

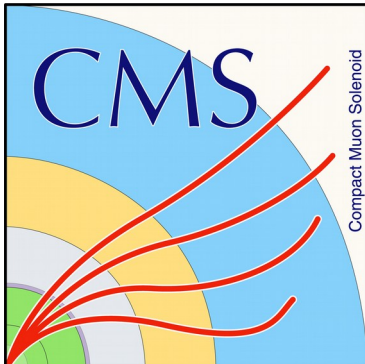
Higgs mass, width and CP @ CMS

Higgs Hunting
Sept 11th 2023



Savvas Kyriacou

On behalf of the
CMS collaboration



JOHNS HOPKINS
UNIVERSITY

Higgs properties

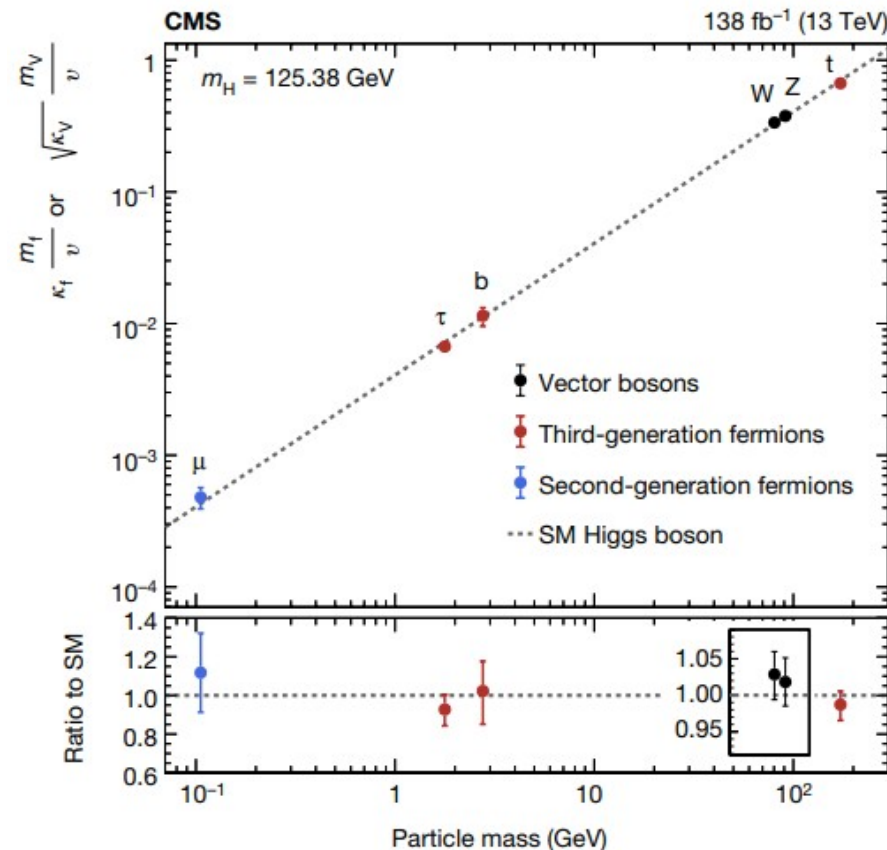
10+1 years since Higgs discovery
@LHC

> Characterize and measure in high precision the boson properties

> Mass

> Width

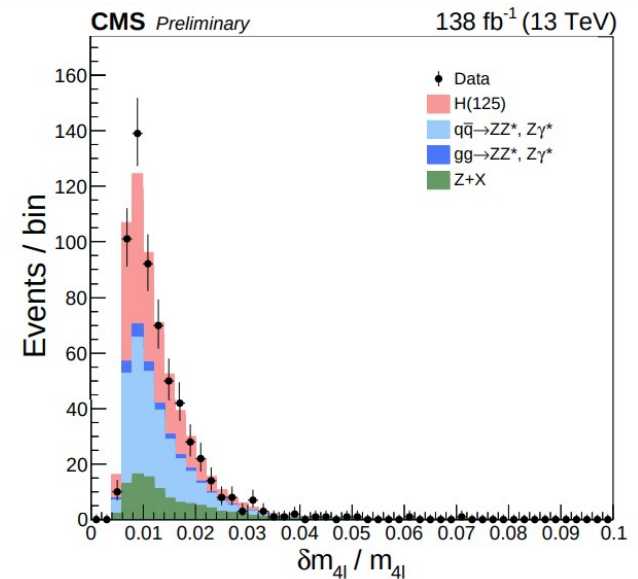
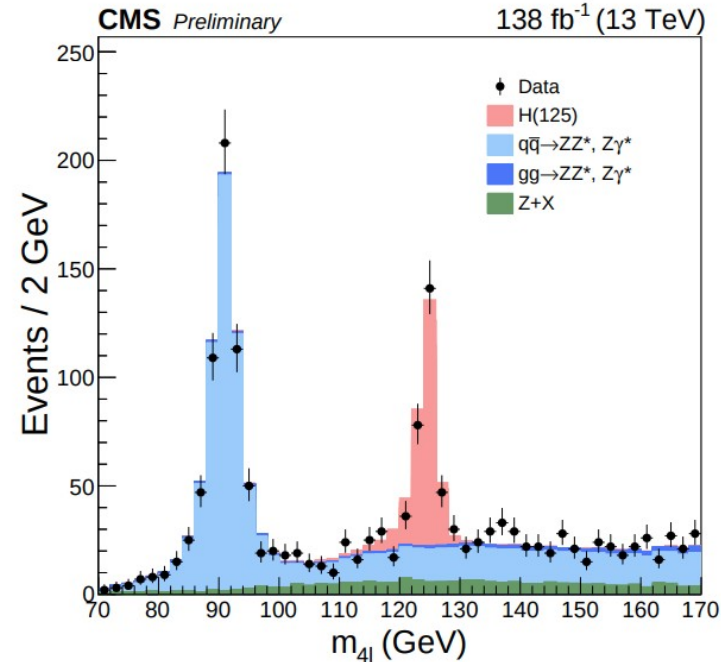
> CP structure of couplings



Mass

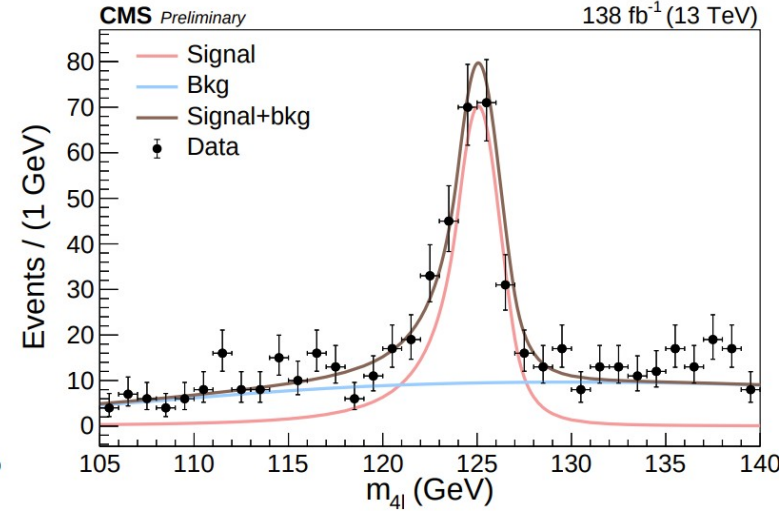
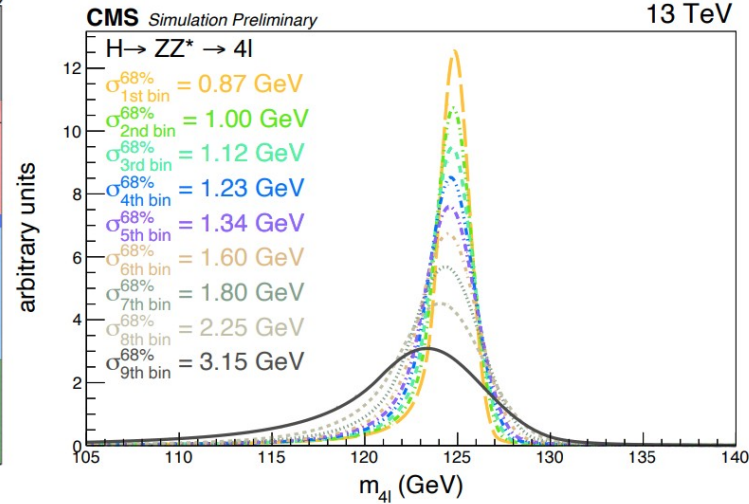
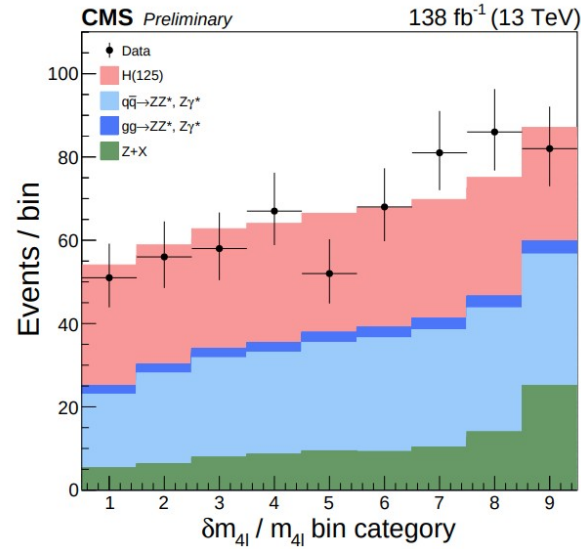
NEW!

- Full Run 2 $H \rightarrow 4l$
- $105 < m_H < 140 \text{ GeV}$
- Measurement improvements
 - Lepton VTXS constrain and BS compatibility
 - Categorize events based on $\delta m_{4l}/m_{4l}$
 - Improve estimates on lepton uncertainties using on-shell Z
 - Improved detector calibration

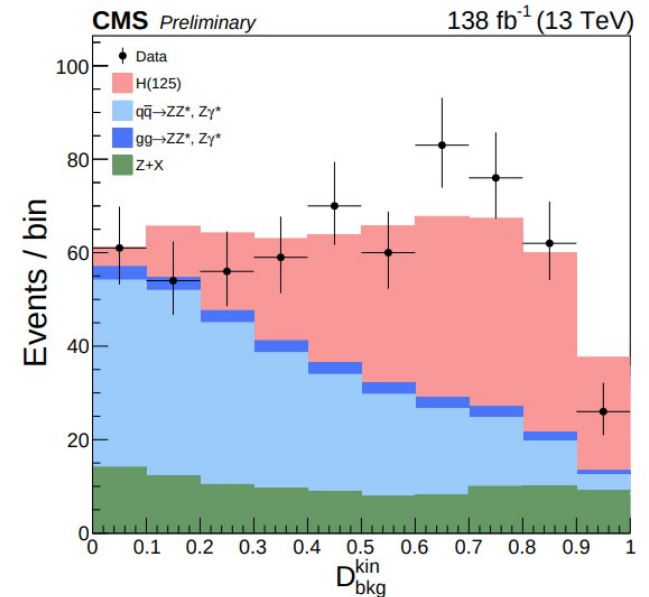


HIG-21-019
(link)

Mass



- 9 resolution-based categories
- Construct m_{4l} line-shape DSCB + Landau
- 9 x 2D fit (m_{4l} , \mathcal{D}_{bkg}^{kin})

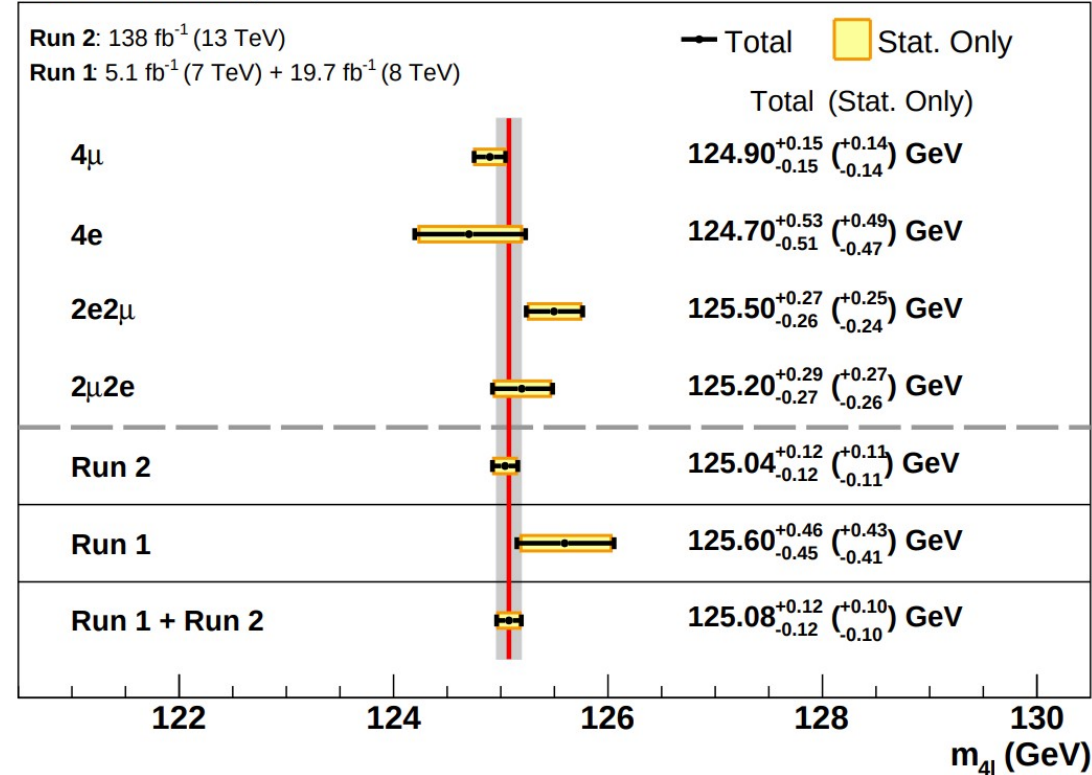


Mass

NEW!

- Combine results with Run 1
- Result statistically limited
- Most precise single channel measurement to date!

CMS Preliminary



$m_H = 125.08 \pm 0.10_{\text{stat}} \pm 0.05_{\text{syst}}$ (GeV)

Higgs Width - on-shell measurement

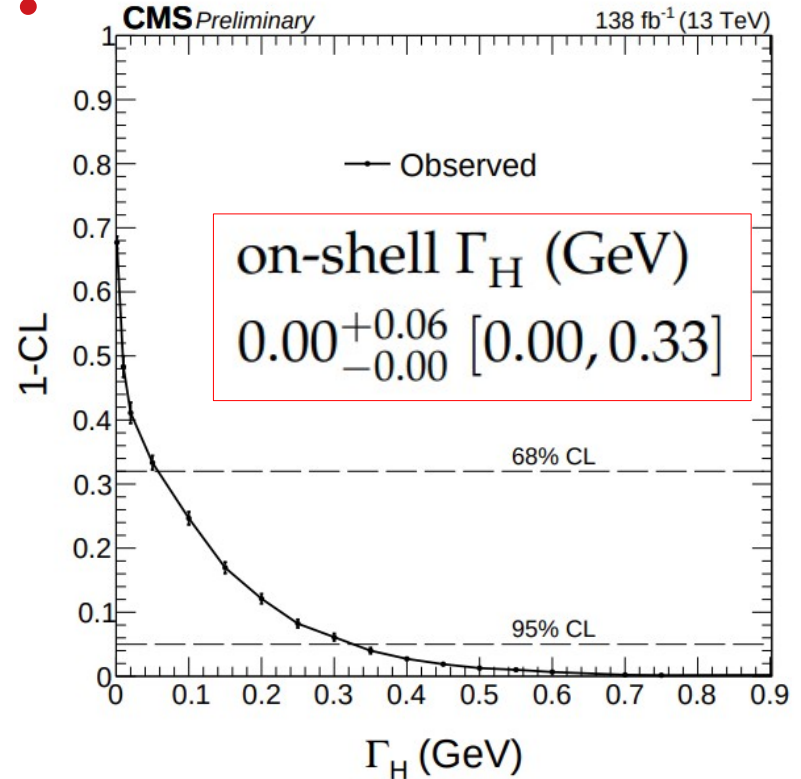
HIG-21-019
(link)



- SM: given $m_H \rightarrow \Gamma_H$ can be calculated
- Measure Higgs width
 - Test of Higgs \rightarrow SM particles
 - A test/complimentary for $H \rightarrow$ invisible particles
- Techniques:
 - **Using the onshell region (mass pole shape)**
 - Using signal strength in on-shell and off-shell production

$$\Gamma_H^{\text{SM}} = 4.1 \text{ MeV}$$

NEW!



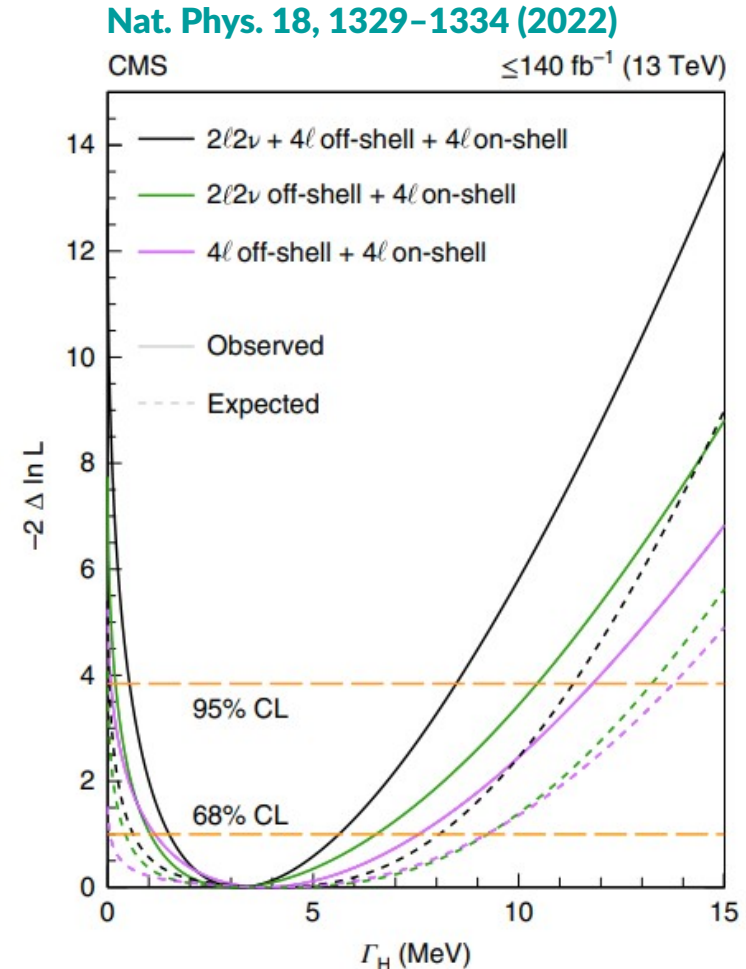
- > Convolute (DSCB + Laundau) x Breit-Wigner
- > Fit m4l line shape
- > measurement **limited by detector resolution**

Higgs Width – off-shell method

- Measure Higgs width:
 - test of Higgs on-shell vs off-shell production
 - test of Higgs \rightarrow SM particles
 - A test/complimentary for $H \rightarrow$ invisible particles
- Techniques:
 - Using the onshell region (mass pole shape)
 - **Using signal strength in on-shell and off-shell production**

$$\Gamma_H^{\text{SM}} = 4.1 \text{ MeV}$$

$$\frac{\sigma_{vv \rightarrow H \rightarrow 4\ell}^{\text{off-shell}}}{\sigma_{vv \rightarrow H \rightarrow 4\ell}^{\text{on-shell}}} \propto \Gamma_H$$

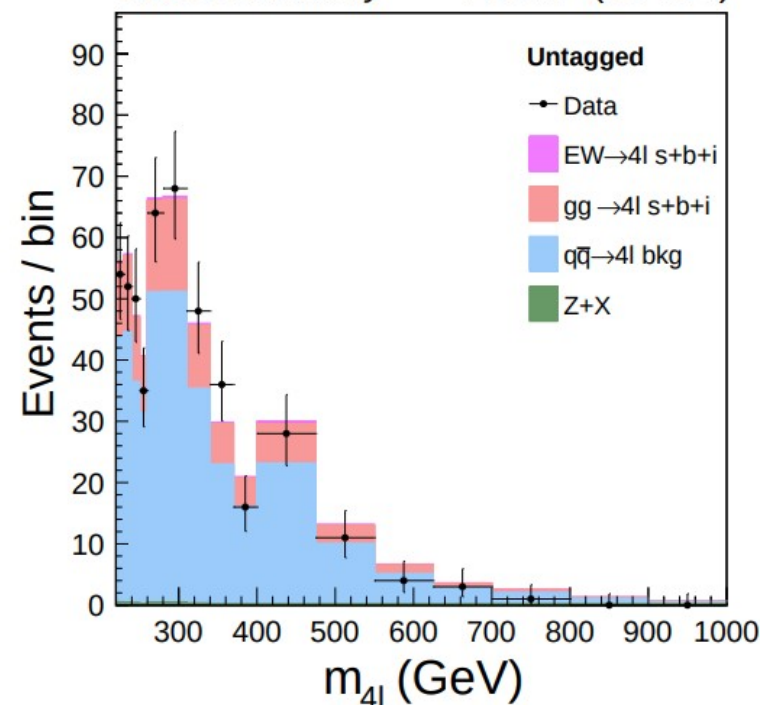


Higgs width - off-shell method

NEW!

- Analyze Full Run2 H→4l
- Select events in H→ ZZ→4l with m4l > 220GeV
- 3 exclusive categories:
 - VBF-tagged
 - VH-tagged Allows measuring μV, μF off-shell
 - Untagged
- Perform template fit and likelihood
- Negative S B interference

CMS Preliminary 138 fb⁻¹ (13 TeV)



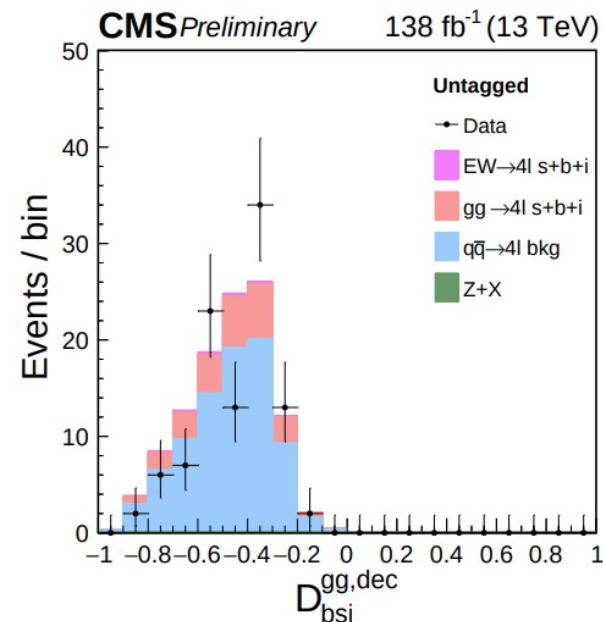
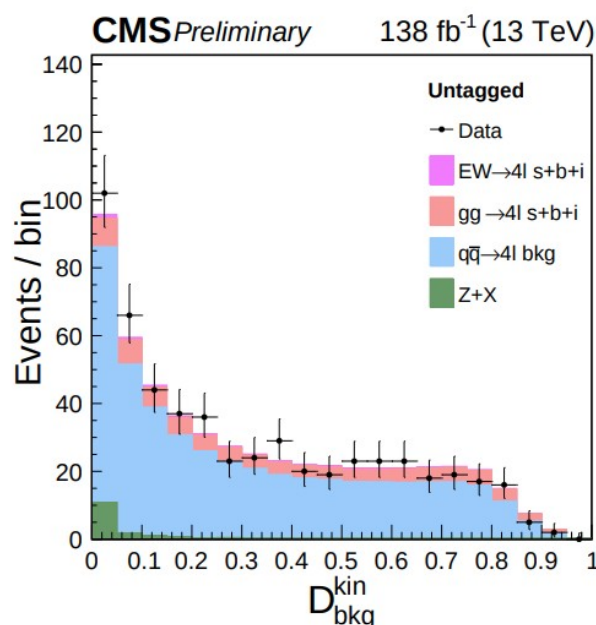
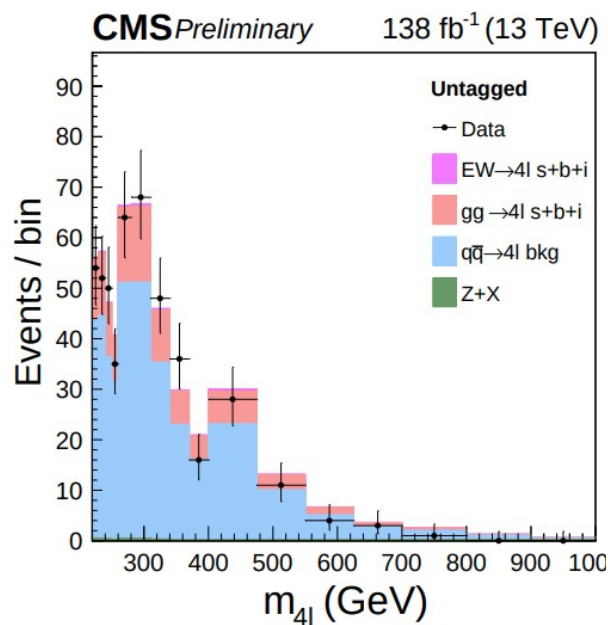
on-shell:

$$\mathcal{P}_{jk}(\vec{x}; \vec{\zeta}_{jk}, \vec{\zeta}) = \mu_j \mathcal{P}_{jk}^{\text{sig}}(\vec{x}; \vec{\zeta}_{jk}) + \mathcal{P}_{jk}^{\text{bkg}}(\vec{x}; \vec{\zeta}_{jk})$$

off-shell:

$$\mathcal{P}_{jk}(\vec{x}; \vec{\zeta}_{jk}, \vec{\zeta}) = \frac{\mu_j \Gamma_H}{\Gamma_0} \mathcal{P}_{jk}^{\text{sig}}(\vec{x}; \vec{\zeta}_{jk}) + \sqrt{\frac{\mu_j \Gamma_H}{\Gamma_0}} \mathcal{P}_{jk}^{\text{int}}(\vec{x}; \vec{\zeta}_{jk}) + \mu_j \mathcal{P}_{jk}^{\text{cross}}(\vec{x}; \vec{\zeta}_{jk}) + \mathcal{P}_{jk}^{\text{bkg}}(\vec{x}; \vec{\zeta}_{jk})$$

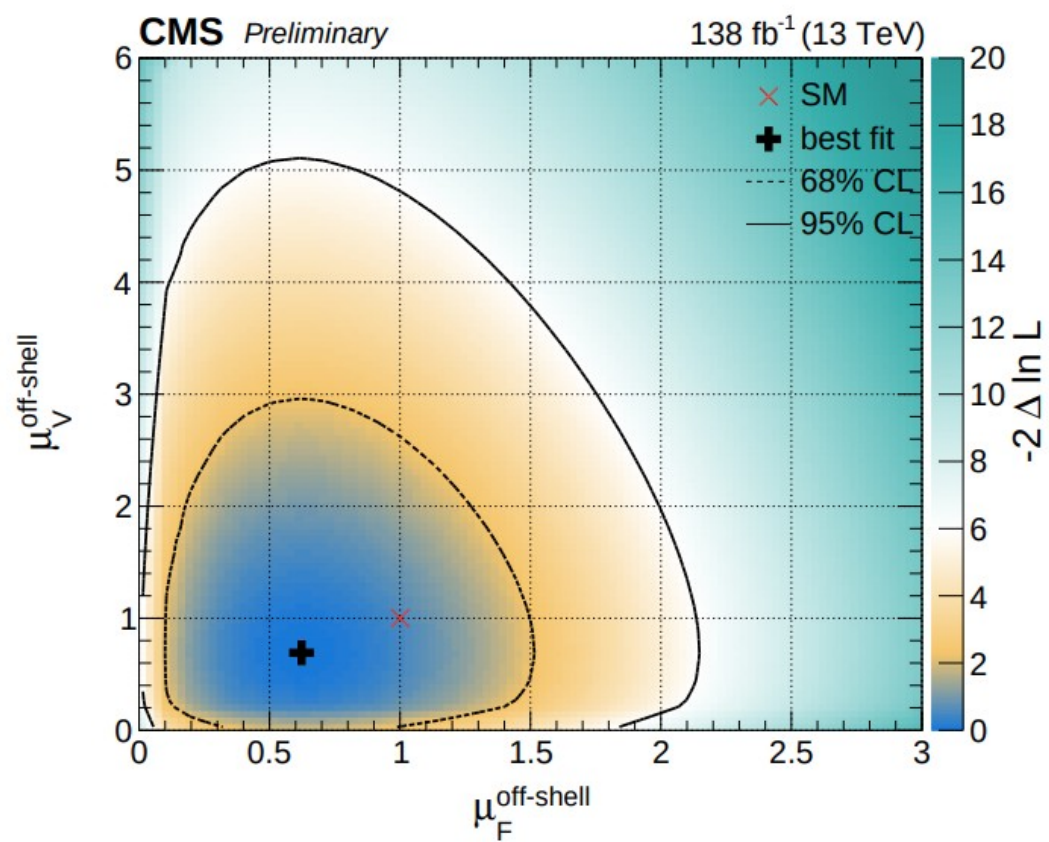
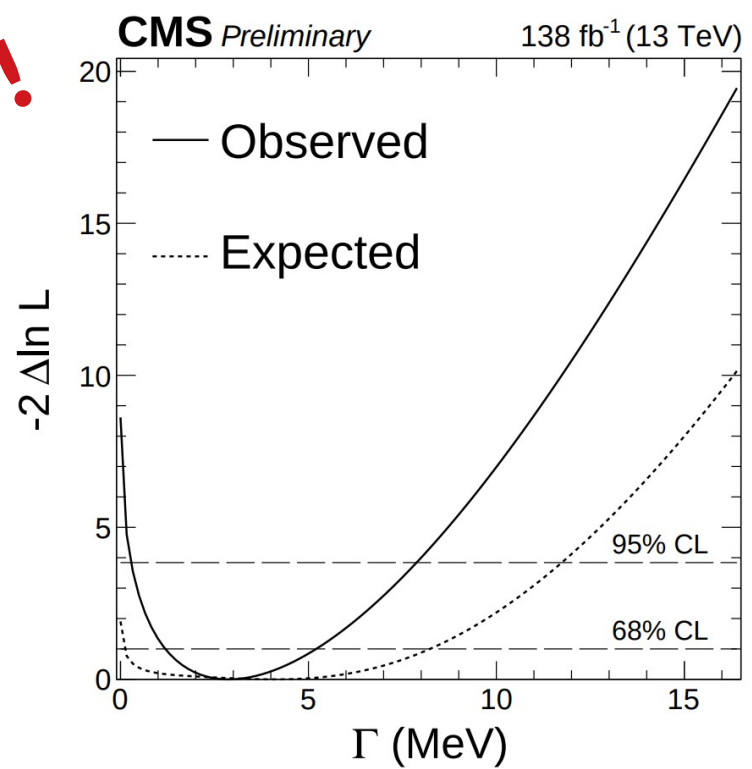
Higgs width - off-shell method



- **Observables:**
M4L + 2 discriminants:
- Measurement is statistically limited
- Main uncertainties related to dominant backgrounds
 - k-factor uncertainties

Higgs width - off-shell method

NEW!



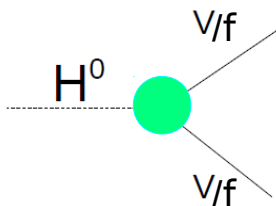
Parameter	Observed	Expected
$\mu^{\text{off-shell}}$	$0.64^{+0.50}_{-0.37}$ [0.06, 1.69]	$1.00^{+0.99}_{-0.97}$ [0.00, 2.80]
$\mu_F^{\text{off-shell}}$	$0.62^{+0.57}_{-0.41}$ [0.03, 1.81]	$1.00^{+1.05}_{-1.00}$ [0.00, 2.93]
$\mu_V^{\text{off-shell}}$	$0.69^{+1.32}_{-0.63}$ [0.00, 3.91]	$1.00^{+3.34}_{-1.00}$ [0.00, 7.65]

Full Run2 H→4l

$$\Gamma_H \text{ (MeV)} = 2.9^{+2.3}_{-1.7} [0.3, 7.9]$$

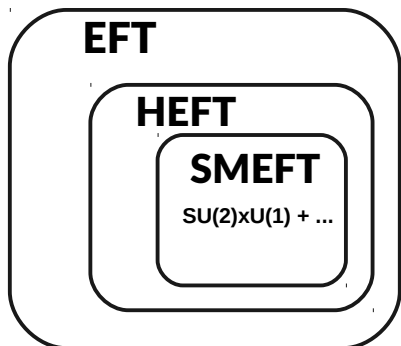
CP - AC measurements

- Study Higgs Couplings:
 - Uncover CPV in Higgs sector
 - Uncover BSM phenomena



- Dedicated measurements
 - Targeted analysis
 - Dedicated sensitive observables to specific couplings
 - Gen + Full Detector simulation of AC effects
(Interference effects, acceptance effects+)

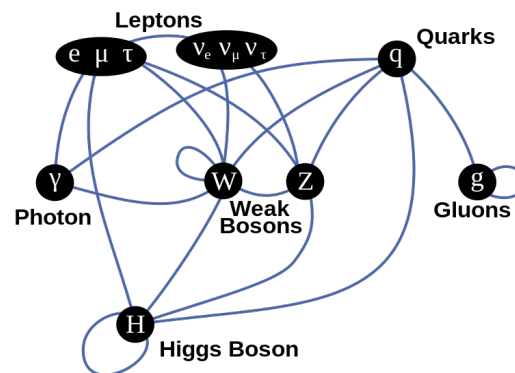
- Utilize EFT



$$\mathcal{L}_{SM} = \mathcal{L}_{SM}^{(4)} + \frac{1}{\Lambda} \sum_k C_k^{(5)} Q_k^{(5)} + \frac{1}{\Lambda^2} \sum_k C_k^{(6)} Q_k^{(6)} + \mathcal{O}\left(\frac{1}{\Lambda^3}\right)$$

Mass eigenstate basis + symmetries → **Higgs basis**

Weak eigenstate basis : **Warsaw basis**



Interference effects **important and valuable**

$$P \propto |A^{tot}|^2$$

$$|A^{tot}|^2 = |A^{prod} \times A^{decay}|^2$$

$$= |(A_1 + A_2 + A_3) \times (B_1 + B_2 + B_3)|^2$$



EFT – basis

Mass eigenstate → Higgs basis

$$A(\text{HVV}) = \frac{1}{v} \left[a_1^{\text{VV}} + \frac{\kappa_1^{\text{VV}} q_{V1}^2 + \kappa_2^{\text{VV}} q_{V2}^2}{(\Lambda_1^{\text{VV}})^2} + \frac{\kappa_3^{\text{VV}} (q_{V1} + q_{V2})^2}{(\Lambda_Q^{\text{VV}})^2} \right] m_{V1}^2 \epsilon_{V1}^* \epsilon_{V2}^*$$

$$+ \frac{1}{v} a_2^{\text{VV}} f_{\mu\nu}^{*(1)} f^{*(2),\mu\nu} + \frac{1}{v} a_3^{\text{VV}} f_{\mu\nu}^{*(1)} \tilde{f}^{*(2),\mu\nu}$$

$$A(\text{Hff}) = -\frac{m_f}{v} \bar{\psi}_f (\kappa_f + i \tilde{\kappa}_f \gamma_5) \psi_f$$

$V = W, Z, g, \gamma$
 $f = \text{leptons} + \text{quarks}$

Approach 1

$$g_1^{WW} = g_1^{ZZ}$$

$$g_2^{WW} = \frac{2}{c_w} g_2^{ZZ} + \frac{2}{s_w} g_2^{\gamma\gamma} + \frac{2}{s_w} c_w g_2^{Z\gamma}$$

$$g_4^{WW} = \frac{2}{c_w} g_4^{ZZ} + \frac{2}{s_w} g_4^{\gamma\gamma} + \frac{2}{s_w} c_w g_4^{Z\gamma}$$

$$\frac{\kappa_1^{WW}}{(\Lambda_1^{WW})^2} (c_w^2 - s_w^2) = \frac{\kappa_1^{ZZ}}{(\Lambda_1^{ZZ})^2} + \frac{2}{M_Z^2} \frac{g_2^{\gamma\gamma} - g_2^{ZZ}}{c_w} + 2 \frac{s_w}{c_w} (c_w^2 - s_w^2) \frac{g_2^{Z\gamma}}{M_Z^2}$$

$$\frac{\kappa_2^{Z\gamma}}{(\Lambda_1^{Z\gamma})^2} (c_w^2 - s_w^2) = \frac{2}{s_w c_w} \left(\frac{\kappa_1^{ZZ}}{(\Lambda_1^{ZZ})^2} + \frac{g_2^{\gamma\gamma} - g_2^{ZZ}}{M_Z^2} \right) + 2 (c_w^2 - s_w^2) \frac{g_2^{Z\gamma}}{M_Z^2}$$

Approach 2: SMEFT

$SU(2) \times U(1)$ + custodial sym.
 set c_w^2 to SM value

custodial sym.
 set $c_w^2 = 1$

$$g_1^{WW} = g_1^{ZZ}$$

$$g_2^{WW} = \frac{2}{c_w} g_2^{ZZ} + \frac{2}{s_w} g_2^{\gamma\gamma} + \frac{2}{s_w} c_w g_2^{Z\gamma}$$

$$g_4^{WW} = \frac{2}{c_w} g_4^{ZZ} + \frac{2}{s_w} g_4^{\gamma\gamma} + \frac{2}{s_w} c_w g_4^{Z\gamma}$$

$$\frac{\kappa_1^{WW}}{(\Lambda_1^{WW})^2} (c_w^2 - s_w^2) = \frac{\kappa_1^{ZZ}}{(\Lambda_1^{ZZ})^2} + 2 s_w^2 \frac{g_2^{\gamma\gamma} - g_2^{ZZ}}{M_Z^2} + 2 \frac{s_w}{c_w} (c_w^2 - s_w^2) \frac{g_2^{Z\gamma}}{M_Z^2}$$

$$\frac{\kappa_2^{Z\gamma}}{(\Lambda_1^{Z\gamma})^2} (c_w^2 - s_w^2) = 2 s_w c_w \left(\frac{\kappa_1^{ZZ}}{(\Lambda_1^{ZZ})^2} + \frac{g_2^{\gamma\gamma} - g_2^{ZZ}}{M_Z^2} \right) + 2 (c_w^2 - s_w^2) \frac{g_2^{Z\gamma}}{M_Z^2}$$

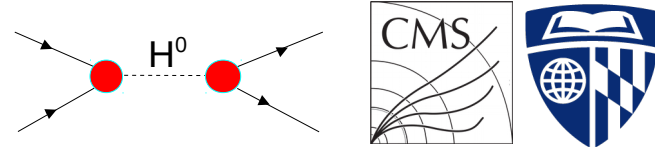
- Natural choice for Higgs couplings
- Less operators

Weak eigenstate: Warsaw basis

- More general - used in EW TOP and Higgs sector
- SMEFT build in ($SU(2) \times U(1)$)
- Has many more dim 6 operators

Rotations between basis feasible and demonstrated in measurements !

HVV: $H \rightarrow 4l$

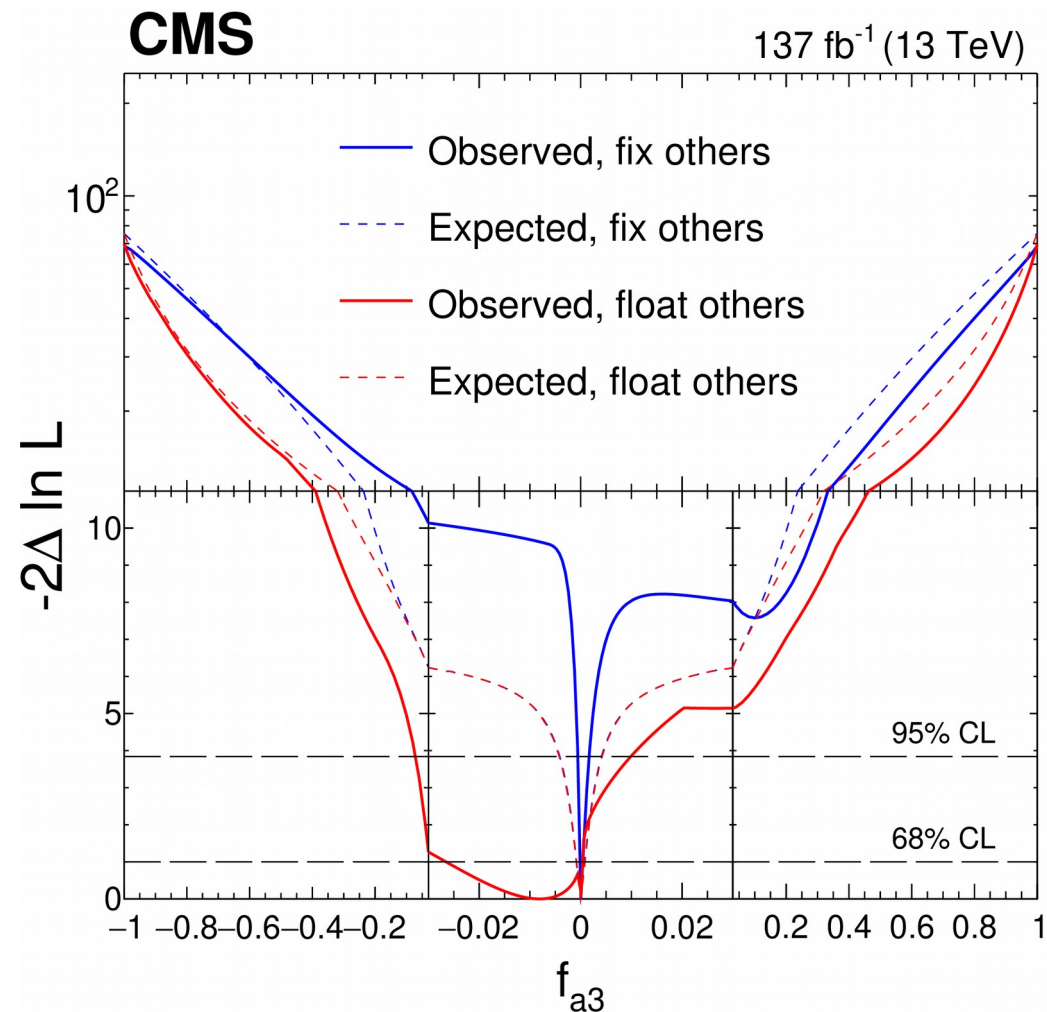
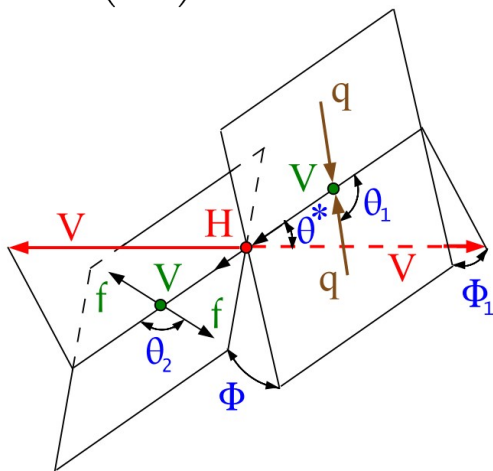


PhysRevD.104.052004

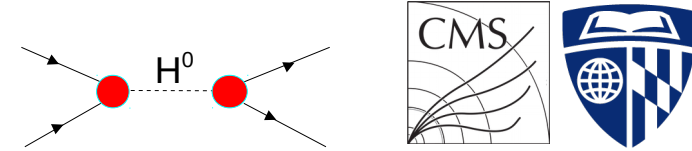
- $2e2\mu, 4e, 4\mu$
- $105 < m_{4l} < 140$ GeV + 6 categories targeting prod. modes.
- Approach 1 with 4 independent A.C. + SM
- Simultaneous scan of all AC considered
- Non-zero minima
- **SM consistent**

Effective fractional xsec:

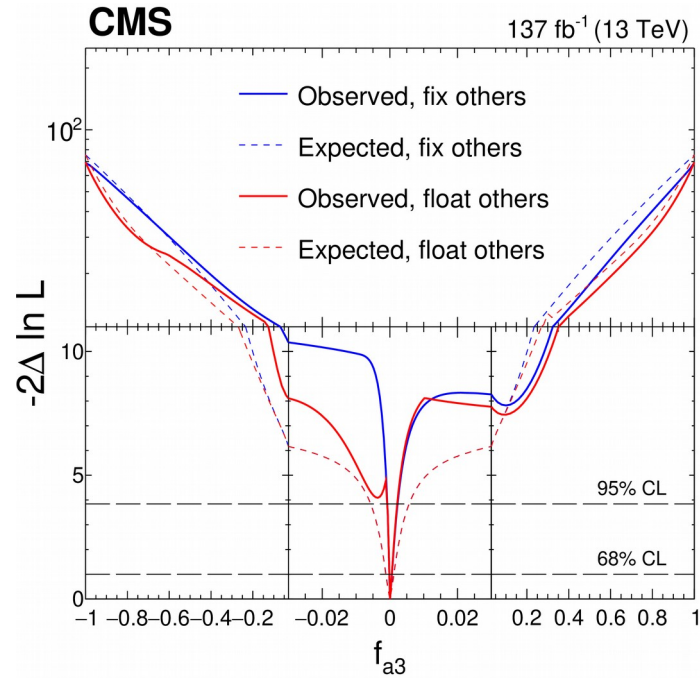
$$f_{ai}^{VV} = \frac{|a_i^{VV}|^2 \alpha_{ii}^{(\text{dec})}}{\sum_j |a_j^{VV}|^2 \alpha_{jj}^{(\text{dec})}} \text{sign} \left(\frac{a_i^{VV}}{a_1} \right)$$



HVV: $H \rightarrow 4l$

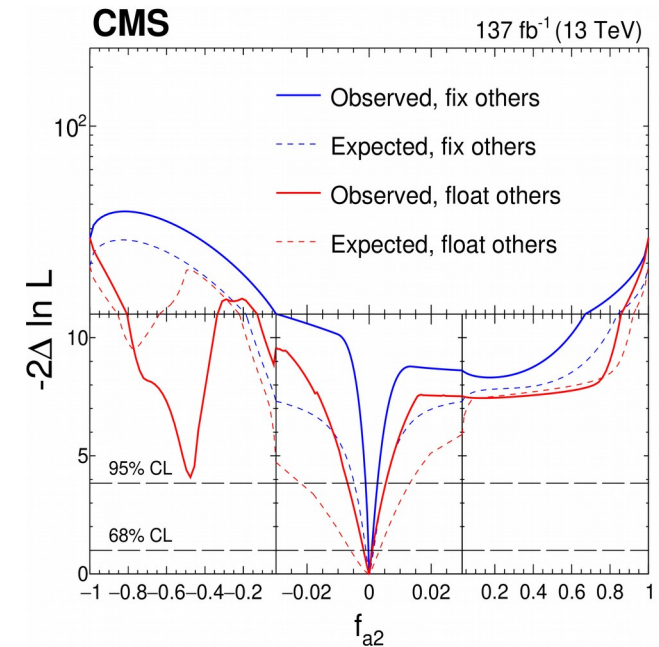


PhysRevD.104.052004

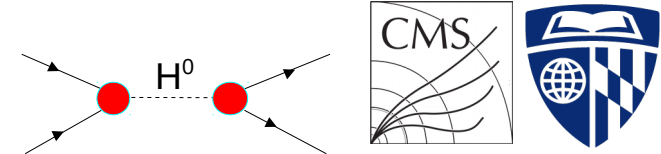


- $SU(2) \times U(1)$ sym. (SMEFT) with only 3 independent A.C.
- **Stringent constraints driven by production information**
- **Full Run2**
- **Minima consistent with SM**

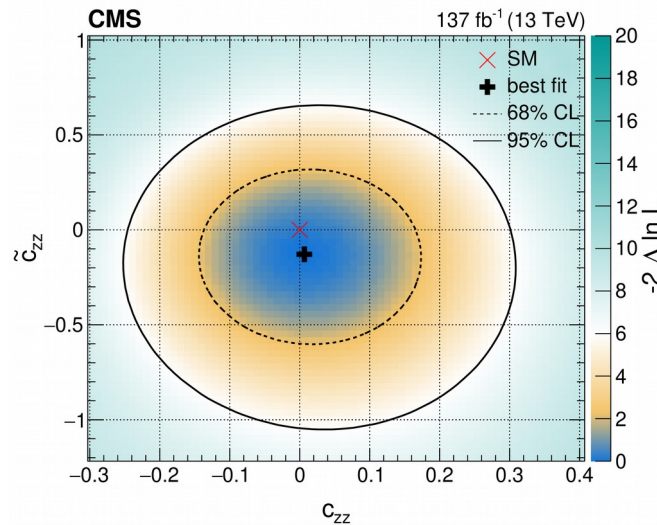
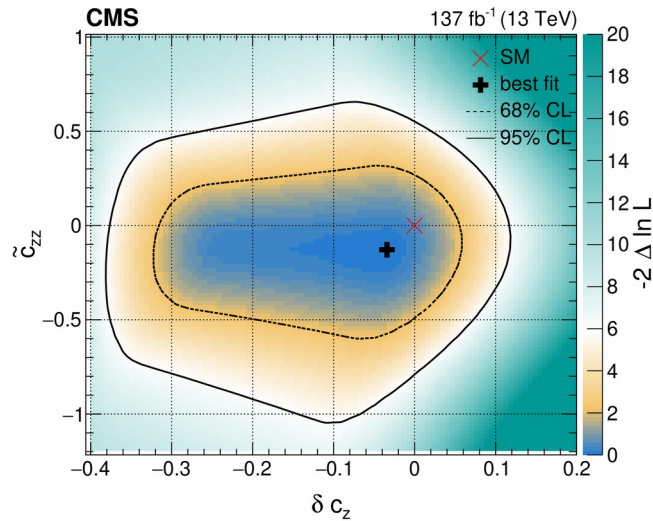
Parameter	Scenario	Observed	Expected	
f_{a3}	Approach 1	best fit	0.00004	0.00000
	$f_{a2} = f_{\Delta 1} = f_{\Delta 1}^{Z\gamma} = 0$	68% CL	$[-0.00007, 0.00044]$	$[-0.00081, 0.00081]$
		95% CL	$[-0.00055, 0.00168]$	$[-0.00412, 0.00412]$
	Approach 1	best fit	-0.00805	0.00000
	float $f_{a2}, f_{\Delta 1}, f_{\Delta 1}^{Z\gamma}$	68% CL	$[-0.02656, 0.00034]$	$[-0.00086, 0.00086]$
		95% CL	$[-0.07191, 0.00990]$	$[-0.00423, 0.00422]$
Approach 2	best fit	0.00005	0.0000	
	float $f_{a2}, f_{\Delta 1}$	68% CL	$[-0.00010, 0.00061]$	$[-0.0012, 0.0012]$
		95% CL	$[-0.00072, 0.00218]$	$[-0.0057, 0.0057]$



HVV: $H \rightarrow 4\ell$

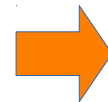


PhysRevD.104.052004



Translated to Warsaw basis:

Channels	Coupling	Observed
VBF & VH & $H \rightarrow 4\ell$	δc_z	$-0.03^{+0.06}_{-0.25}$
	c_{zz}	$0.01^{+0.11}_{-0.10}$
	$c_{z\Box}$	$-0.02^{+0.04}_{-0.04}$
	\tilde{c}_{zz}	$-0.11^{+0.30}_{-0.31}$

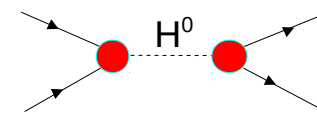


Channels	Coupling	Observed	Expected
VBF & VH & $H \rightarrow 4\ell$	$c_{H\Box}$	$0.04^{+0.43}_{-0.45}$	$0.00^{+0.75}_{-0.93}$
	c_{HD}	$-0.73^{+0.97}_{-4.21}$	$0.00^{+1.06}_{-4.60}$
	c_{HW}	$0.01^{+0.18}_{-0.17}$	$0.00^{+0.39}_{-0.28}$
	c_{HWB}	$0.01^{+0.20}_{-0.18}$	$0.00^{+0.42}_{-0.31}$
	c_{HB}	$0.00^{+0.05}_{-0.05}$	$0.00^{+0.03}_{-0.08}$
	$c_{H\tilde{W}}$	$-0.23^{+0.51}_{-0.52}$	$0.00^{+1.11}_{-1.11}$
	$c_{H\tilde{W}B}$	$-0.25^{+0.56}_{-0.57}$	$0.00^{+1.21}_{-1.21}$
	$c_{H\tilde{B}}$	$-0.06^{+0.15}_{-0.16}$	$0.00^{+0.33}_{-0.33}$

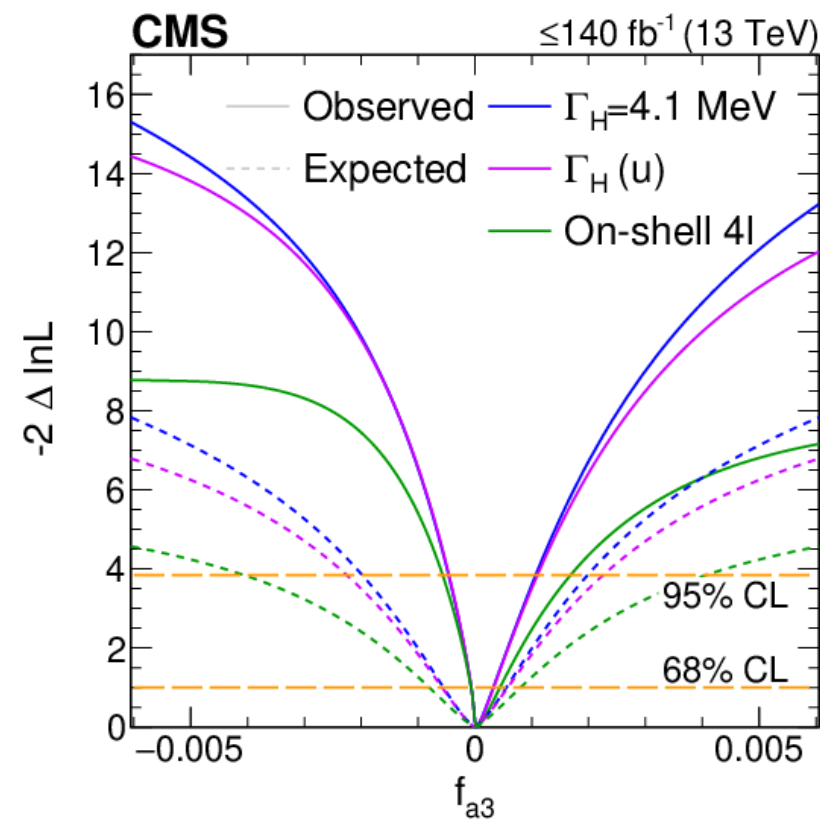
Off-shell studies in $H \rightarrow 4l + 2l2\nu$



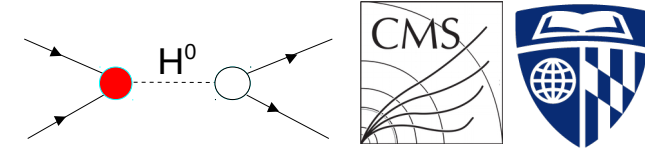
Nat. Phys. 18, 1329–1334 (2022)



- Use same formalism as on-shell $H \rightarrow 4l$ AC analysis
- $M_{4l} > 220$ GeV (2e2μ, 4e, 4μ)
- Design categories targeting ggF + EW production of the Higgs
- Use ME based observables + m_{4l}
- Consider 1 AC at a time
- Constrain Higgs width + AC
- Combine with $H \rightarrow ZZ \rightarrow 2l2\nu$

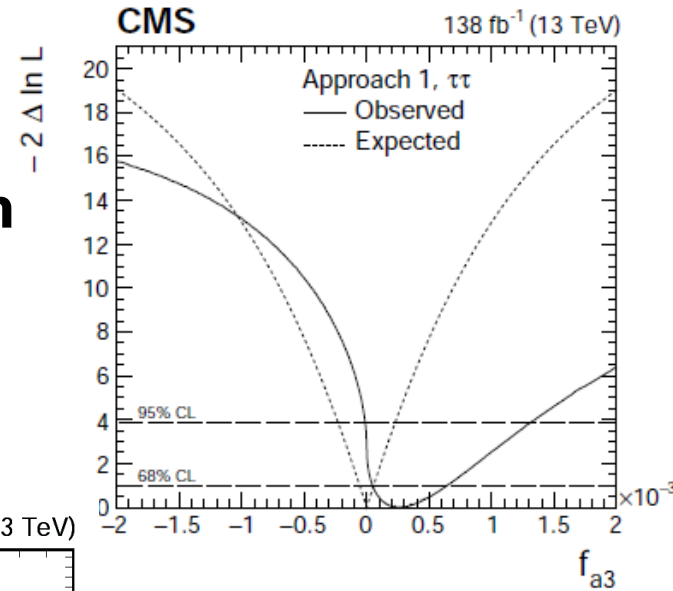


HVV: $H \rightarrow \tau\tau + H \rightarrow 4l$

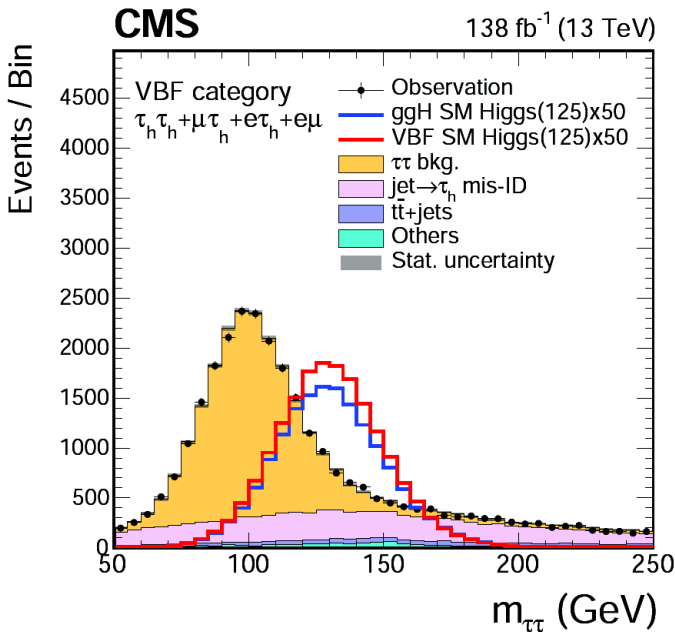
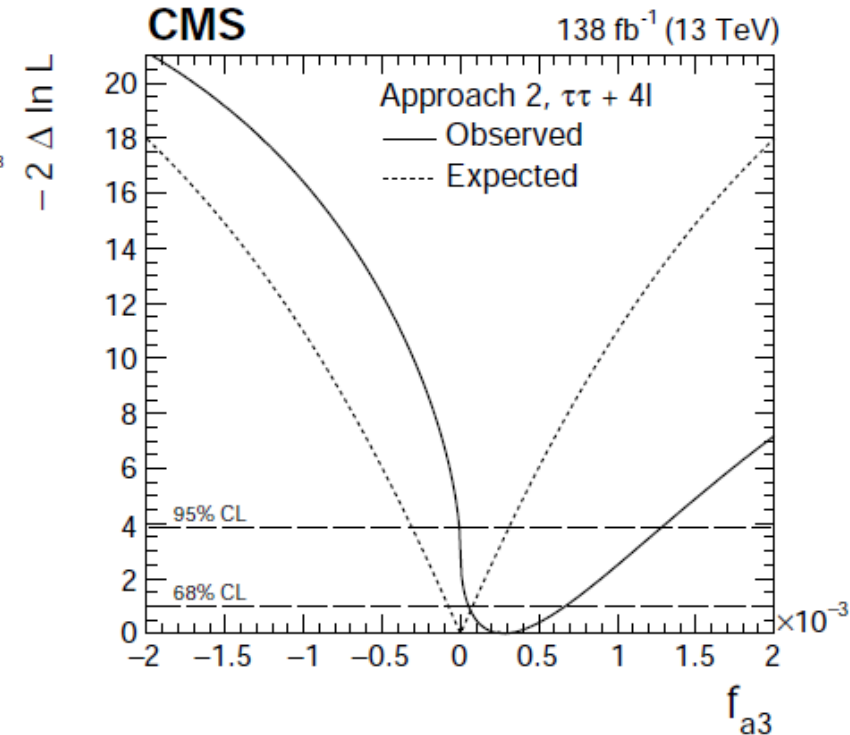


PhysRevD.108.032013

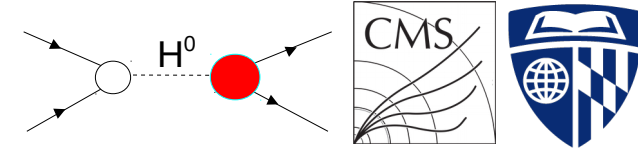
- Single AC scans
- Study production
- Utilize ME discr.



Combine results with H4l



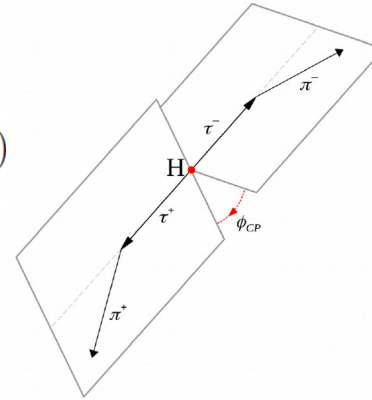
Yukawa $\tau\tau H : H \rightarrow \tau\tau$ CMS



JHEP06(2022)012

$$\mathcal{L}_Y = -\frac{m_\tau}{v} H (\kappa_\tau \bar{\tau} \tau + \tilde{\kappa}_\tau \bar{\tau} i \gamma_5 \tau)$$

$$\frac{d\Gamma}{d\phi_{CP}} (H \rightarrow \tau^+ \tau^-) \sim 1 - b(E^+) b(E^-) \frac{\pi^2}{16} \cos(\phi_{CP} - 2\alpha^{H\tau\tau})$$



Full Run2 data

Decay vertex probed

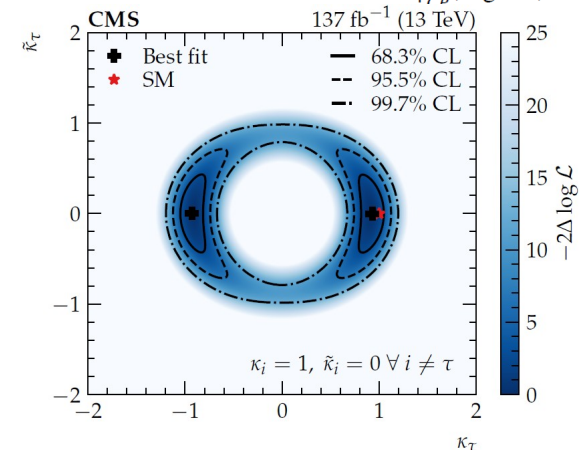
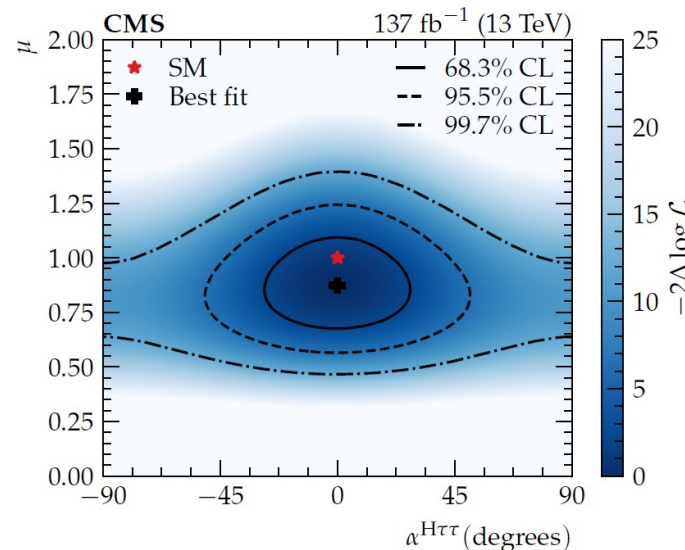
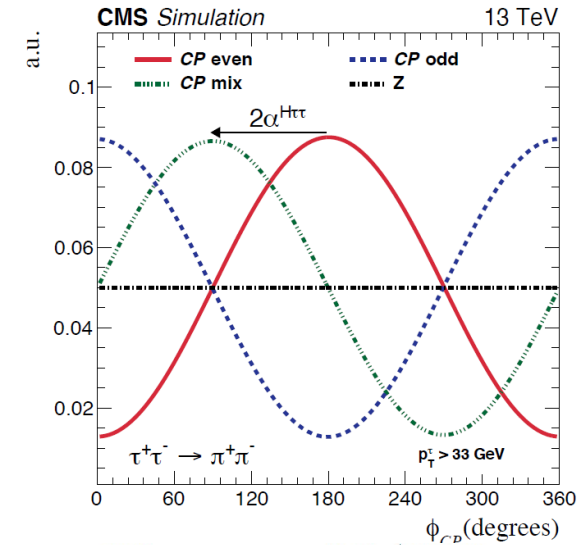
Use decays to $\tau\tau$ pair to measure CP odd/even mixing in $H\tau\tau$

Use $\sim 70\%$ of τ BR:

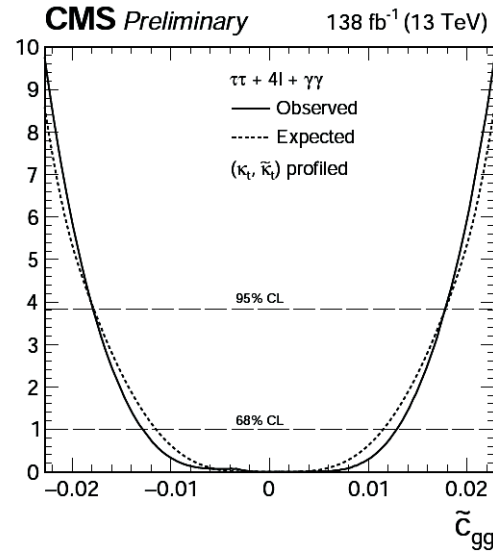
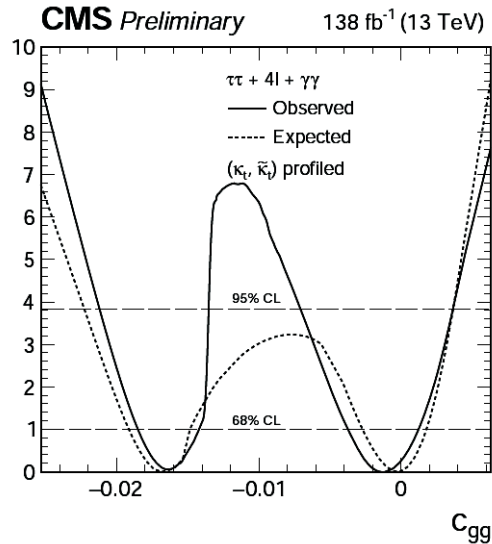
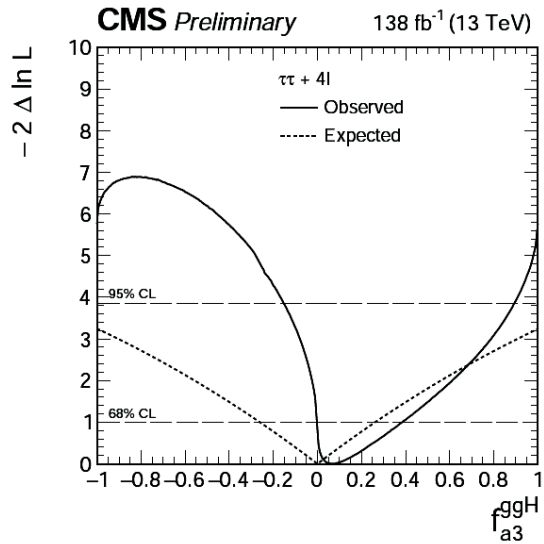
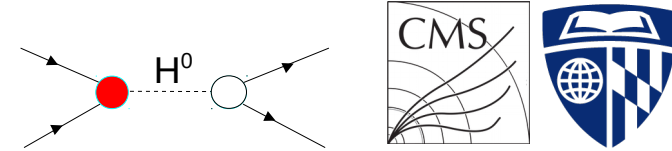
$$\tau_h \tau_h, \tau_\mu \tau_h + \tau_e \tau_h$$

4 reconstruction methods of ϕ_{CP}

Pure CP odd excluded at 3σ



Hgg : using ggF in 4l, γγ, ττ CMS



PhysRevD.108.032013
PhysRevD.104.052004

$$D_{CP}^{ggH} = \frac{\mathcal{P}_{SM-0-}^{ggH}}{\mathcal{P}_{SM}^{ggH} + \mathcal{P}_{0-}^{ggH}}$$

$$c_{gg} = -\frac{1}{2\pi\alpha_S} a_2^{gg}$$

$$\tilde{c}_{gg} = -\frac{1}{2\pi\alpha_S} a_3^{gg}$$

Combination of H→4l,
H→ττ, H→γγ

FULL RUN2

Measure CP sensitive fa_{3}^{ggH} and μ_{ggH}

Use events in VBF2J to study ggH category

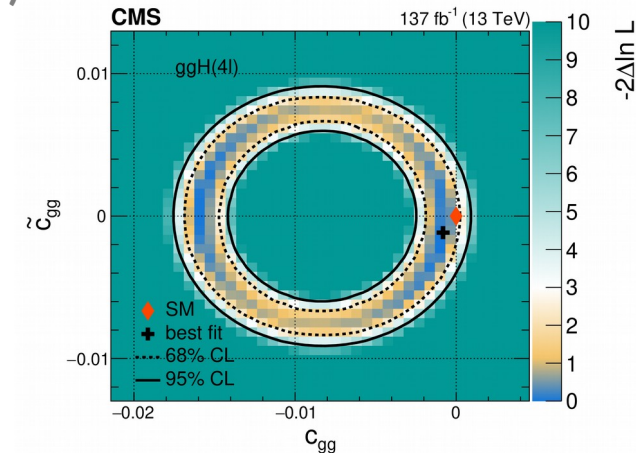
4 couplings fit simultaneously:

Constrain k_{top} measured from the tH, ttH process and study c_{gg}

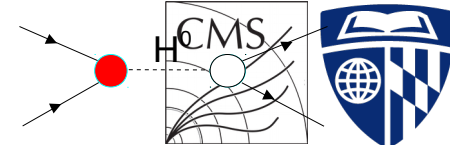
tH & ttH & ggH

(ttH, tH from: H→4l H→γγ)

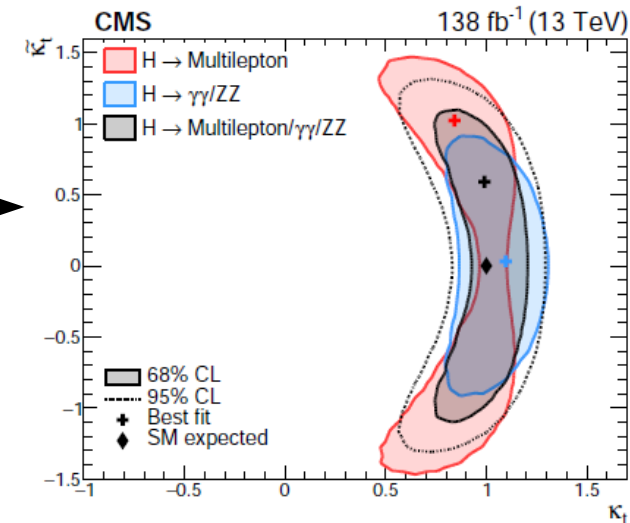
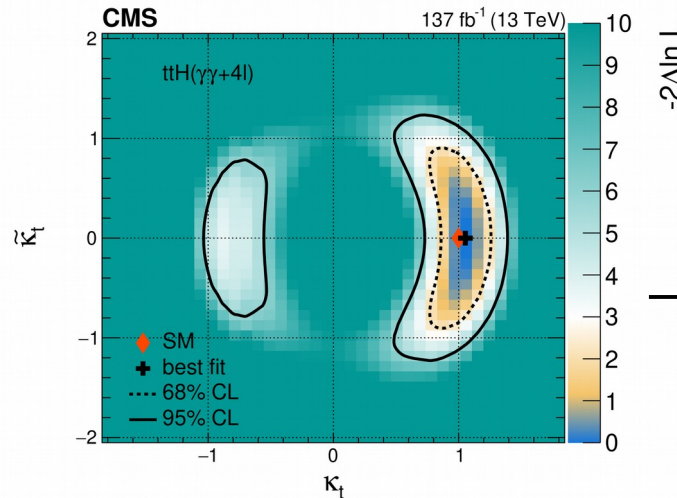
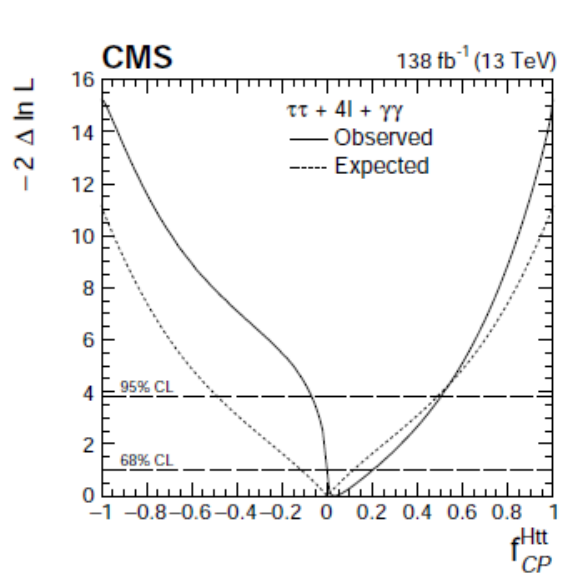
Parameter	Scenario		68% CL / (10 ⁻²)
c_{gg}	Profiled	Observed	$-0.11^{+0.20}_{-0.26} \cup [-1.85, -1.42]$
		Expected	$0.00^{+0.18}_{-0.27} \cup [-1.91, -1.48]$
\tilde{c}_{gg}	Profiled	Observed	0.00 ± 1.29
		Expected	0.00 ± 1.15
c_{gg}	Fixed	Observed	$-0.08^{+0.07}_{-0.15} \cup [-1.65, -1.54]$
		Expected	$0.00^{+0.06}_{-0.14} \cup [-1.73, -1.50]$
\tilde{c}_{gg}	Fixed	Observed	$0.22^{+0.28}_{-0.22} \cup [-0.50, 0.00]$
		Expected	0.00 ± 0.45



Yukawa ttH : $ttH(ggH), H \rightarrow 4l/\gamma\gamma/\tau\tau/WW$



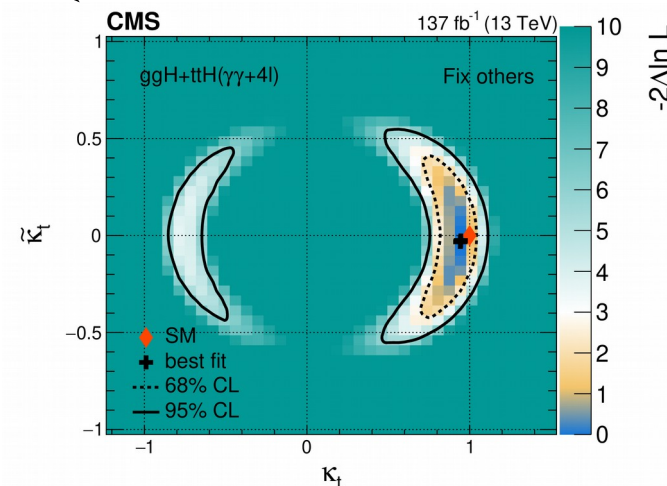
PhysRevD.108.032013
JHEP07(2023)092



- Measure f_{CP}^{Htt} in production
- Combine
 - $H \rightarrow 4l$
 - $H \rightarrow \tau\tau$
 - $H \rightarrow \gamma\gamma$
 + Also multi-lepton ($\tau\tau/WW$) + $ZZ + \gamma\gamma$

- Combine measurements with uncorrelated μ_s
- Interpret as top couplings

$$A(Hff) = -\frac{m_f}{v} \bar{\psi}_f (\kappa_f + i\tilde{\kappa}_f \gamma_5) \psi_f$$



Summary

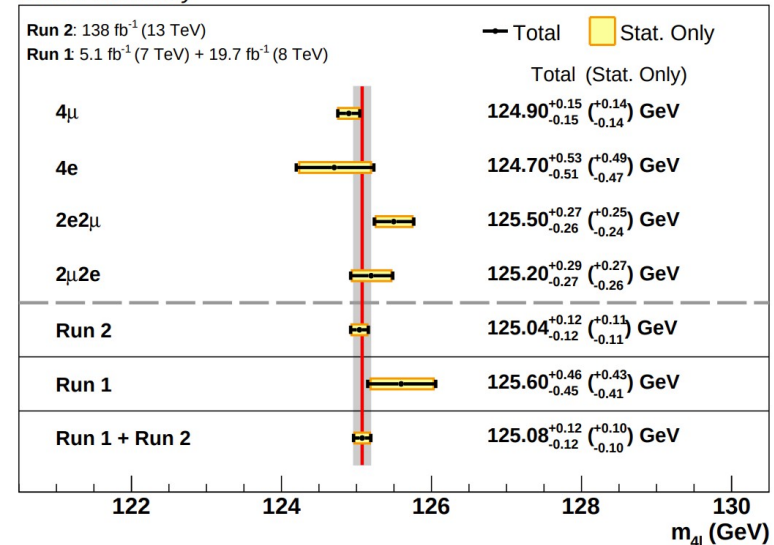
- **New Full Run2 Mass + width** results from CMS in $H \rightarrow 4l$
- $H \rightarrow 4l$ mass measurement most precise in a single channel

$$m_H = 125.08 \pm 0.12 \text{ (GeV)}$$

uncert < 0.1% !

- A.C. measured within EFT framework
- Combinations with multiple final states
- **CPV well constrained**
- > New AC results tomorrow by Angela!

CMS Preliminary

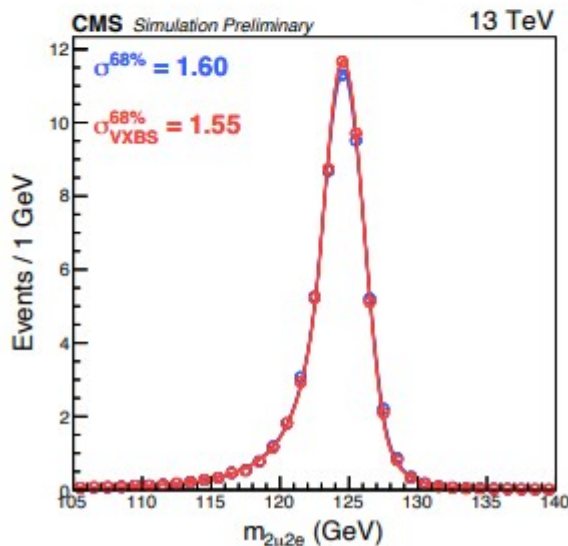
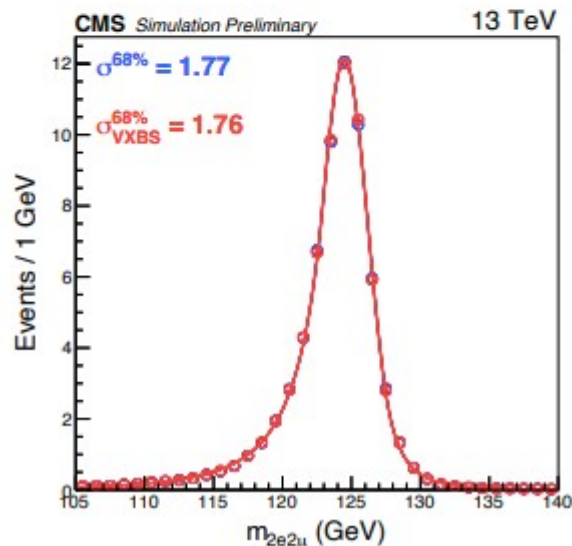
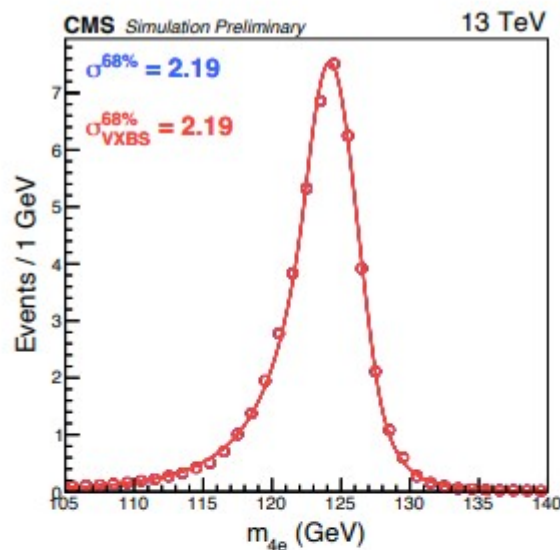
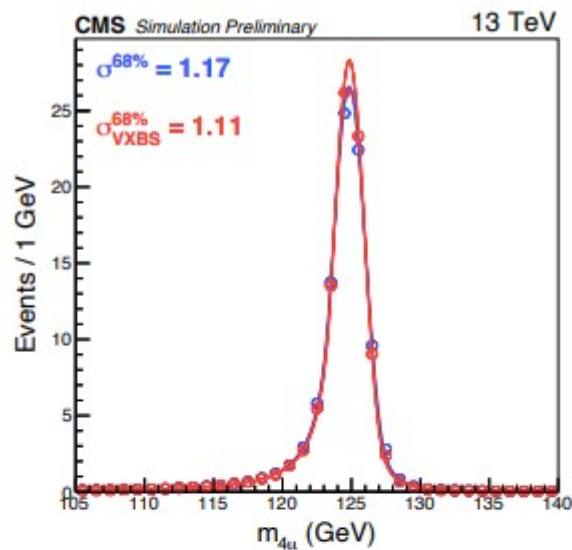


Parameter	Observed
m_H (GeV)	125.08 ± 0.12
on-shell Γ_H (GeV)	0.00 ^{+0.06} _{-0.00} [0.00, 0.33]
off-shell Γ_H (MeV)	2.9 ^{+2.3} _{-1.7} [0.3, 7.9]



Additional material

Mass VTX constraint



Effective Lagrangian and couplings (Higgs basis)

(arXiv:2002.09888)

$$\begin{aligned}
 \mathcal{L}_{\text{hvv}} = & \frac{h}{v} \left[(1 + \delta c_z) \frac{(g^2 + g'^2)v^2}{4} Z_\mu Z_\mu + c_{zz} \frac{g^2 + g'^2}{4} Z_{\mu\nu} Z_{\mu\nu} + c_{z\Box} g^2 Z_\mu \partial_\nu Z_{\mu\nu} + \tilde{c}_{zz} \frac{g^2 + g'^2}{4} Z_{\mu\nu} \tilde{Z}_{\mu\nu} \right. \\
 & + (1 + \delta c_w) \frac{g^2 v^2}{2} W_\mu^+ W_\mu^- + c_{ww} \frac{g^2}{2} W_{\mu\nu}^+ W_{\mu\nu}^- + c_{w\Box} g^2 (W_\mu^- \partial_\nu W_{\mu\nu}^+ + \text{h.c.}) + \tilde{c}_{ww} \frac{g^2}{2} W_{\mu\nu}^+ \tilde{W}_{\mu\nu}^- \\
 & + c_{z\gamma} \frac{e\sqrt{g^2 + g'^2}}{2} Z_{\mu\nu} A_{\mu\nu} + \tilde{c}_{z\gamma} \frac{e\sqrt{g^2 + g'^2}}{2} Z_{\mu\nu} \tilde{A}_{\mu\nu} + c_{\gamma\Box} g g' Z_\mu \partial_\nu A_{\mu\nu} \\
 & \left. + c_{\gamma\gamma} \frac{e^2}{4} A_{\mu\nu} A_{\mu\nu} + \tilde{c}_{\gamma\gamma} \frac{e^2}{4} A_{\mu\nu} \tilde{A}_{\mu\nu} + c_{gg} \frac{g_s^2}{4} G_{\mu\nu}^a G_{\mu\nu}^a + \tilde{c}_{gg} \frac{g_s^2}{4} G_{\mu\nu}^a \tilde{G}_{\mu\nu}^a \right],
 \end{aligned}$$

$$\mathcal{L}_{hff} = -\frac{m_f}{v} \bar{\psi}_f (\kappa_f + i \tilde{\kappa}_f \gamma_5) \psi_f h$$



$$\begin{aligned}
 \delta c_z &= \frac{1}{2} g_1^{ZZ} - 1, & c_{zz} &= -\frac{2s_w^2 c_w^2}{e^2} g_2^{ZZ}, & c_{z\Box} &= \frac{M_Z^2 s_w^2}{e^2} \frac{\kappa_1^{ZZ}}{(\Lambda_1^{ZZ})^2}, & \tilde{c}_{zz} &= -\frac{2s_w^2 c_w^2}{e^2} g_4^{ZZ}, \\
 \delta c_w &= \frac{1}{2} g_1^{WW} - 1, & c_{ww} &= -\frac{2s_w^2}{e^2} g_2^{WW}, & c_{w\Box} &= \frac{M_W^2 s_w^2}{e^2} \frac{\kappa_1^{WW}}{(\Lambda_1^{WW})^2}, & \tilde{c}_{ww} &= -\frac{2s_w^2}{e^2} g_4^{WW}, \\
 c_{z\gamma} &= -\frac{2s_w c_w}{e^2} g_2^{Z\gamma}, & \tilde{c}_{z\gamma} &= -\frac{2s_w c_w}{e^2} g_4^{Z\gamma}, & c_{\gamma\Box} &= \frac{s_w c_w}{e^2} \frac{M_Z^2}{(\Lambda_1^{Z\gamma})^2} \kappa_2^{Z\gamma}, \\
 c_{\gamma\gamma} &= -\frac{2}{e^2} g_2^{\gamma\gamma}, & \tilde{c}_{\gamma\gamma} &= -\frac{2}{e^2} g_4^{\gamma\gamma}, & c_{gg} &= -\frac{2}{g_s^2} g_2^{gg}, & \tilde{c}_{gg} &= -\frac{2}{g_s^2} g_4^{gg}.
 \end{aligned}$$

Necessary to consider impact of AC in Γ :

$$\sigma(i \rightarrow H \rightarrow f) \propto \frac{(\sum \alpha_{jk} g_j g_k) (\sum \alpha_{lm} g_l g_m)}{\Gamma_{\text{tot}}}$$

$$\Gamma_{\text{tot}} = \sum_f \Gamma_f = \Gamma_{\text{tot}}^{\text{SM}} \times \sum_f \left(\frac{\Gamma_f^{\text{SM}}}{\Gamma_{\text{tot}}^{\text{SM}}} \times \frac{\Gamma_f}{\Gamma_f^{\text{SM}}} \right) = \Gamma_{\text{tot}}^{\text{SM}} \times \sum_f (\mathcal{B}_f^{\text{SM}} \times \mathcal{R}_f(\tilde{g}_j))$$