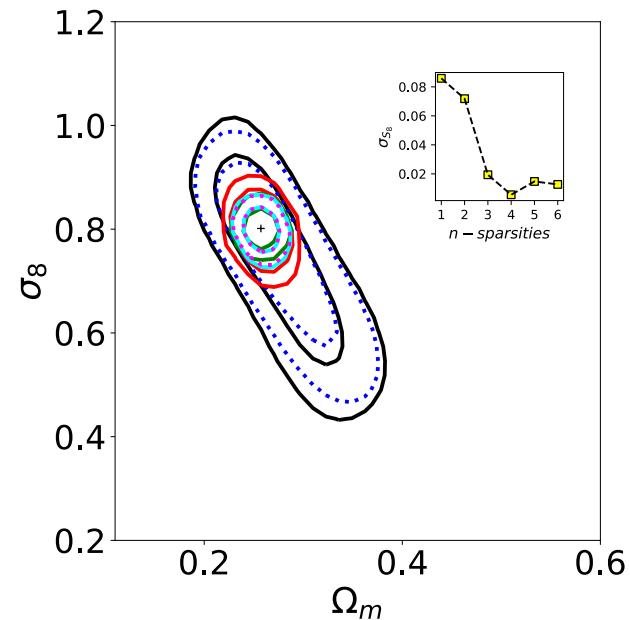
Non-Parametric Cluster Mass Estimates



- Mass Estimates $\Delta = 200, 500, 1000, 2500$
- $N_s = 6$ sparsities
- Correlations + Propagation of theoretical model errors

MCMC Analysis

- Additional sparsities break S_8 degeneracy
- Constraints saturate at $N_s = 4$
- Practically requires mass measurements beyond 2-parameter profile fit



Sparsity Systematic Effects

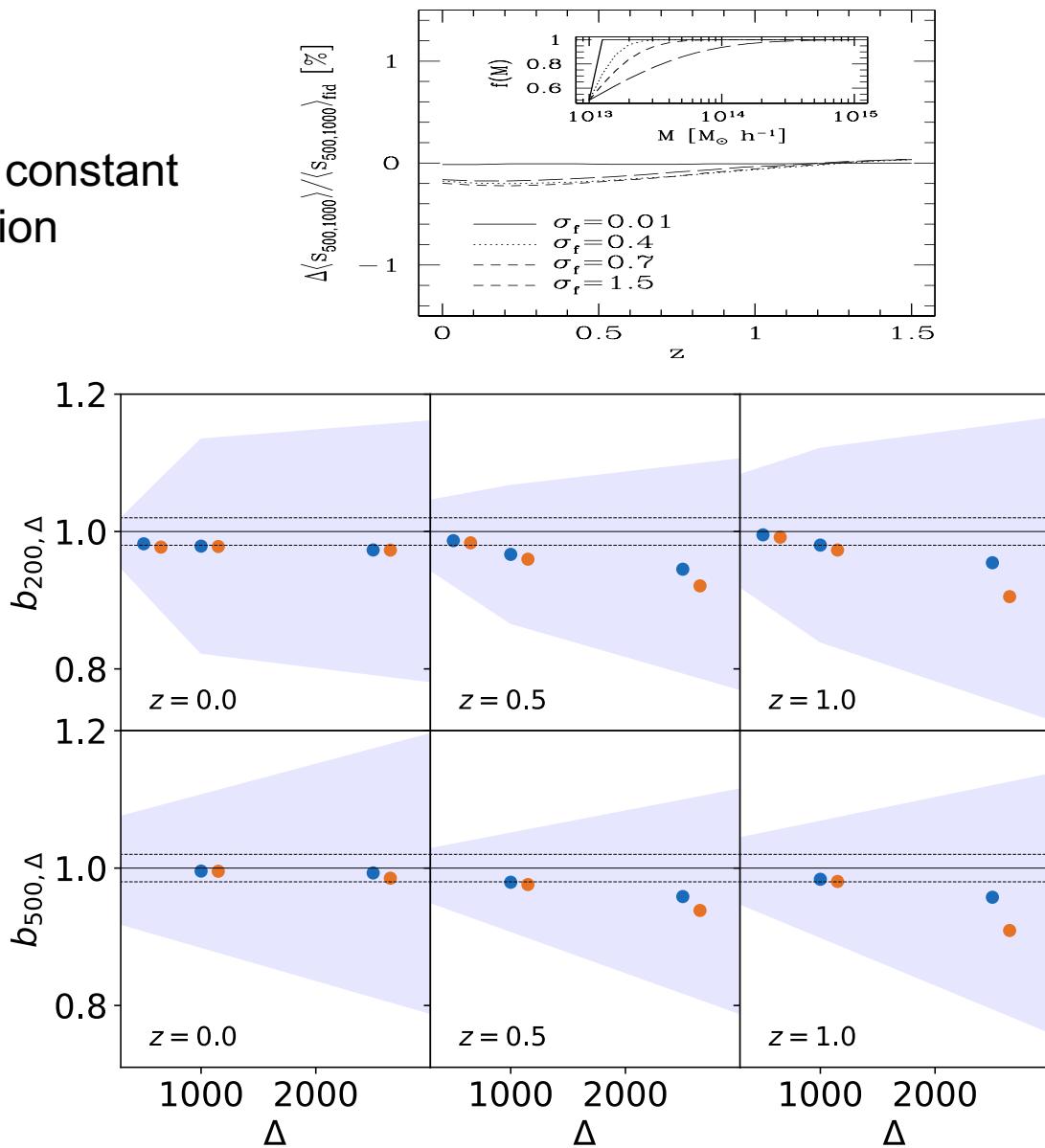
Selection Effects

- Sub-percent level
- Consistent with near constant sparsity – mass relation

Corasaniti et al. (2018)

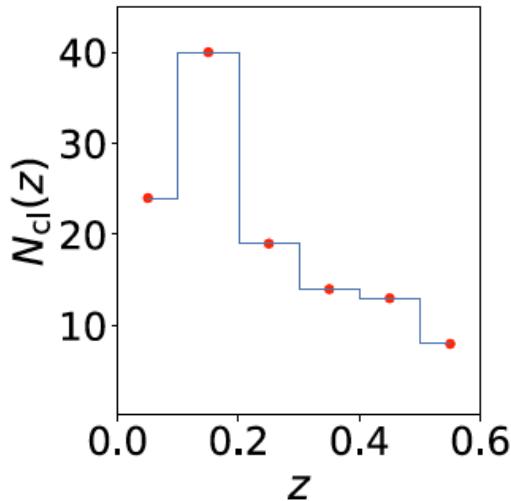
Radial Dependent Mass Bias

- Preliminary analysis of The300
- < 1-2% at $z = 0$
- Increases at $z > 0$ and larger overdensities
- Baryons induce correlations in the inner halo region



Impact on Cosmological Inference

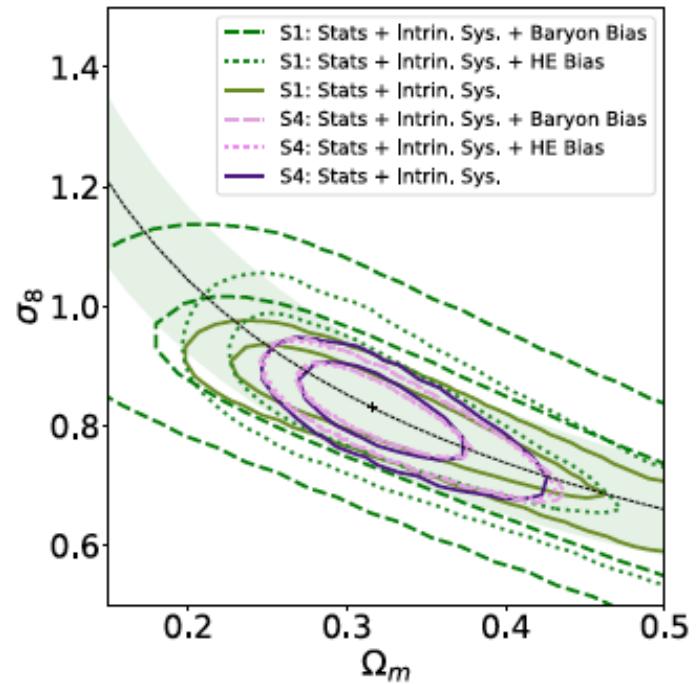
CHEXMATE-like Sample

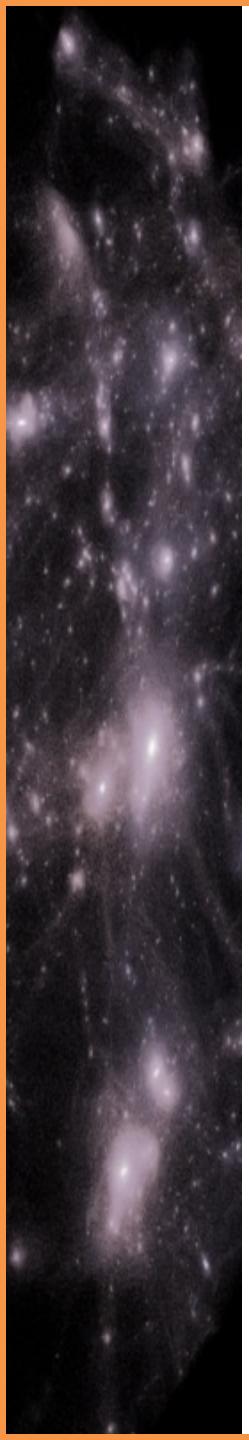


- 118 Clusters in $0 < z < 0.6$
- $e_{MA} = 0.23, 0.15, 0.11 \& 0.10$ (for $\Delta = 200, 500, 1000 \& 2500$)
- Propagate radial mass bias & HE bias
- Single vs Multiple ($n=4$) sparsities

MCMC Constraints

- Significant Effect on Single Sparsity inferred constraints
- Negligible Effect on Multiple Sparsity case
- \sim percent level errors on Ω_m and σ_8





Conclusions

- Non-parametric Probe of Halo Mass Assembly History
- Capture Information Beyond Concentration Parameter
- Minimal Systematics
- Observational Proxy of Cluster Cosmology and Astrophysics

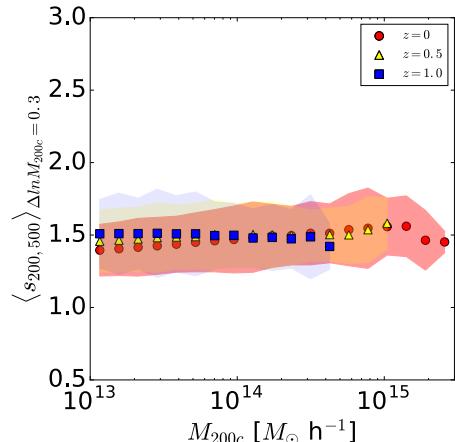
Sparsity Ensemble Properties

RayGalGroupSims Analysis

- $L_{\text{box}} = 2.6 \text{ Gpc}/h$; $N_p = 4096^3$
- SOD Halos ($M_{200c} > 10^{13} M_{\text{sun}}/h$)
- Nearly constant (<10% variation across 2 orders in mass)
- Intrinsic scatter bounded to ~20%
- Trend independent of Δ_1 and Δ_2

Corasaniti et al. (2018)

MultiDark-Planck2 Analysis



- $L_{\text{box}} = 1 \text{ Gpc}/h$; $N_p = 3840^3$
- SOD Halos ($M_{200c} > 10^{13} M_{\text{sun}}/h$)

Corasaniti & Rasera (2019)

