Unclear title:

Solidifying vacuum: phase structure of the electroweak model in a strong magnetic field

Clarifying title:

Solidifying and evaporating vortex solid liquid — made, by the way, from nothing* possessing superconductivity and superfluidity at the same time** and all that requires just one simple ingredient: magnetic field*** ...

*) yes, vacuum is the most "nothing" of all available nothings
 **) yes, the transport should be <u>dissipationless</u>
 ***) disclaimer: to make all that we need strong magnetic field

Solidifying vacuum: phase structure of the electroweak model in a strong magnetic field

(first-principle results from lattice simulations)

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Department of Physics, West University of Timişoara, Romania Institut Denis Poisson, CNRS, Tours, France Motivation:

Check emergence of a superconducting phase due to vacuum instability in strong magnetic field background

Based on:

PHYSICAL REVIEW LETTERS 130, 111802 (2023)

Phase Structure of Electroweak Vacuum in a Strong Magnetic Field: The Lattice Results

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Scales of magnetic field in (particle) (astro)physics - I



(T = Tesla) 1 T = 10⁴ G (G = Gauss)

10° T – QED scale; the Schwinger limit $B^{\text{QED}} = \frac{m_{e}^{2}}{e} \simeq 4 \times 10^{9} \text{ T}$



SL Adler, Annals Phys. 67, 599 (1971)

 vacuum can act as a "magnetic lens" which is able to distort and magnify images



NJ Shaviv, JS Heyl, Y. Lithwick, MNRAS 306, 333 (1999) [astro-ph/9901376]

(similar to gravitational lens)



loudspeaker

NMR imaging



magnetar surfaces SA Olausen, VMKaspi, "The McGill magnetar catalog" AP SS 212, 6 (2015) [arXiv:1309.4167]



cores of magnetars

D Lai and SL Shapiro AJ 383, 745 (1991) CY Cardall, M Prakash, JM Lattimer AJ 554, 322 (2001) [astro-ph/0011148]

Images: Physics Today, Wikipedia, free resources

Scales of magnetic field in (particle) (astro)physics - II

$10^{16} T - QCD$ scale

$B^{\text{QCD}} = \frac{m_p^2}{e} \sim 10^{16} \,\text{T}$

- magnetic catalysis (enhancement of chiral symmetry breaking)
 SP Klevansky, RH Lemmer, Phys. Rev. D 39, 3478 (1989);
 KG Klimenko, Z. Phys. C 54, 323 (1992);
 great review: IA Shovkovy, Lect. Notes Phys. 871, 13 (2013).
- vacuum superconductivity?

MN Ch., Phys. Rev. D 82, 085011 (2010); PRL 106, 142003 (2011)



transient fields (10^{-24} s) in heavy-ion collisions

V Skokov, A Yu Illarionov, V Toneev, Int. J. Mod. Phys. A 24, 5925 (2009); WT Deng, XG Huang, Phys. Rev. C 85, 044907 (2012)

10²⁰ T – EW scale

$$B^{\rm EW} = \frac{m_W^2}{e} \sim 10^{20} \,\mathrm{T}$$

- change in vacuum structure

NK Nielsen, P Olesen, Nucl. Phys. B 144, 376 (1978);
VV Skalozub, Sov. J. Nucl. Phys. 28, 1 (1978);
VV Skalozub, Sov. J. Nucl. Phys. 28, 1 45, 6 (1987)
J Ambjorn, P Olesen, Phys. Lett. B 214, 565 (1988);
J Ambjorn, P Olesen, Nucl. Phys. B 315, 606 (1989)

Early Universe?

T Vachaspati, PLB 265, 258 (1991); D Grasso, HR Rubinstein, Phys. Rept. 348, 163 (2001)

you are here



Images: BNL, Physics Today

Scales of magnetic field in particle/astro-physics - III



Change of vacuum structure in strong magnetic field

1) QCD scale, B ~ 10¹⁶ T, associated with the ρ -meson condensation [M.Ch., PRD 80, 054503 (2009); PRL 106, 142003 (2011)]

possible weak crossover transition via inhomogeneous condensation of composite ρ -meson states, difficult to see – not this talk

2) EW scale, B ~ 10²⁰ T, proceeds via the W boson condensation [J. Ambjorn, P. Olesen, PLB 214, 565 (1988); NPB 315, 606 (1989)

inhomogeneous condensation, looks classical, easy, indisputable — this talk

more interesting, in fact

Free charged spin-1 relativistic particle in magnetic field

- Energy of a relativistic particle in the external magnetic field B_{ext} :

$$\varepsilon_{n,s_z}^2(p_z) = p_z^2 + (2n - 2s_z + 1)eB_{\text{ext}} + m^2$$

momentum along the magnetic field axis non

nonnegative integer number th

0

projection of spin on the magnetic field axis

Critical magnetic field:

 $eB_c = m^2$

(the external magnetic field is directed along the *z*-axis)

Instability for quantum numbers:

 $p_z = 0; n = 0; s_z = +1$

For *W* bosons (if we disregard interactions):

$$M_W^2(B) = M_W^2 - |eB|$$

The critical field is:

$$B_c^{\rm EW} = \frac{M_W^2}{e} \simeq 1.1 \times 10^{20} \,\mathrm{T}$$

Electroweak vacuum should become unstable toward W condensation!

Vacuum instability, what is the nature of the new phase?

... the one which is just about the (first) critical field.

1) Condensation of W bosons

[VV Skalozub (1987); J Ambjorn, P Olesen (1988), (1989)]

2) Vacuum superconductivity

[M.Ch., PRD 80, 054503 (2009)]

Vacuum should enter the new exotic phase which

- a) is anisotropically superconducting
- **b) but does not possess Meissner effect**

(= no screening of magnetic field by a charged condensate)

Superconductivity of the vacuum is interesting and nontrivial phenomenon. The first step to establish the vacuum superconductivity is to make sure that

1) the vacuum instability towards the new phase exists;

- 2) the new phase has appropriate condensates (consistent with the theory);
 - → aim of this work

What theory says about the phase structure?

(Weinberg-Salam model in strong magnetic field at T=0)



$$\begin{array}{lll} \mbox{EW Lagrangian:} & \mathcal{L} = -\frac{1}{4} W^a_{\mu\nu} W^{a,\mu\nu} - \frac{1}{4} X_{\mu\nu} X^{\mu\nu} + (D_\mu \Phi)^{\dagger} (D^\mu \Phi) - \lambda \left(|\Phi|^2 - v^2/2 \right)^2 \\ & D_\mu = \partial_\mu - ig \tau^a W^a_\mu / 2 - ig' X_\mu / 2 \\ & W^a_{\mu\nu} = \partial_\mu W^a_\nu - \partial_\nu W^a_\mu + g \epsilon^{abc} W^b_\mu W^c_\nu \\ & X_{\mu\nu} = \partial_\mu X_\nu - \partial_\nu X_\mu \end{array} \begin{array}{ll} \mbox{Particles:} \\ & W^a_\mu - W \mbox{-bosons (massive vector),} \\ & Z_\mu - Z \mbox{-boson (massive vector),} \end{array}$$

Ordinary vacuum, symmetry breaking:

$$SU(2)_L \times U(1)_X \rightarrow U(1)_{\rm em}$$

- A_{μ} photon (massless vector),
- Φ Higgs particle (massive scalar)

Superconducting phase, what to expect (theory)

Solution of classical equations of motion (at a set of Higgs masses) Transition at the vicitiny of the first critical field: $B_c = M_W^2/e$



[J Van Doorsselaere, H Verschelde, M.Ch., PRD 88, 065006 (2013)]



Superconducting phase, inhomogeneity (theory)

Vortex structure in superconducting (W) and superfluid (Z) condensates



[Jos Van Doorsselaere, Henri Verschelde, M.Ch., Phys. Rev. D 88, 065006 (2013)]

Visually (and distantly) similar but physically very different from the Abrikosov lattice in type-2 superconductors

Theoretical expectations based on classical equations of motion:

- -Magnetic field leads to condensation of charged W bosons
- -Condensation of the W's leads to a condensation of neutral Z bosons
- → Coexisting superconducting and superfluid condensates

Our Aim No. 2: Check the nature of the (superconducting? - check) phase

"Reality = classical picture + quantum fluctuations"

(+ magnetic-field-induced vortex lattice will vibrate and generate phonon modes!)

Check the picture in first-principle lattice simulations



Wilson: $S_W = \sum_{plaquettes} S_P$, where $S_P = \beta \left(1 - \frac{1}{N} Re Tr U_P\right)$

Electroweak theory on the lattice

- fermions play no essential role in the mechanism, we exclude them

background hypermagnetic field gives magnetic field in the broken phase
 Dynamical fields:

•
$$U_{x,\mu} = \exp\left(i\frac{\sigma_i}{2}W_{x,\mu}^i\right) \in SU(2)$$
 • $\theta_{x,\mu} \in \mathcal{R}$ • $\phi_x = \begin{pmatrix} \phi_{1,x} \\ \phi_{2,x} \end{pmatrix}$

$$S = \beta \sum_{x,\mu < \nu} \left(1 - \frac{1}{2} \operatorname{Tr} U_{x,\mu\nu} \right) + \frac{\beta_Y}{2} \sum_{x,\mu < \nu} \theta_{x,\mu\nu}^2 \quad \text{(gauge)}$$
$$+ \sum_x \left(-\kappa \phi_x^{\dagger} \phi_x + \lambda \left(\phi_x^{\dagger} \phi_x \right)^2 \right) \quad \text{(Higgs)}$$
$$+ \sum_{x,\mu} \left| \phi_x - e^{i \left(\theta_{x,\mu} + \theta_{x,\mu}^B \right)} U_{x,\mu} \phi_{x+\hat{\mu}} \right|^2 \quad \text{(interaction)}$$

Boundary condition: periodic Magnetic field : along Z direction Lattice size: 64×48^3

Parameters: β , β_Y , κ , λ , $\theta^B_{x,\mu}$. Where is physical point?

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Pioneering study: high temperature, 3d dimensionally reduced model around the EW crossover: K Kajantie, M Laine, J Peisa, K Rummukainen, and ME Shaposhnikov, Nucl. Phys. B 544, 357 (1999) [arXiv:hep-lat/9809004]

Finding a physical point

 $e \approx 0.303$ $m_H \approx 125.3 \text{ GeV}$ $g \approx 0.642$ $m_Z \approx 91.2 \text{ GeV}$ $g' \approx 0.344$ $m_W \approx 80.4 \text{ GeV}$ $\sin^2 \theta_W \approx 0.223$ Fix κ , λ , β , β_Y to find physical point.

Four lattice couplings fix the three physical masses (W,Z,H) as well as the lattice spacing *a*.





Introducing (hyper)magnetic field

- Magnetic field has a sense only in the broken phase
- We introduce the hypermagnetic field B_Y associated with $U(1)_Y$ symmetry:
 - it gives the magnetic field in the broken phase $g'B_Y = eB$
 - a genuine field in the unbroken phase (presumably, at high B_{Y})

On the periodic lattice of size $L_s^3 \times L_t$, the total magnetic flux is quantized.

The background magnetic field:

$$B_Y = (0, 0, B_Y), \qquad B_Y = \frac{2}{g'} \cdot \frac{2\pi k}{(L_s a)^2}$$

magnetic number: $k \in \mathbb{Z}$ number of elementary fluxes: 2k

For chosen lattice spacing ($m_H a \simeq 0.3$), for our lattice ($48^3 \times 64$) one gets elementary step (resolution) in magnetic field: $\delta B_Y \simeq 0.15 m_W^2/g'$ or $\delta B \simeq 0.15 m_W^2/e$

Mean Higgs condensate in (hyper)magnetic field



Result 2. The strength: both transitions are smooth crossovers, no singularity. Expectations, classical approach: the transition is of the <u>second</u> order perturbation theory: the transition is of the <u>first</u> order \checkmark Reality, first-principle simulations: the transition is of the <u>infinite</u> order (crossover) Result 3. The high-field phase ($B > B_{c2}$): symmetry-restored phase, OK with theory.

General view - I



General view - II

Z-vortex condensate





a cross-section of a typical configuration in the xy plane

General view - III



Not a "usual" type-II superconductor: magnetic field is strong
 <u>outside</u> the vortex cores and it is suppressed inside the vortices!

a cross-section of a typical configuration in the xy plane

Nature of the intermediate phase

 $eB = 1.1M_W^2$ $B_{c1} < B < B_{c2}$



The blue (green) surfaces denote the equipotential surfaces of the W condensate (the Higgs condensate).

The lines denote the lines of the hypermagnetic field.

Result 4. No crystalline order for vortices (presumably, due to quantum fluctuations). (Classical) theory predicts the hexagonal vortex solid. Not OK with theory. The vacuum presumably becomes a liquid made of vortices.

No vortex lattice

No clear vortex lattice at the physical point (at physical parameters)



ordered (lattice) vortex state

perturbed (liquid/gas) state

Compare with the unphysical ("more classical") case **Fluctuations of Higgs (superconducting phase)**



Conclusions

- 1. We found the phase structure of zero-temperature electroweak theory in the magnetic-field background from first-principle lattice simulations
- 2. The phase structure is qualitatively consistent with the theory based on solutions of classical EW equations of motions



- 3. Some differences with the theory, the role of quantum fluctuations is crucial:
 - vortices share some similarities with the Ambjorn-Olesen solution
 - no crystal lattice formation (of the Abrikosov type)
 - the vortices form either gas or liquid (fluctuating vortex medium)
 - the transitions are not phase transitions but the smooth crossovers (difficult/impossible to see from thermodynamics)
 quenched QCD
- 4. A similar phase in QCD at strong magnetic field? (no phase transition, a smooth appearance of the inhomogeneous phase).

[Braguta et al. PoS LATTICE2013 (2014) 362]

