



# NAICRO

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des 2 Infinis



## Horizon of UHECRs in Galaxy Clusters

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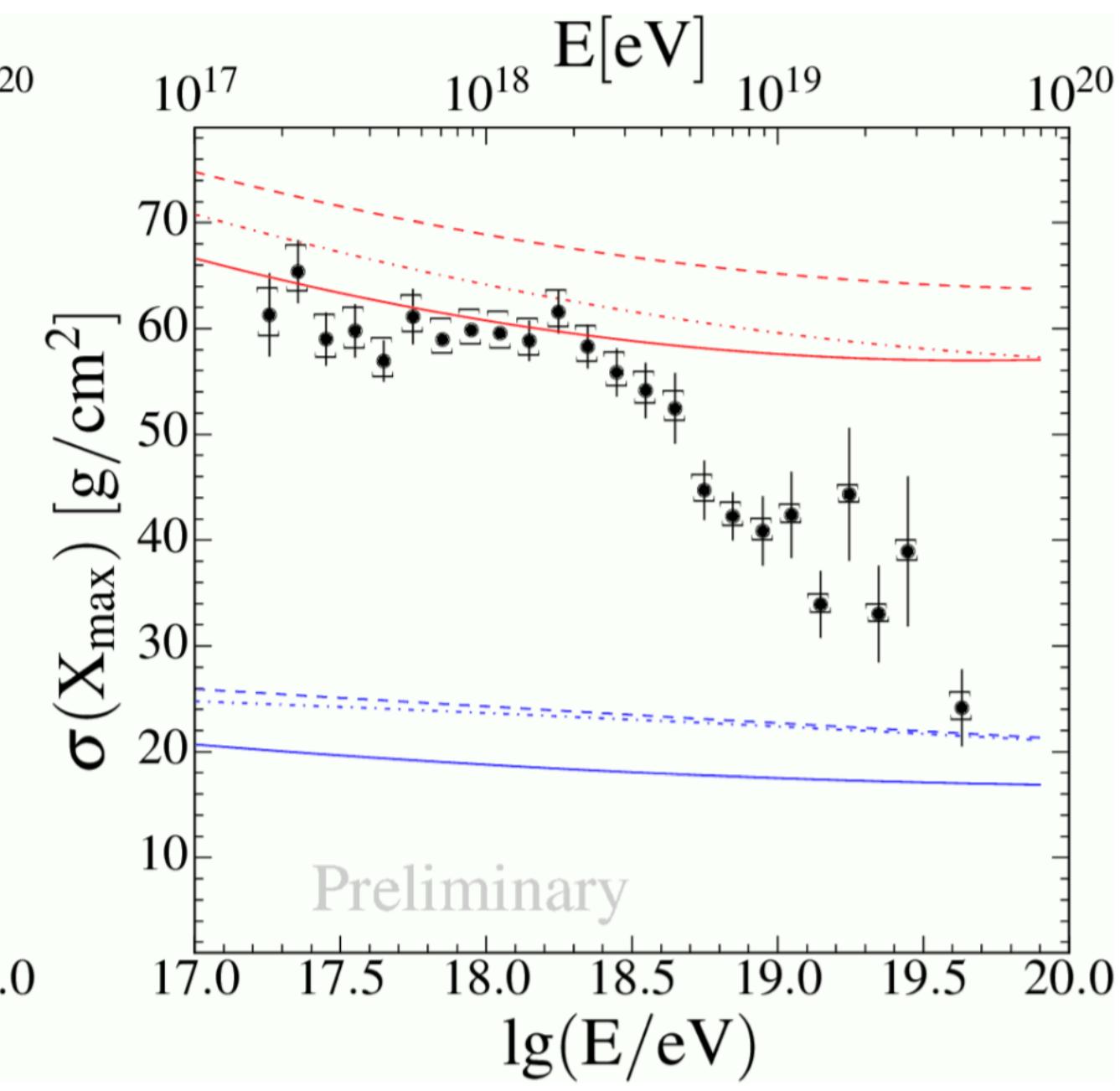
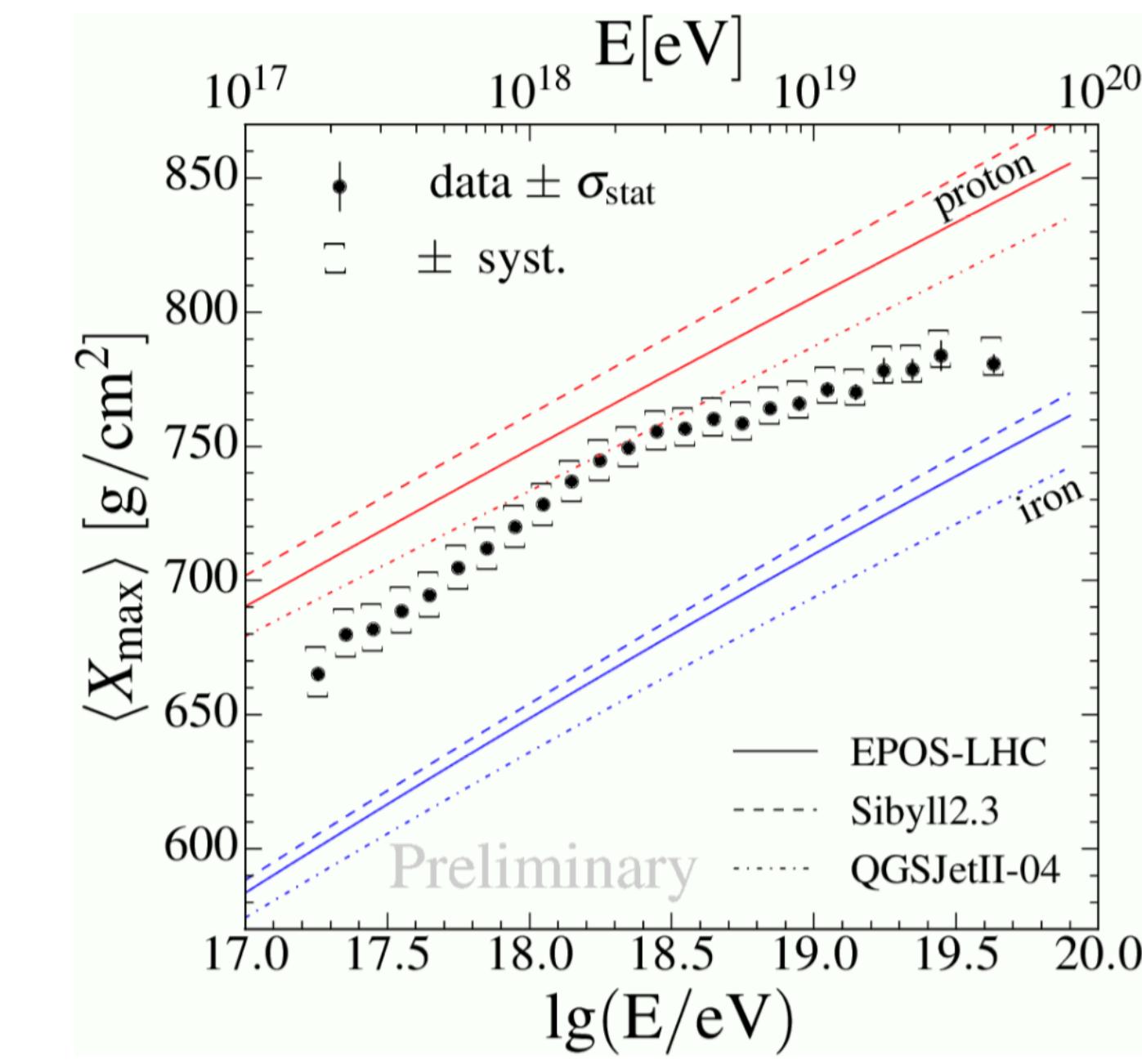
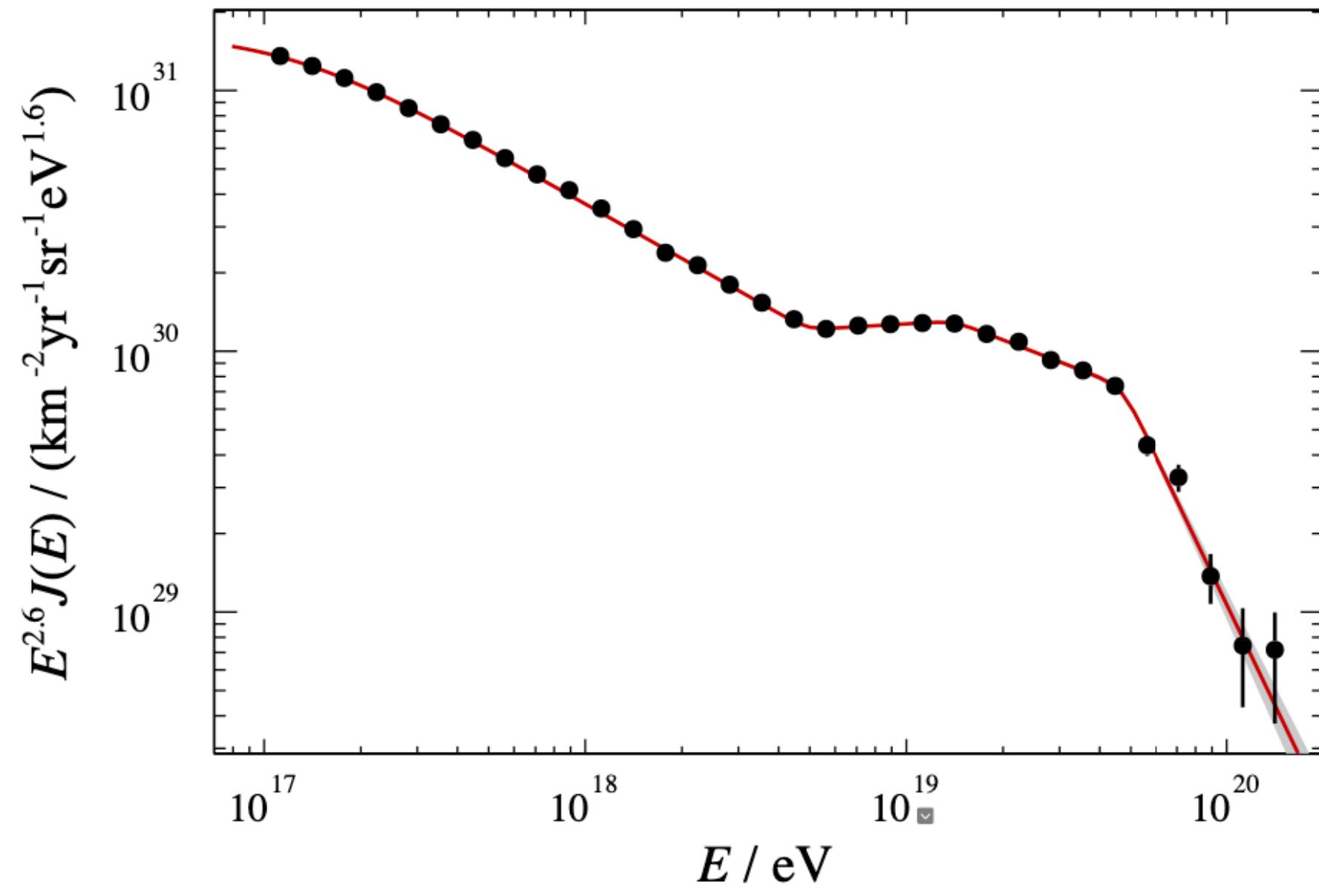
Astroparticle Symposium, 24/11/2022

# Outline

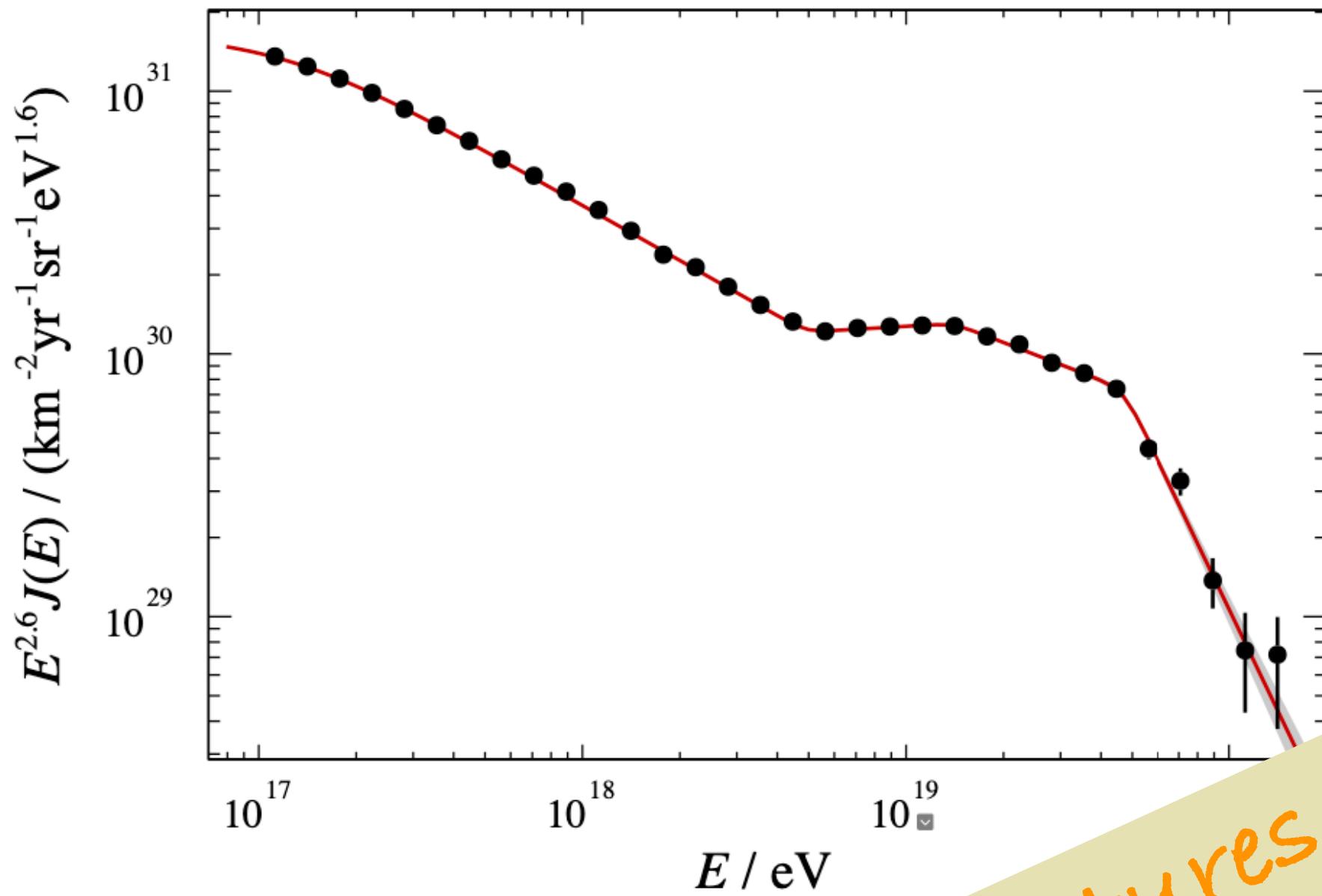
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- ★ Motivation: astrophysical interpretation of UHECRs measurements
- ★ Details of the Clusters' environment
- ★ Propagation of UHECRs in Galaxy Clusters
- ★ Conclusions and future perspectives

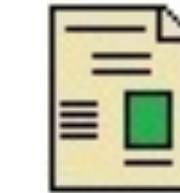
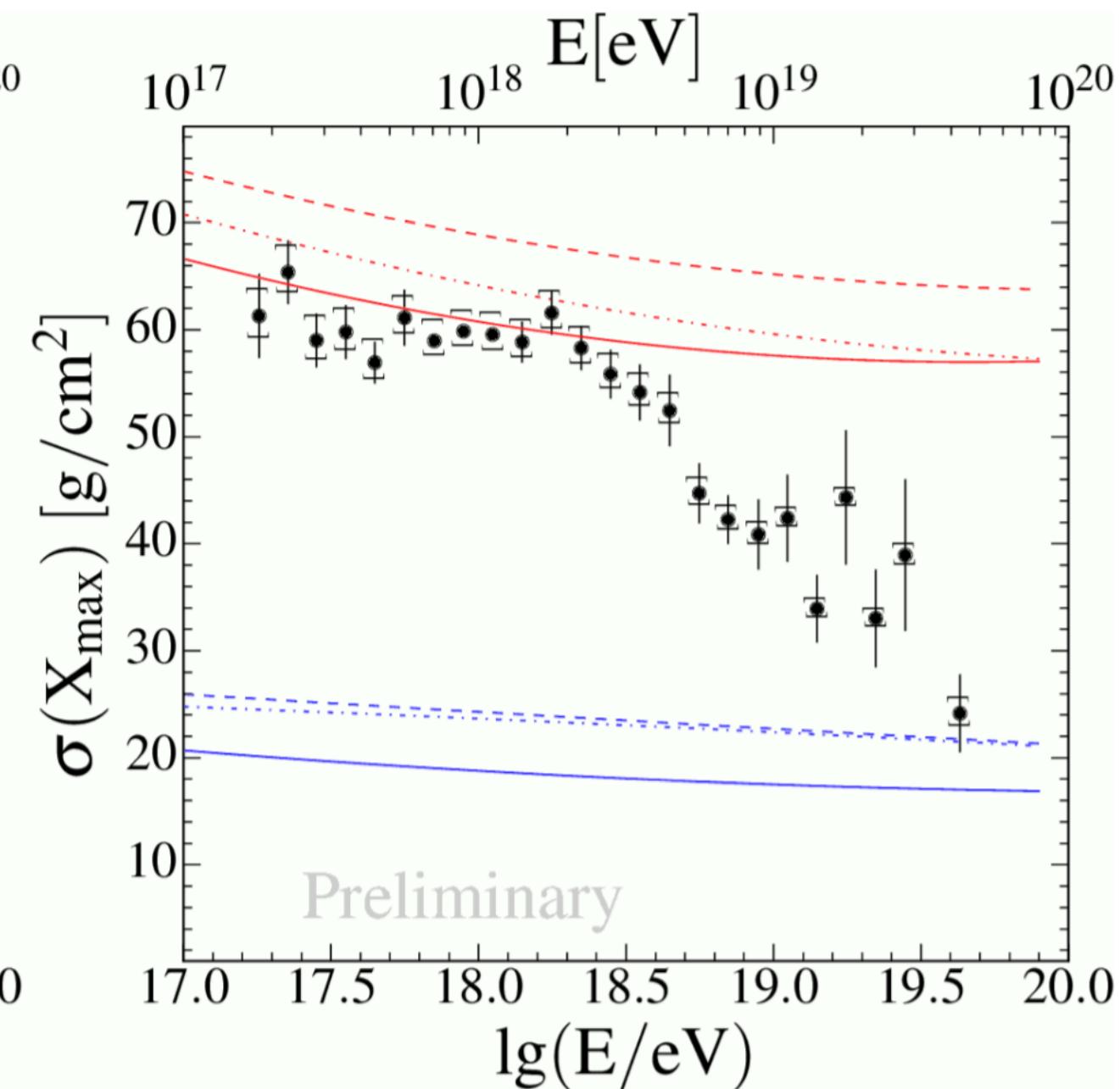
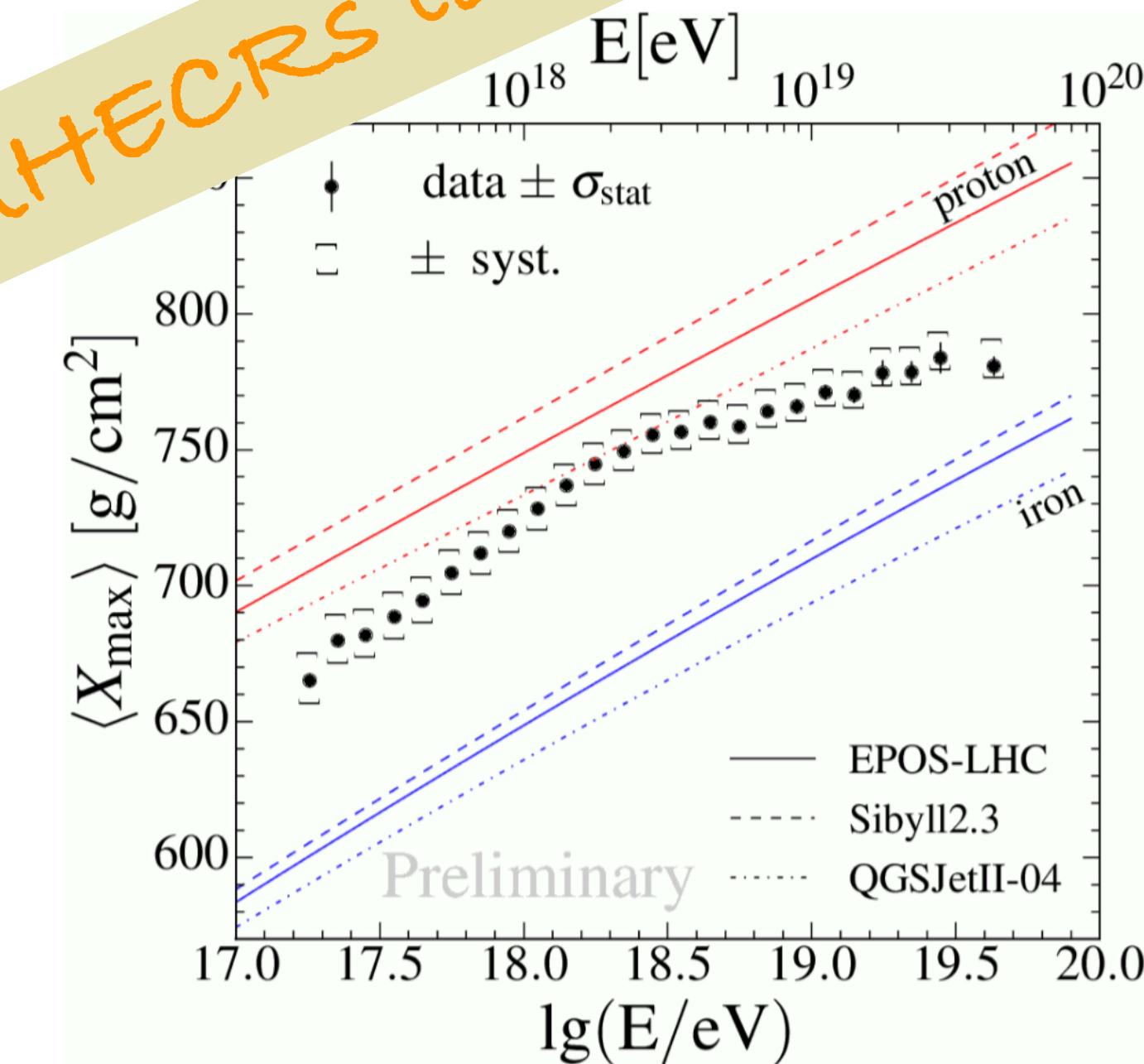
# UHECRs measurements



# UHECRs measurements



*It is possible to link features in the UHECRs to astrophysical processes?*



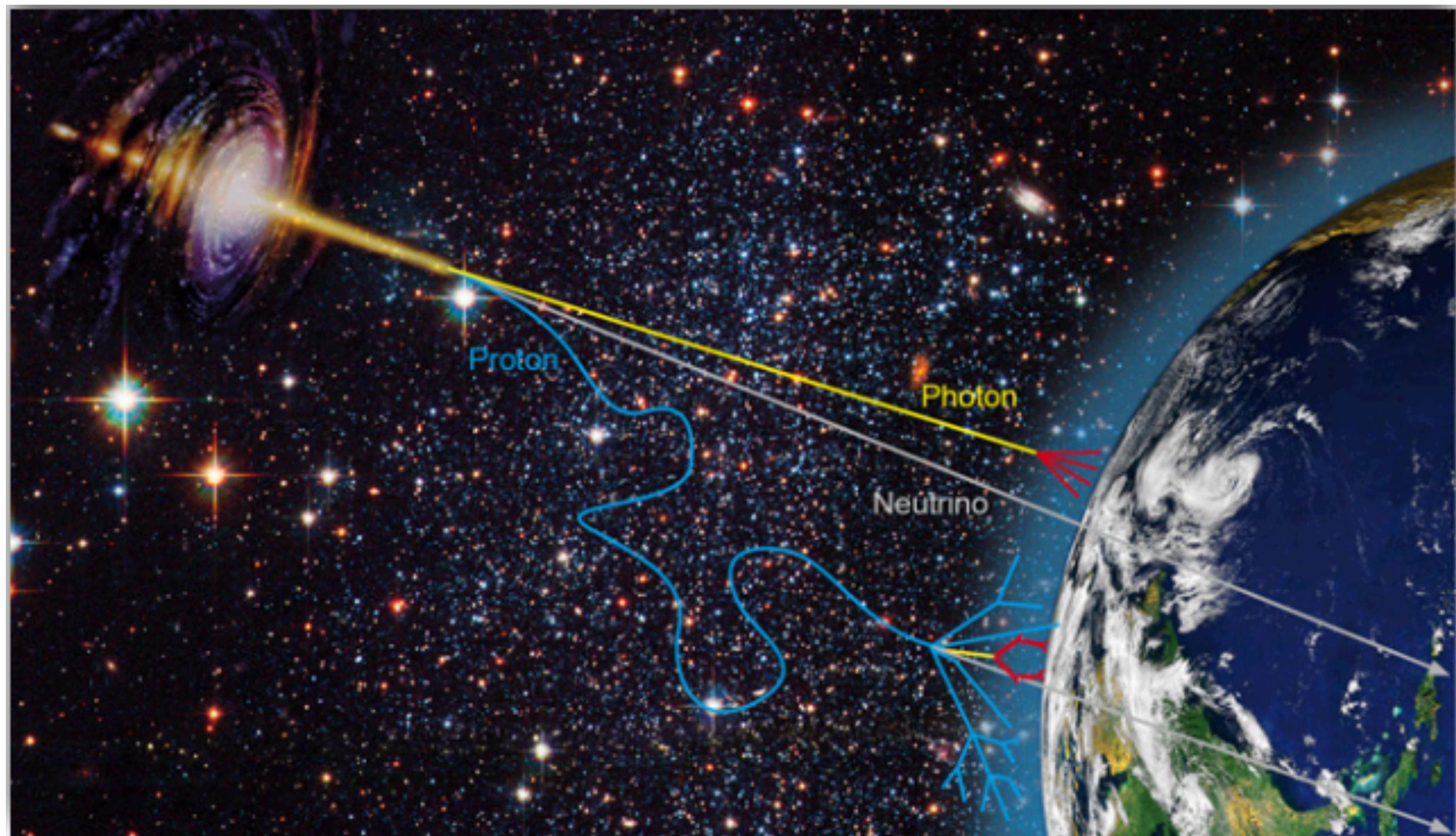
# UHECRs sources

Connection of observables at Earth to theoretical models including UHECR properties → Propagation of UHECRs

Several codes for UHECR propagation available:

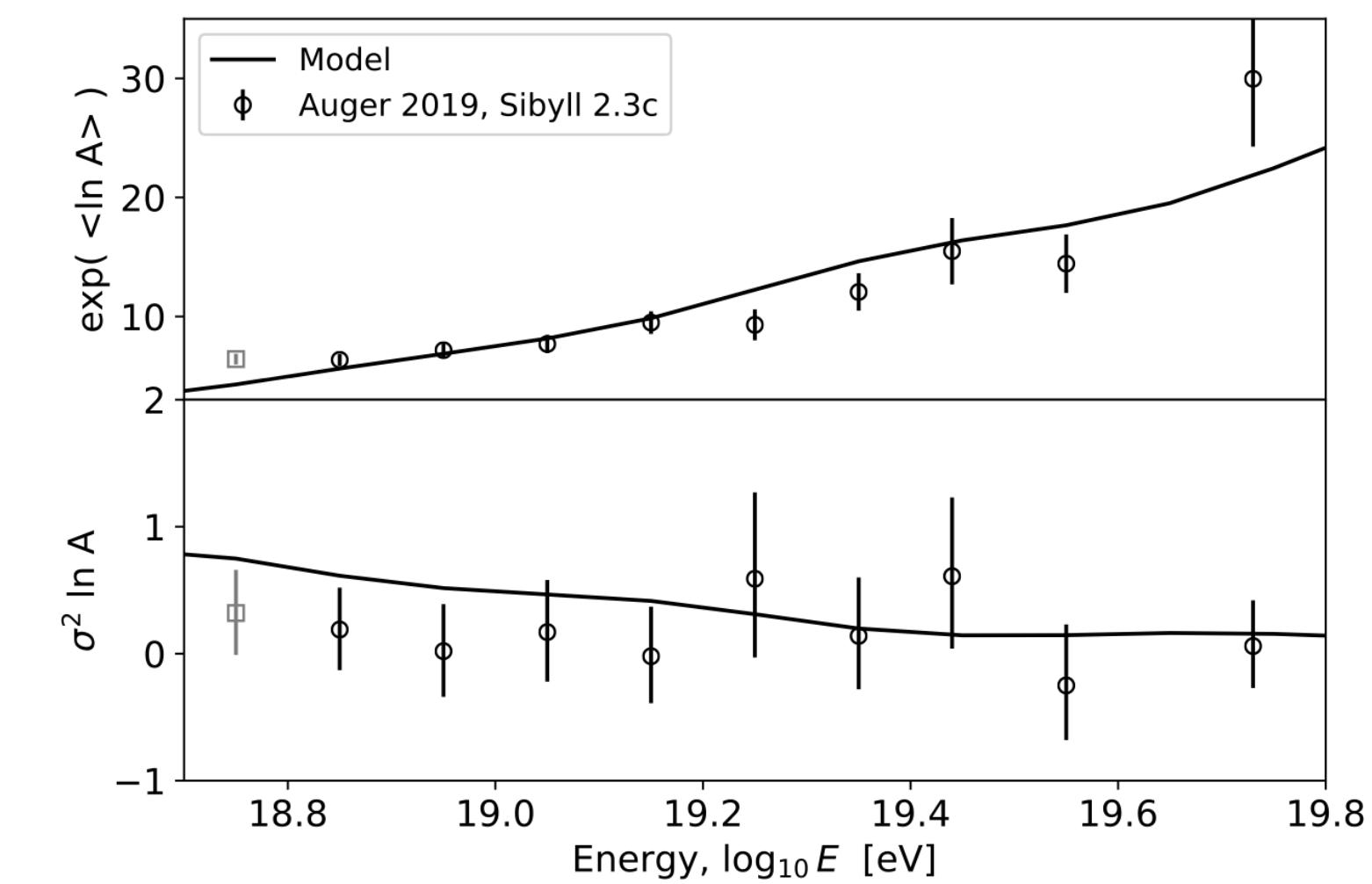
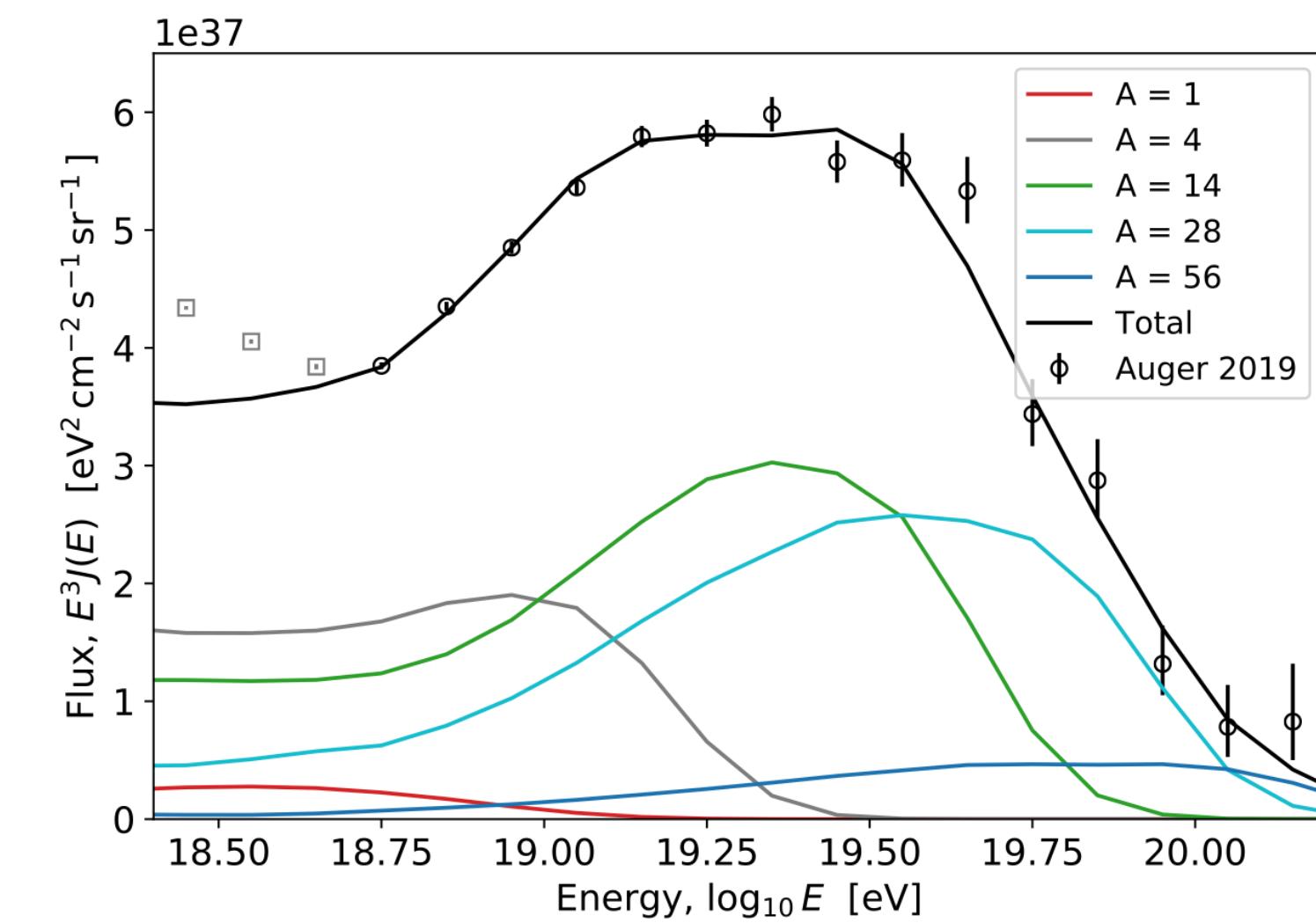
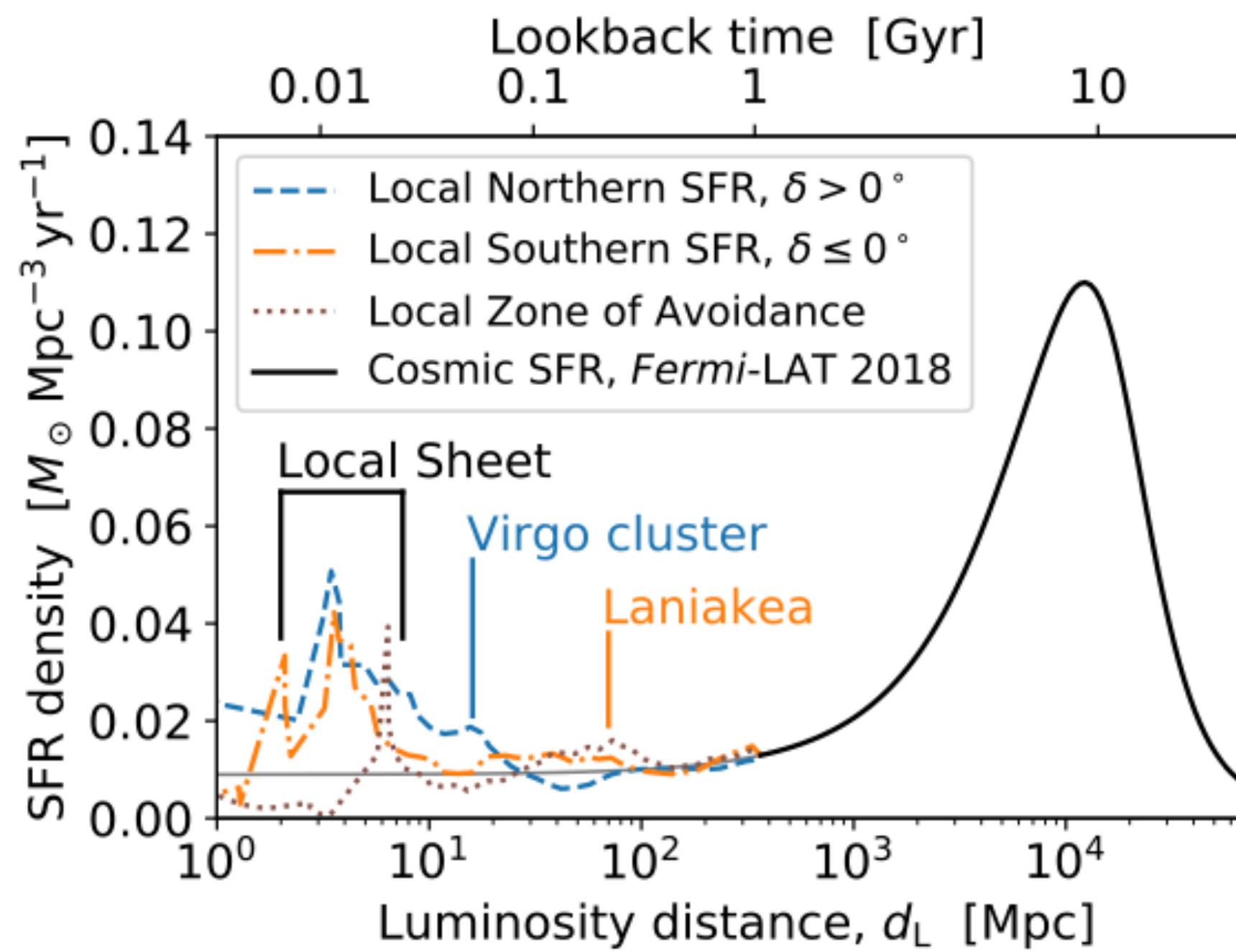
- \* SimProp (Aloisio et al., JCAP 2017)
- \* CRPropa (Alves Batista et al., JCAP 2016)

Combining two or more UHECRs observables it is possible to infer something about the sources of UHECRs → See @Sullivan's talk!

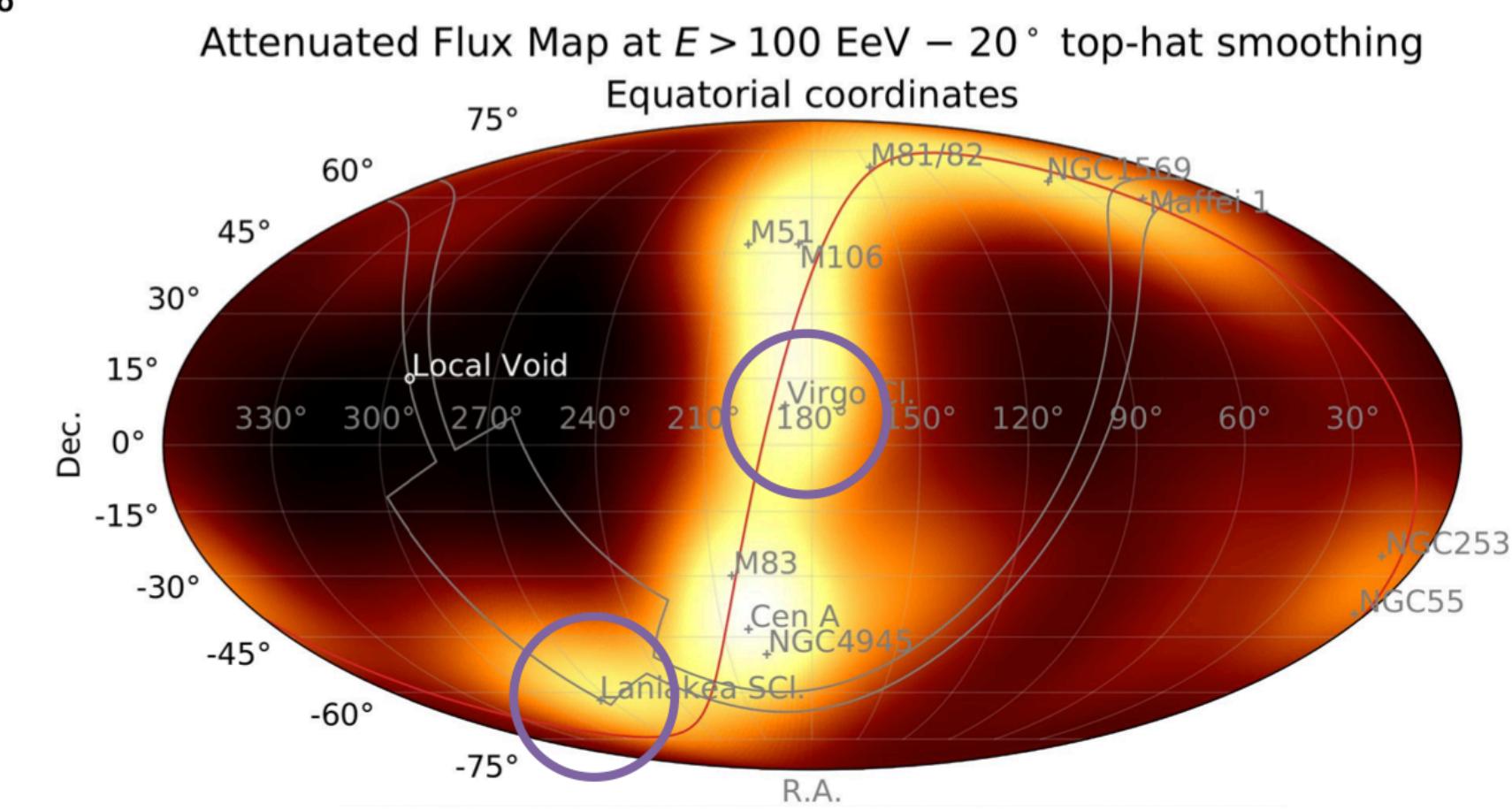
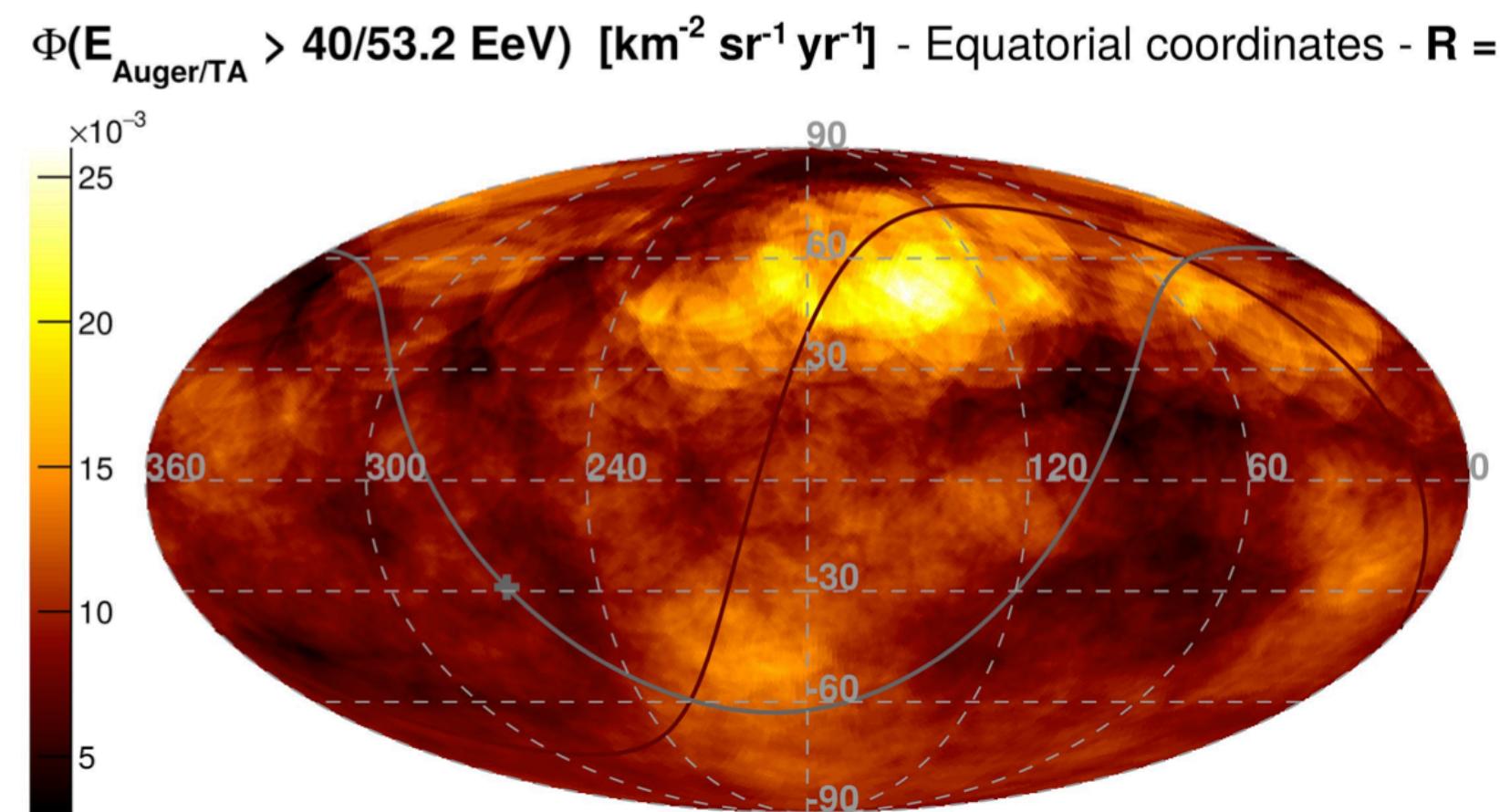


# Motivation

- \* Assumption: UHECR production rate follows matter (ex: Star Formation Rate)
- \* Fit of energy spectrum and composition using a catalogue which reconstructs the 3D distribution of the most extreme sources in the Universe.



# Motivation



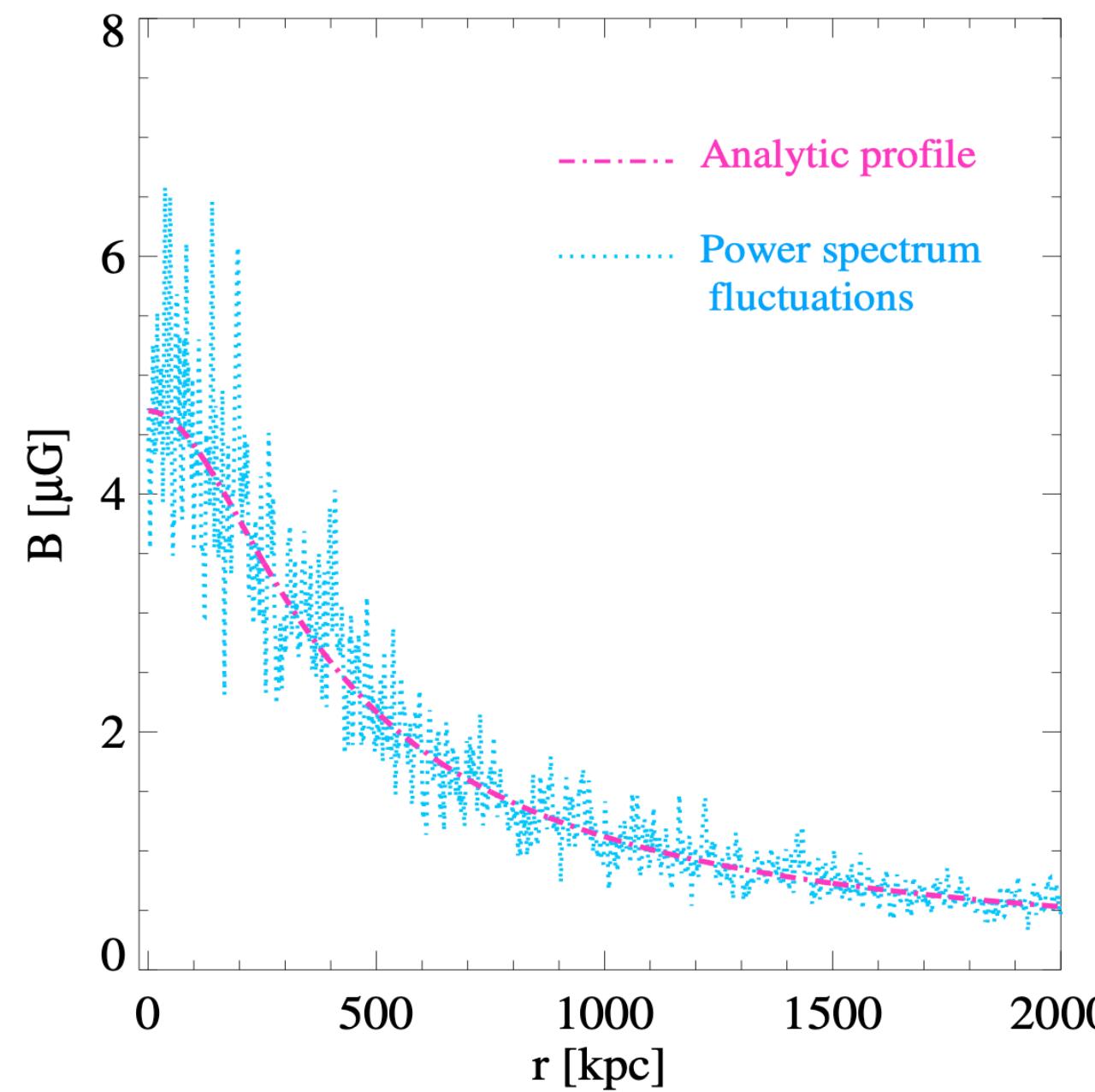
Why don't we  
see nearby  
clusters or  
superclusters?



# Motivation



Study the propagation of UHECRs in  
Galaxy Clusters' environment!



$$\frac{L_{eff}}{L}(E, Z) \simeq \cos\theta \simeq 1 + \frac{\theta^2}{2} \simeq 65 \left( \frac{10^{20} \text{ eV}}{E} \right)^2 \left( \frac{L}{1 \text{ Mpc}} \right) \left( \frac{L_{coh}}{10 \text{ kpc}} \right) \left( \frac{B}{1 \mu\text{G}} \right)^2 \left( \frac{Z}{26} \right)^2$$



Possible trapping due to clusters'  
magnetic field!



A. Bonafede et al., A&A 513, A30 (2010)



D. Hooper, et al., Phys. Rev. D 77, 103007

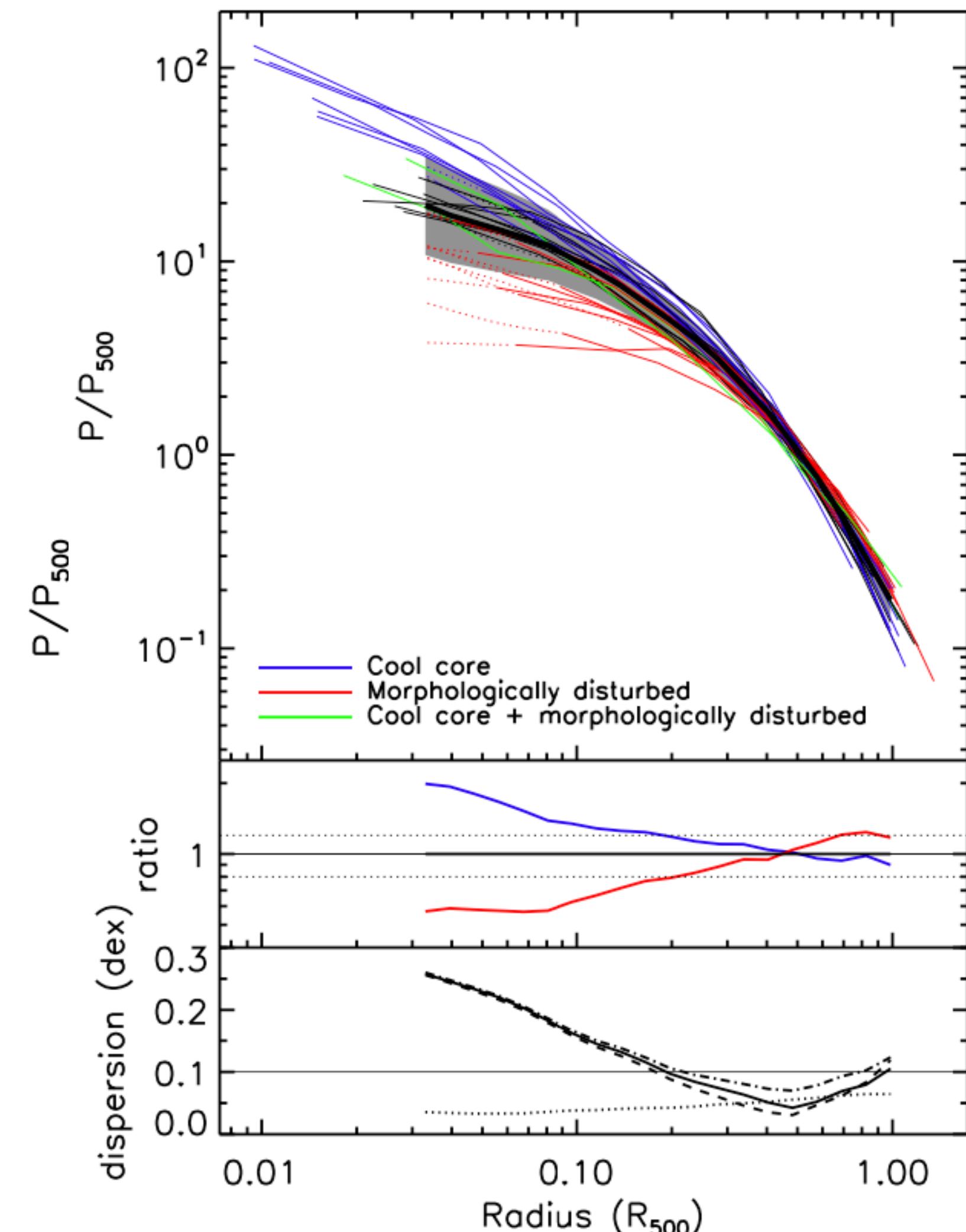
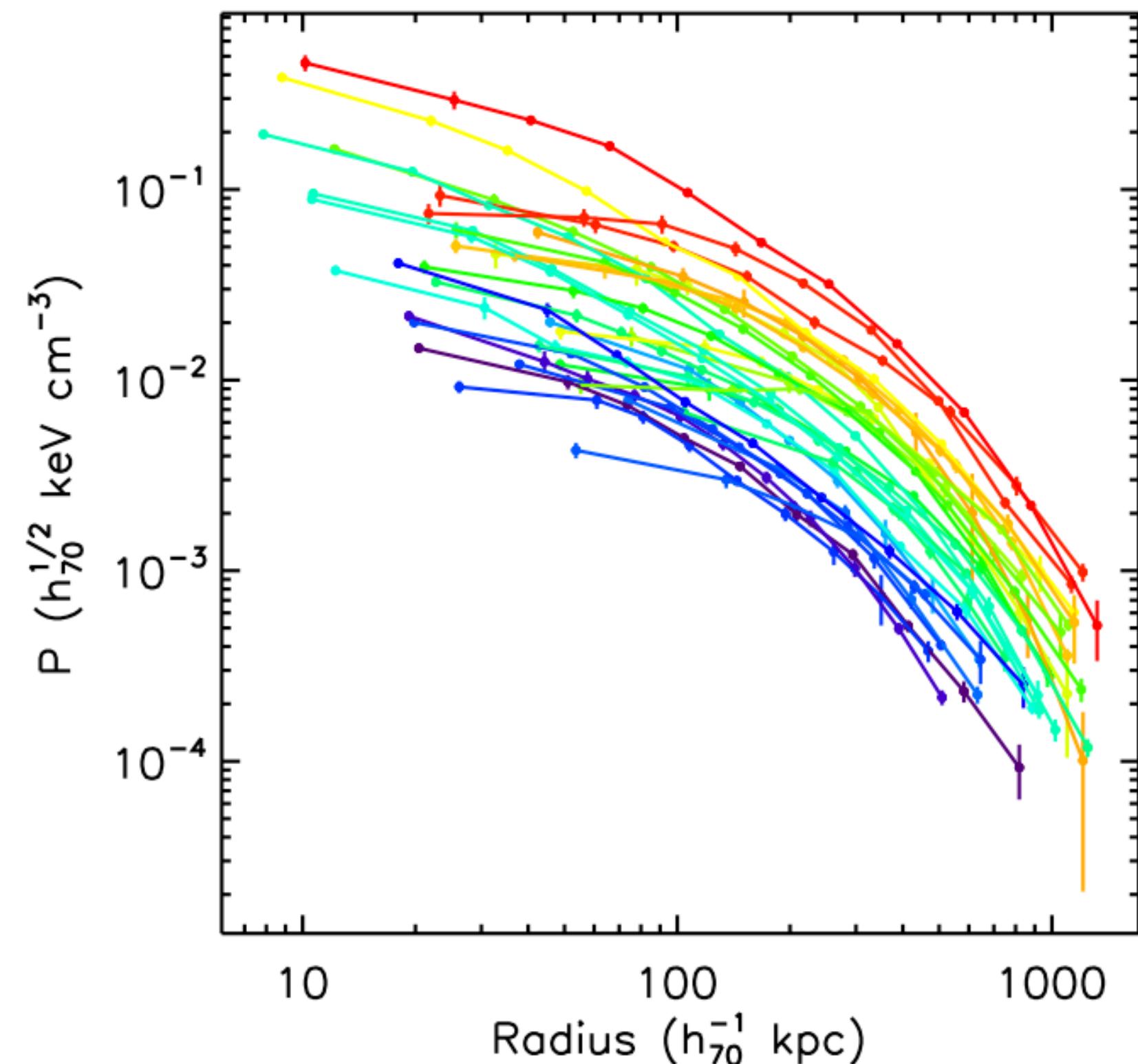
# The universal galaxy cluster pressure profile

- \* Self-similarity: approximation all their properties depend only on mass and redshift;
- \*  $(M, z) \rightarrow$  pressure profile for any cluster.

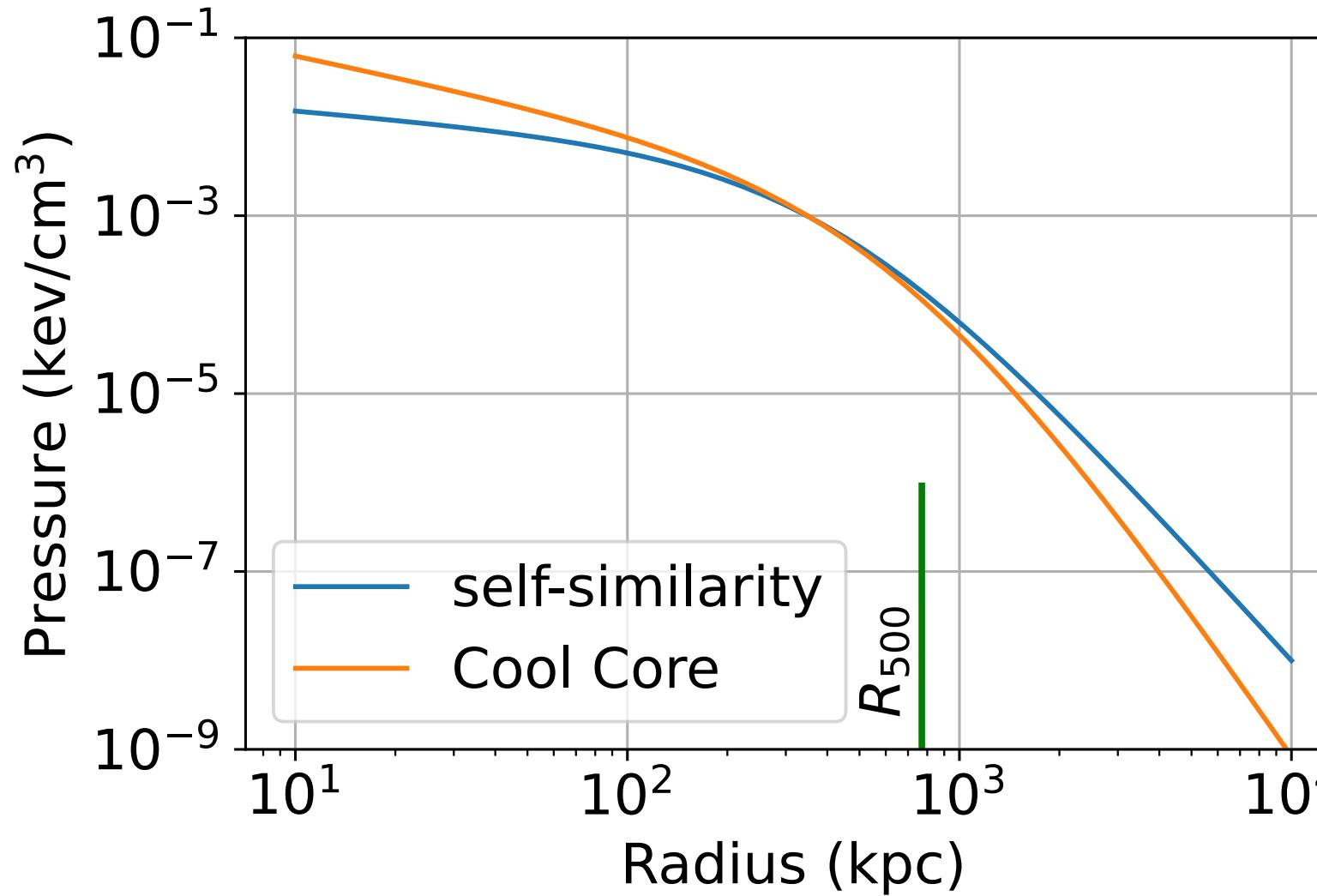
$$P(r) = \frac{P_0 \cdot P_{500} \cdot f(M, z)}{(x/r_p)^\gamma \cdot (1 + (x/r_p)^\alpha)^\frac{\beta - \gamma}{\alpha}}$$

with  $P_0$  normalisation factor

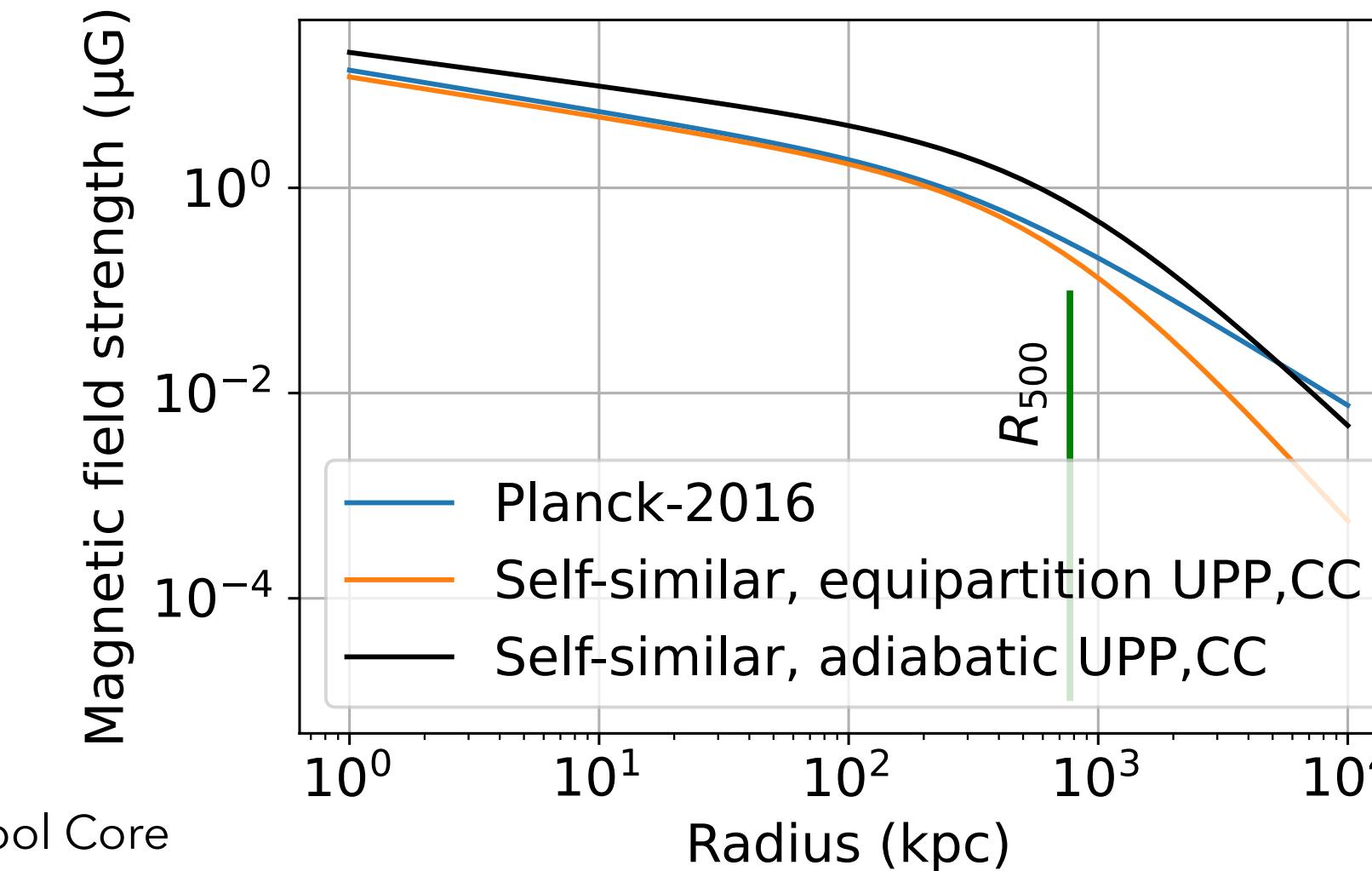
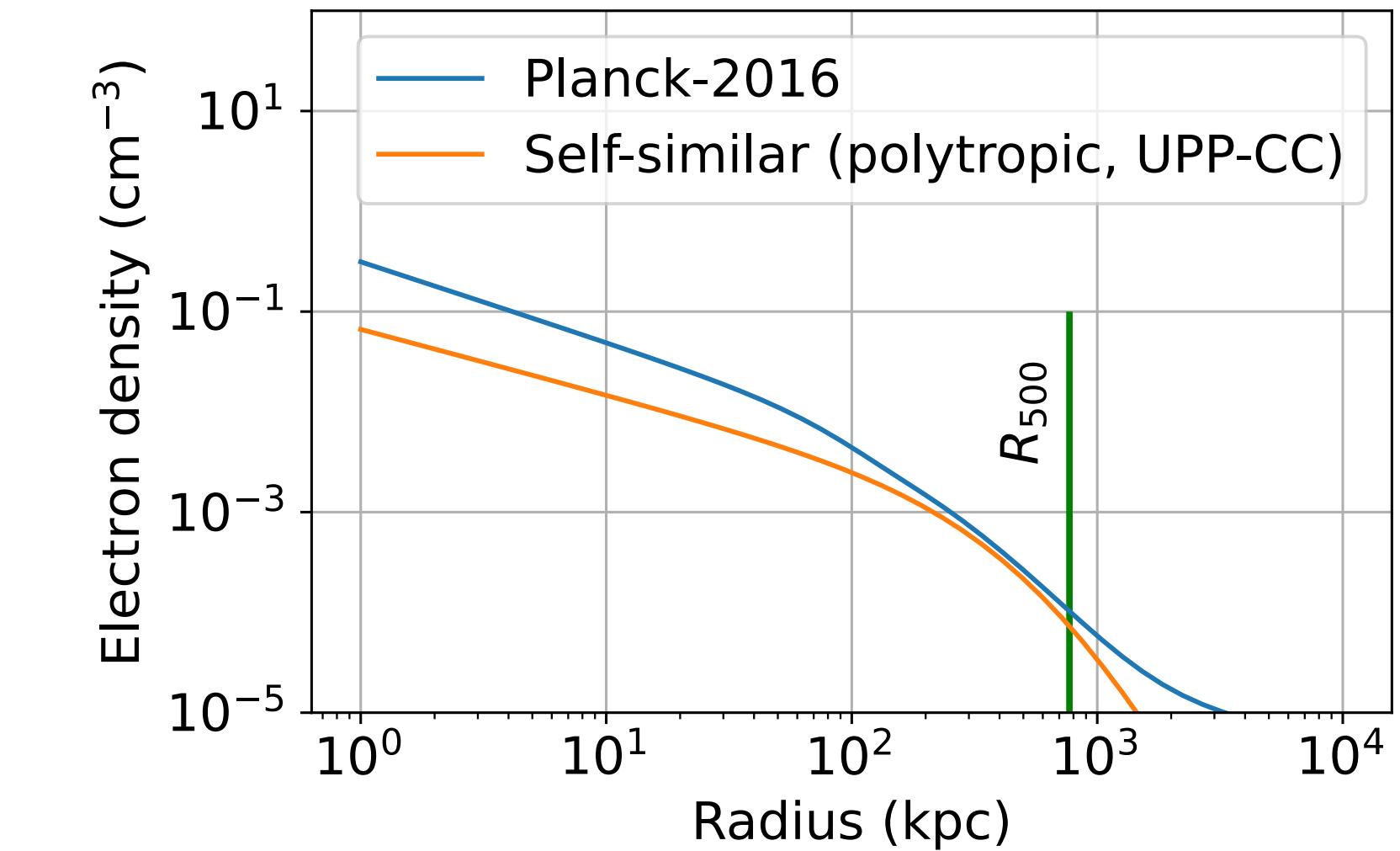
$\alpha, \beta, \gamma$  and  $r_p$  are fitted parameters.



# Virgo Cluster



\*UPP,CC = Universal Pressure Profile for Cool Core

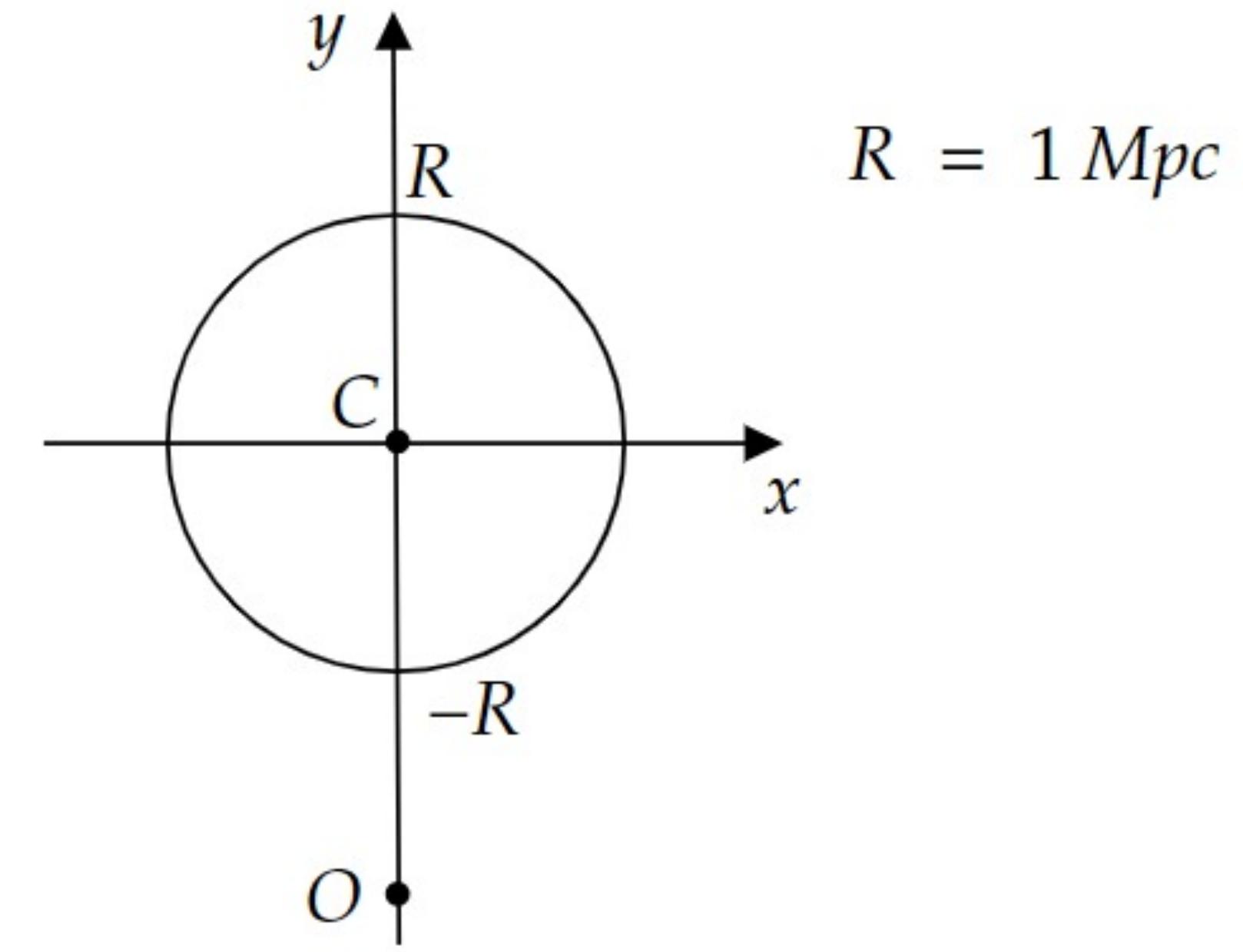


# Source-propagation in Galaxy Clusters

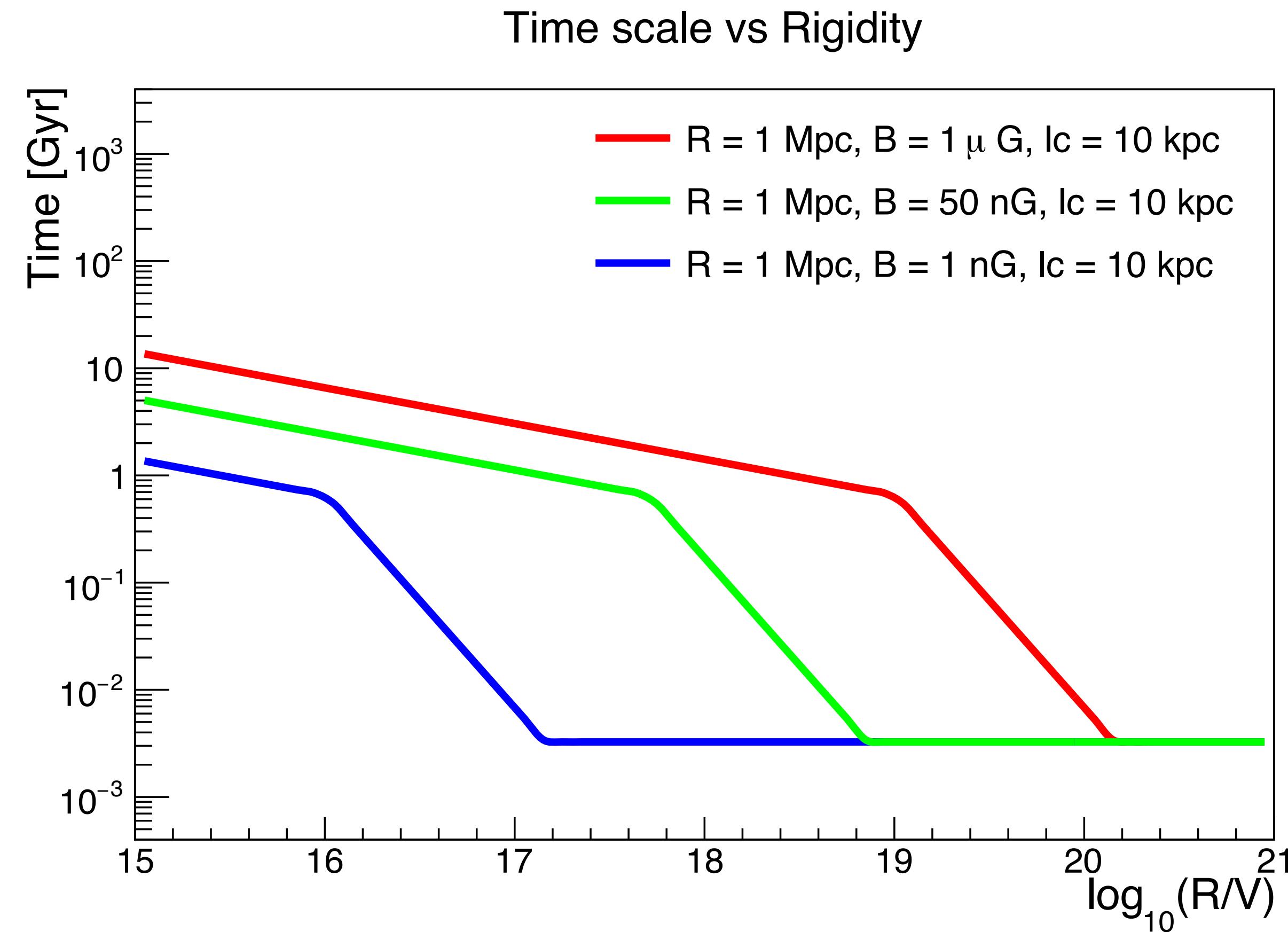
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- \* Propagation in source computed using SimProp;
- \* Computation of interaction and diffusion times;
- \* Inclusion of magnetic field effect on propagation;
- \* Including radial dependence.

New!



# Diffusion and interaction times



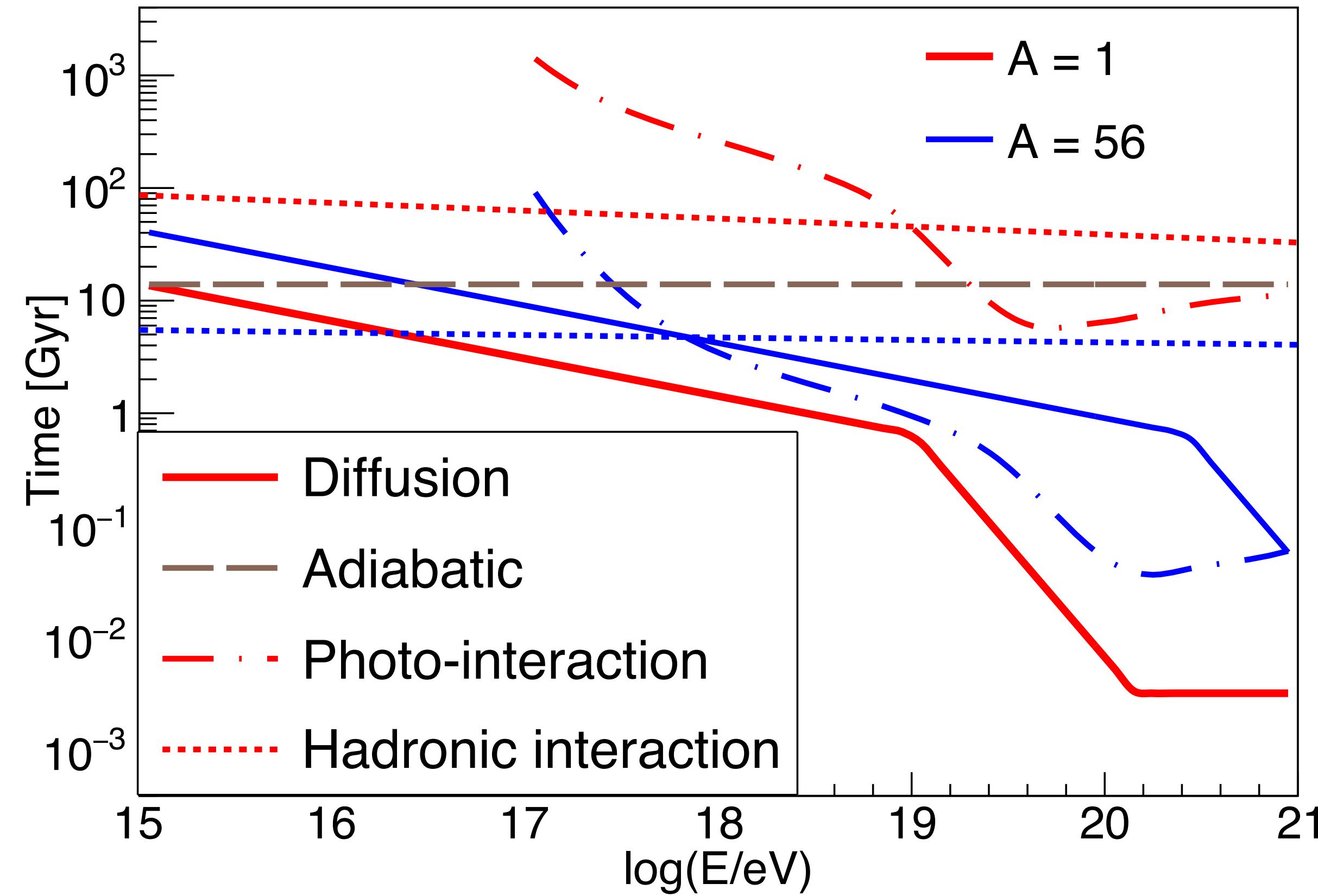
Diffusion

$$\tau_D = \frac{R^2}{D}$$

Depends on the  
slope in energy and  
on the coherence  
length  $l_c$



# Diffusion and interaction times



Interactions with CMB and EBL:

$$\frac{1}{\tau} = \frac{1}{2\Gamma^2} \int_{\epsilon'_{\min}}^{2\Gamma\epsilon} \int_{\epsilon=0}^{+\infty} \frac{n_\gamma(\epsilon)}{\epsilon^2} d\epsilon \sigma(\epsilon') \epsilon' d\epsilon'$$

Interactions with protons and helium nuclei:

$$\tau = (n_{ICM} \cdot \sigma \cdot c)^{-1}$$

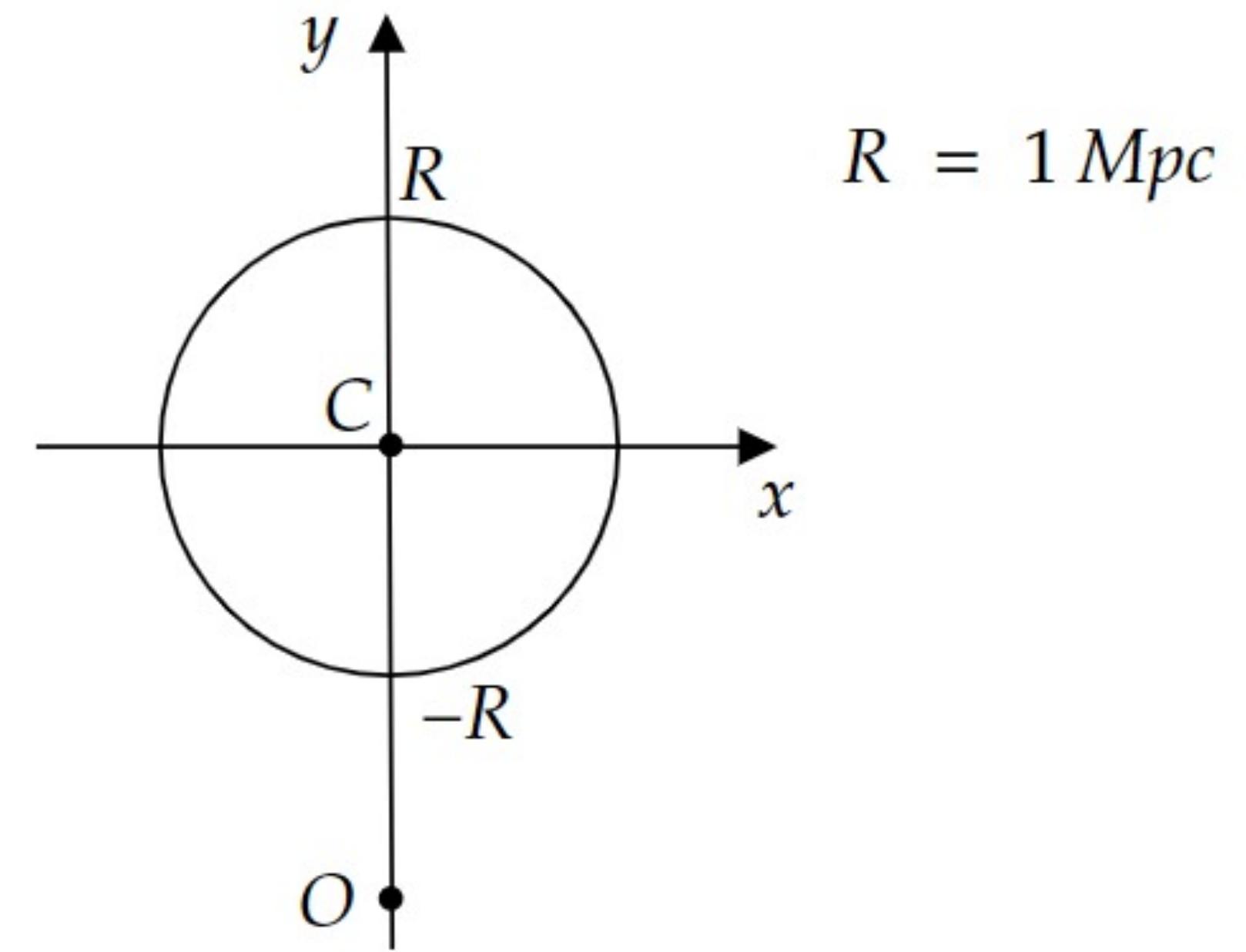


# Procedure for escape:

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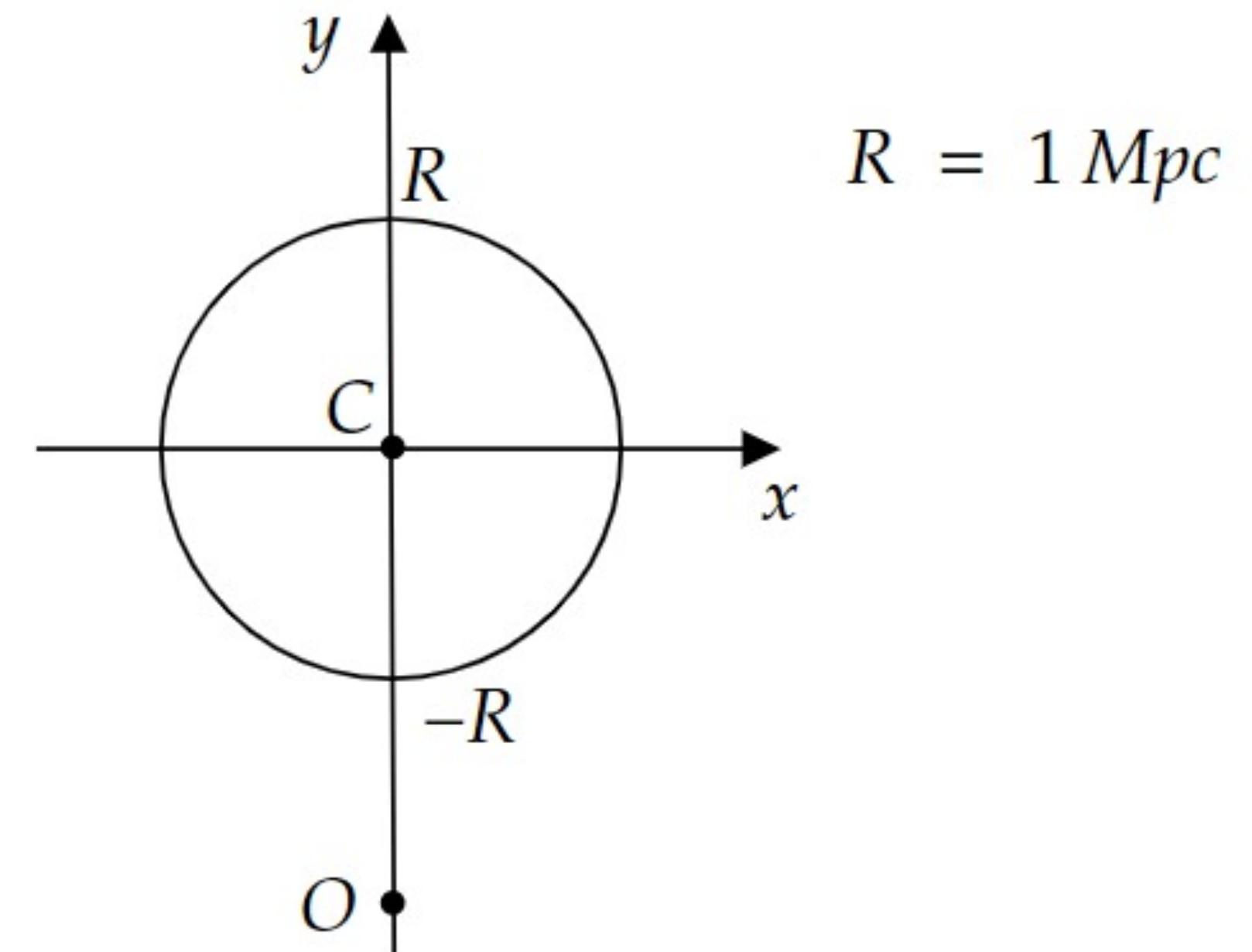
Fixed number of steps for each particles



# Procedure for escape:

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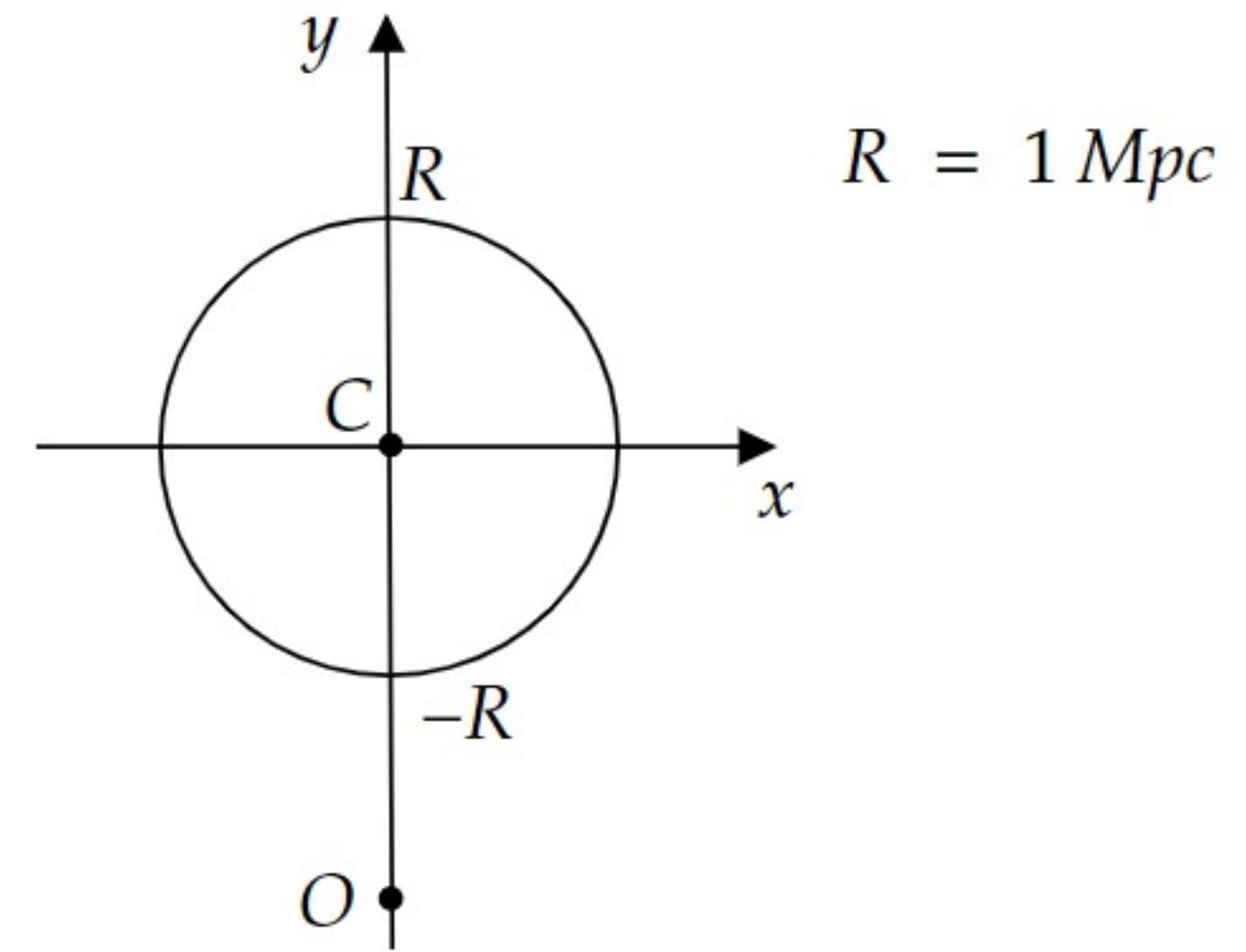
- \* Fixed number of steps for each particles
- \* Propagation from  $y \in [-R, R]$  to  $-R$



# Procedure for escape:

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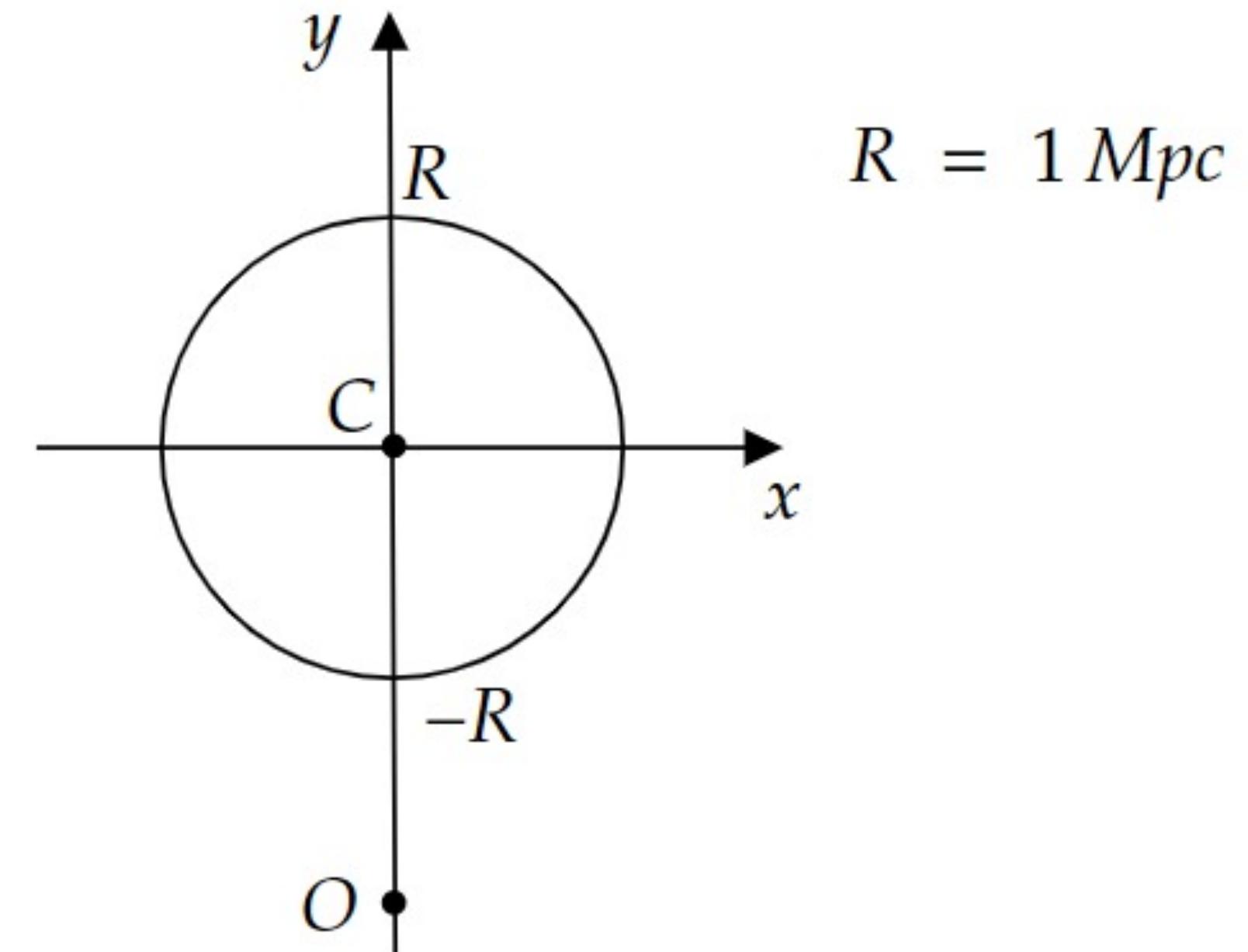
- \* Fixed number of steps for each particles
- \* Propagation from  $y \in [-R, R]$  to  $-R$
- \* At each step, if the diffusion time is shorter than the interaction times, particle is propagated to the next step, otherwise it interacts



# Procedure for escape:

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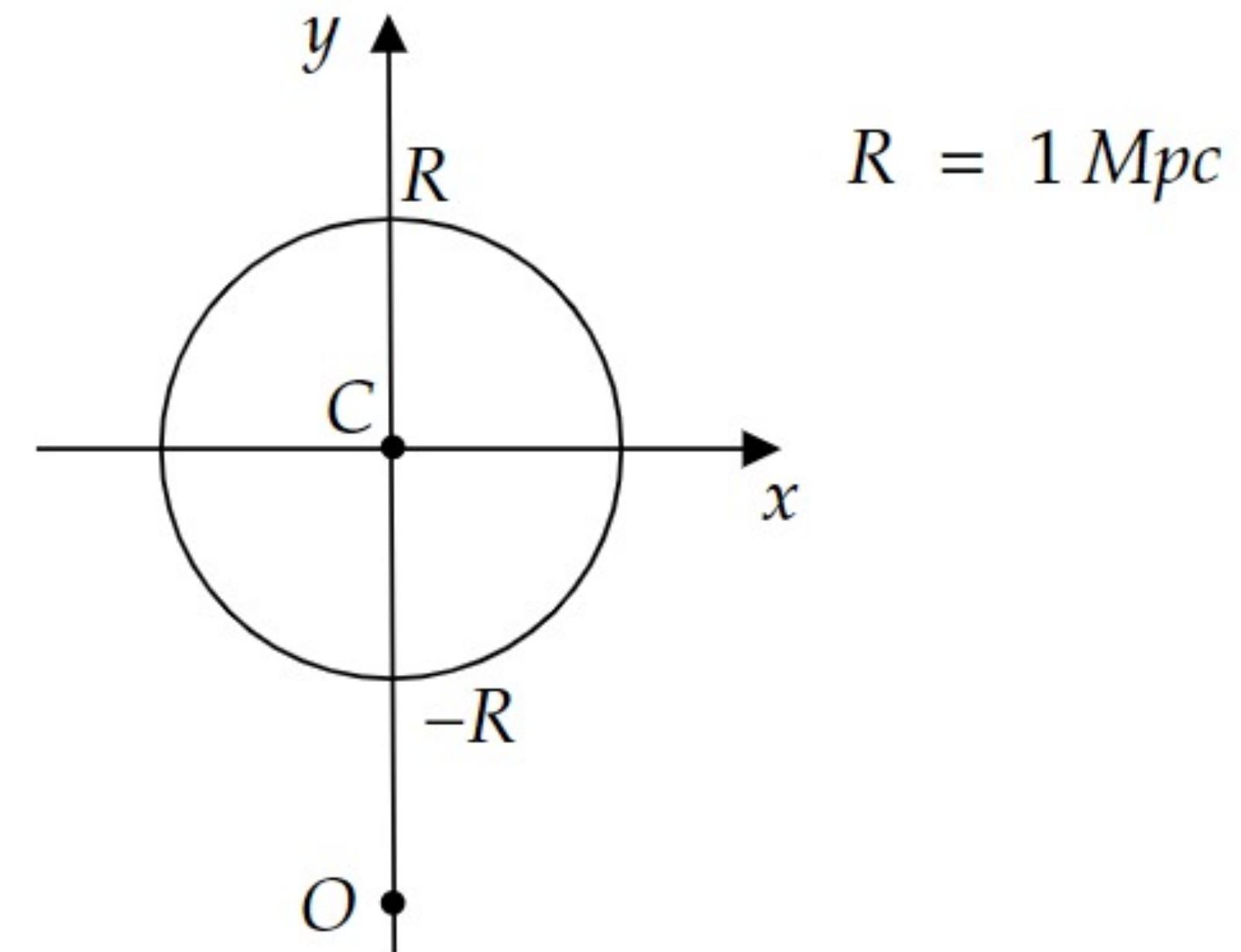
- \* Fixed number of steps for each particles
- \* Propagation from  $y \in [-R, R]$  to  $-R$
- \* At each step, if the diffusion time is shorter than the interaction times, particle is propagated to the next step, otherwise it interacts
- \* If, at step  $n > n_{\text{stepmax}}$ , the diffusion time is shorter than the interaction times, particle escape



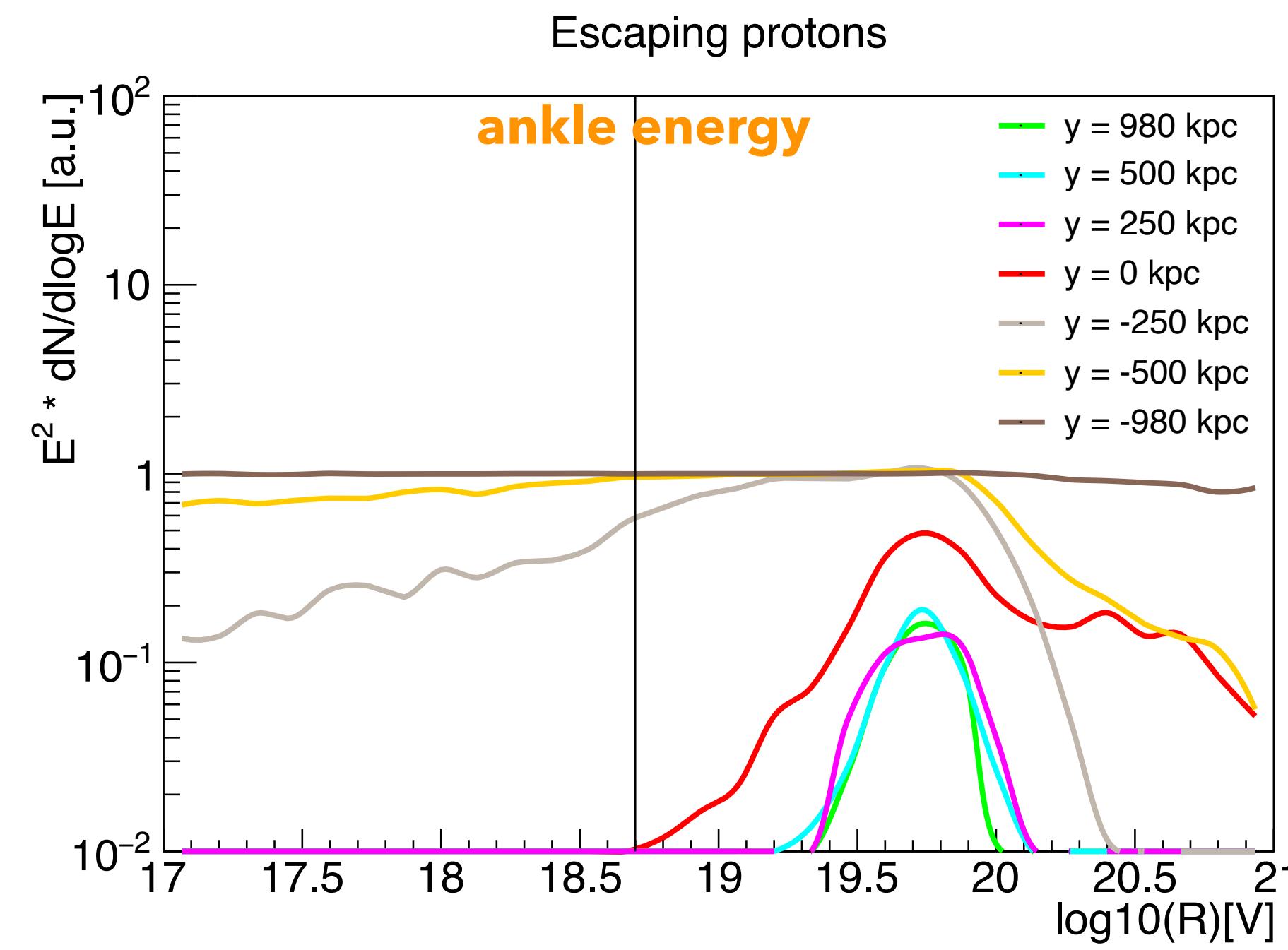
# Procedure for escape:

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- \* Fixed number of steps for each particles
- \* Propagation from  $y \in [-R, R]$  to  $-R$
- \* At each step, if the diffusion time is shorter than the interaction times, particle is propagated to the next step, otherwise it interacts
- \* If, at step  $n > n_{\text{stepmax}}$ , the diffusion time is shorter than the interaction times, particle escape
- \* If a particle is propagated and it reach a time in the source  $>$  time of the Universe: particle is trapped!



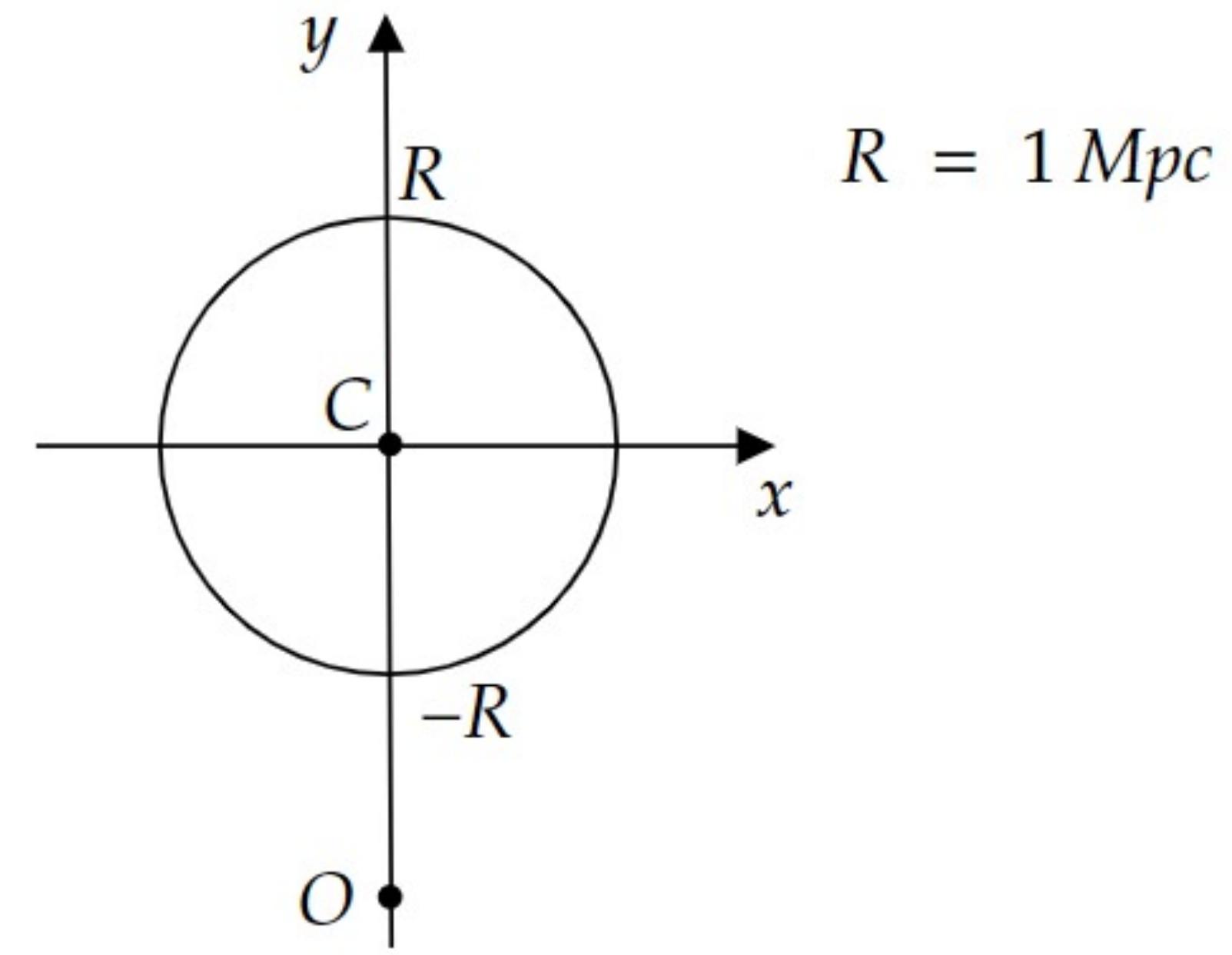
# Parametrizing the escaping flux



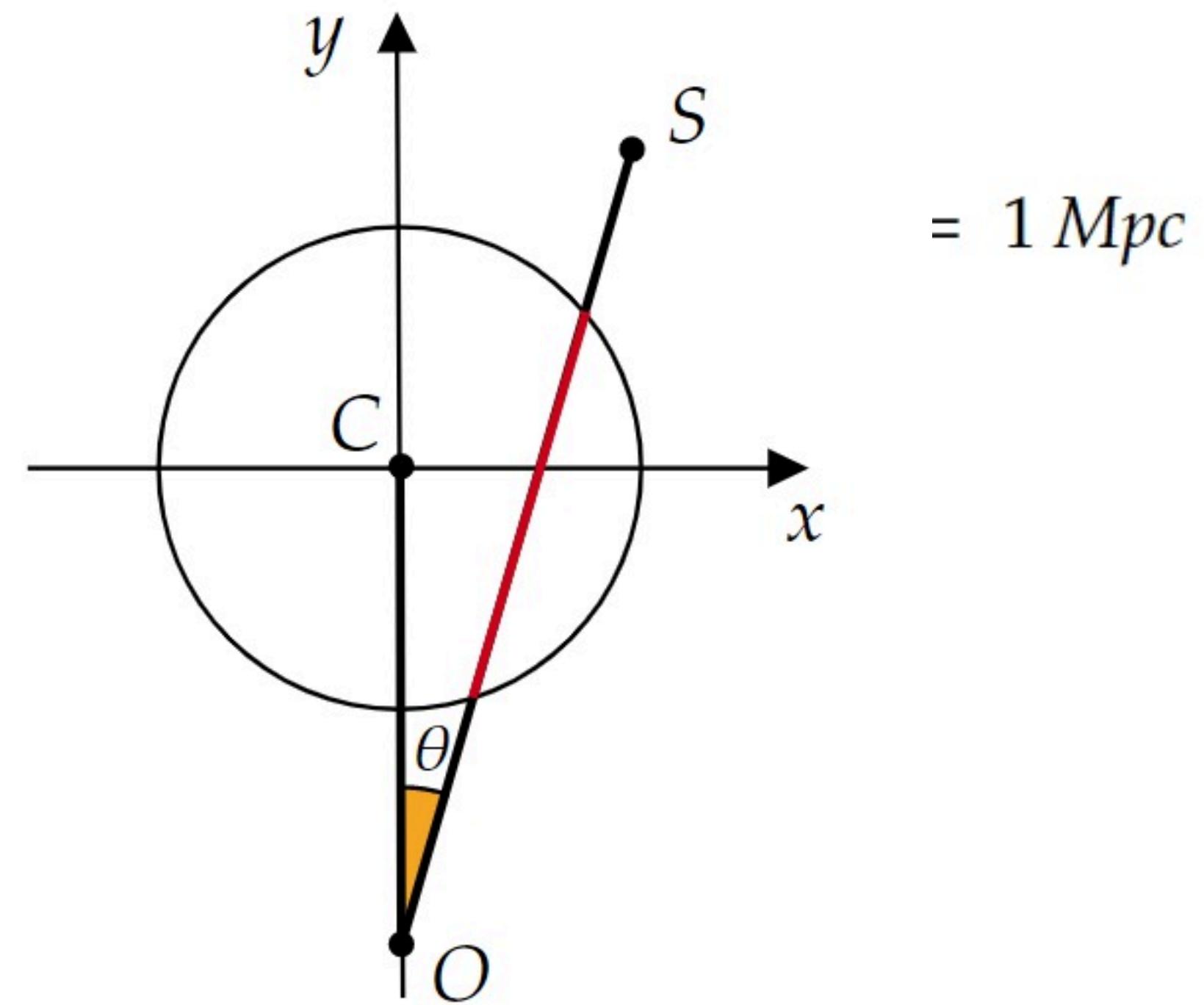
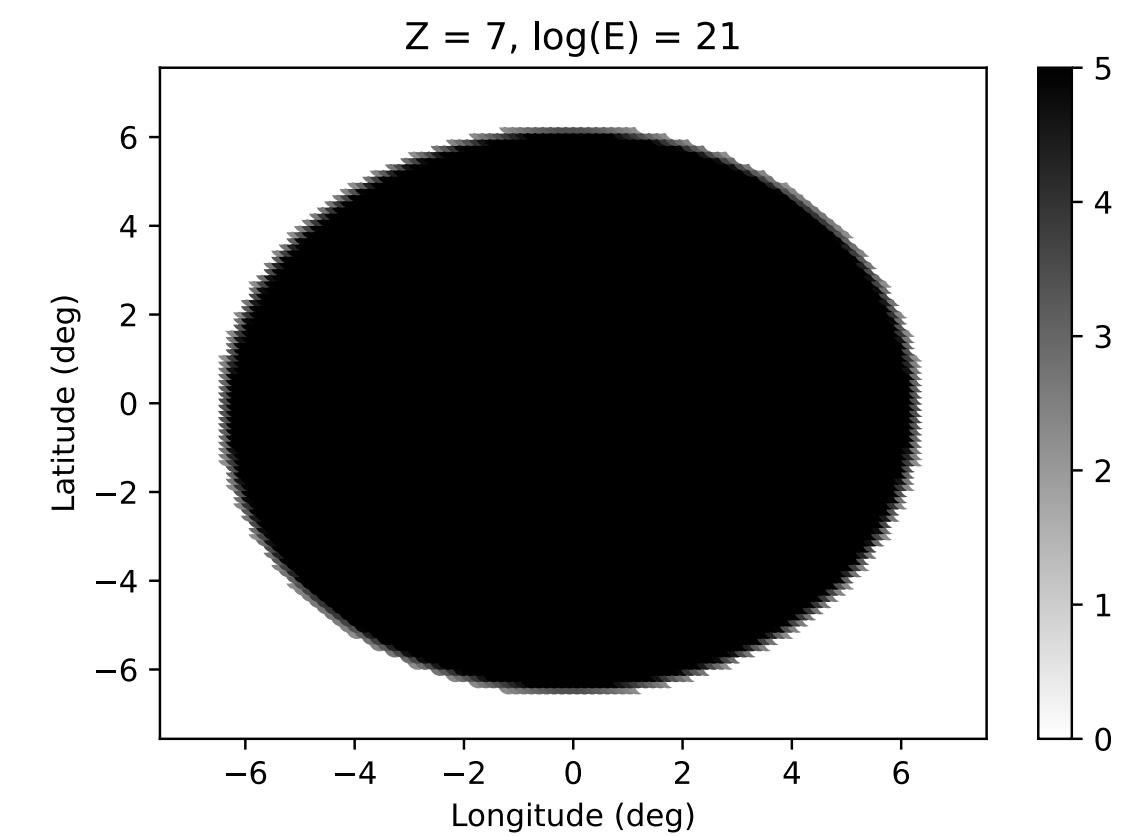
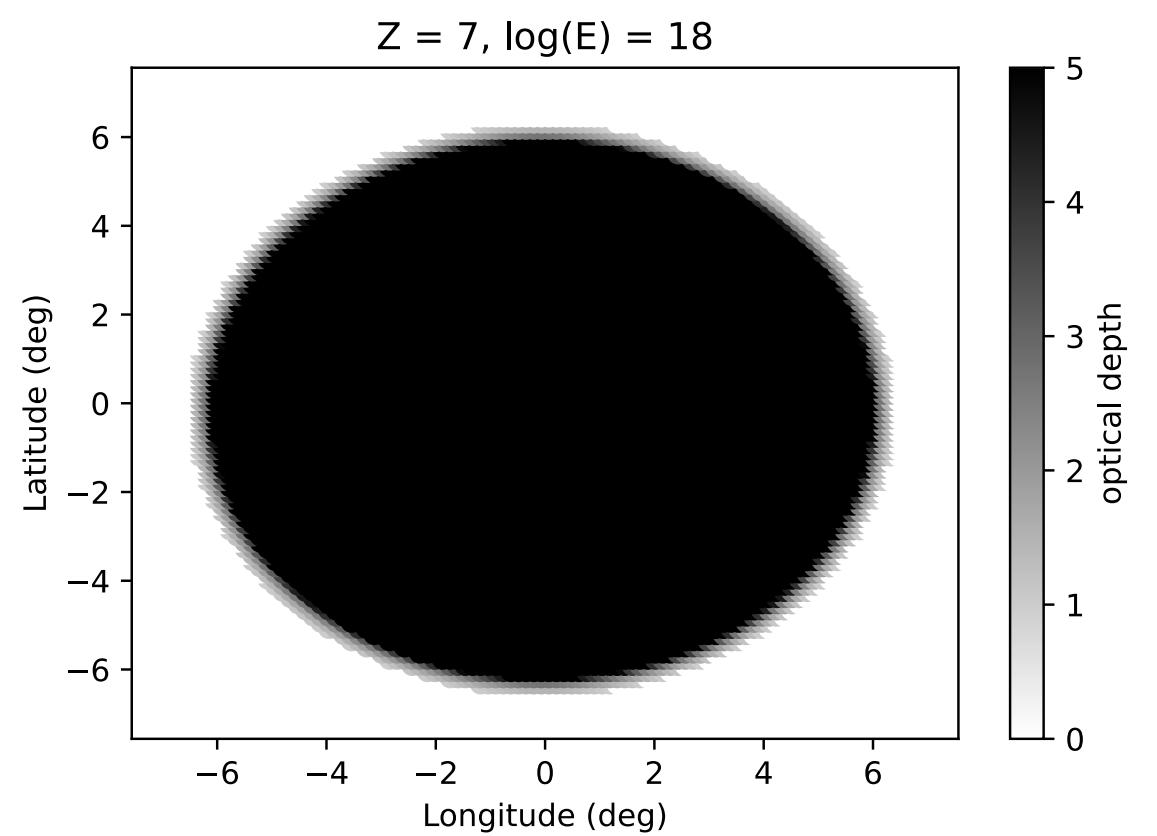
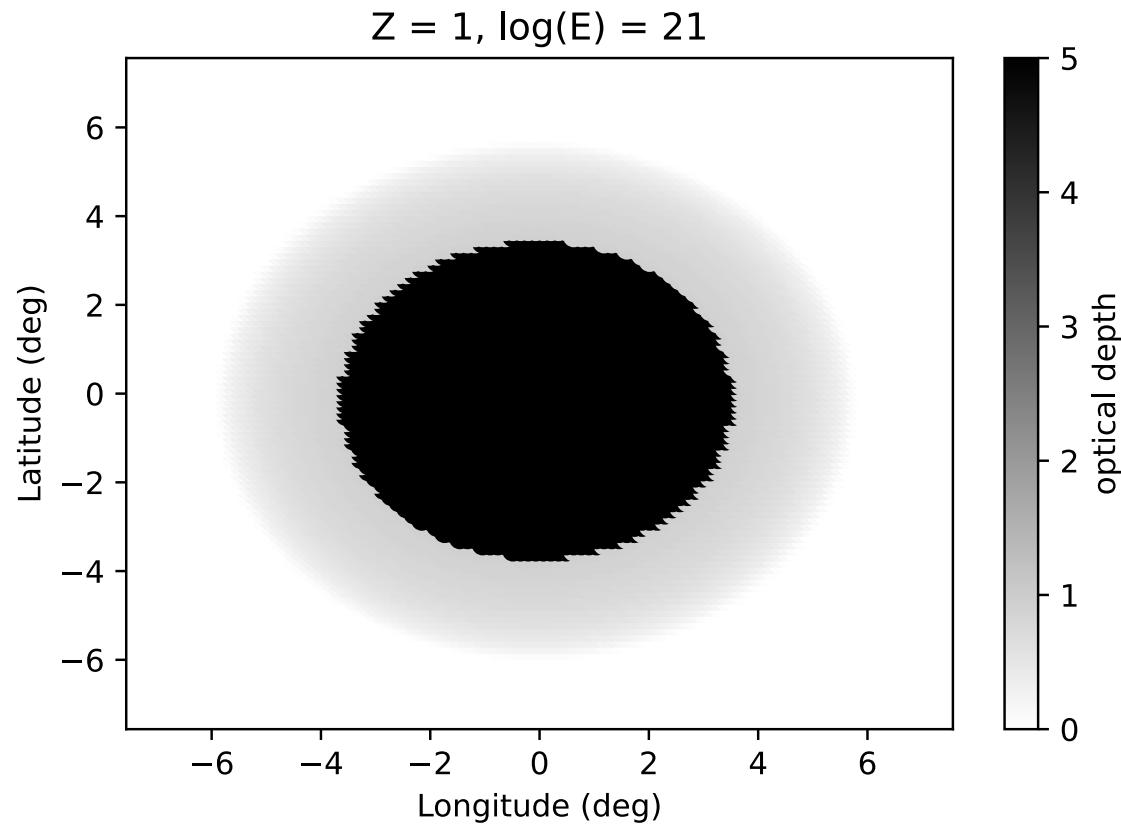
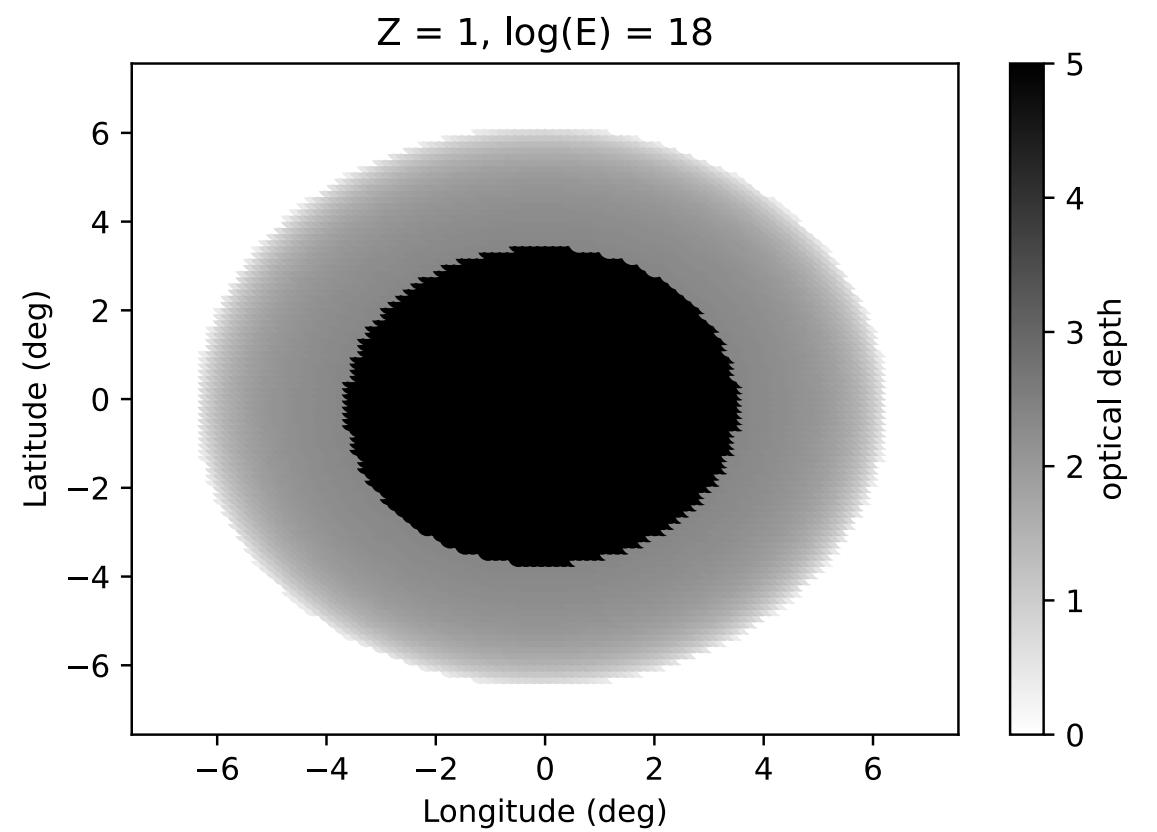
\*Inject protons with  $\Phi \propto E^{-2}$

\*Simulate Virgo environment

\*Parametrize the escaping flux as a function of the injection point

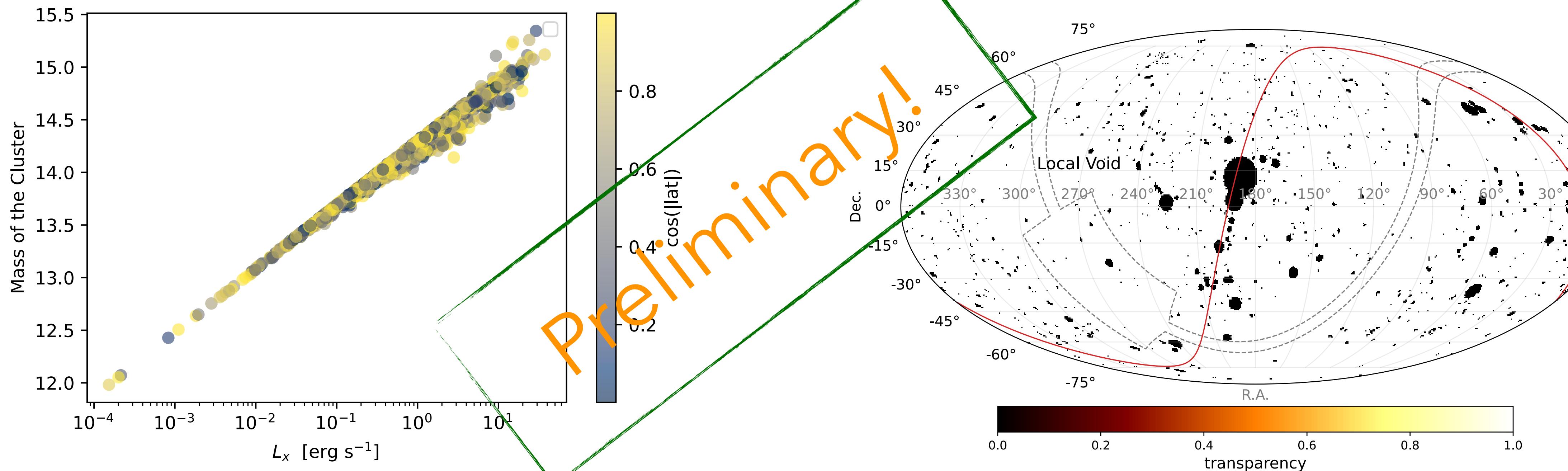


# Filtering



We should not see Virgo Cluster!

# Catalogue



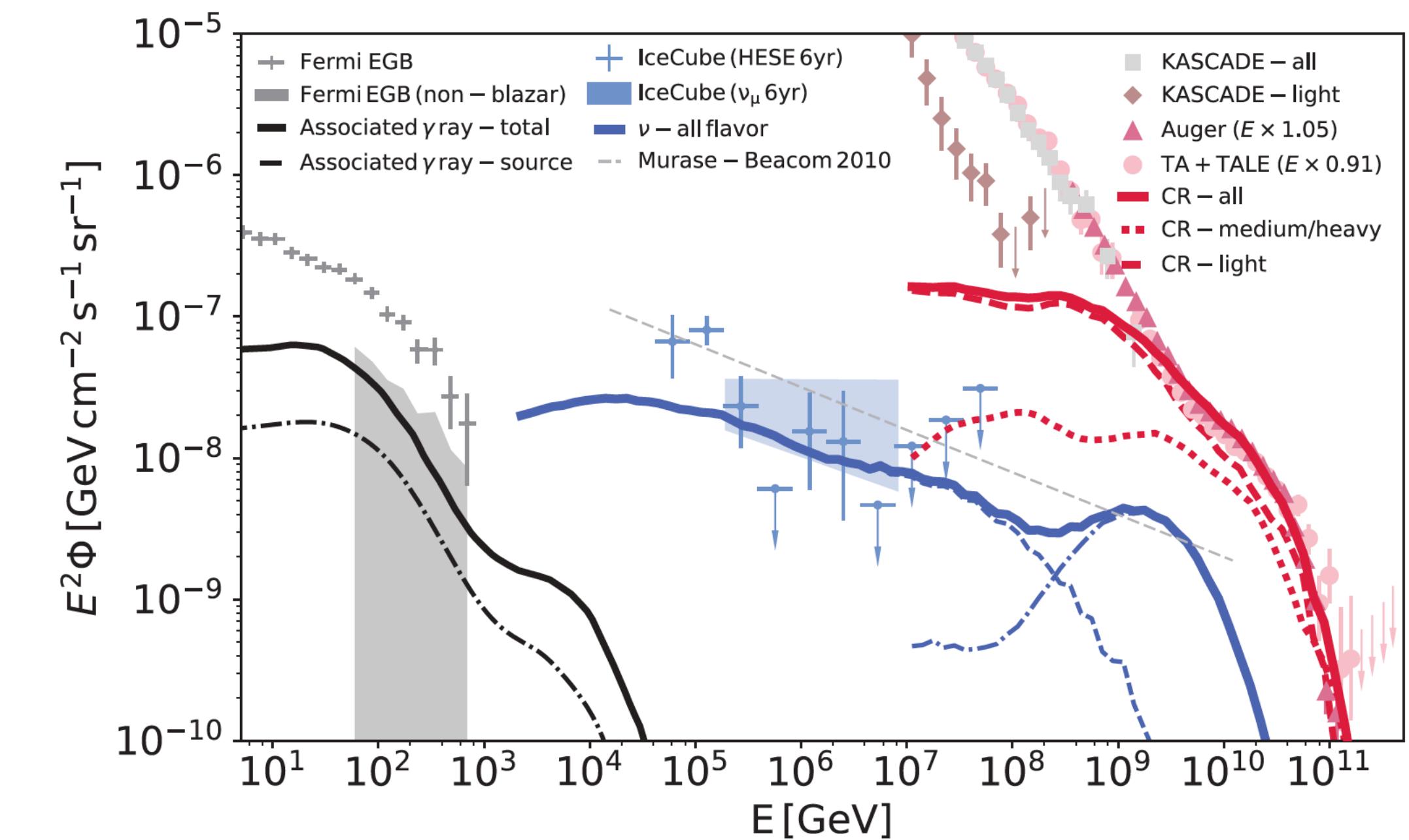
Mass of clusters as measured by NORAS, REFLEX and CIZA. The color bar represent different the latitude of the observed clusters.

# Summary and future perspectives

- Modelling the environment of Galaxy Cluster;
- Computing the propagation in the magnetised environment;
- Parametrising the escaping primary fluxes;
- Possibility to connect the parameter at the source to the fitted parameter at Earth;

## Future perspectives

- Universal parametrisation for Clusters;
- Compute the secondary fluxes (neutrinos, gamma);
- Perform a fit of spectrum, composition and arrival directions.





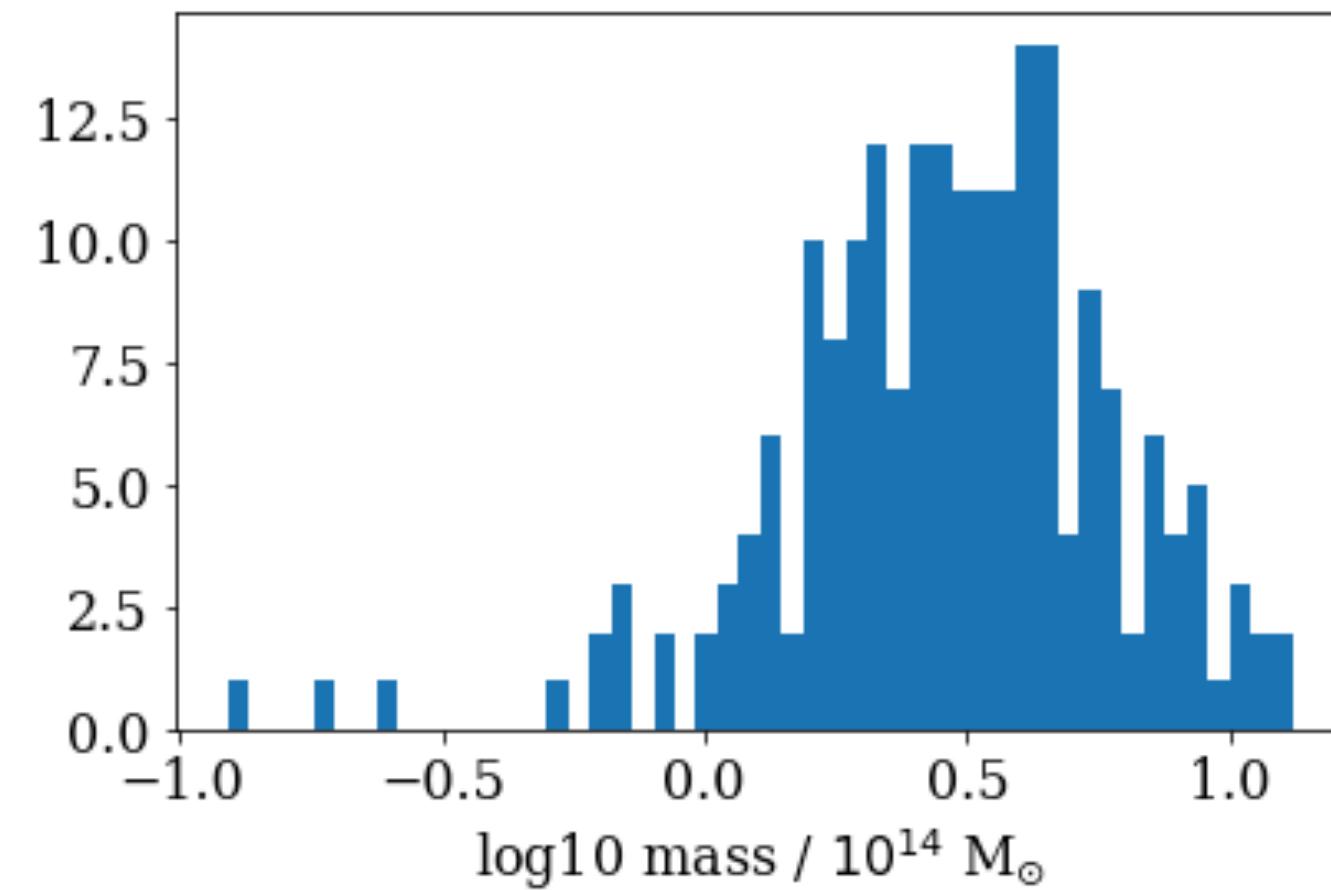
Thanks for your attention!

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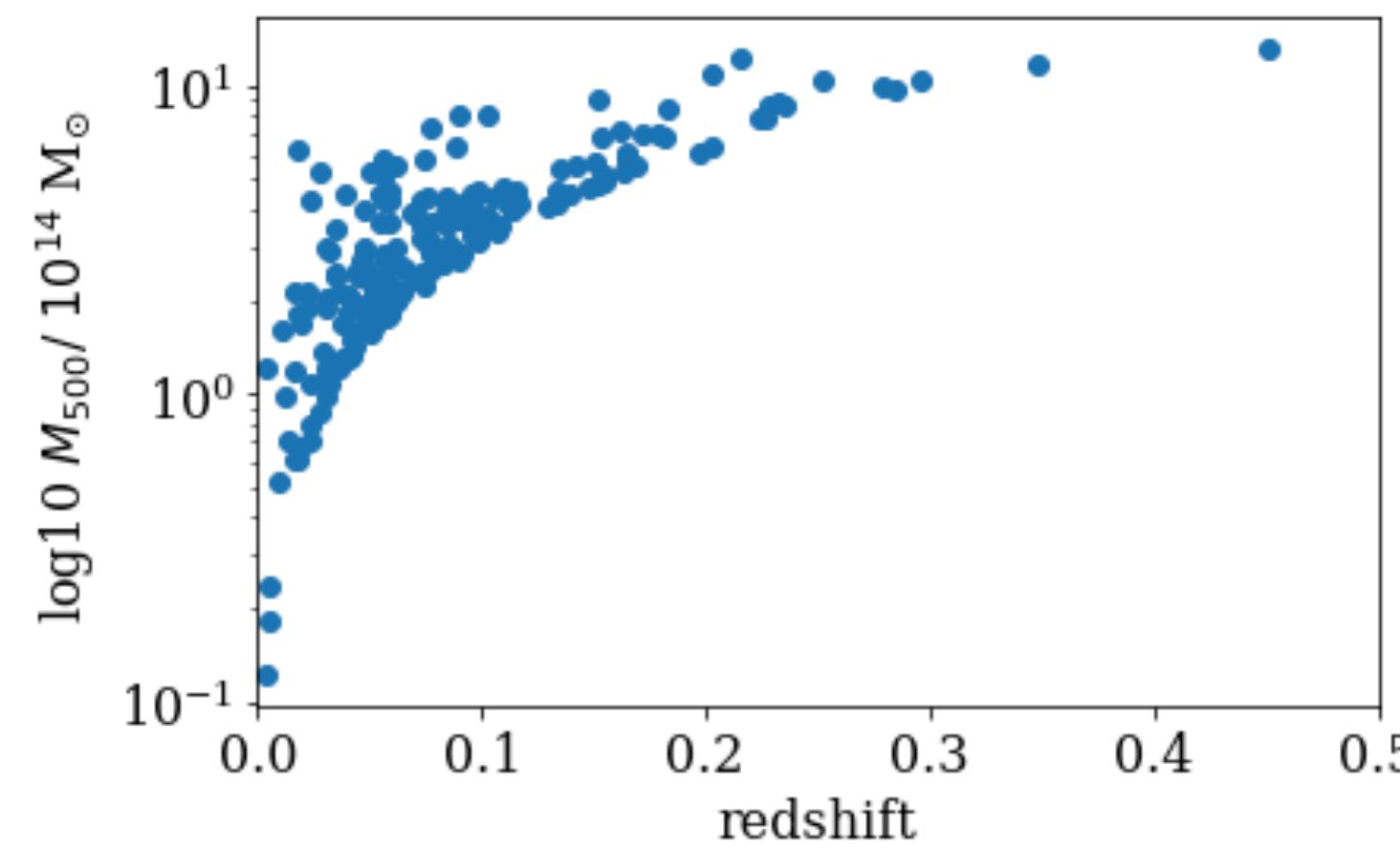
Backup slides

# Distribution in mass and redshift of the sample

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Performing a scan between  $10^{14}$  and  $10^{15}$  solar masses corresponds to values of the magnetic field at the center of the cluster between 3 and 8 micro Gauss.



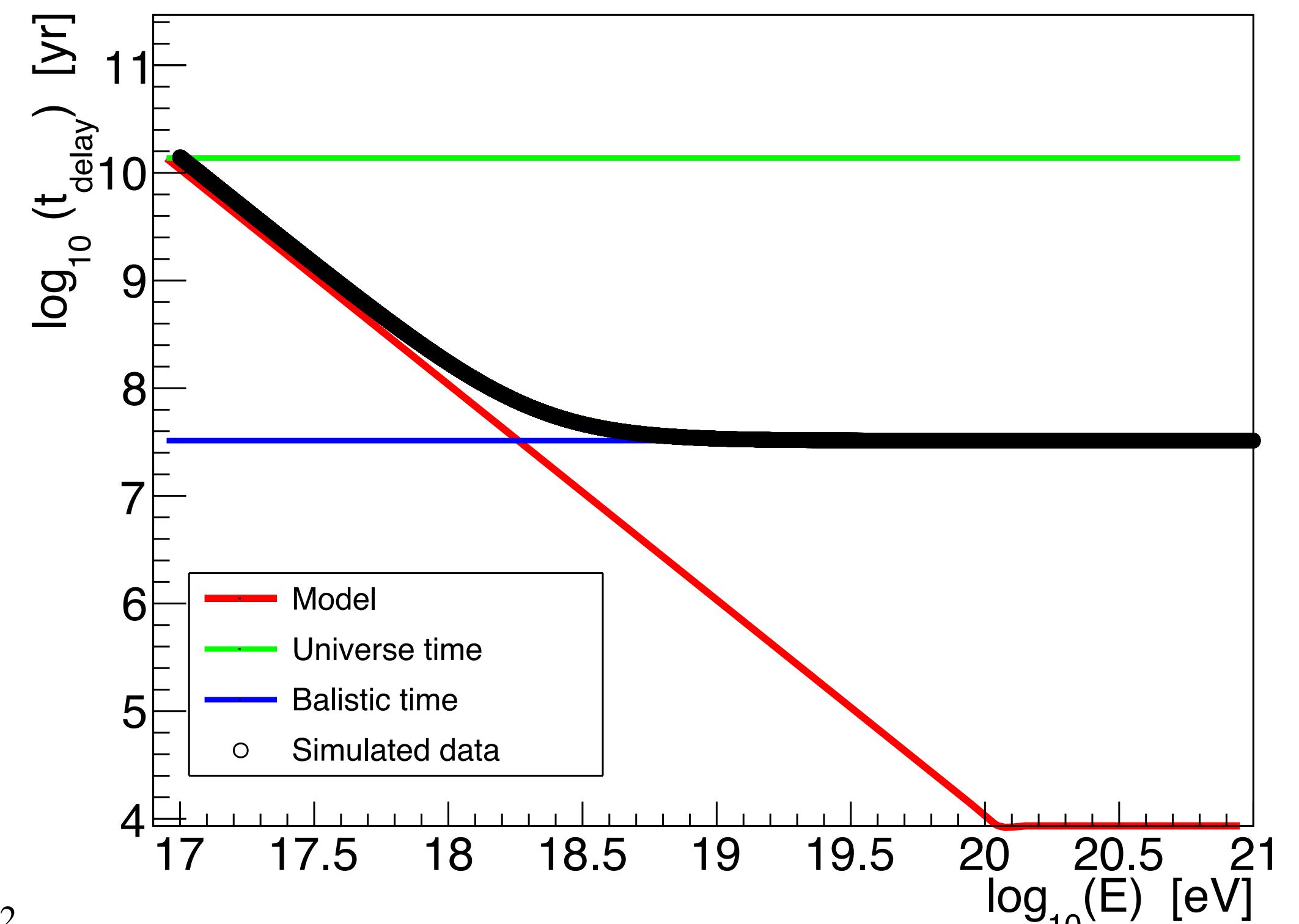
# Magnetic field in the source

Charged particle moving through a uniform magnetic field undergoes an angular deflection upon traversing a distance,  $L_{coh}$ , of  $\alpha = \frac{L_{coh}}{R_L}$

A particle traversing a distance,  $L$ , suffers an overall angular deflection given by

$$\theta(E, Z) \simeq \left( \frac{L}{L_{coh}} \right) \alpha$$

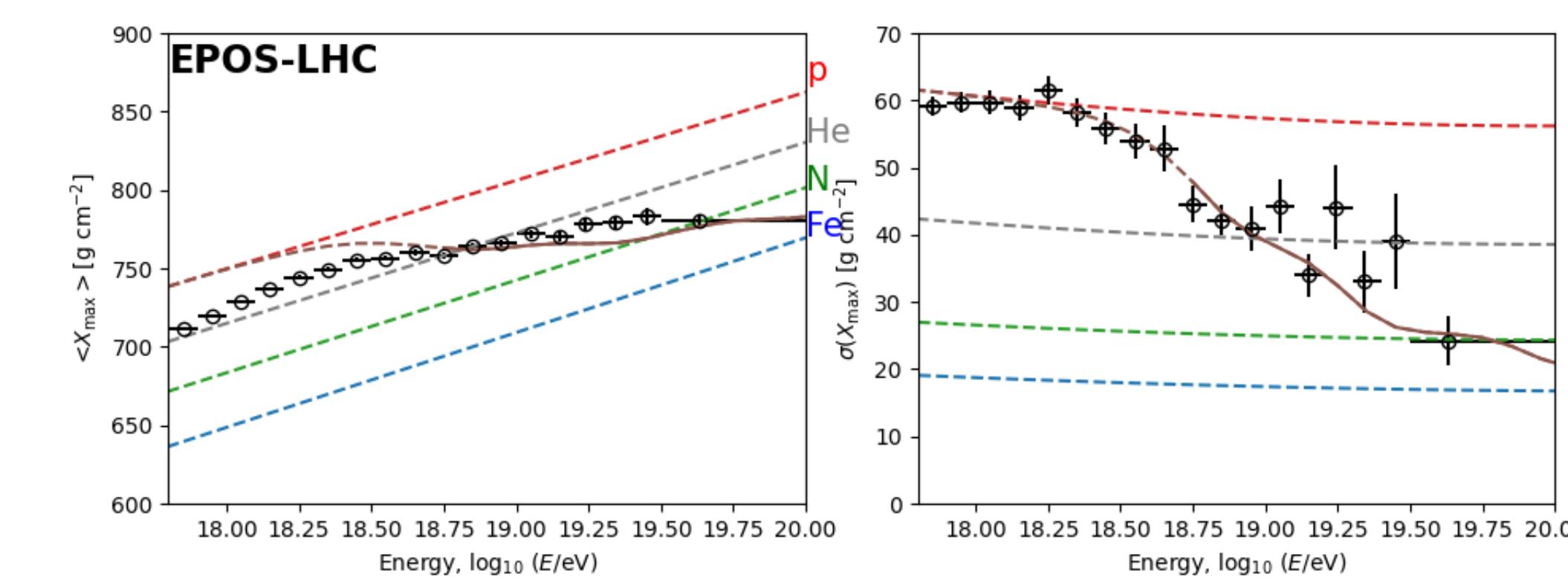
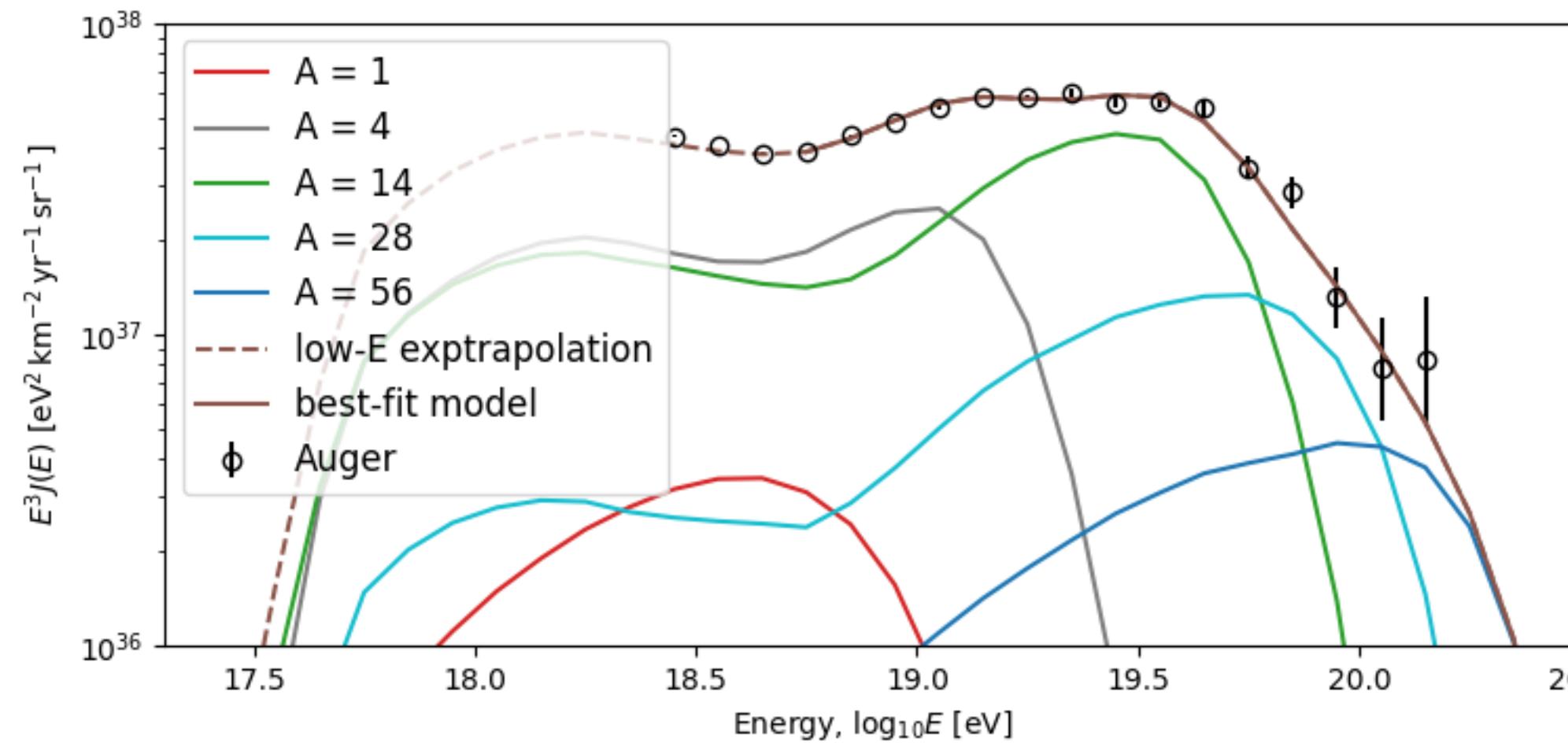
$$\frac{L_{eff}}{L}(E, Z) \simeq \cos\theta \simeq 1 + \frac{\theta^2}{2} \simeq 65 \left( \frac{10^{20} \text{ eV}}{E} \right)^2 \left( \frac{L}{1 \text{ Mpc}} \right) \left( \frac{L_{coh}}{10 \text{ kpc}} \right) \left( \frac{B}{1 \mu\text{G}} \right)^2 \left( \frac{Z}{26} \right)^2$$



# EG propagation and comparison to data

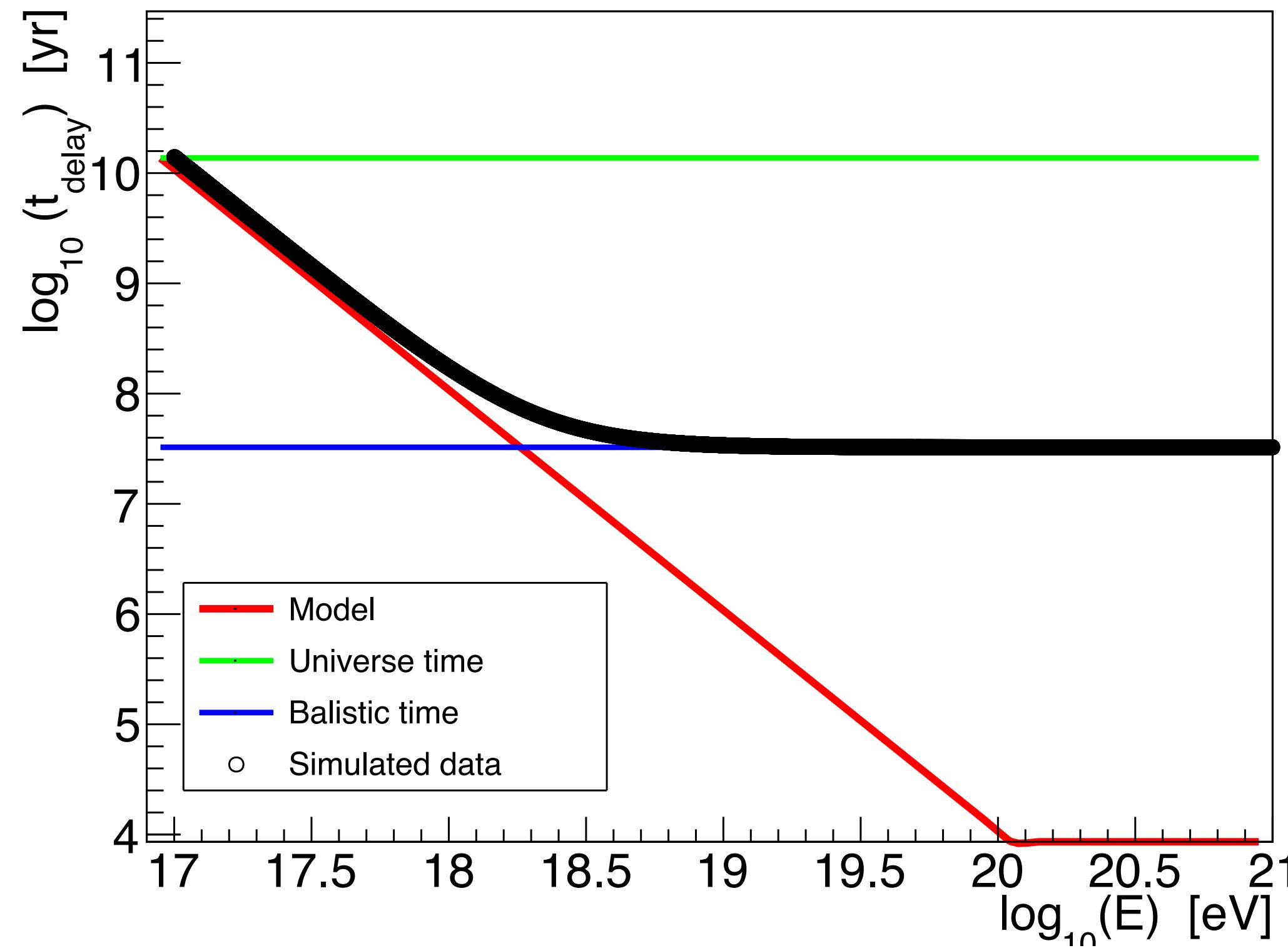
Combined fit code capable to:

- \* Use a 5D tensor, coming from SimProp simulations, to compute the extra-galactic propagation;
- \* Fit simultaneously energy spectrum and mass observables (lnA, mean Xmax or Xmax distributions) above the ankle;
- \* Producing sky maps;

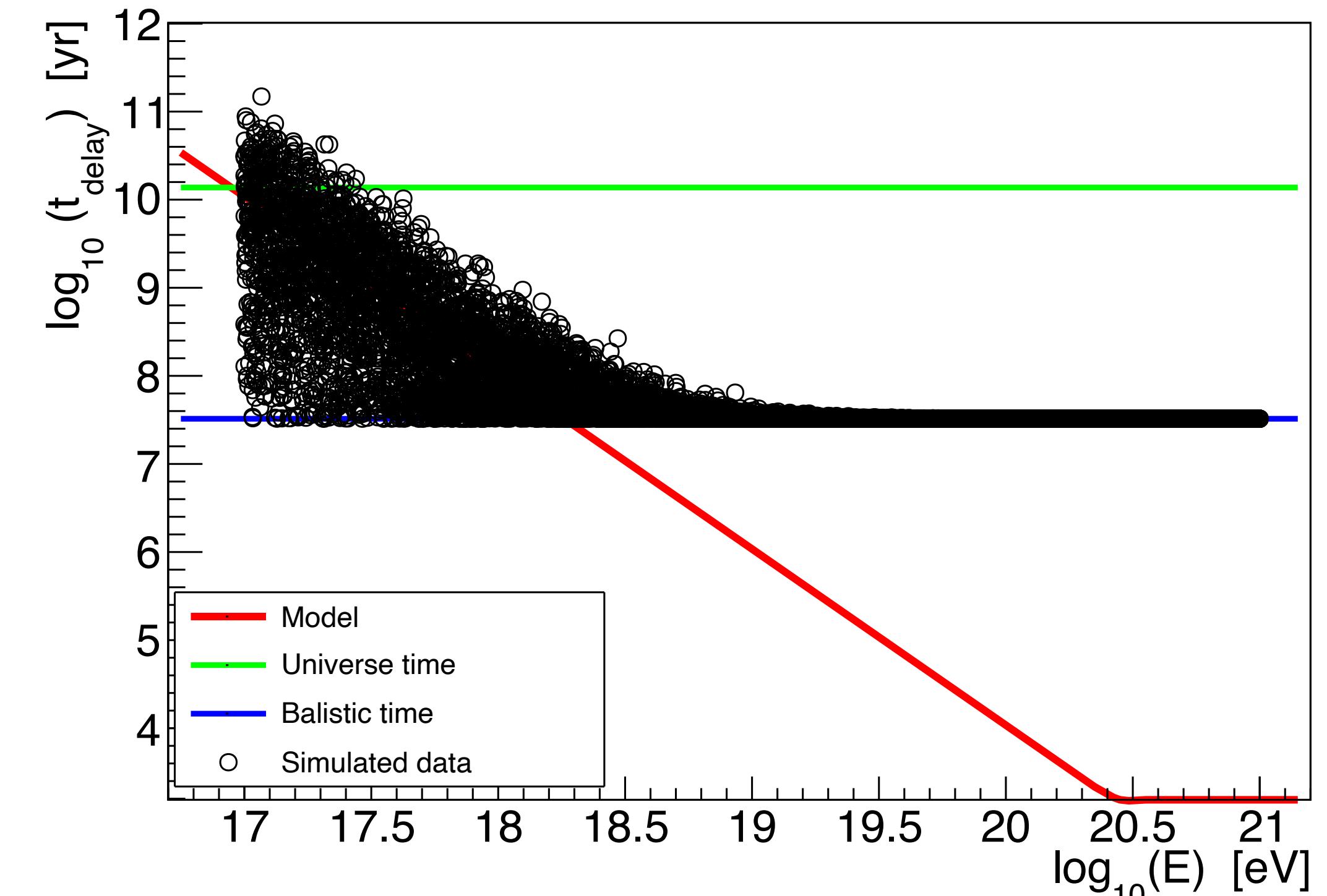


# Magnetic field in the source

No randomisation

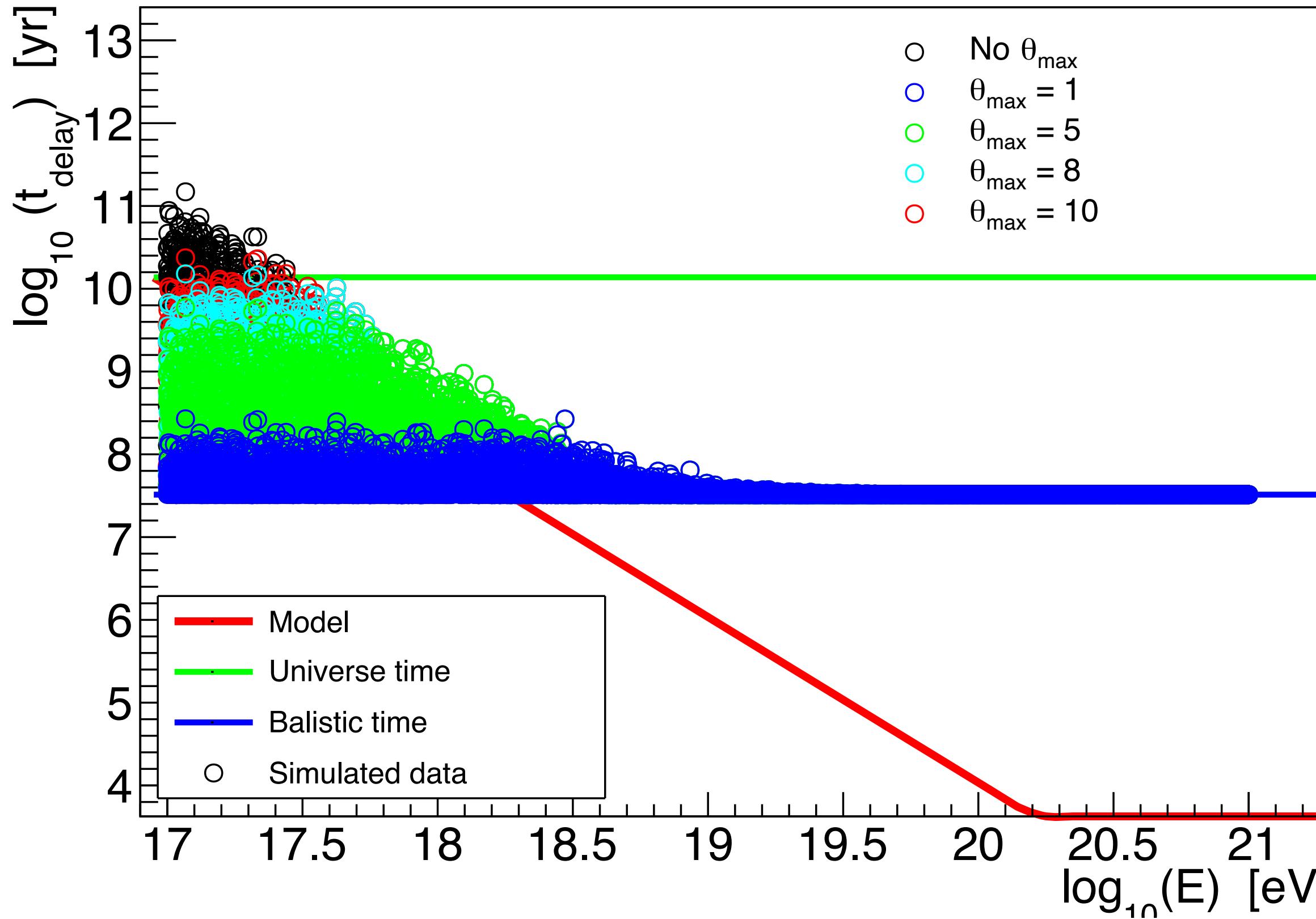


Randomisation

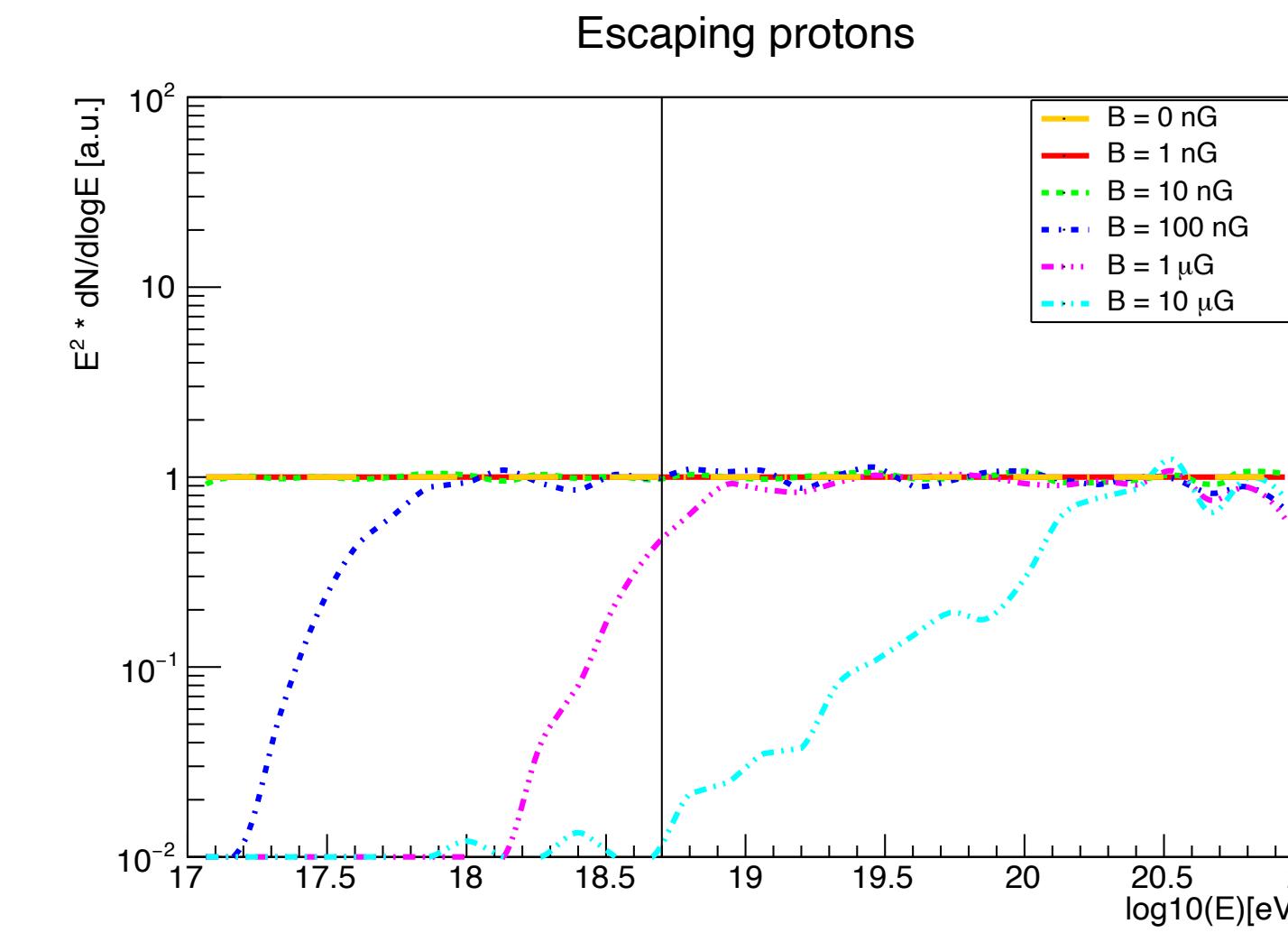
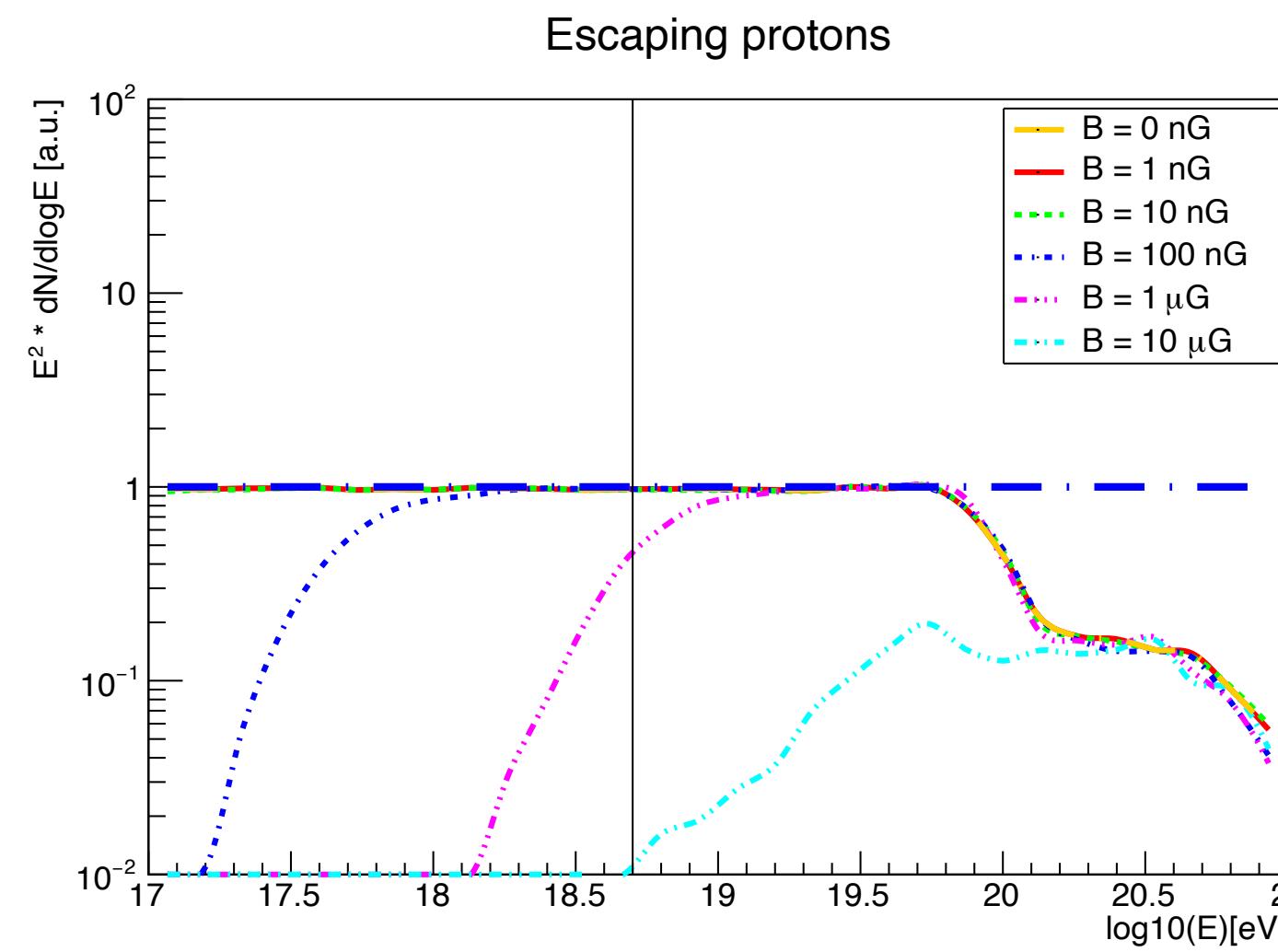


# Small angle approximation is justified?

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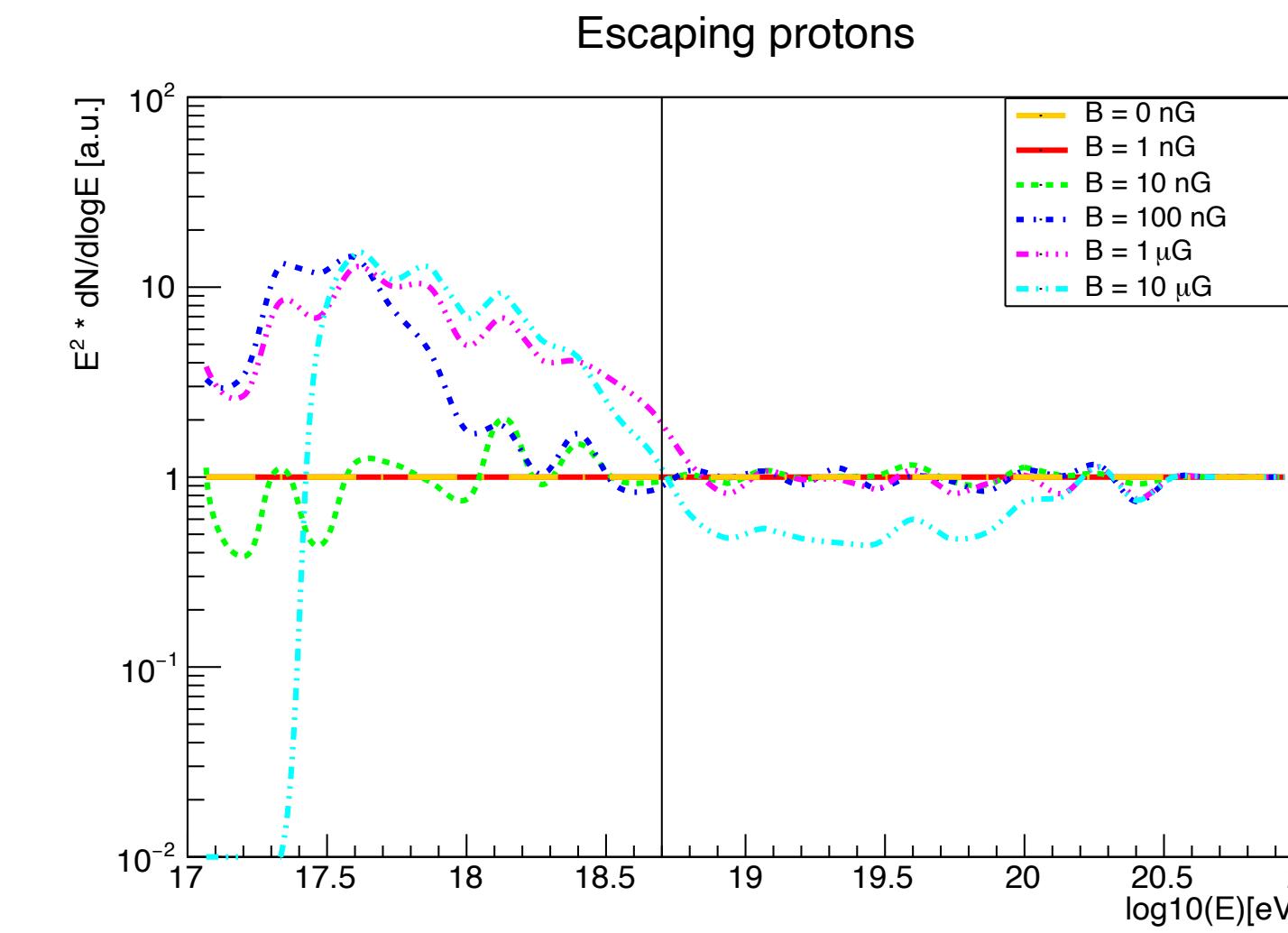
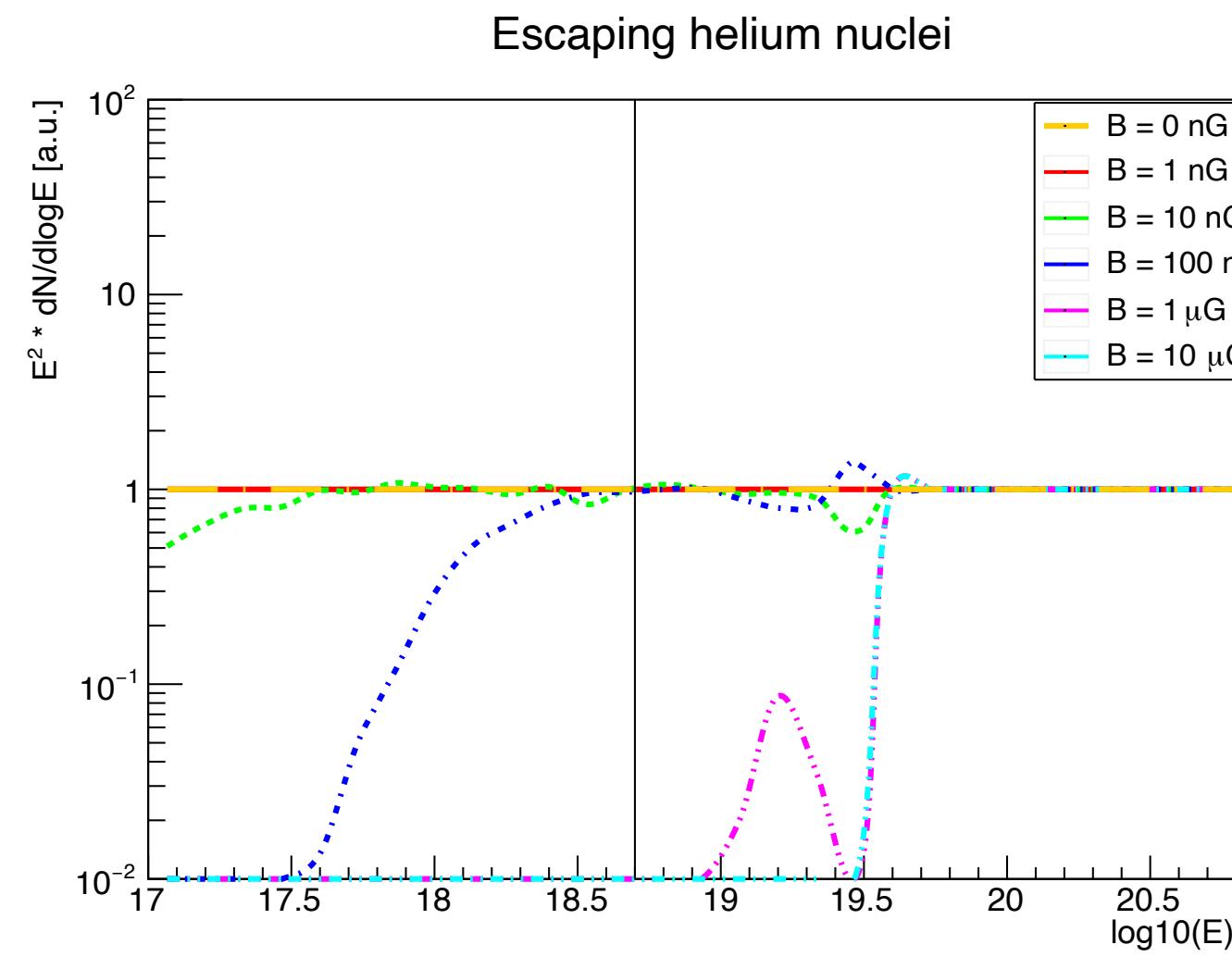
# Injecting protons



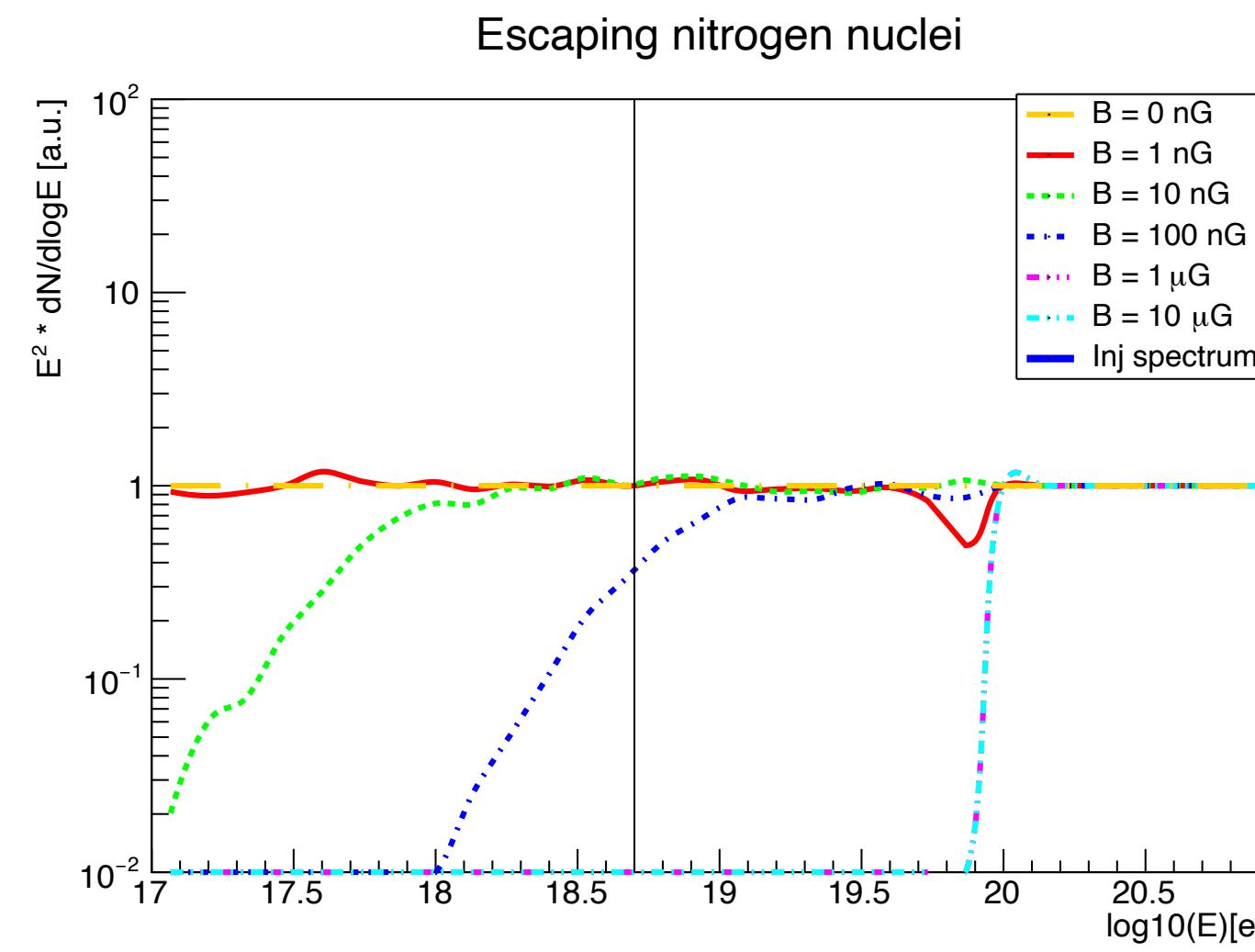
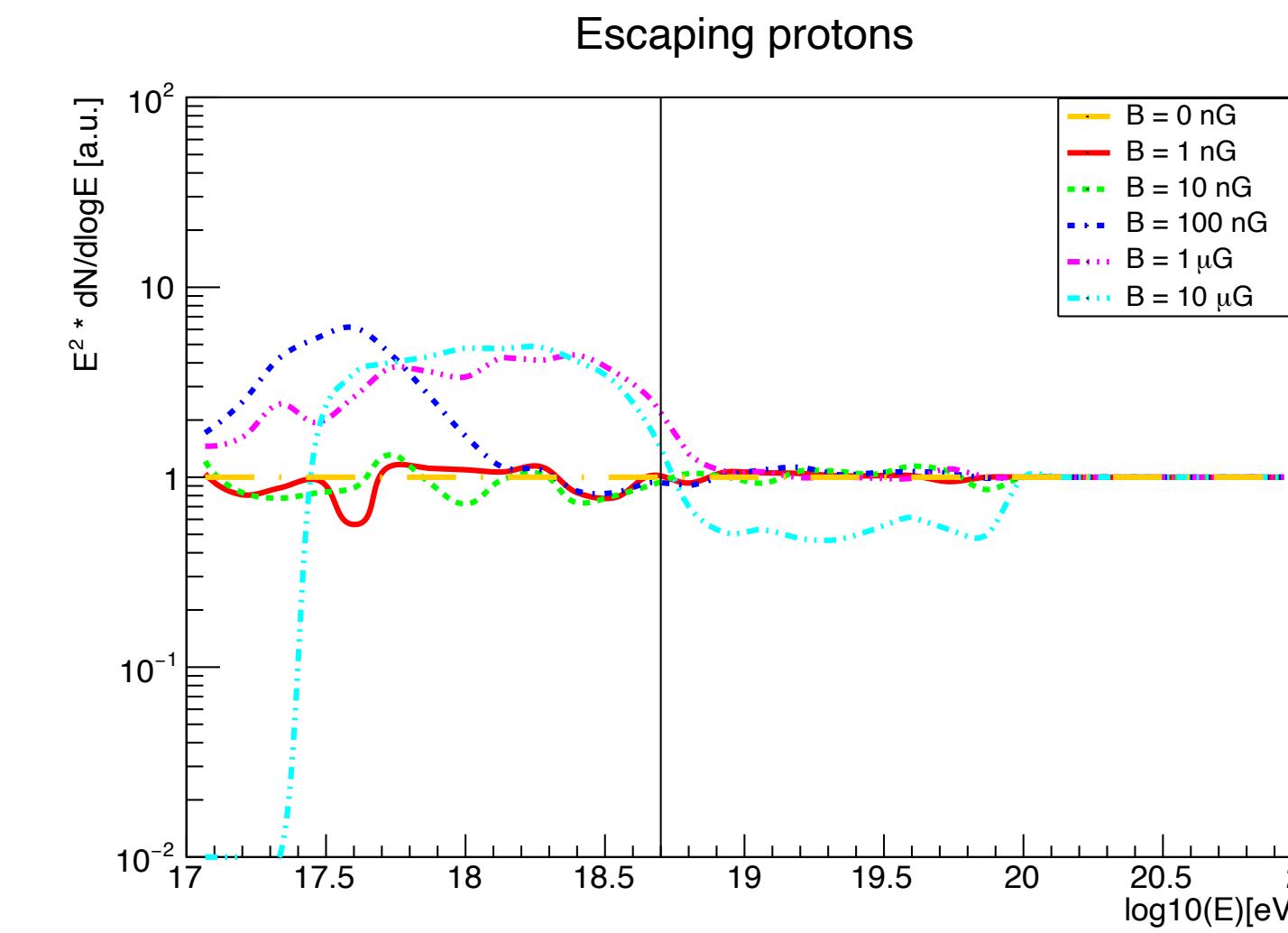
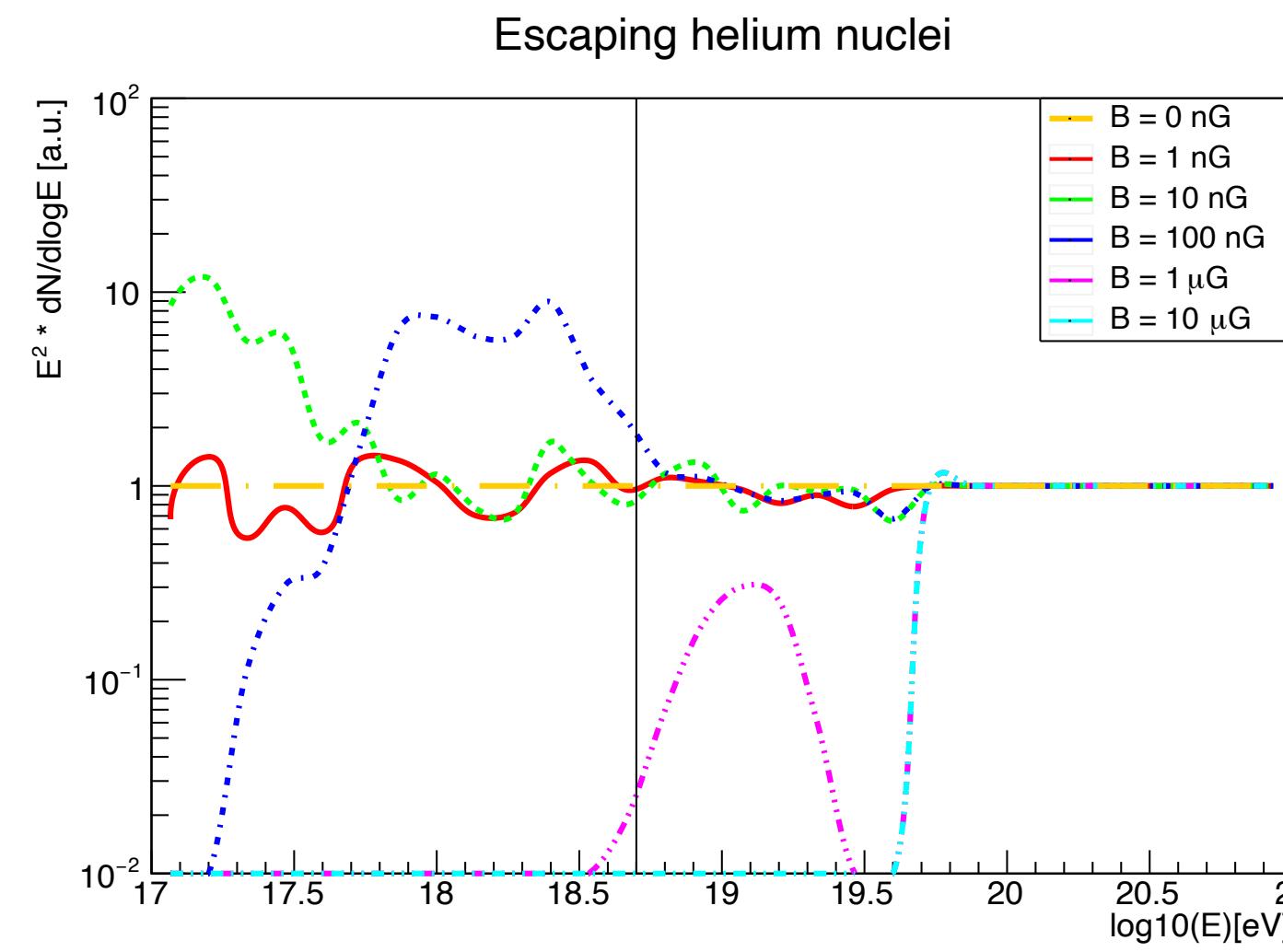
Normalized to the injection spectrum

Normalized to  $B = 0$

# Injecting Helium



# Injecting Nitrogen



# Injecting Silicon

