

*FCC\_ee Injector Complex*  
**WP04: Transfer lines and Damping Ring**

# **Damping Ring summary**

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**(a) INFN – Laboratori Nazionali di Frascati**

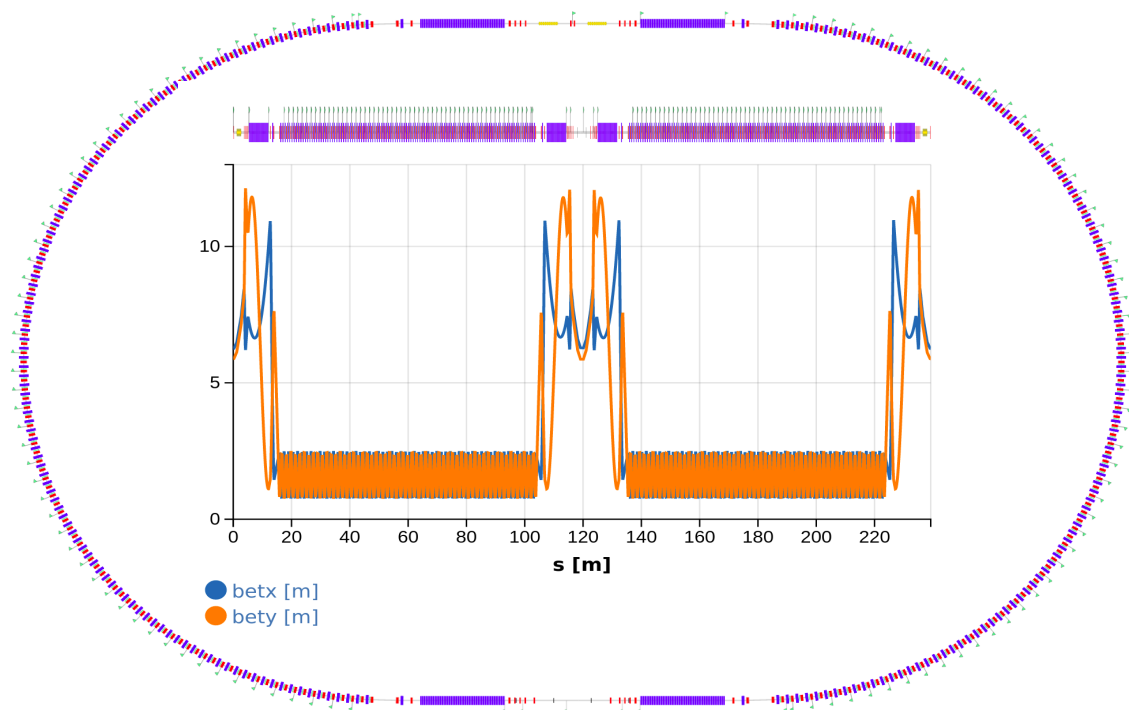
**(c) Kirikalle University, Turkey**

# Outline

- DR optics
- Longitudinal acceptance
- Dynamical aperture
- Collective effects preliminar evaluation
- Injetion/extraction timing scheme
- Conclusions

# DR optics

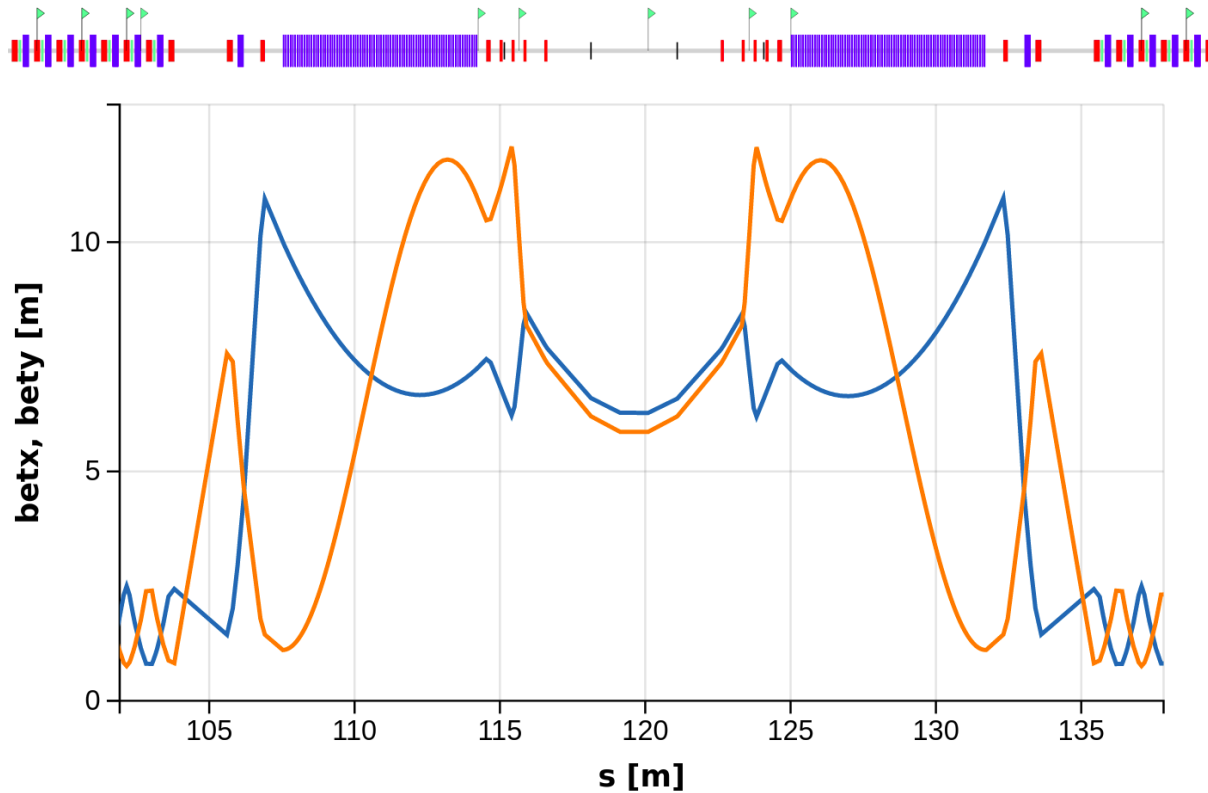
# Damping ring layout



Parameter	FCC_ee DR
Circumference	239.2 m
Harmonic number	319
Eq. Emittance (x/y/z)	1.01 nm/ - / 1.46 $\mu\text{m}$
Dipole length, Field	0.21 m, 0.66 T
Wiggler #, Length, Field	4, 6.64 m, 1.8 T
Cavity #, Length, Voltage	2, 1.5 m, 4 MV
Bunch stored #, charge	18 , 4.0 nC
Damping Time (x/y/z)	10.8 / 10.8 / 5.4 ms
Store Time	42.5 ms
Energy loss per turn	0.227 MV
SR Power Loss (WGL )	15.7 kW

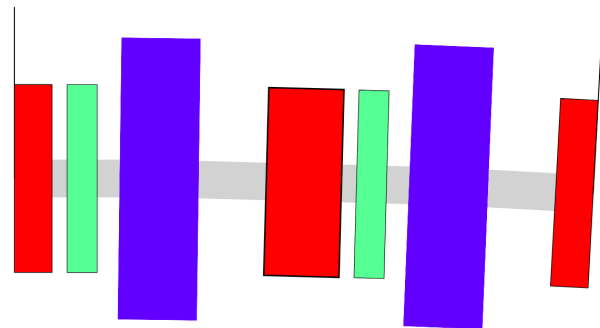
Following the FCC-ee injector review report recommendations, the reference design for the DR is the one initially provided by K. Oide and S. Ogur in 2019. Newest design suited for multibunch operation have been abandoned.

# DR optics details

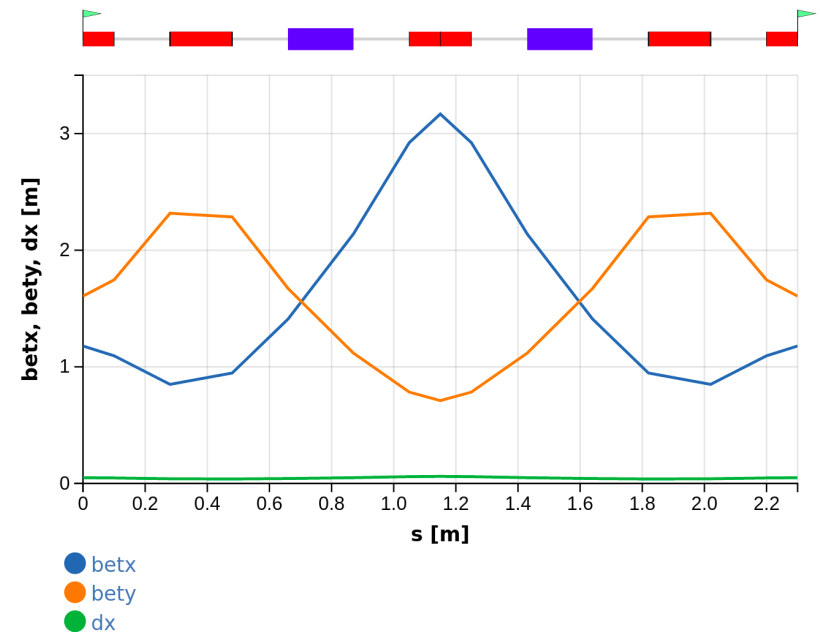


● betx  
● bety

DR DBA Cell



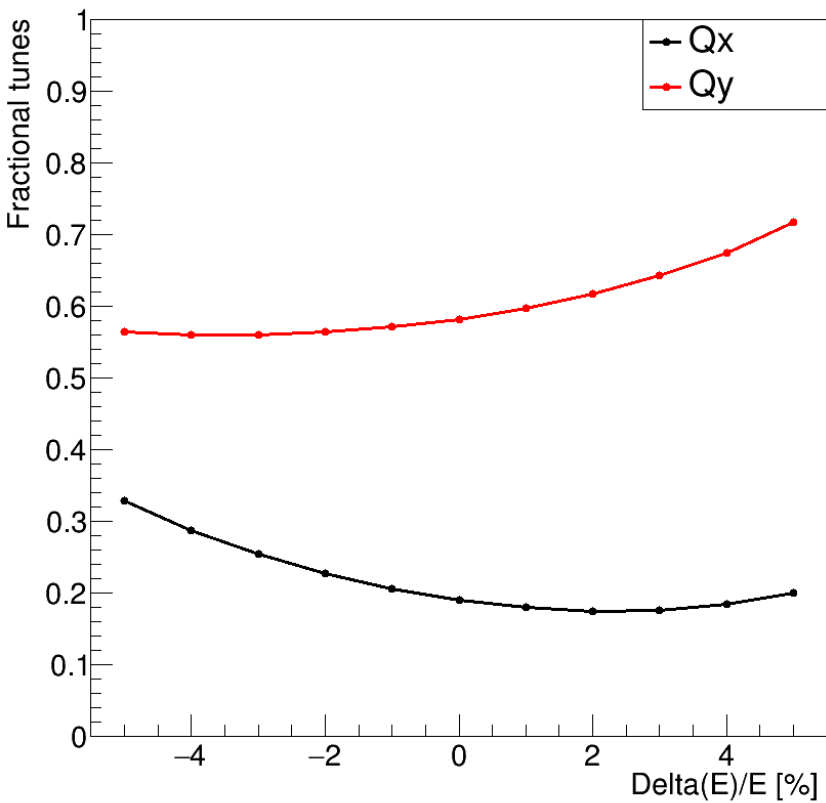
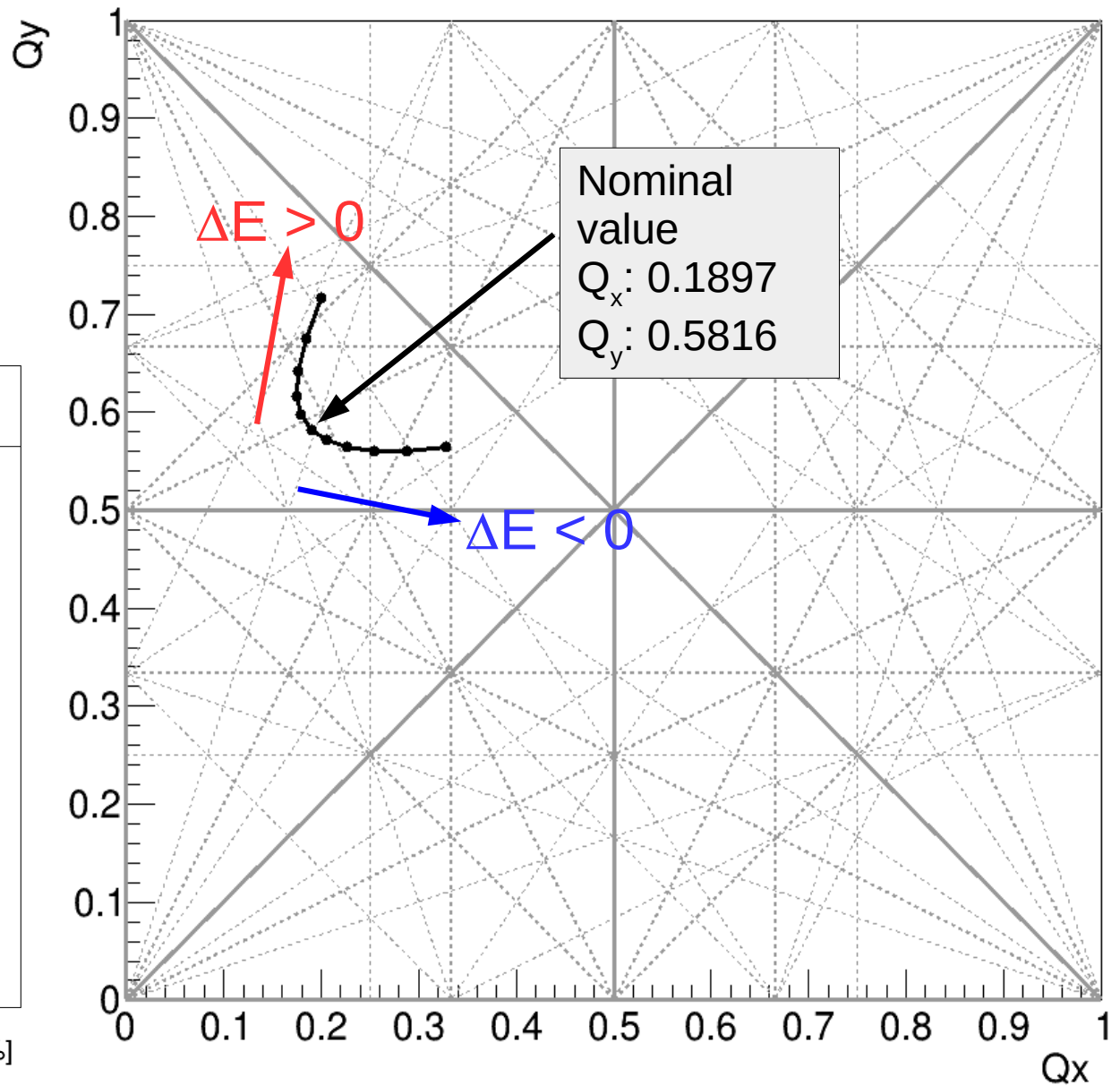
Straight section details.  
Two of the four wigglers are shown.  
Straight sections are designed to host RF cavities and Injection/Extraction equipments.



● betx  
● bety  
● dx

# Tune diagram

Tune variation as a function of energy for the nominal lattice



# DR longitudinal acceptance

# Energy Acceptance at injection for e<sup>+</sup> beam

$$\left(\frac{\Delta E}{E_s}\right) = \pm\beta \sqrt{\frac{eV}{\pi h \alpha_c E_s} \mathcal{R}(\varphi_s)}$$

$$\mathcal{R}(\varphi_s) = [2 \cos \varphi_s + (2\varphi_s - \pi) \sin \varphi_s]$$

If an energy acceptance of the order of

$$\left(\frac{\Delta E}{E_s}\right) \sim 6\%$$

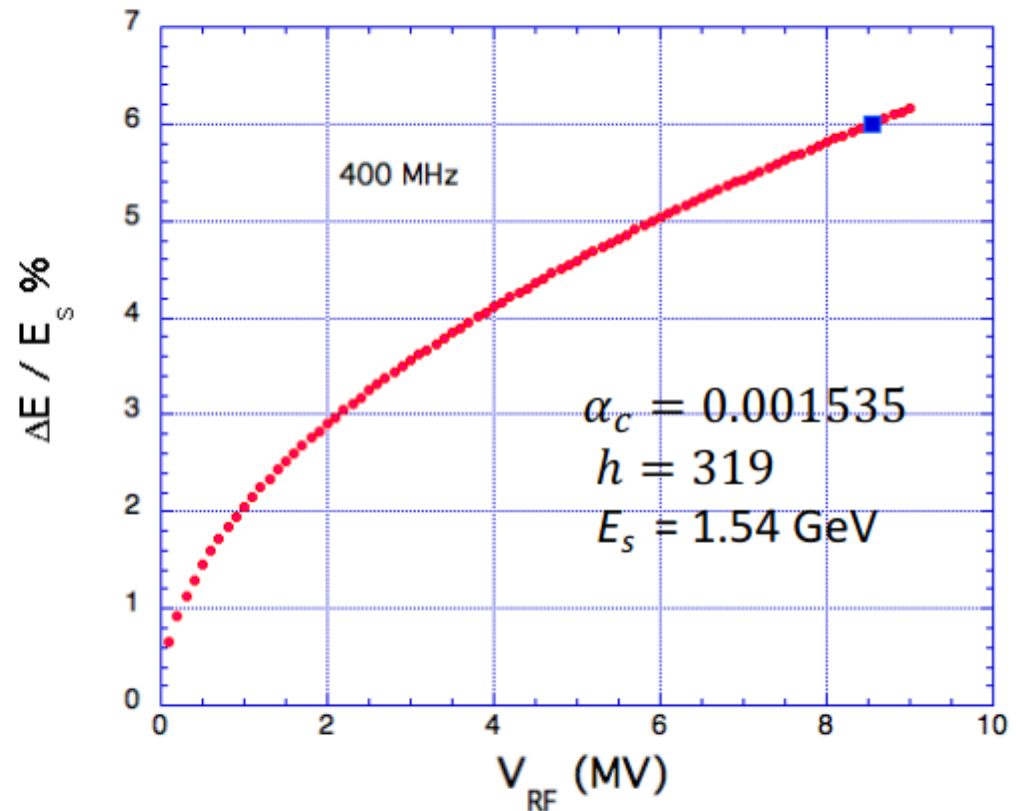
is requested in injection

$$V_{RF} = 8.53 \text{ MV}$$

SC RF cavities working at 400 MHz and providing at least 4 MV are considered.

Minimum RF cavity voltage request to compensate the energy lost per turn is

$$E_{LT} = 0.225 \text{ MV}$$





# DR Beam Dynamics Parameters

Relying on DR parameters:

$$E_s = 1.54 \text{ GeV}$$

$$L = 239.2628817 \text{ m}$$

$$\alpha_c = 0.001535$$

$$h = 319$$

	V= 8MV	V= 6MV	V= 4MV	V= 2MV
$U_0$ [KeV]	227.1			
$DE/E_s$	$0.71 \cdot 10^{-3}$			
$\Omega_s$ [KHz]	25.313	21.918	17.888	12.618
$T_0$ [ $\mu$ sec]	0.79801			
$\omega_0$ [ $s^{-1}$ rad]	$7.87 \cdot 10^6$			
$v_s$	0.003215	0.00278	0.002272	0.0016
$L_{\text{bunch}}$ [m]	<b>0.00207</b>	0.00239	0.00293	0.00415
$\varphi_s$ [rad]	0.0283967	0.0378663	0.0568164	0.113817
$(E - E_s)$ [GeV]	0.124	0.107	0.0862	0.058
$\Delta\varphi$ [unit of $\pi$ ]	1.8	1.7769	1.7269	1.6016
$L_{\text{bucket}}$ [m]	0.6788	0.6664	0.6476	0.6006

Short bunch length can be an issue for:

lifetime,

injection must be carefully tuned,

impedance and bunch lengthening must be evaluated,

Beam coupling with RF system

CSR,

IBS,

beam instability impact

# Separatrix

$W$  -  $\Phi$  representation, canonical coordinates

$$W_{bh} = \frac{L}{\pi h c} \sqrt{\frac{e V E_s}{2 \pi h \eta_{tr}}}$$

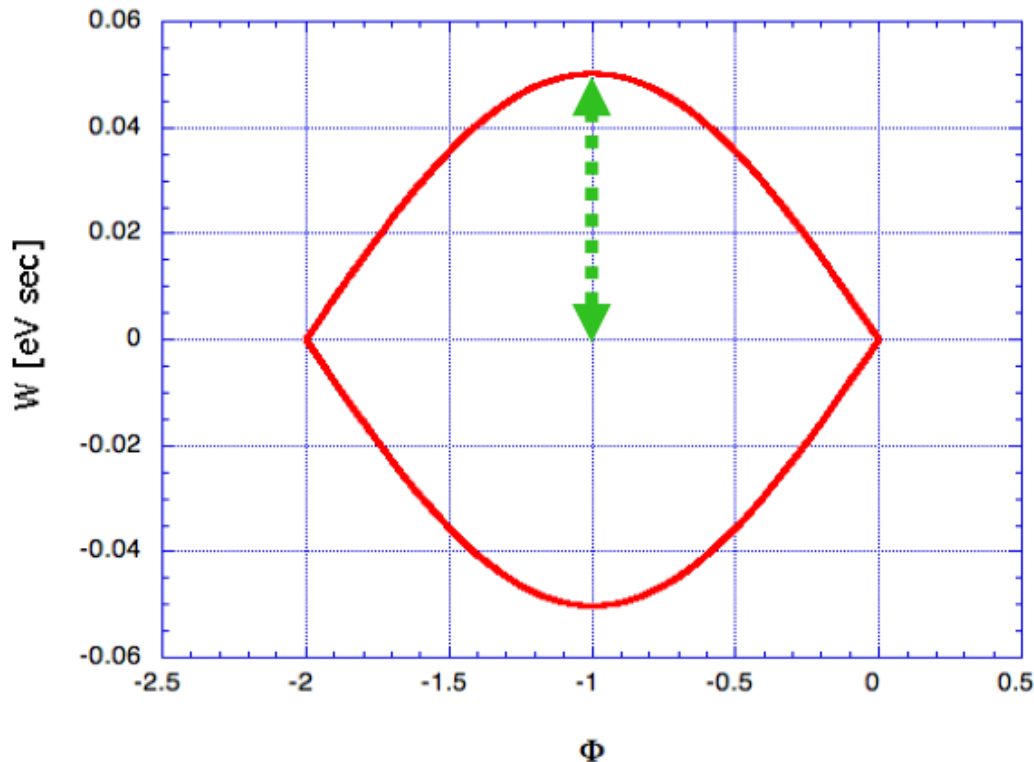
$$A_{bk} = 2 \int_0^{2\pi} W d\phi = 8 W_{bh}$$

$$\frac{1}{\Omega_s} \frac{d\phi}{dt} = \frac{2\pi c}{L} \sqrt{\frac{2\pi h^3 \eta_{tr}}{E_s e V \cos \phi_s}} W$$

The area of the bucket is an adiabatic invariant, **longitudinal acceptance**

Bunch area is **longitudinal emittance**

$$\varepsilon_t = 4\pi \sigma_E \sigma_t \text{ [eV sec]}$$



Assuming:

$$\alpha_c = 0.001535$$

$$h = 319$$

$$V = 8 \text{ MV}$$

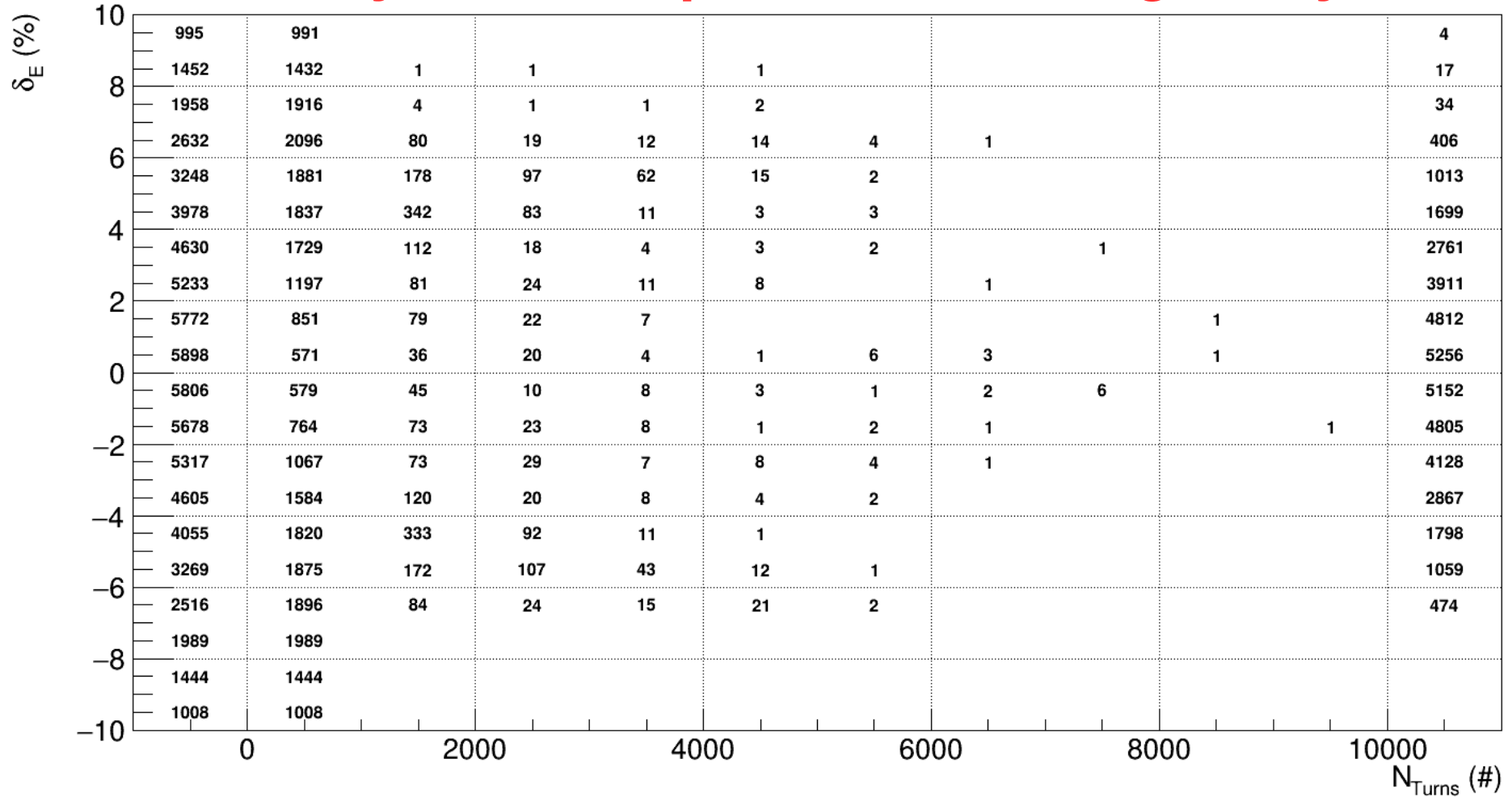
$$E_s = 1.54 \text{ GeV}$$

$$W_{bh} = 0.0501813 \text{ (eV sec)}$$

$$A_{bk} = 0.401451 \text{ (eV sec rad)}$$

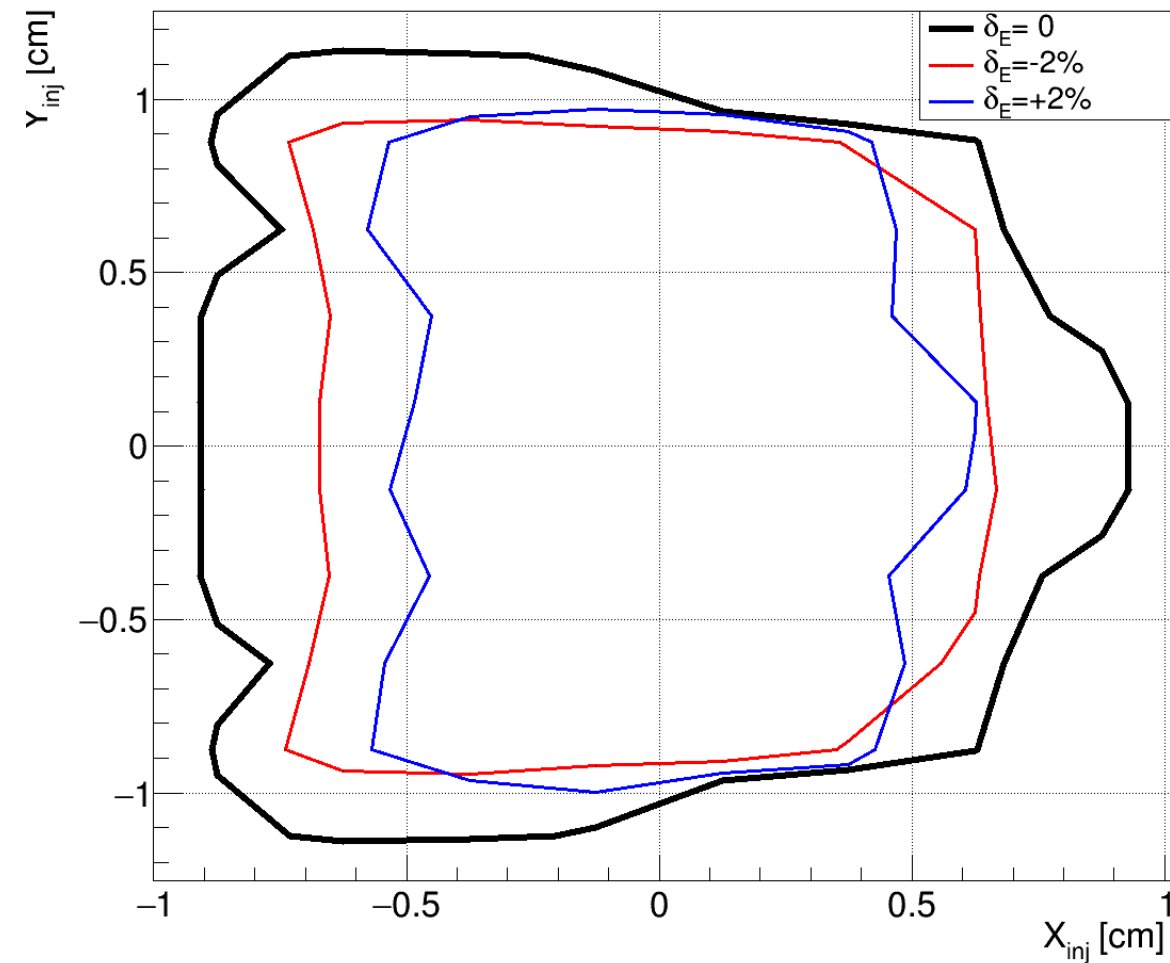
# DR dynamical aperture

# DR dynamical aperture: Tracking study



Tracking has been performed with PTC (MAD-X interface) for 10k turns. Initial distribution are Gaussian with nominal emittance (CDR  $\epsilon_x:1.29$   $\epsilon_y:1.22$   $10^{-6}$ m rad). Complete tracking has been performed, including radiation loss and RF effects. In the table the numbers refers to the particles lost at a given turn (1k width). The first column is the number of initial particles. The range of energy considered is quite large in order to estimate the acceptance as a function of the energy deviation.

# DR dynamical aperture



Tracking has been performed with PTC (MAD-X interface).

2000 turns has been tracked ( $\sim 15\%$  damping time). The estimated loss of accuracy is below 1% at the nominal energy.

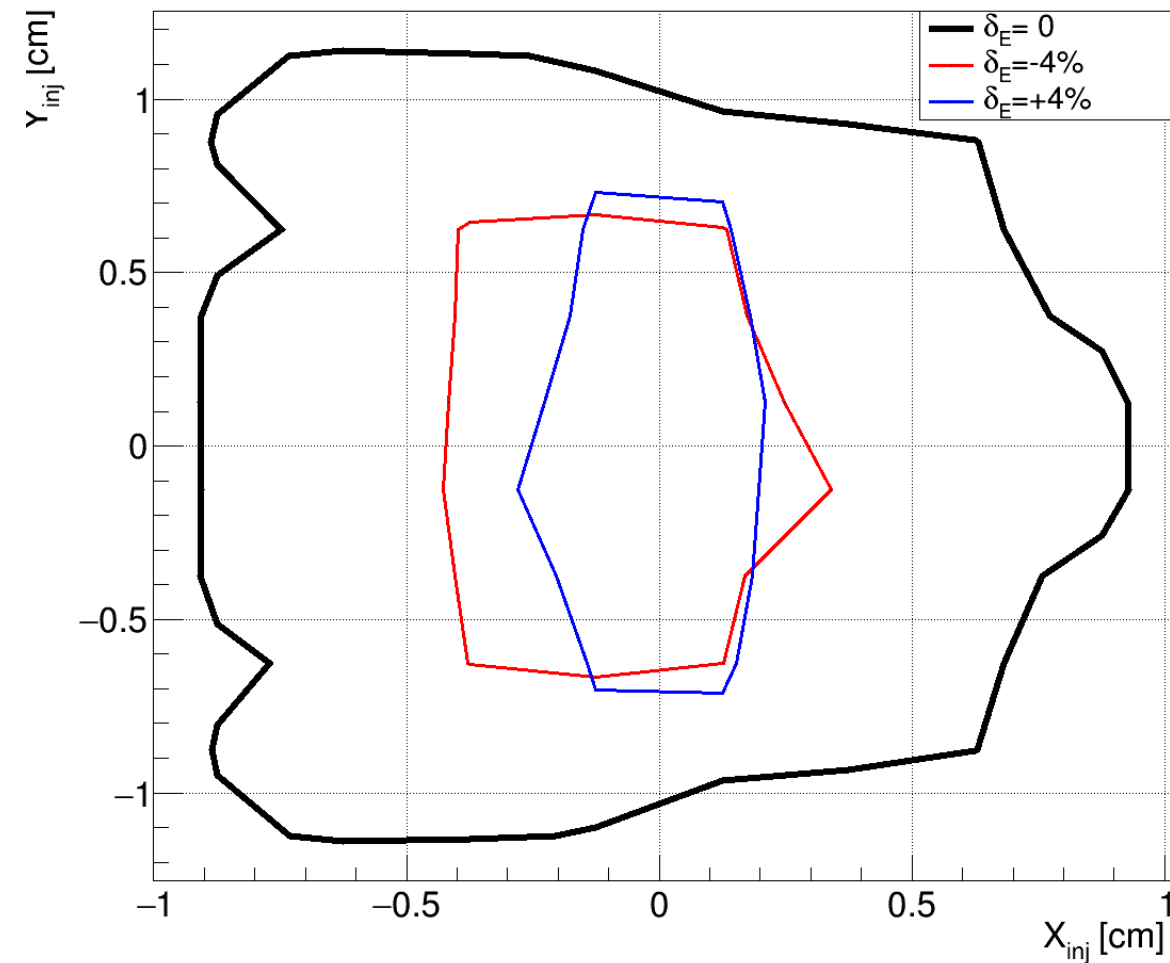
The phase space have been sampled up to  $3 \times 3$  cm<sup>2</sup> in the transverse plane. Only on-axis particles have been simulated ( $x'/y'=0$ ).

Radiation damping has been neglected allowing a much faster tracking of the DR.

The stability region in the transverse plane have been evaluated for different energy deviation, in the range between  $\pm 2\%$ .

Contours represents regions where at least 90% of the initial conditions leads to a successful tracking. A probability definition is needed in order to take into account the average value over the surface.

# DR dynamical aperture



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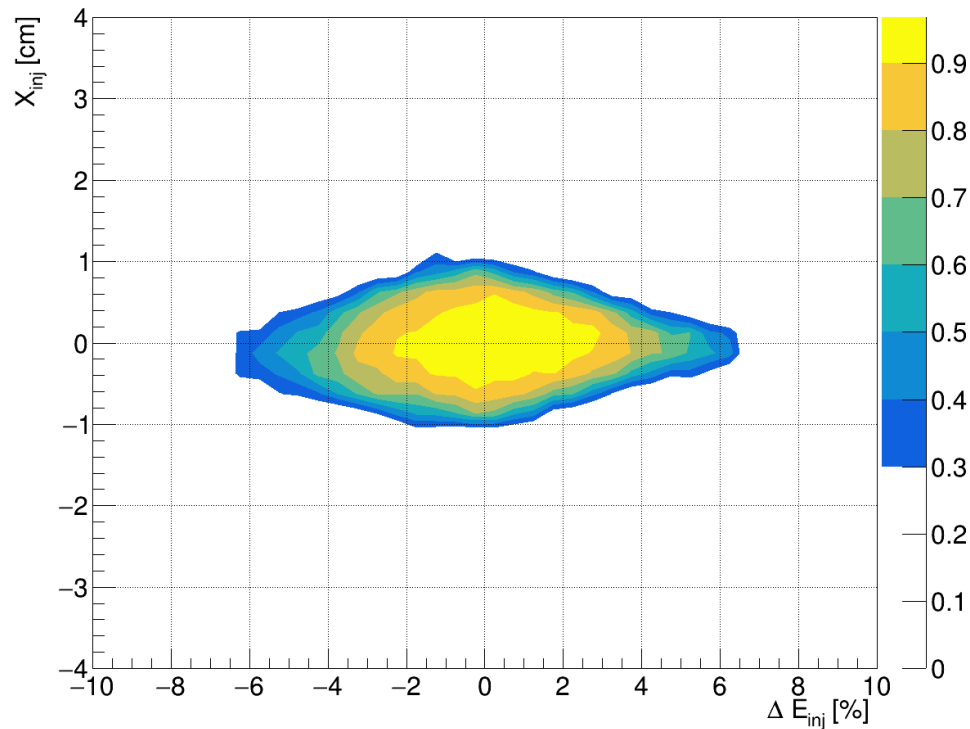
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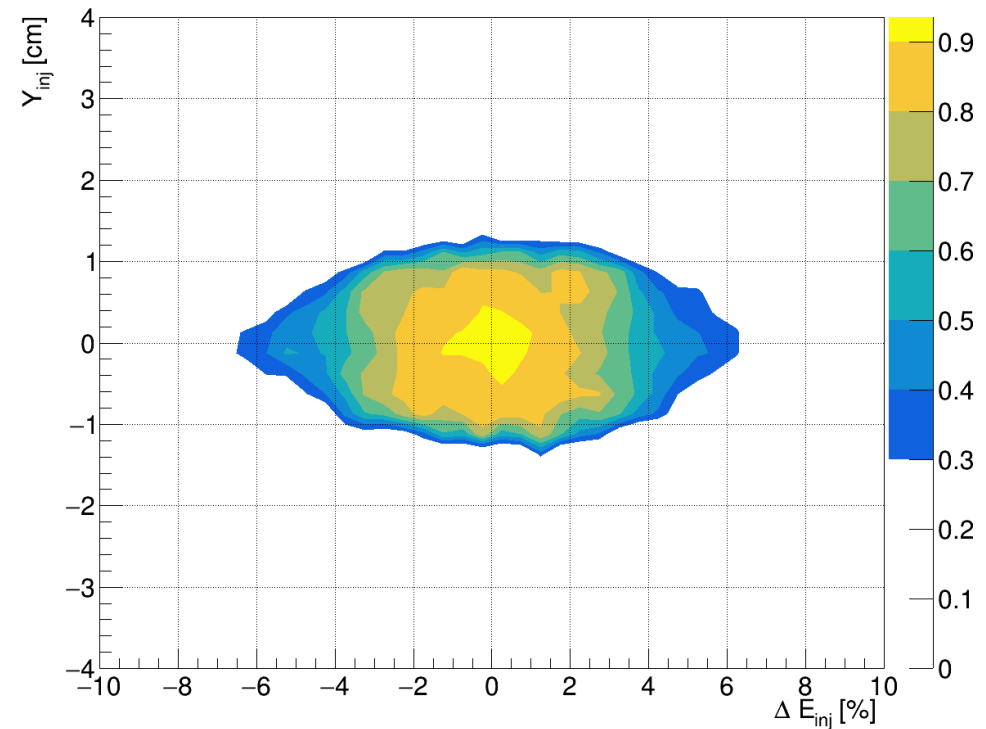
For larger energy variations ( $\pm 4\%$ ) the stability region shrinks considerably and it is clearly not symmetric w.r.t. the energy variation itself in the transverse plane being considerably smaller at higher energy (blue) w.r.t. lower energies (red). For reference the stability region at the nominal energy has been reported.

# DR acceptance probability

pDR: acceptance density @ Ebeam = 1.54 GeV



pDR: 55-95% Aperture @ Ebeam = 1.54 GeV

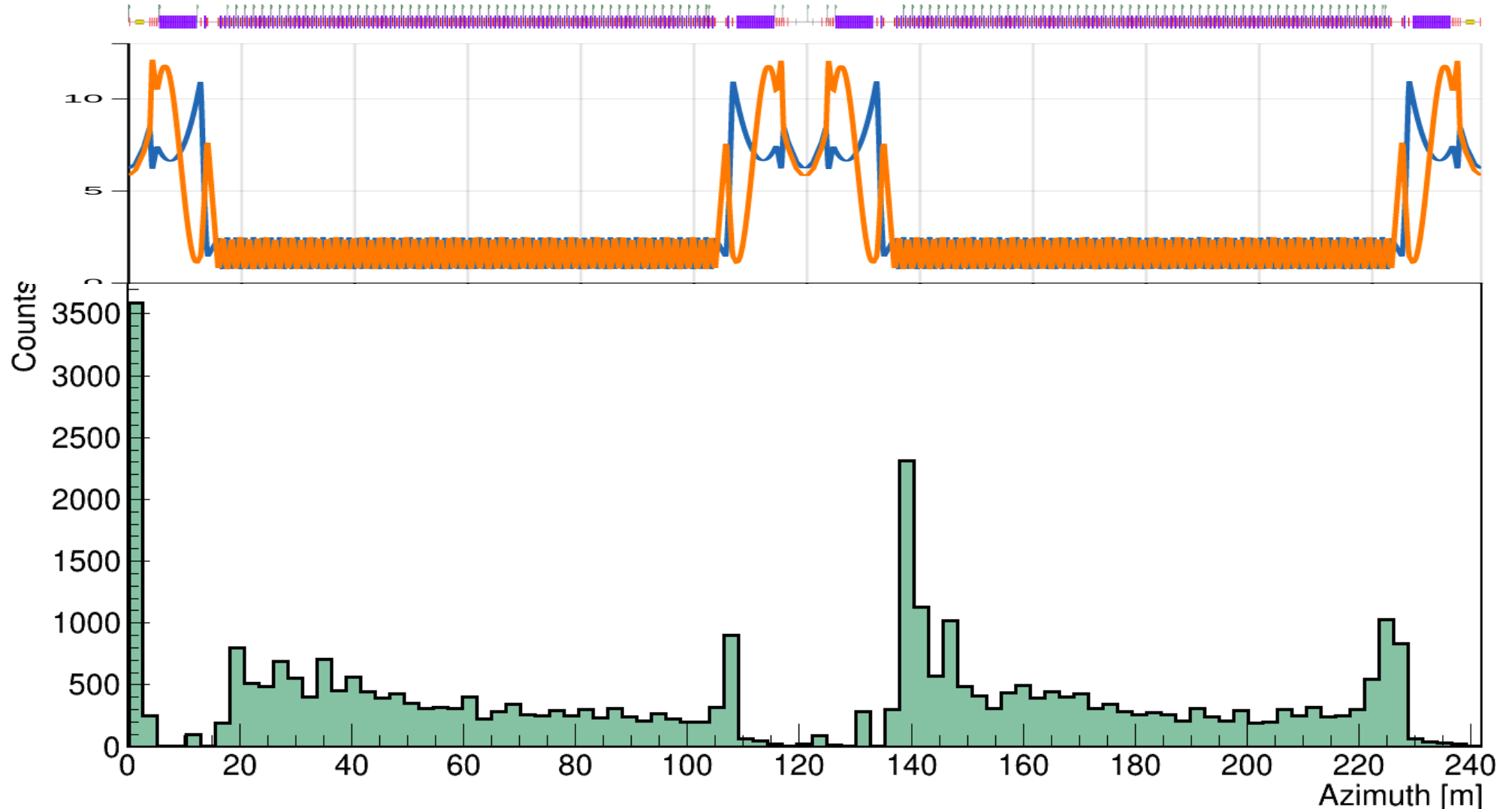


DR acceptance probability has been evaluated starting with nominal CDR beam at the injection: Gaussian profile with nominal width at the injections ( $\sigma \sim 2\text{mm}$  in both planes). The energy distribution has been assumed Gaussian with 5% resolution.

The color map represent the projection of the survival probability associated to the different position in space: horizontal and vertical, respectively as a function of energy deviation.

A full matrix in phase space will be delivered to reshape particle distribution at the positron source.

# DR: particle loss distribution



Tracking has been performed starting with nominal CDR beam at the injection: Gaussian profile with nominal width ( $\sigma \sim 2\text{mm}$  in both planes). The energy distribution has been assumed Gaussian with 5% resolution.

The plot shows the distribution of losses around the ring (lattice on top)



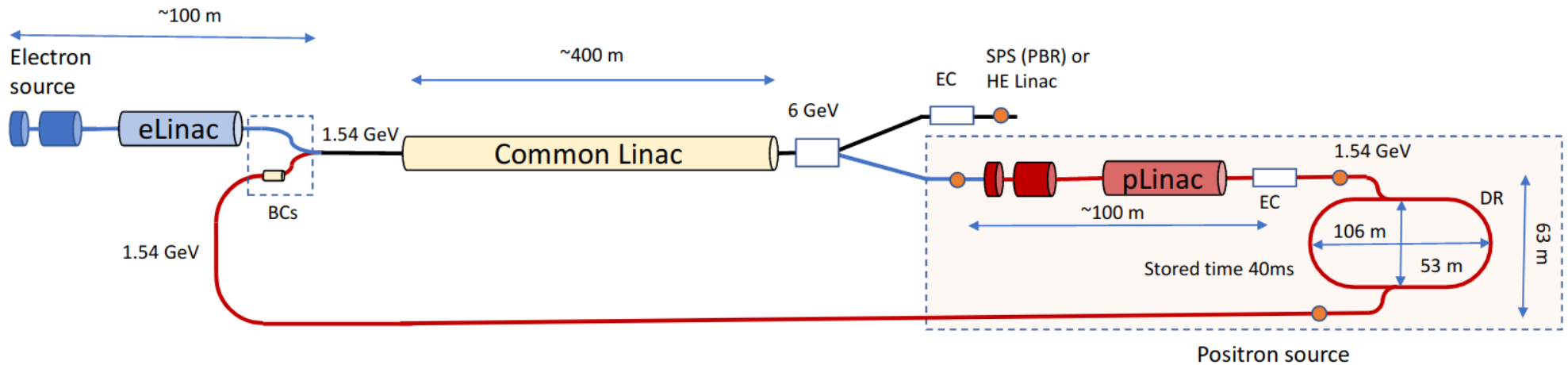
# Collective effects

- *Collective effects can limit the ultimate performance of any accelerator. In this respect, an analytical estimation of intensity thresholds and impedance budgets have been performed for the current DR design.*
- Based on the analytical estimations, **No major limitations** are expected due to **IBS, TMCI and CSR.**
- Concerning the **SC**, the tune shift at the equilibrium state might be an issue.
- The Boussard criterion is below the longitudinal impedance assuming a **vacuum chamber radius of 10 mm**. 35 mm radius is needed (need discussion with expert).
- It was shown that the **neutralization density exceeds the e-cloud instability threshold** for the equilibrium state. **This should be investigated with comprehensive simulations.**
- The **fast rise times** of the FII can be compensated with a **feedback system**, provided a vacuum pressure of **10<sup>-9</sup> mbar** are achieved **for the DR.**

Parameters	Parameters accounting for Collective Effects
$\delta Q_{x/y}$ - @inj. (e <sup>-</sup> )	0.004/0.003
$\delta Q_{x/y}$ - @inj. (e <sup>+</sup> )	1.8x10 <sup>-4</sup> /1.04x10 <sup>-5</sup>
$\delta Q_{x,y}$ - @eq. (e <sup>-</sup> and e <sup>+</sup> )	0.01/ <b>0.09</b>
Emit. growth by IBS @inj. (e <sup>-</sup> ) [%]	78
Emit. growth by IBS @inj. (e <sup>+</sup> ) [%]	6
$Z_0^{  }$ [ $\Omega$ ]	1
$(Z_0^{  }/n)^{th}$ [ $\Omega$ ] - @inj. (e <sup>-</sup> )	14
$(Z_0^{  }/n)^{th}$ [ $\Omega$ ] - @inj. (e <sup>+</sup> )	2585
$(Z_0^{  }/n)^{th}$ [ $\Omega$ ] - @eq.	<b>0.1</b>
$Z_L^{-}$ [M $\Omega$ /m]	<b>0.95</b>
$R_{th}$ [M $\Omega$ /m] @inj. for e <sup>-</sup>	12.06
$R_{th}$ [M $\Omega$ /m] @inj. for e <sup>+</sup>	3.54
$R_{th}$ [M $\Omega$ /m] @eq.	3.78
$\delta Q_{ion}$ @inj./@eq.	0.003/<<
$\tau_{inst}$ [t <sub>rev</sub> ] @inj./eq.	770/14
$\rho_{neutr}$ [10 <sup>11</sup> /m <sup>3</sup> ]	<b>125.06</b>
$\rho_{th}$ [10 <sup>11</sup> /m <sup>3</sup> ] @inj.	1634
$\rho_{th}$ [10 <sup>11</sup> /m <sup>3</sup> ] @eq.	<b>22.06</b>
Štupakov parameter @eq.	<b>3.18</b>
$\rho/b$ @eq.	0.73
$0.5\rho\Lambda^{-3/2}$ (m)@eq.	0.65
$\sigma_z$ (m) @eq	0.003
Štupakov parameter @inj. e <sup>-</sup> /e <sup>+</sup>	<b>0.22/0.0001</b>
$\rho/b$ @inj. e <sup>-</sup> /e <sup>+</sup>	0.73
$0.5\rho\Lambda^{-3/2}$ (m) @inj. e <sup>-</sup> /e <sup>+</sup>	33.8/>>
$\sigma_z$ (m) @inj. e <sup>-</sup> /e <sup>+</sup>	0.001/0.0034

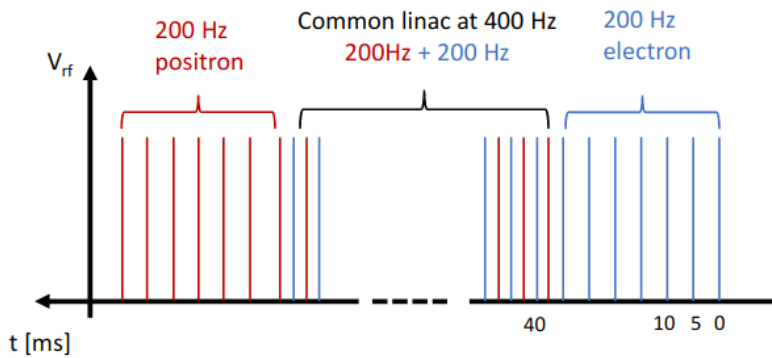
# Injection/Extraction timing scheme

# Injector current general layout

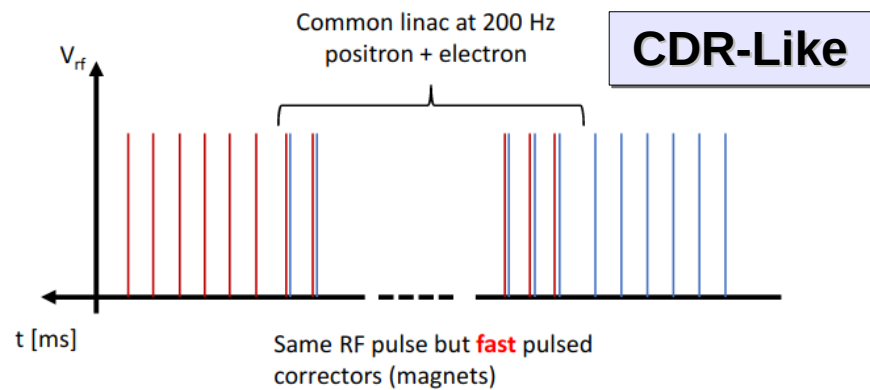


**NEW**

Common linac: repetition rate 1



Common linac: repetition rate 2



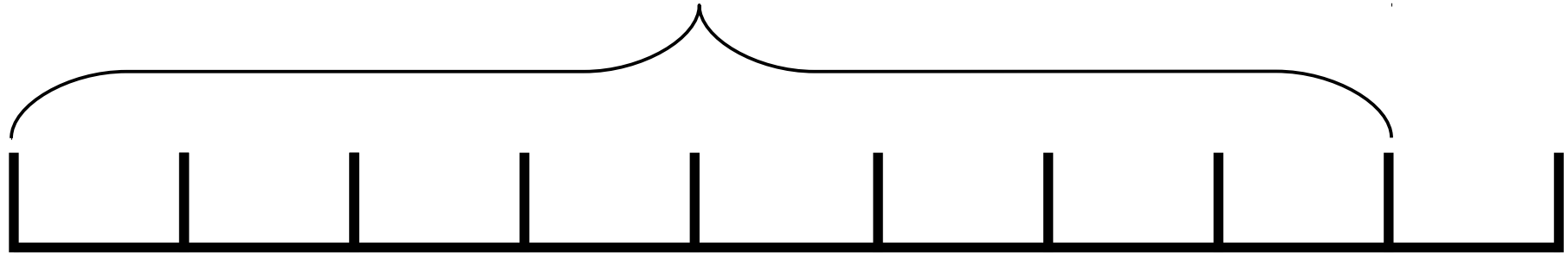
New baseline for FCC\_ee Injector complex is under evaluation.

In the current scheme two low energy linac's are used for electron and positron and only the high energy linac is common.

DR should allow to damp the beam and delay extraction to allow single species operations for the common linac.

# Timing: DR Injection

$N_p$  LINAC pulse (2 bunch per pulse) stored in DR



#pls	0	1	2	3	4	[...]			np-1	np
#bkt	0	$\Delta b$	$2\Delta b$	$3\Delta b$	[...]				$0=h$	$\Delta b$

$\Delta_b = INT[h/N_p]$  Space between first bunch for each pulse

$$T_{gun} = iT_1 + \Delta_b T_{RF} (i \% np)$$

Gun has been phased with DR RF so that the "first" gun pulse arrives at the DR in the #bkt=0

$$\Delta T_{DR} = (N_p - 1)T_1 \geq m\tau_{x/y}$$

Store time

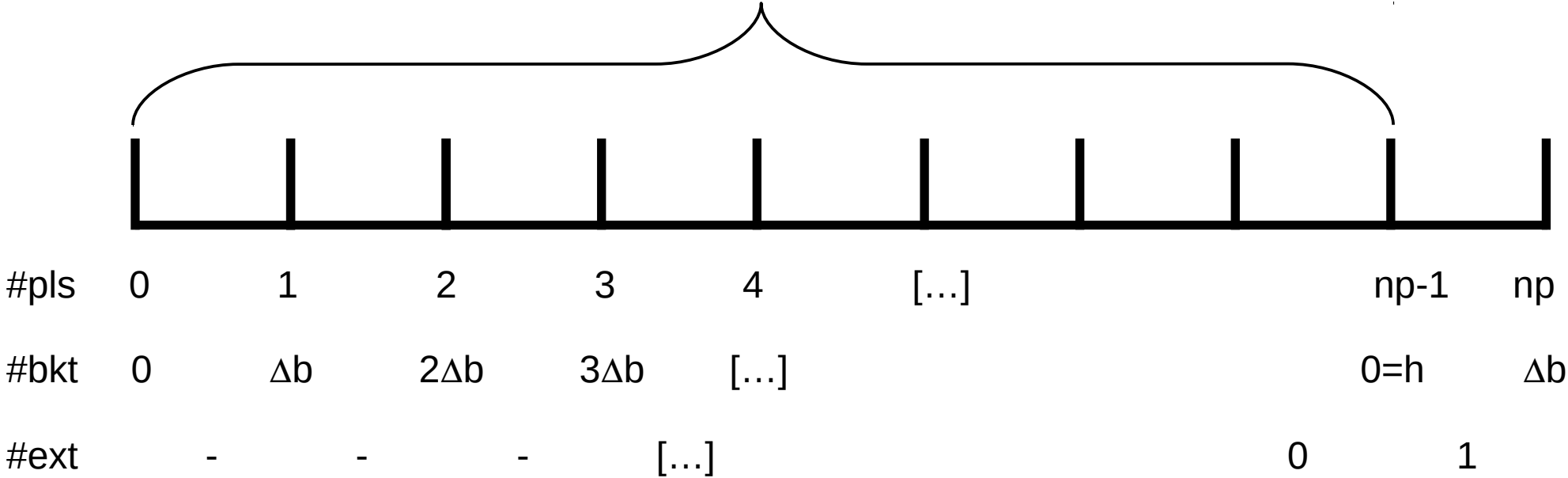
To store for at least 4 damping times

$$N_p \geq 9 \quad \Rightarrow \quad \Delta_b \leq 35$$

$$h \% N_p \neq 0 \Rightarrow \Delta_b \equiv \Delta_b(i)$$

With  $\Delta_b = 35$  the last filled bucket is the 281<sup>st</sup> 38 bucket before the 319<sup>th</sup>

# Timing: DR Extraction



$$T_{EXT} = T_{gun} + \Delta T_{DR} + T_S/2 + T_2 - \Delta T_{12}$$

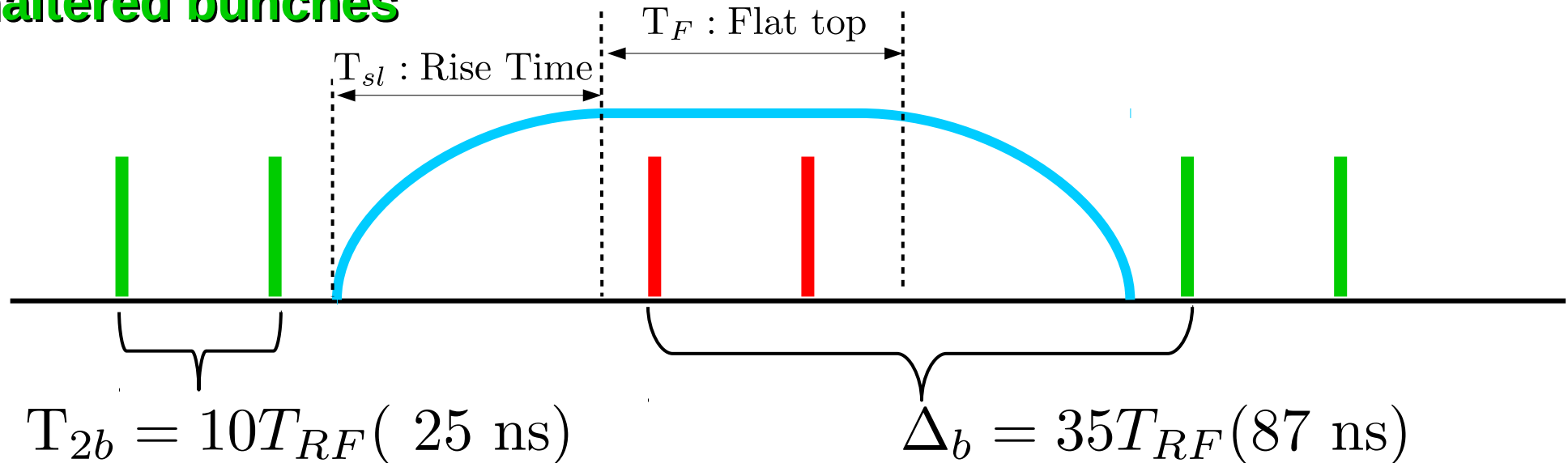
Arrival + Storage time

Half turn to reach the extraction section

Phasing with “empty” L2 pulses.  
 $\Delta_{12}$  accounts for propagation time from DR to L2  
 Time is measured in  $T_S$  units

# Timing: Extraction kickers details

## Unaltered bunches



## Kicked bunches

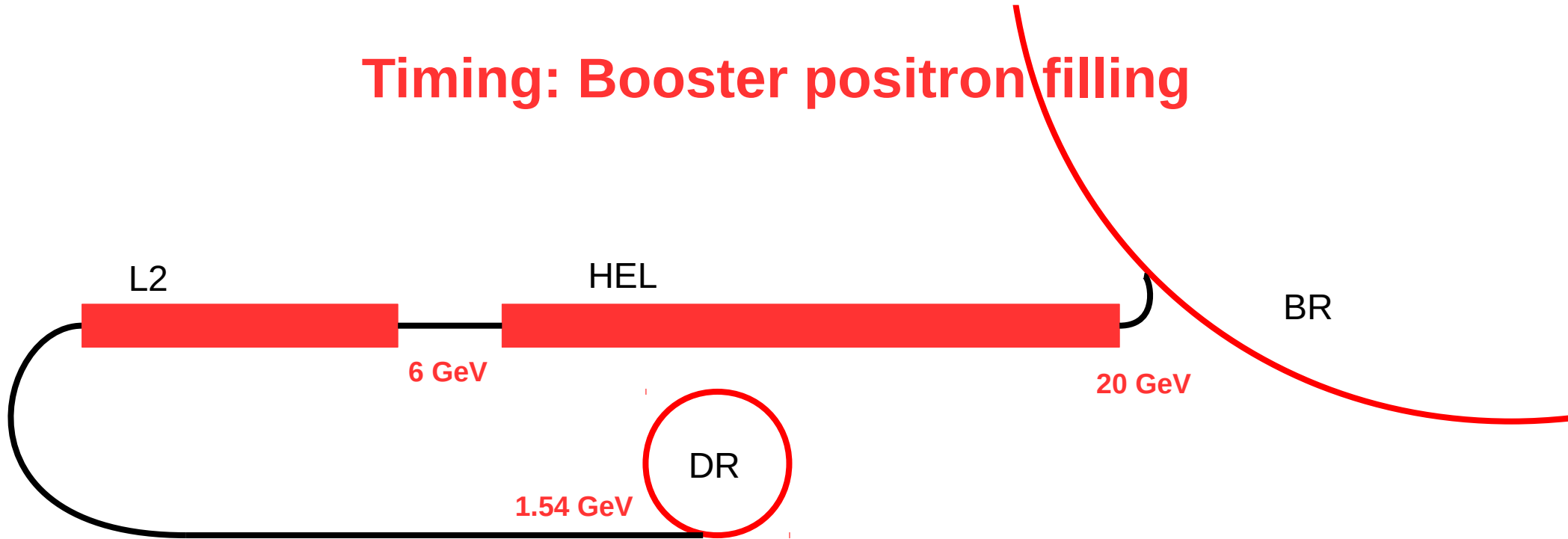
Time differences between the two bunches of the same pulse (25 ns) and between different pulses stored (87.5 ns) has the following implications on kickers pulses:

$$T_{sl} + T_F \leq 35T_{RF} \quad \wedge \quad T_F \geq T_{2b}$$

$$T_{sl} \leq 62 \text{ ns} \quad T_F \geq T_{2b} = 25 \text{ ns}$$

Reasonable values could be:  $T_{sl} = 50 \text{ ns}$  and  $T_F = 30 \text{ ns}$

# Timing: Booster positron filling



$\Delta T_{DB}$  : Time from DR to BR

$T_S^D$  : DR Revolution period:  $\sim 1 \mu\text{s}$

$T_S^B$  : BR Revolution period:  $\sim 300 \mu\text{s}$

Extracting from the DR at the “nominal” delay time of 42.5 ms will fill, conventionally, the bunch “0” (actually the first pair of buckets).

Varying the turn of extraction allows to fill other buckets.

The homogeneous filling of the BR with all the 10k bunch at Z pole could require large time difference in extraction.

The impact on the common LINAC have to be considered.



# Summary/Conclusions

## DR Longitudinal acceptance

- RF requirements to allow largest energy acceptance have been evaluated. Assuming SC RF cavity, two cells are needed.
- Large energy acceptance imply short bunch length. Potential issue

## DR Dynamical aperture:

- Tracking has been performed with PTC
- **The maximal aperture is 3.5 sigma of the injected beam**
- At the nominal injected beam emittance (CDR) a reduction of 50% is expected

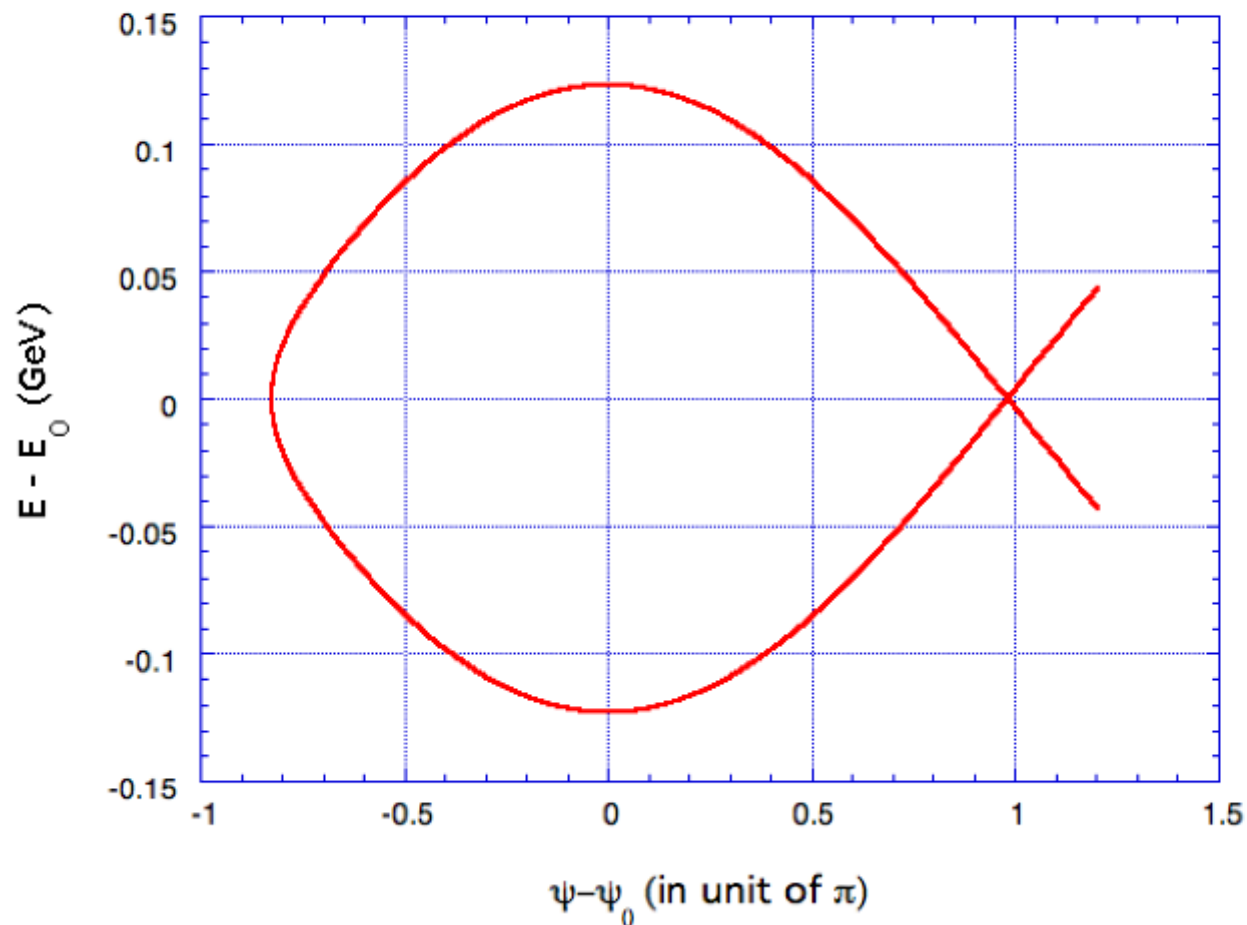
## Timing:

- DR filling scheme allows to have extracted pulses after 42.5 ns.
- The scheme of L2 at 400 Hz Rep Rate is feasible
- Tunability of L1 effective repetition rate is requested to be within  $0.8 \mu\text{s}$   $O(10^{-4})$
- Tunability of L2 effective repetition rate is requested to be at least  $150 \mu\text{s}$
- DR KCK's time requirement have been defined and seems not prohibitive

# SPARES

# Separatrix

$\Delta E - \Delta\Psi$  representation



$$\alpha_c = 0.001535$$

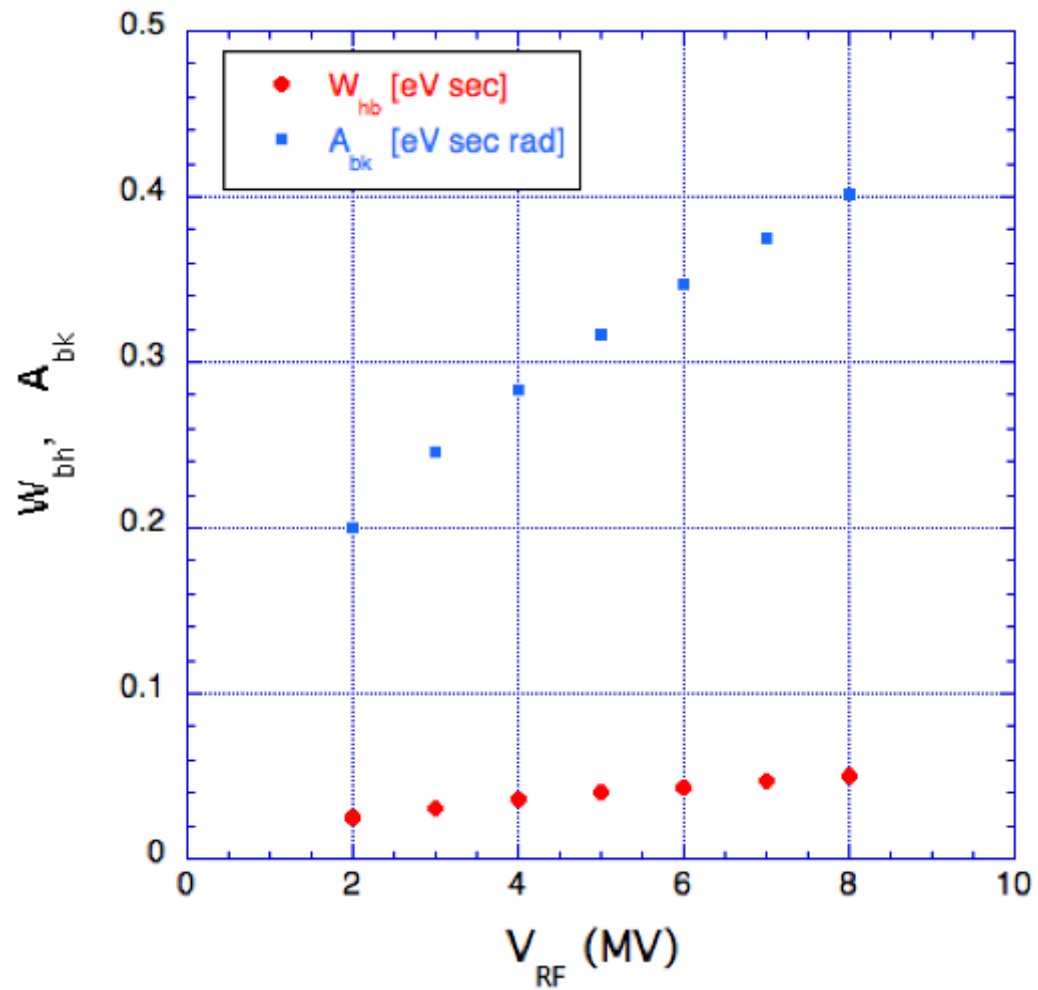
$$h = 319$$

$$V = 8 \text{ MV}$$

$$E_s = 1.54 \text{ GeV}$$

$$\varphi_s = 0.028 \text{ rad}$$

# Separatrix vs. VRF



## Timing: Some definitions

$R_1(T_1)$  : Repetition rate (Period) L1: 200 Hz

$R_2(T_2)$  : Repetition rate (Period) L2: 400 Hz

$RF(T_{RF})$  : DR Radio Frequency (RF Period): 400 MHz

$\Delta T_{ep}$  : Delay between Electron Gun and DR injection

$T_S$  : DR Revolution period:  $\sim 0.8 \mu s$

h: DR harmonic number: 319

$N_p$  : Number of LINAC pulses stored (2 bunch each)

$\tau_{x/y}$  : Damping time:  $\sim 10.8$  ms

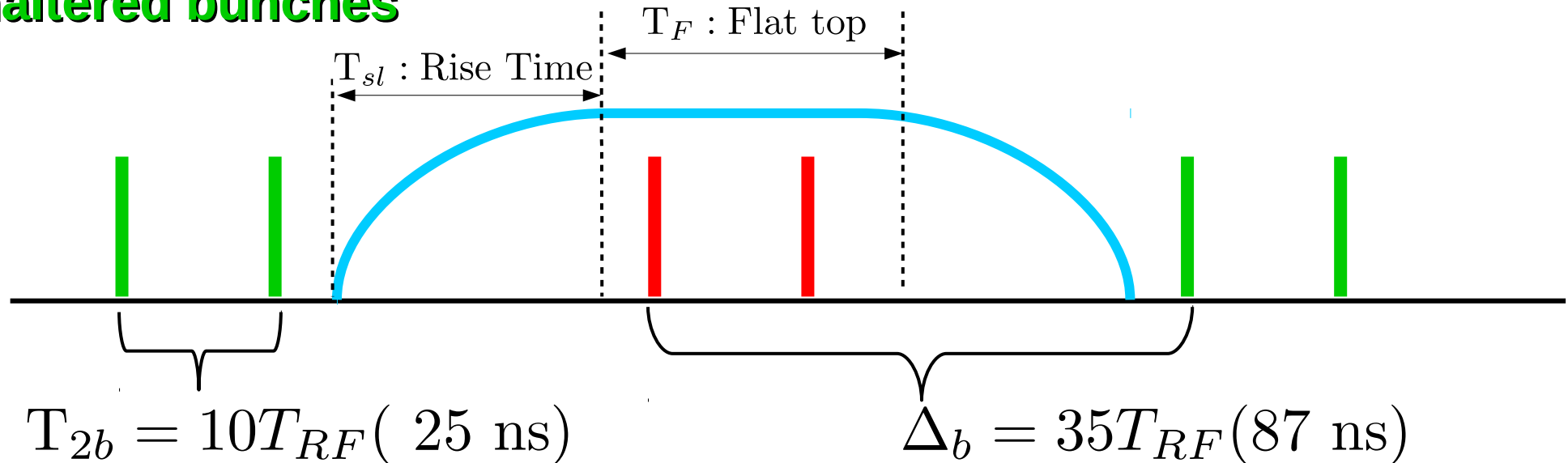
$\Delta_b$  : Number of bucket delay between first bunch for each pulse

$T_{2b}$  : Time difference between two bunch in the same pulse

The number of stored pulses depends on the time needed to damp the incoming positron beam.

# Timing: Extraction kickers details

## Unaltered bunches



## Kicked bunches

Time differences between the two bunches of the same pulse (25 ns) and between different pulses stored (87.5 ns) has the following implications on kickers pulses:

$$T_{sl} + T_F \leq 35T_{RF} \quad \wedge \quad T_F \geq T_{2b}$$

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