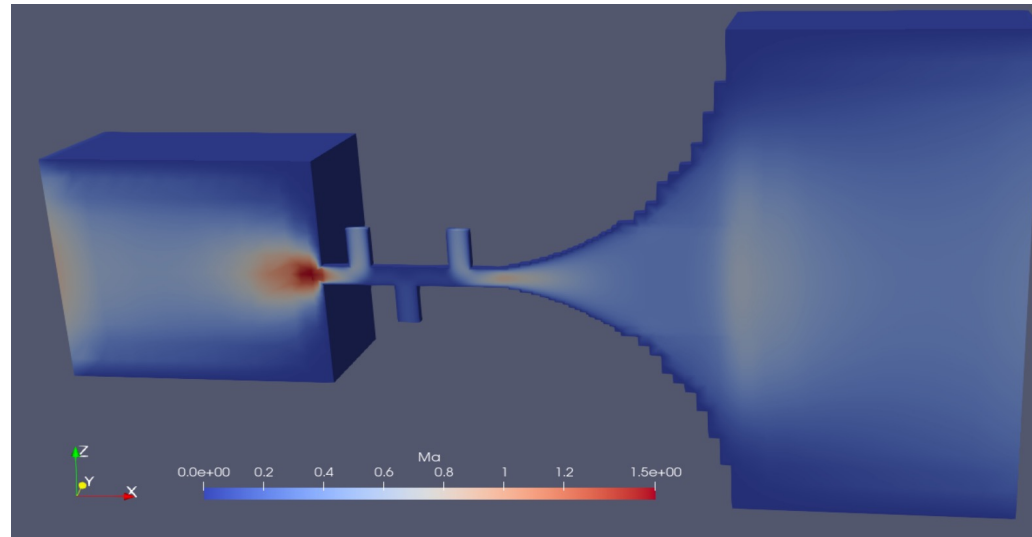


Development of a Two-Stage 150 MeV Laser-Plasma Electron Injector Using Massive Particle-in-Cell Computing Combined with Fluid Simulation



Pierre Drobniak

Thanks to the organisers

Francesco Massimo & Damien Minenna



And many thanks to my collaborators and colleagues

1 = IJCLab
2 = LLR
3 = LPGP
4 = CEA-Irfu
_ : supervisors

E. Baynard¹, A. Beck², C. Bruni¹, K. Cassou¹, C. Guyot¹, G. Kane¹,
S. Kazamias¹, V. Kubytsky¹, N. Lericheux¹, B. Lucas¹, F. Massimo³,
D. Minenna⁴, P. Nghiem⁴, M. Pittman¹, A. Specka¹

From theory to experimental
electron production

10k+ configurations

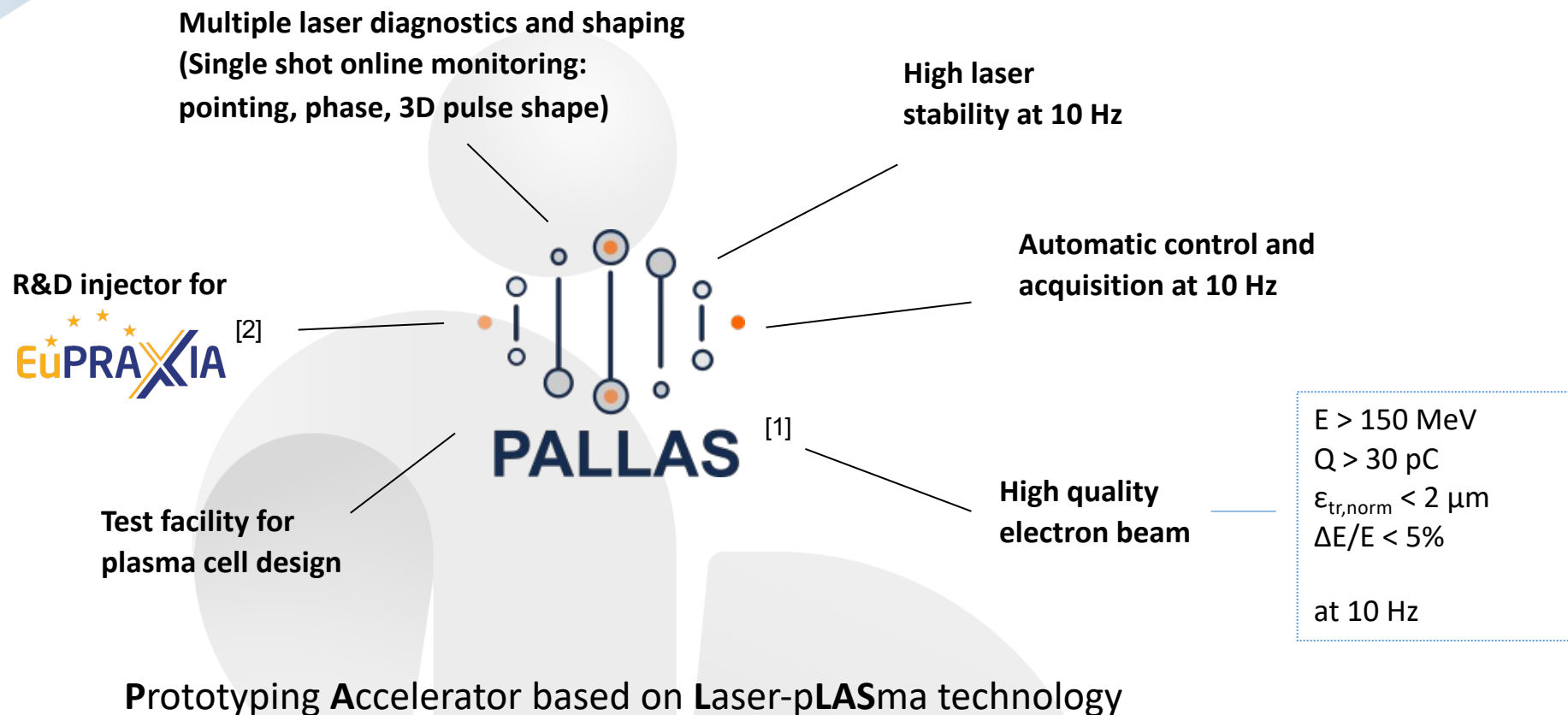
Smilei)^[1]

Development of a Two-Stage 150 MeV Laser-Plasma Electron Injector Using Massive Particle-in-Cell Computing Combined with Fluid Simulation

Open  FOAM^[2]

[1] <https://smileipic.github.io/Smilei/>

[2] <https://www.openfoam.com/>



[1] <https://pallas.ijclab.in2p3.fr/>

[2] <http://www.eupraxia-project.eu/>

Laser parameters (LaseriX platform [1]):

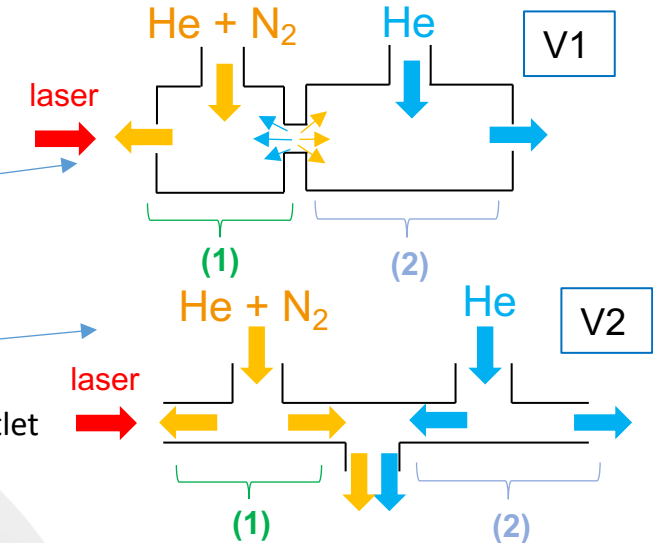
- 810 nm ($\Delta\lambda = 30$ nm)
- 5th order FGB (Flattened Gaussian Beam [2])
- 1.6 ± 0.1 J (on target)
- $\tau_{\text{FWHM}} = 35 \pm 5$ fs
- $f = 1.5$ m
- $w_0 = 19$ μm
- $a_0 \approx 1.40$ (4×10^{18} W/cm²)
- $x_R = 1.4$ mm

Injection scheme:

- self-truncated ionisation injection [3][4]
- He doped with N₂
- $a_{0,\text{BSI},\text{N5}^+} = 2.21$ & $a_{0,\text{BSI},\text{N6}^+} = 2.77$ [5] -> need for **self-focusing**

Cell design

- Inspiration from [3], [4] and [6]
two-chamber cell (1) + (2)
(1): self-focusing + injection
(2): acceleration + filter
- **Prototype V1:**
 - Same pressure in both chambers, to **prevent dopant convection** from (1) to (2)
- **Prototype V2:**
 - **Diffusion** is sucked out by central outlet
- Play with N₂ concentration to shape **overall** electronic density



[1] <https://www.ijclab.in2p3.fr/en/platforms/laserix/>

[2] Gori, F. (1994). Flattened gaussian beams. *Optics Communications*, 107(5-6), 335-341.

[3] Pak et al. (2010). Injection and trapping of tunnel-ionized electrons into laser-produced wakes. *Physical review letters*, 104(2), 025003.

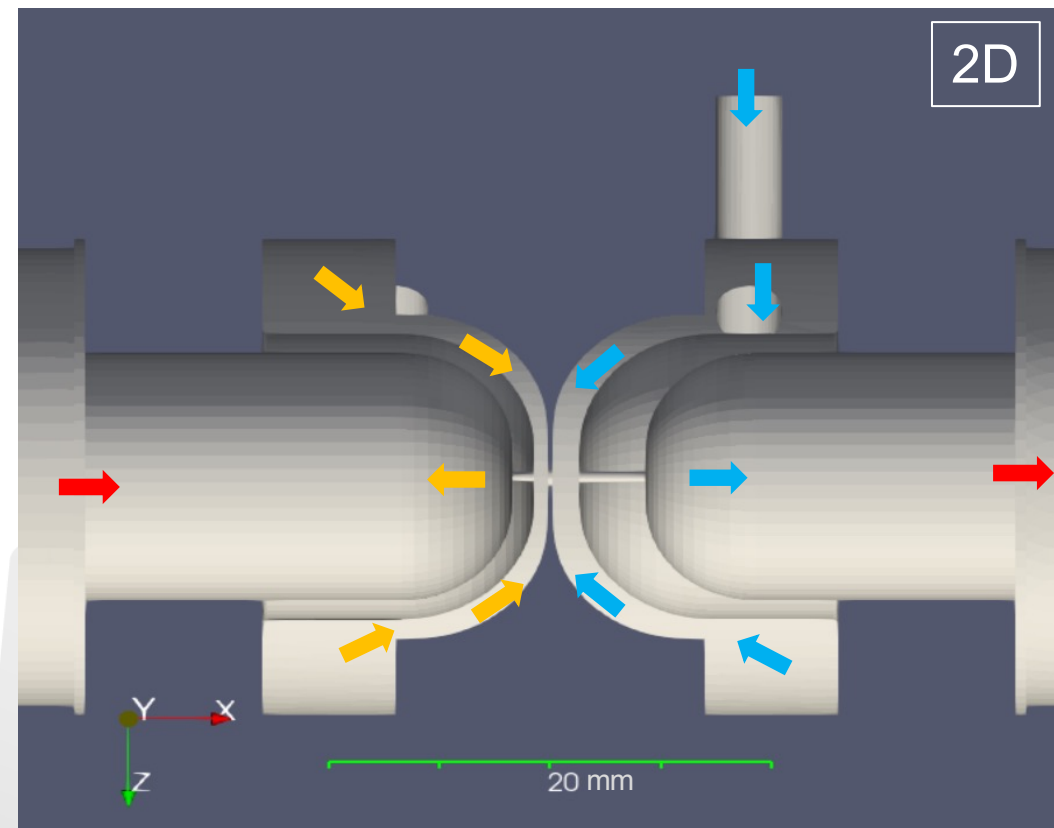
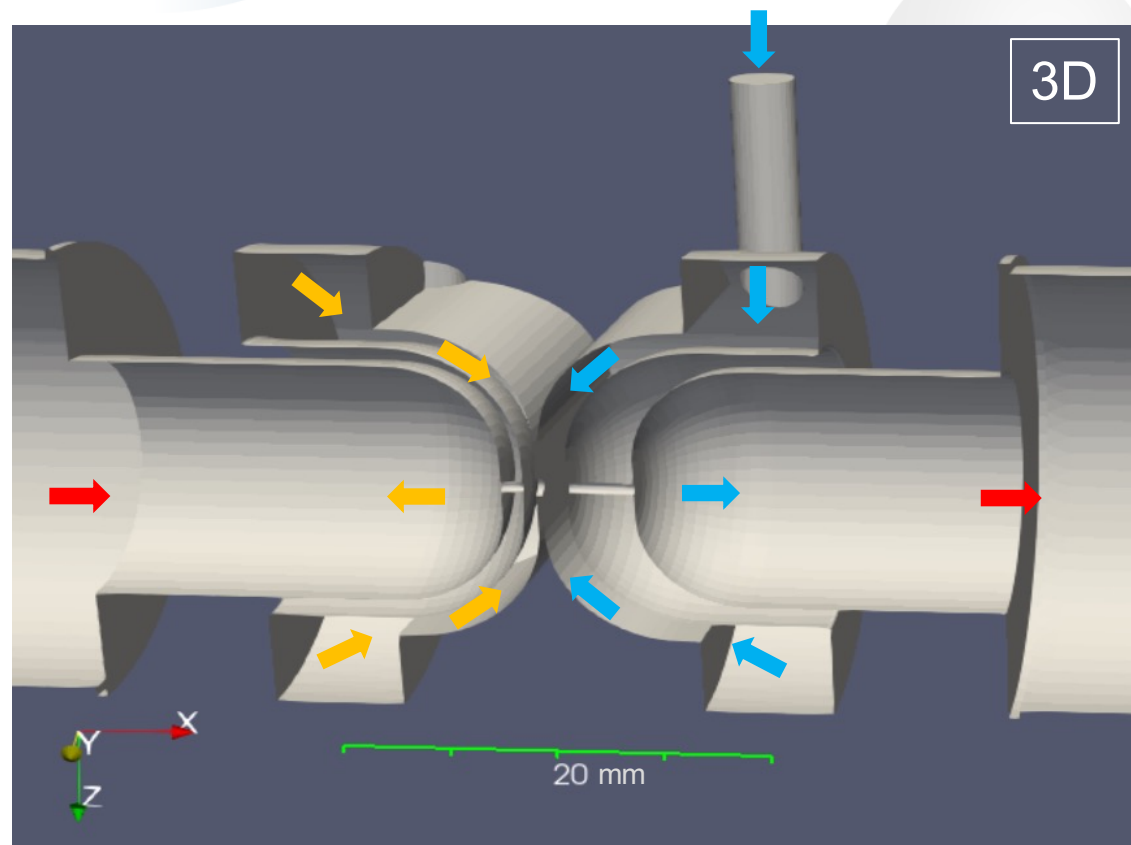
[4] Golovin et al. (2015). Tunable monoenergetic electron beams from independently controllable laser-wakefield acceleration and injection. *Physical Review Special Topics-Accelerators and Beams*, 18(1), 011301.

[5] Couperus, J. P. (2018). *Optimal beam loading in a nanocoulomb-class laser wakefield accelerator* (No. HZDR--093). Helmholtz-Zentrum Dresden-Rossendorf (Germany).

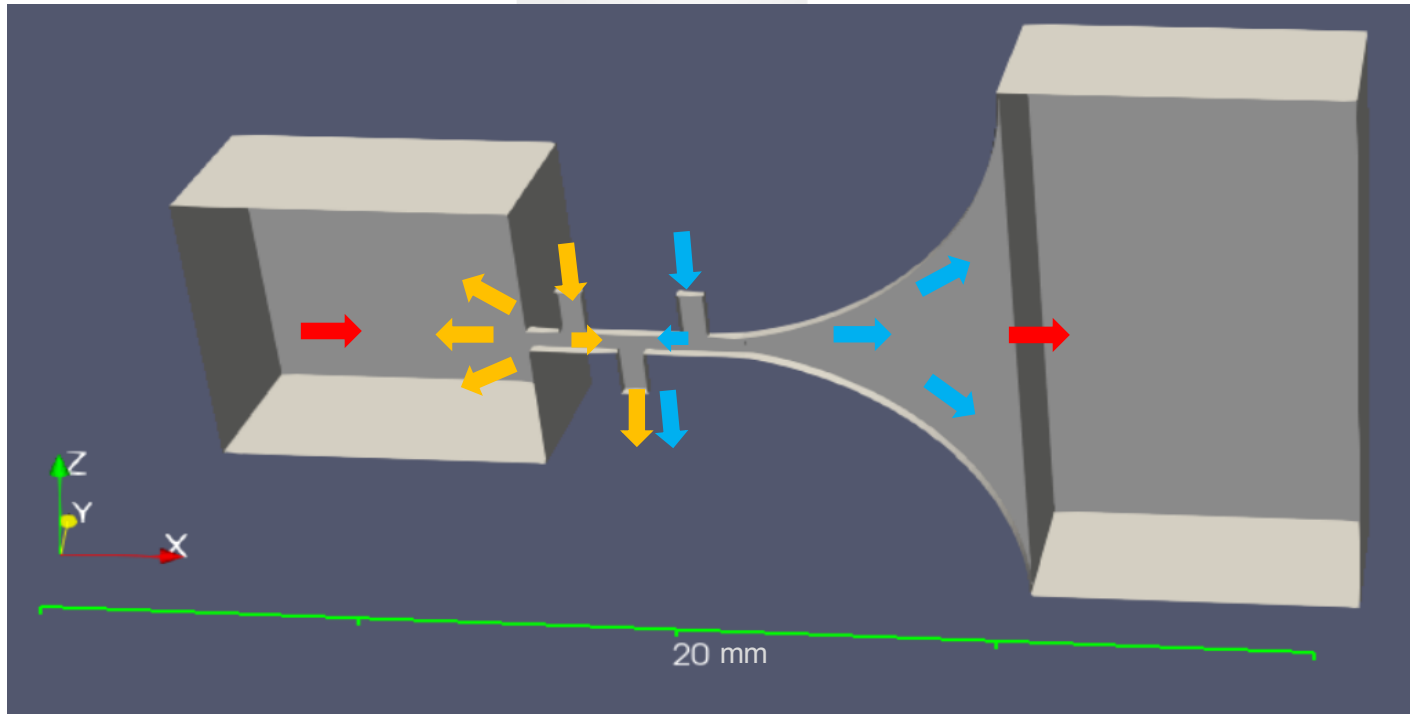
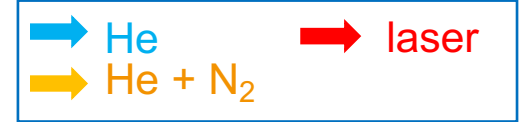
[6] Jalias et al. (2021). Bayesian optimization of a laser-plasma accelerator. *Physical review letters*, 126(10), 104801.

Prototype V1: two tank chambers, 2 inlets, 2 outlets

→ He
→ He + N₂
→ laser



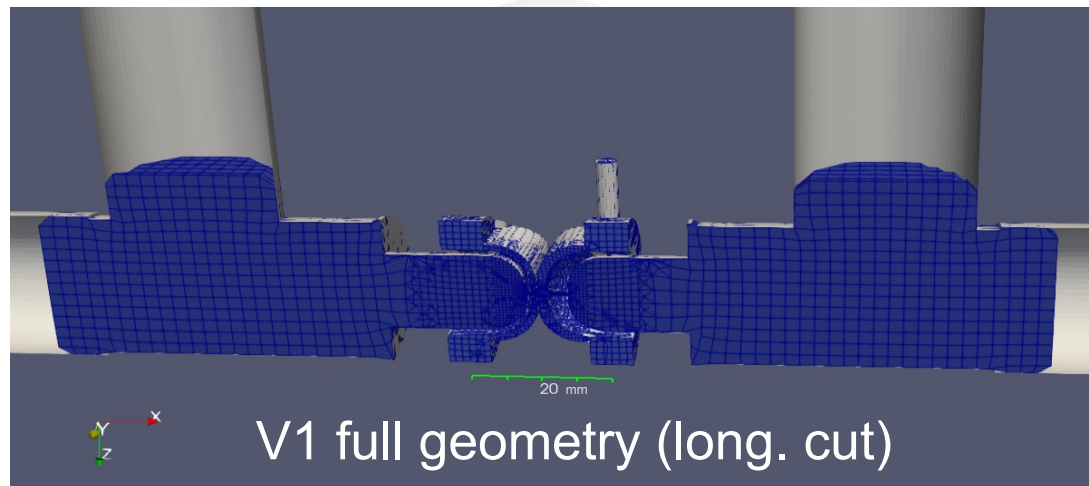
Prototype V2: 2 flows, 2 inlets, 3 outlets



Meshing tool:
snappyHexMesh

Careful with cells
shape
=> Courant Number
might explode

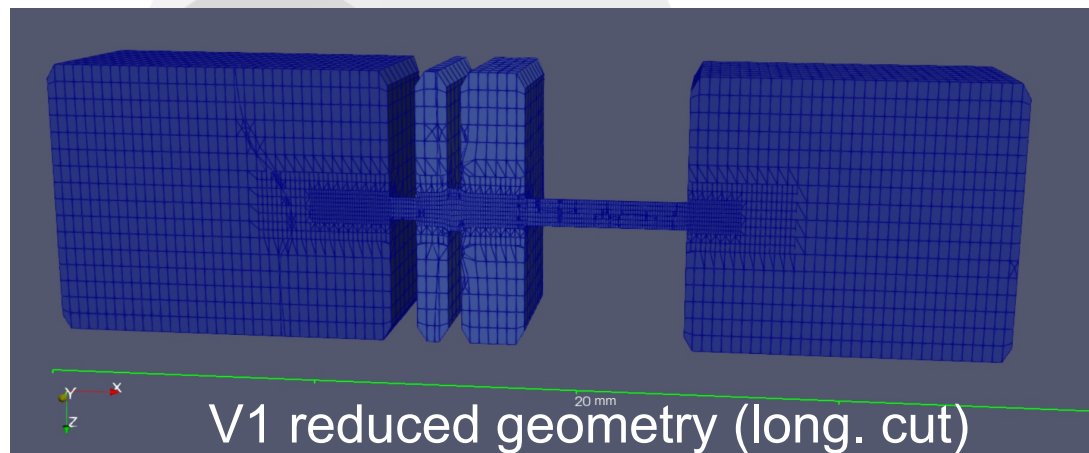
On prototype V1



Full geometry

70 000 cells

20 sec meshing on 1 proc.

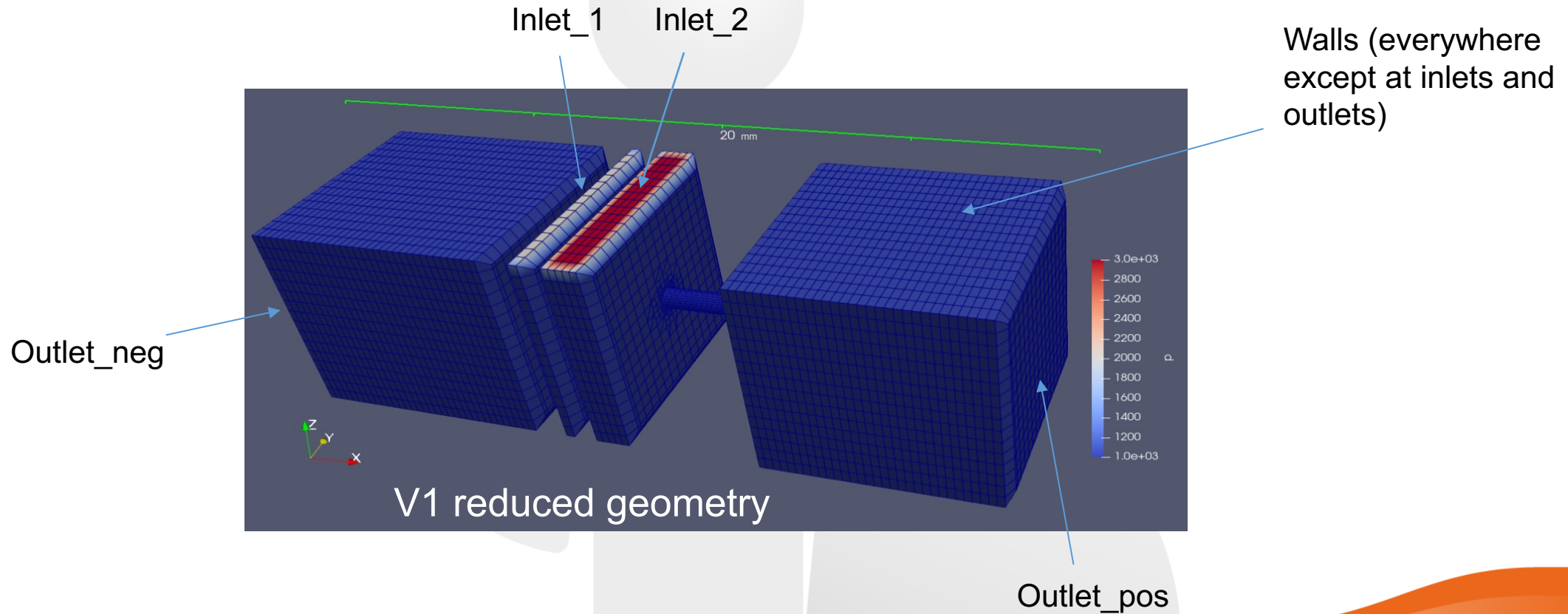


Reduced geometry

50 000 cells

8 sec meshing on 1 proc.

6.1 Definition of patches



6.2 Set inlets and outlets

Boundary conditions

Walls:

- Pressure P: « zero gradient »
- Velocity U: « no slip »
- Temperature T: « fixed value » (293K)

Inlets:

- P: « zero gradient » & U: « flow rate »
or P: « fixed value » & U: « zero gradient »
- Temperature T: « fixed value » (293K)

Outlets:

- P: « zero gradient » & U: « flow rate »
or P: « fixed value » & U: « zero gradient »
- Temperature T: « fixed value » (293K)

Example: boundary conditions with pressure values only

Walls:

- P: « zero gradient »
- U: « no slip »
- Temperature T: « fixed value » (293K)

Inlets:

- P: « fixed value » for ex. $p_{inlet_1} = p_{inlet_2} = 30$ mbar
- U: « zero gradient »
- Temperature T: « fixed value » (293K)

Outlets:

- P: « fixed value » for ex. $p_{outlet_neg} = p_{outlet_neg} = 1$ mbar
- U: « zero gradient »
- Temperature T: « fixed value » (293K)

6.3 Set initial values

Initial values

For patches:

- Same as boundary conditions

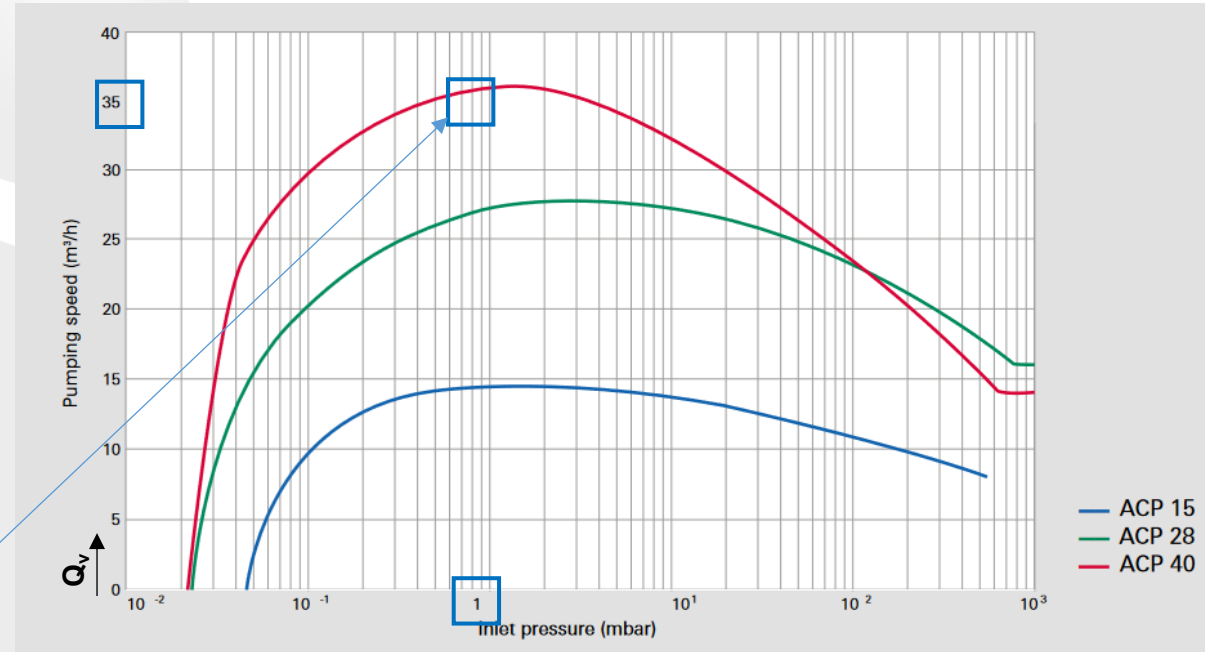
For the internal fields:

- $P = \text{a few mbar}$
- $U = 0$
- $T = 293 \text{ K}$

Careful with
pressure
difference at $t = 0$

6.4 Check if feasible (at end of simulation)

- Energy sucked out by the pump cannot be higher in simulation than what the curve describes.
- > check that Q_{pV} (throughput $[\text{Pa m}^3/\text{s}] = [\text{J/s}]$) is not higher than what pump can develop.
- **Example:** for fixed outlet pressure values
 - (1) note the fixed pressure value
 - (2) check the simulation flow Q_v
 - (3) compute $Q_{pV} = Q_v \times p$
 - (4) Verify Q_{pV} feasible by pump for the given pressure value



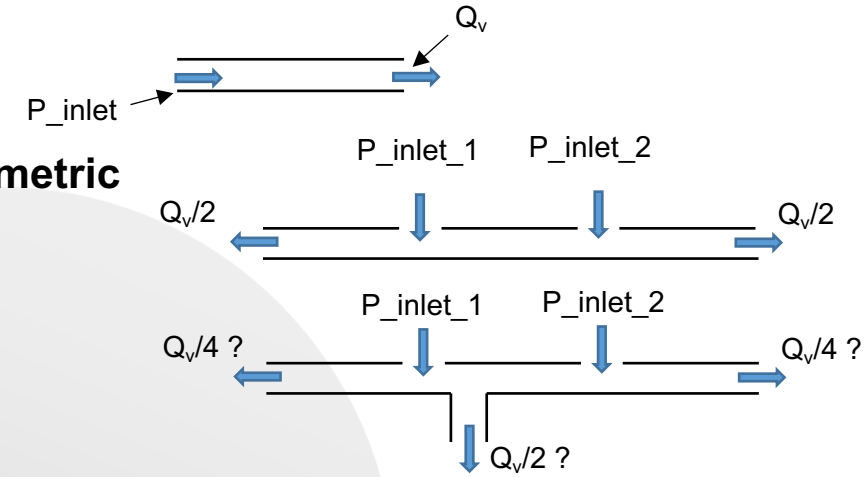
Characteristics of primary vacuum pump (Pfeiffer ACP40)

6.5 Comments

- With a flow pressure in the range of 10-100 mbar, setting a boundary condition at 1 mbar **or lower** does not influence the flow in the channel (only change is in Q_v at the very end + strong gas expansion)
- **Easier to set pressure boundary conditions** at outlet than pumping rates, because pumping rates on different outlets depends on each pipe **conductance** (which might be tricky to compute)
- > simply chose a single primary vacuum pressure for all outlets
(assumes all patches are in the same primary vacuum tank)

For flow boundary conditions (assuming you know the pump characteristics):

- Easy when there is only **one** outlet
-> Set pumping flow Q_v (m³/s) on the outlet patch
- Easy when the geometry and expected result are **symmetric**
(you know how the flow is distributed)
- **Difficult** when geometry is more **complex**
(no information on the flow distribution)
-> need for **conductance** values... not direct



Flow:

- Compressible (Ma ~1 or higher)
- Laminar (Re < 2000)

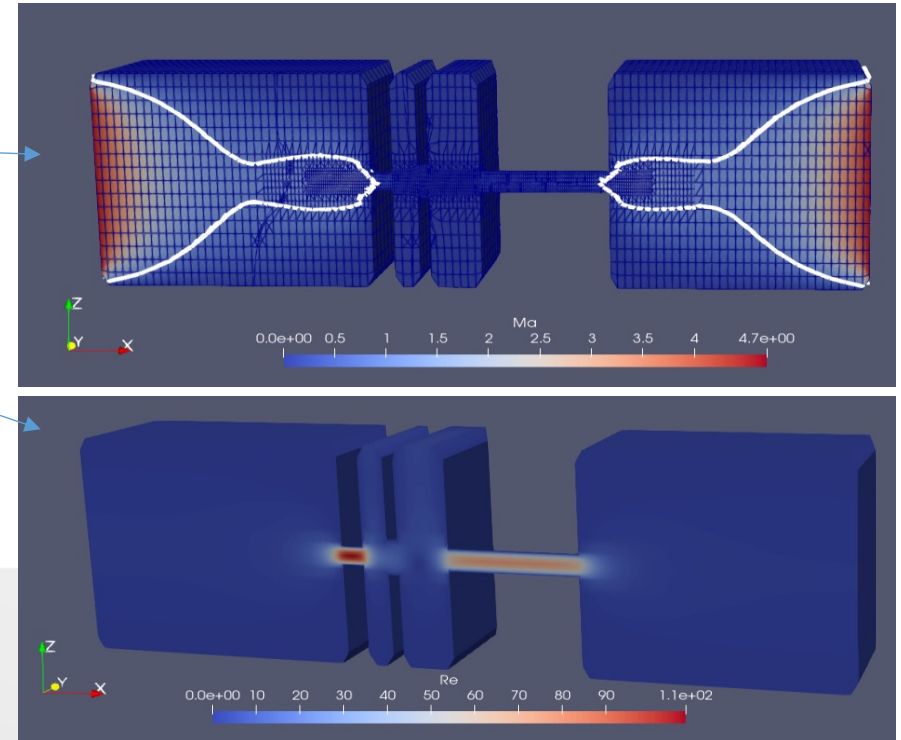
$$Re = \frac{\rho UL}{\mu}$$

Gas:

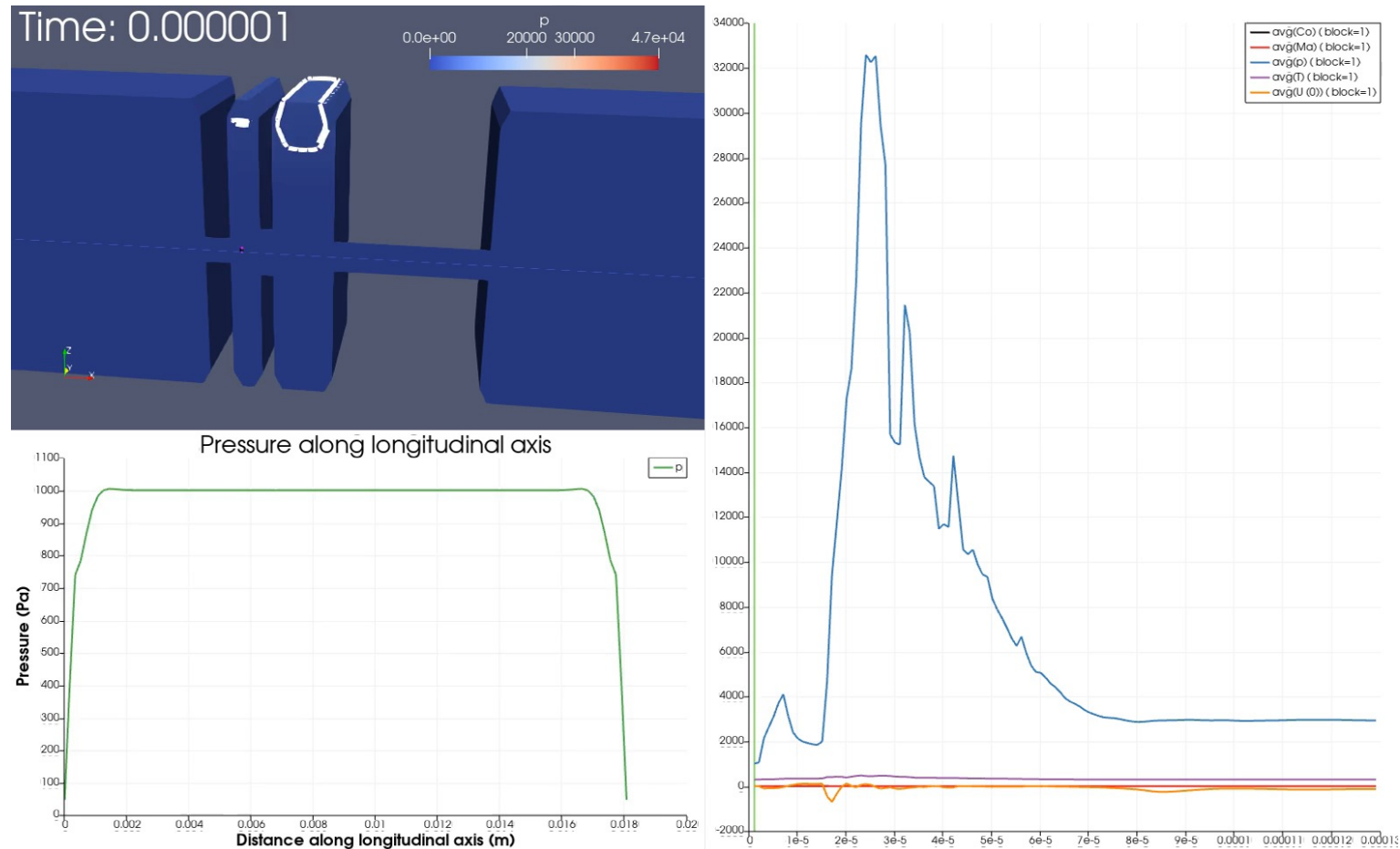
- Only Helium (enough for flow modelling)
- Possible to have **multiple** gases but « **non-miscible** » (diffusion cannot be modelled with OpenFOAM presently)

Solver:

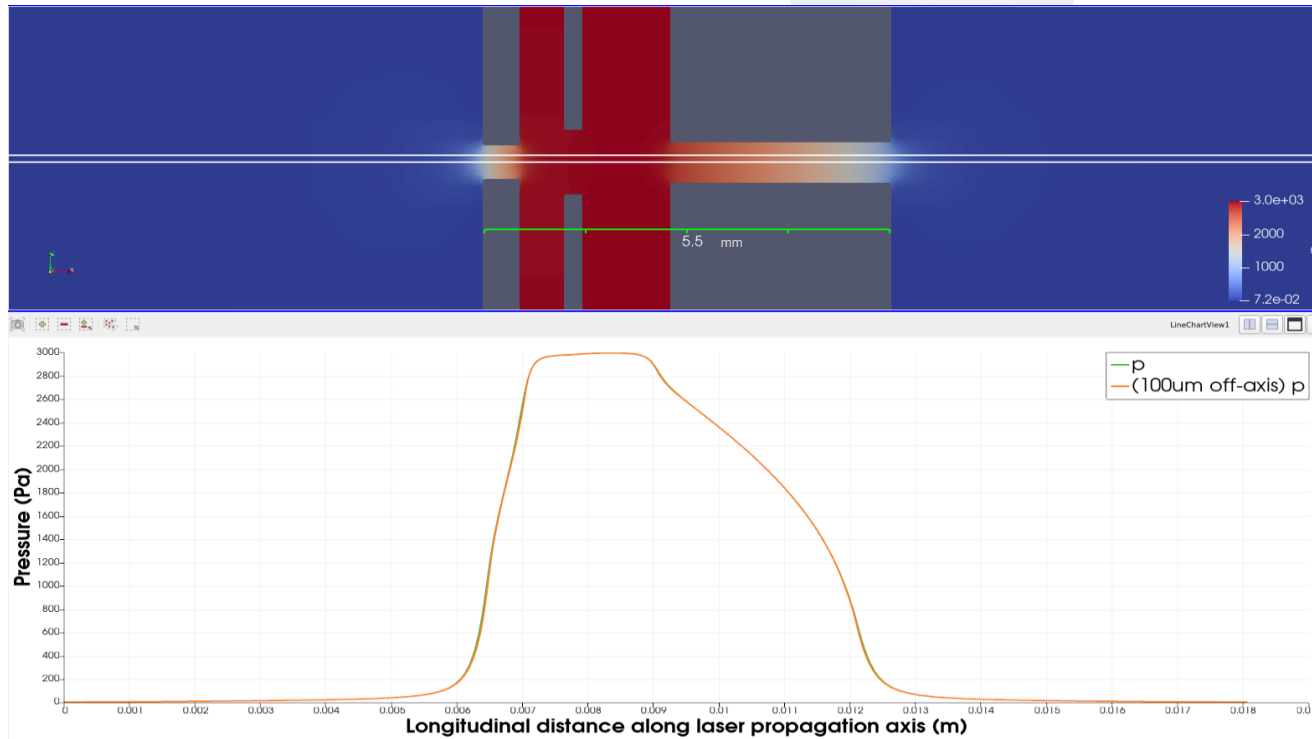
- rhoPimpleFoam



8. Fluid simulations results



Longitudinal plot along laser propagation axis



Plot along long. axis:

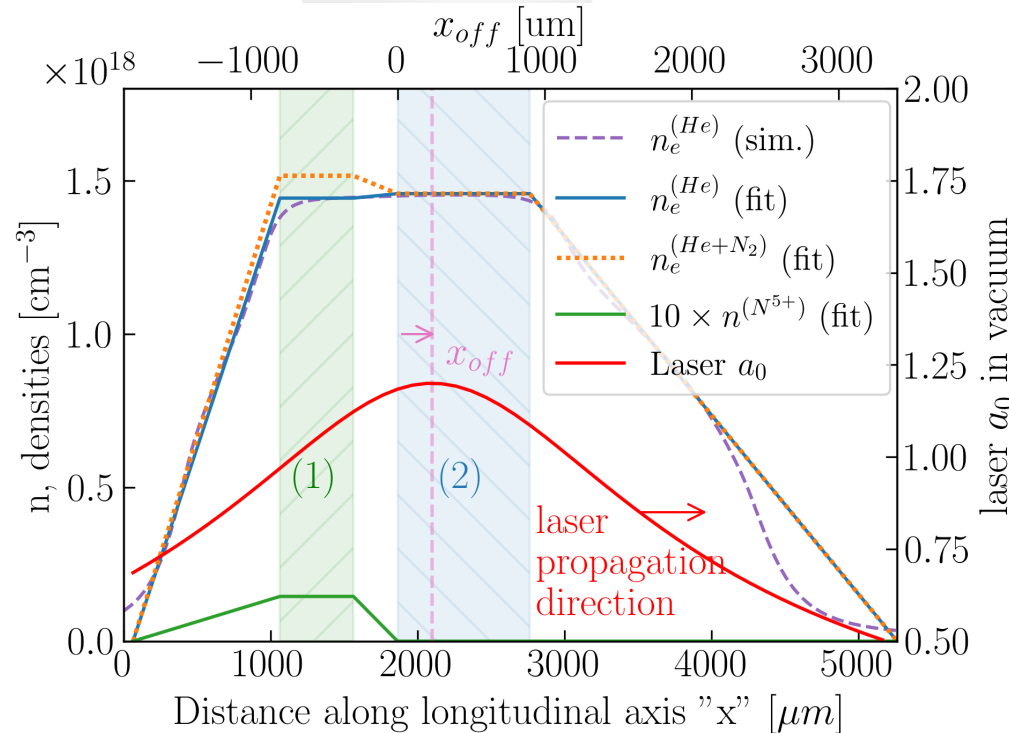
- no difference with 100μm off-axis curve

Computation time

- On 1 proc ~ 20 min (V1 reduced geometry)
- Simulated time: ~ 100 μs (enough for steady state)

Profile for PIC simulations:

- Polygonal fit to the simulated profile

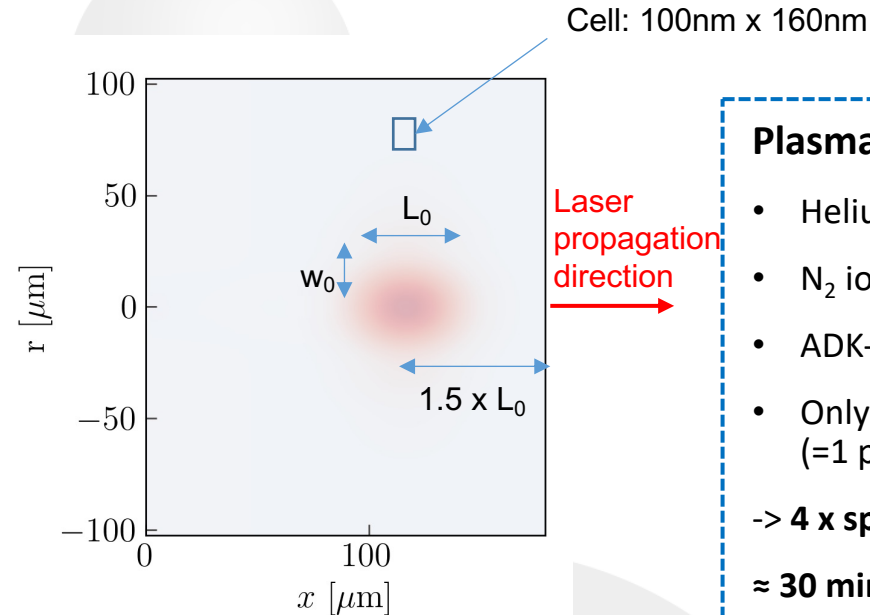


Solver:

- **Smilei)**
- Cylindrical geometry (with 1 Azimutal Mode)
- Envelope approximation [1]

Laser parameters :

- 810 nm
- 5th order FGB
- $\tau_{FWHM} = 35$ fs (Gaussian, unchirped)
- $w_0 = 19$ μm
- $a_0 \in [1.10 ; 1.85]$



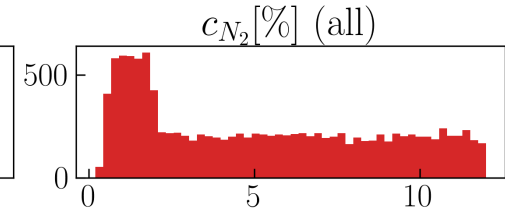
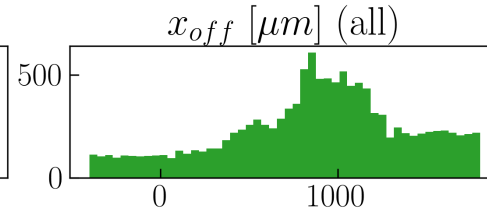
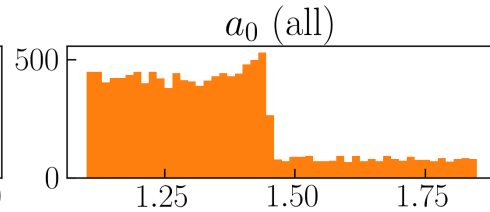
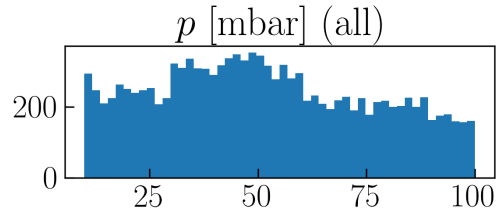
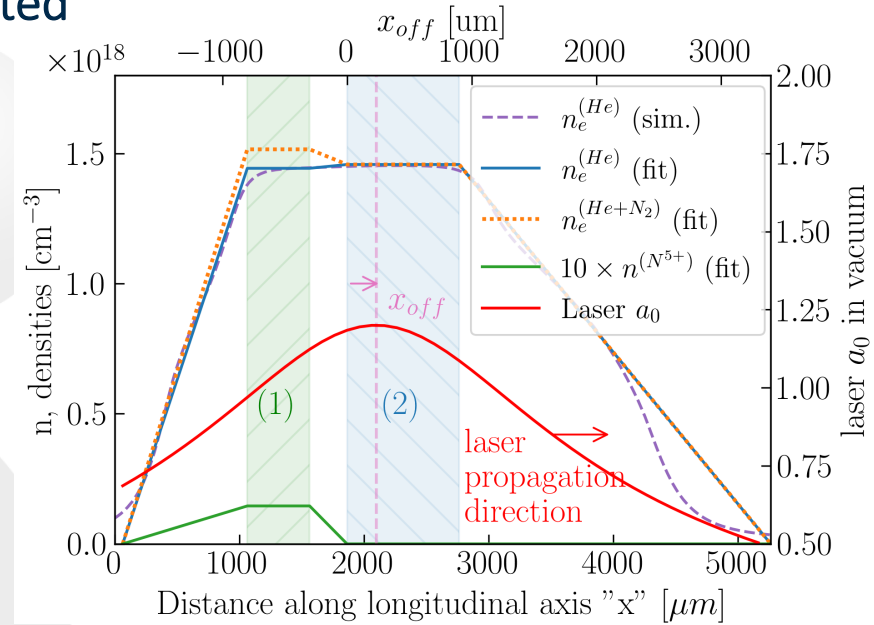
Plasma parameters:

- Helium fully ionised
 - N₂ ionised up to N⁵⁺
 - ADK-tunnel ionisation of N⁵⁺ & N⁶⁺
 - Only 1 **macro Particle Per Cell** (=1 ppc)
- > **4 x speedup** compared to 8 ppc
- ≈ 30 min / sim**
- > ≤ **10%** difference compared to 8 ppc in energy, spread, charge and emittance.

[1] Massimo et al. "Numerical modeling of laser tunneling ionization in particle-in-cell codes with a laser envelope model." *Physical Review E* 102.3 (2020): 033204.

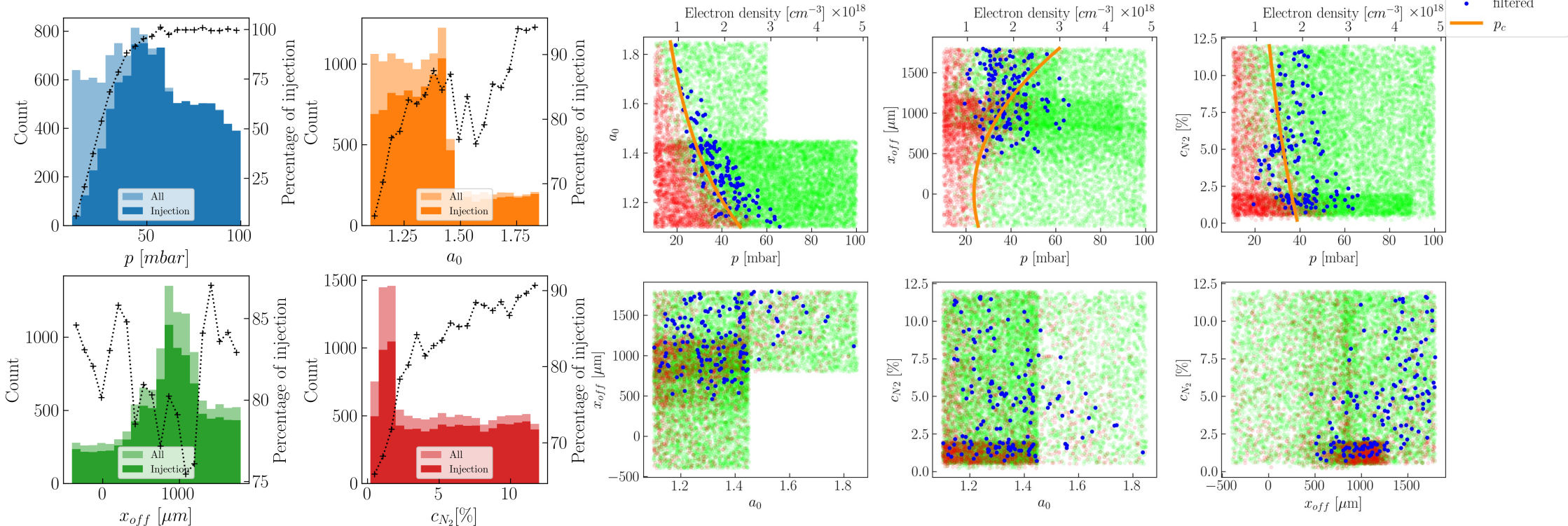
11.1 Configurations investigated

- 5 Random Scans (RS)
- 5 x 2401 = **12 005 configurations**
- 5 x 4 h < **1 day**



11.2 Injection positions

(Filter = $Q > 30$ pC & $E_{\text{med}} > 150$ MeV & $\delta E_{\text{mad}} < 5\%$ & $\varepsilon_{y,n} < 2 \mu\text{m}$)



11.3 Beams generated

$$f_1 = \frac{E_{med}^2 Q}{\sigma_{mad} \epsilon_{y,n}} \quad \text{S1}$$

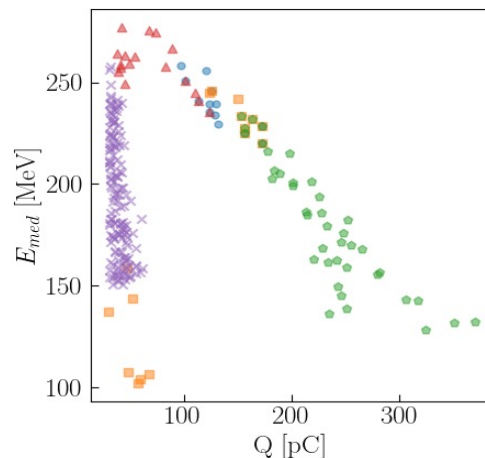
$$f_2 = \frac{E_{med} \sqrt{Q}}{\sigma_{mad}} \quad \text{S2}$$

$$f_3 = \frac{E_{med} Q}{\sigma_{mad}} \quad \text{S3}$$

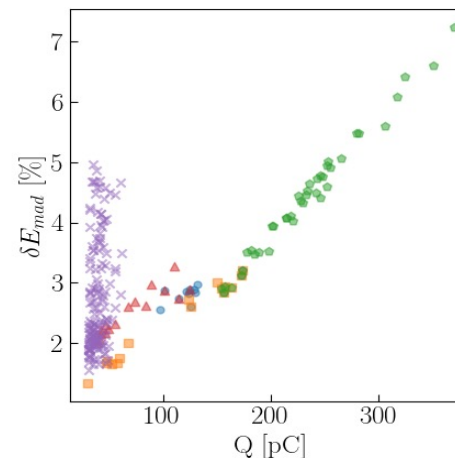
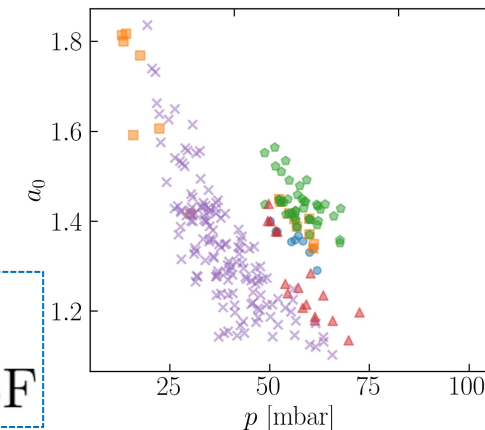
$$f_4 = \frac{E_{med} Q}{\sigma_{mad} \sqrt{\epsilon_{y,n} \epsilon_{z,n}}} \quad \text{S4}$$

- Set =
cut each f at 10%
of their max.

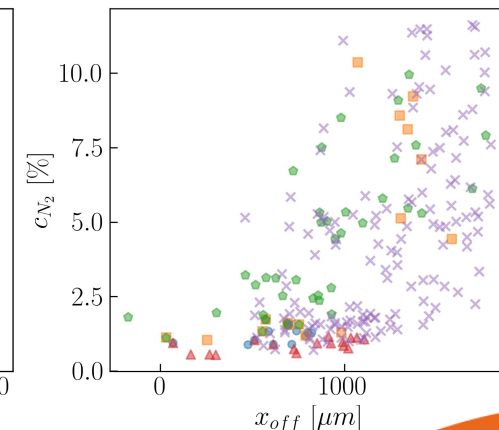
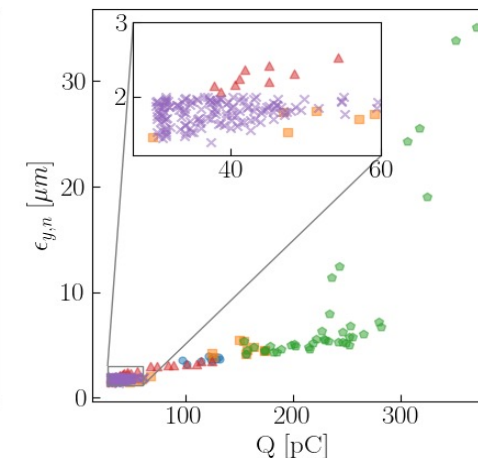
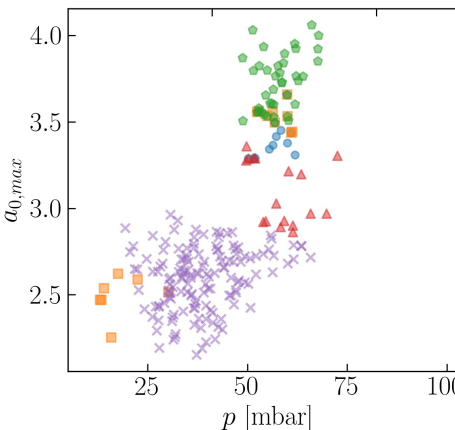
In Filter =
 $Q > 30 \text{ pC} \ \& \ E_{med} > 150 \text{ MeV}$
 $\& \ \delta E_{mad} < 5\% \ \& \ \epsilon_{y,n} < 2 \text{ } \mu\text{m}$ **SF**



Electron density $[cm^{-3}] \times 10^{18}$



Electron density $[cm^{-3}] \times 10^{18}$



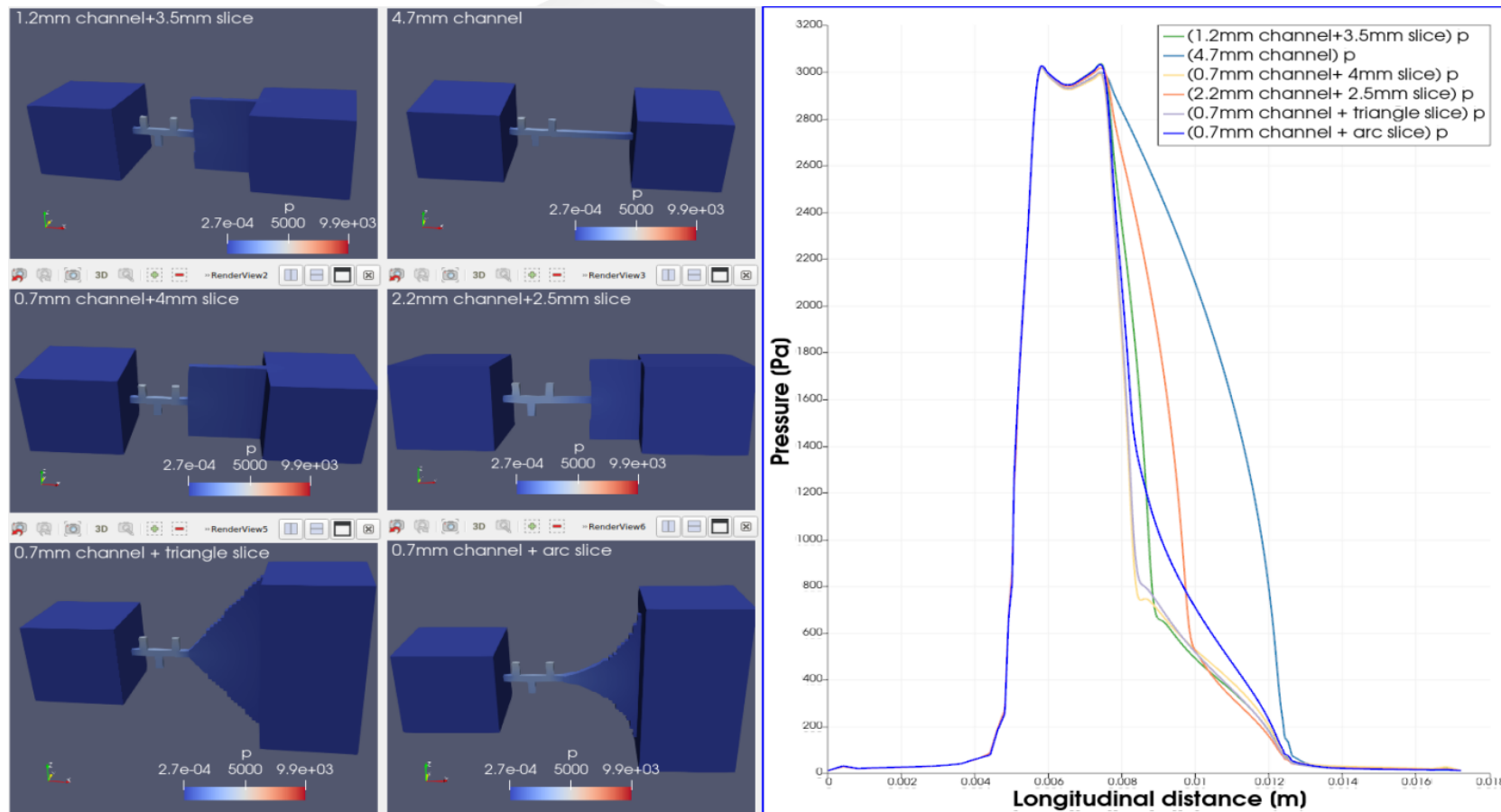
Sum-up

- Ability to generate density profile with fluid simulations
 - Fast meshing (few *s*)
 - Fast simulations (few *min*)
- Applied to massive PIC random scans
- Several beams found which satisfy **Filter** = $Q > 30 \text{ pC} \ \& \ E_{\text{med}} > 150 \text{ MeV} \ \& \ \delta E_{\text{mad}} < 5\% \ \& \ \epsilon_{y,n} < 2 \text{ } \mu\text{m}$
- PIC results open to scientific community

Next steps:

- Compare OpenFOAM results with other codes (Ansys Fluent) + check interface for diffusion
- Shape the plasma outramp...

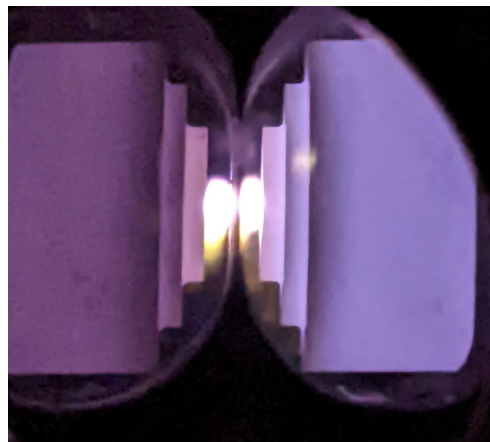
Outramp optimisation to preserve emittance growth (already investigated in [1][2])



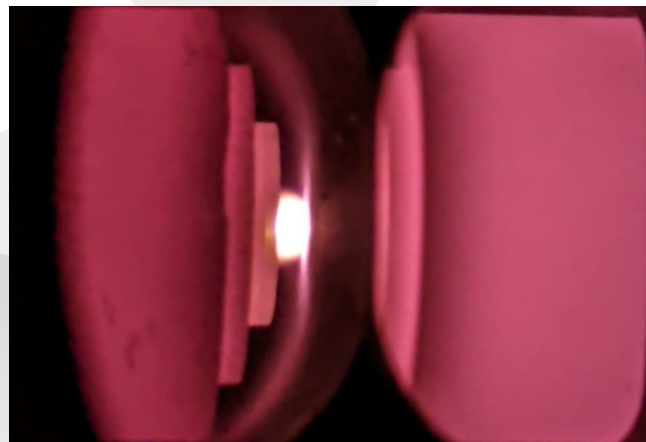
[1] Li, Xiangkun, Antoine Chancé, and Phu Anh Phi Nghiem. "Preserving emittance by matching out and matching in plasma wakefield acceleration stage." *PRAB* 22.2 (2019): 021304.

[2] Dommair, Irene, K. Floettmann, and A. R. Maier. "Emittance conservation by tailored focusing profiles in a plasma accelerator." *PRSTAB* 18.4 (2015): 041302.

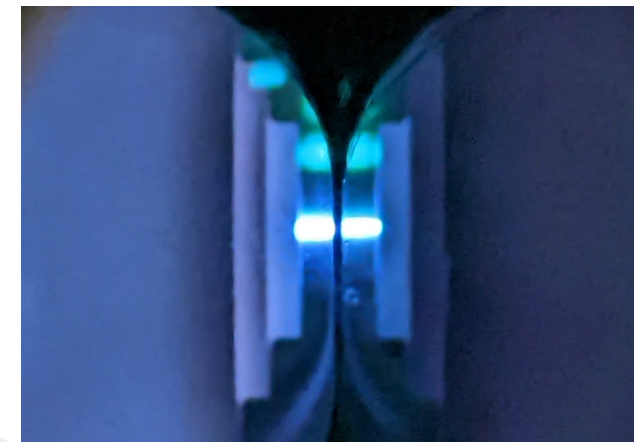
Thank you



Helium plasma
(with IR absorptive filter)



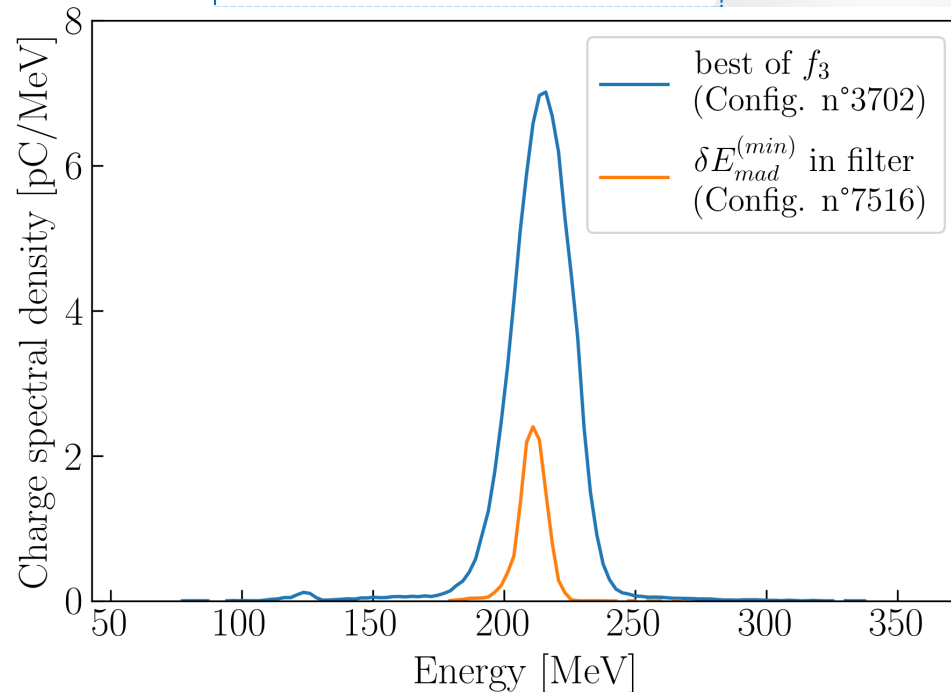
Helium plasma
(no IR absorptive filter)



N₂ plasma
(with IR absorptive filter)

Merci

We select 2 configurations



	Best of f_3 (high charge)	Lowest δE_{mad} in filter
N°	3702	7516
Scan origin	RS3	RS5
p [mbar]	58.6	47.8
a_0	1.43	1.23
X_{off} [μm]	558	1680
c_{N_2} [%]	1.88	6.17
$a_{0,\text{max}}$	3.73	2.58
Q [pC]	198	30
E_{med} [MeV]	215	212
δE_{mad} [%]	3.53	1.55
$\epsilon_{y,n}$ [μm]	5.03	1.74