

History of a hot hidden dark sector

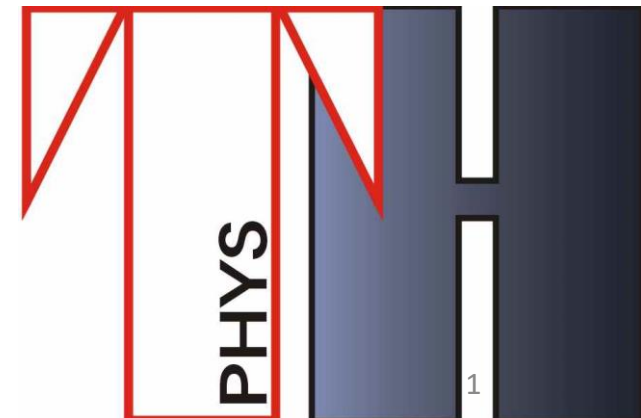
Jean Kimus,
Michel H. G. Tytgat,
Rupert Coy



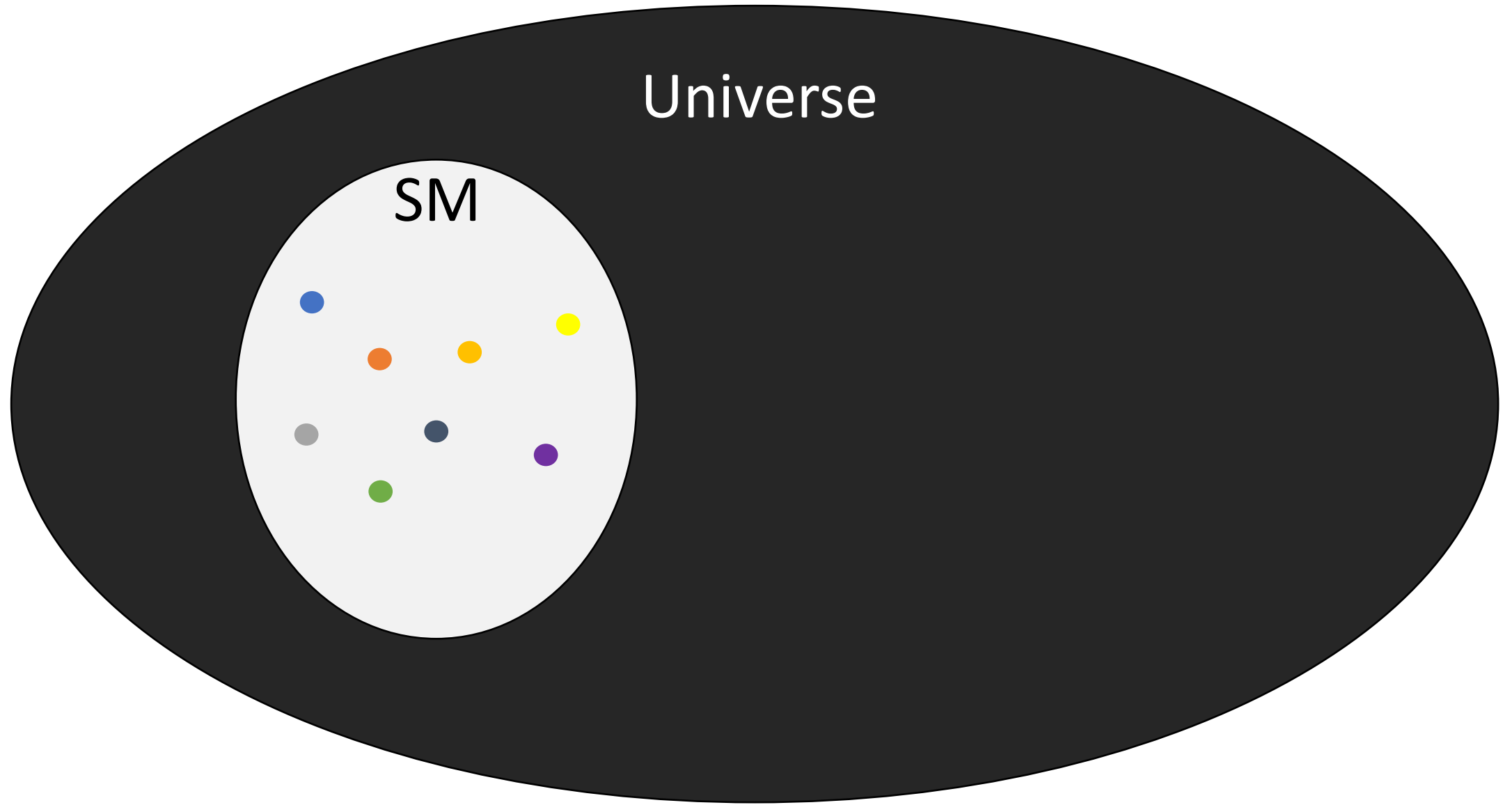
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AstroParticle Symposium 2023

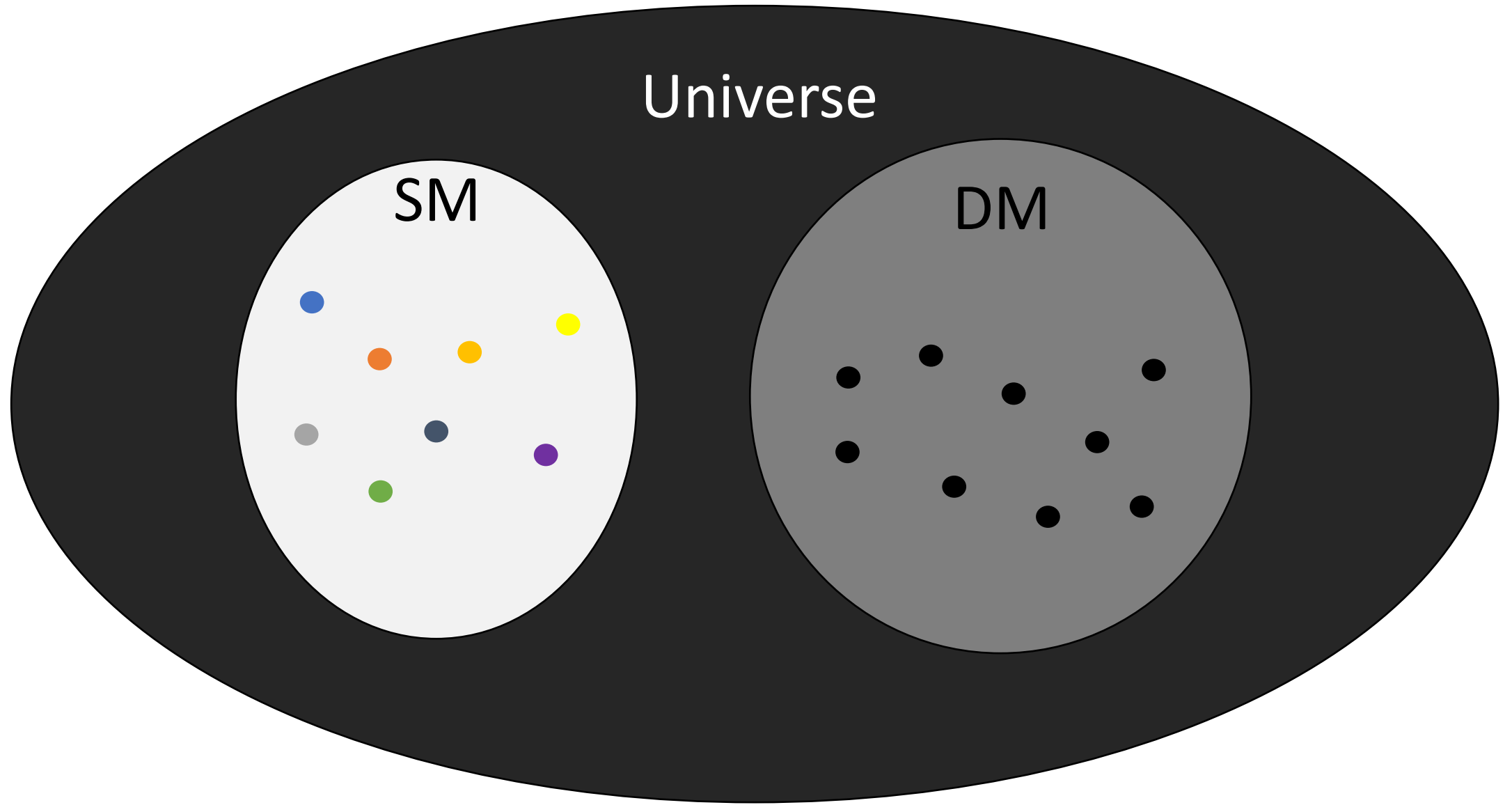
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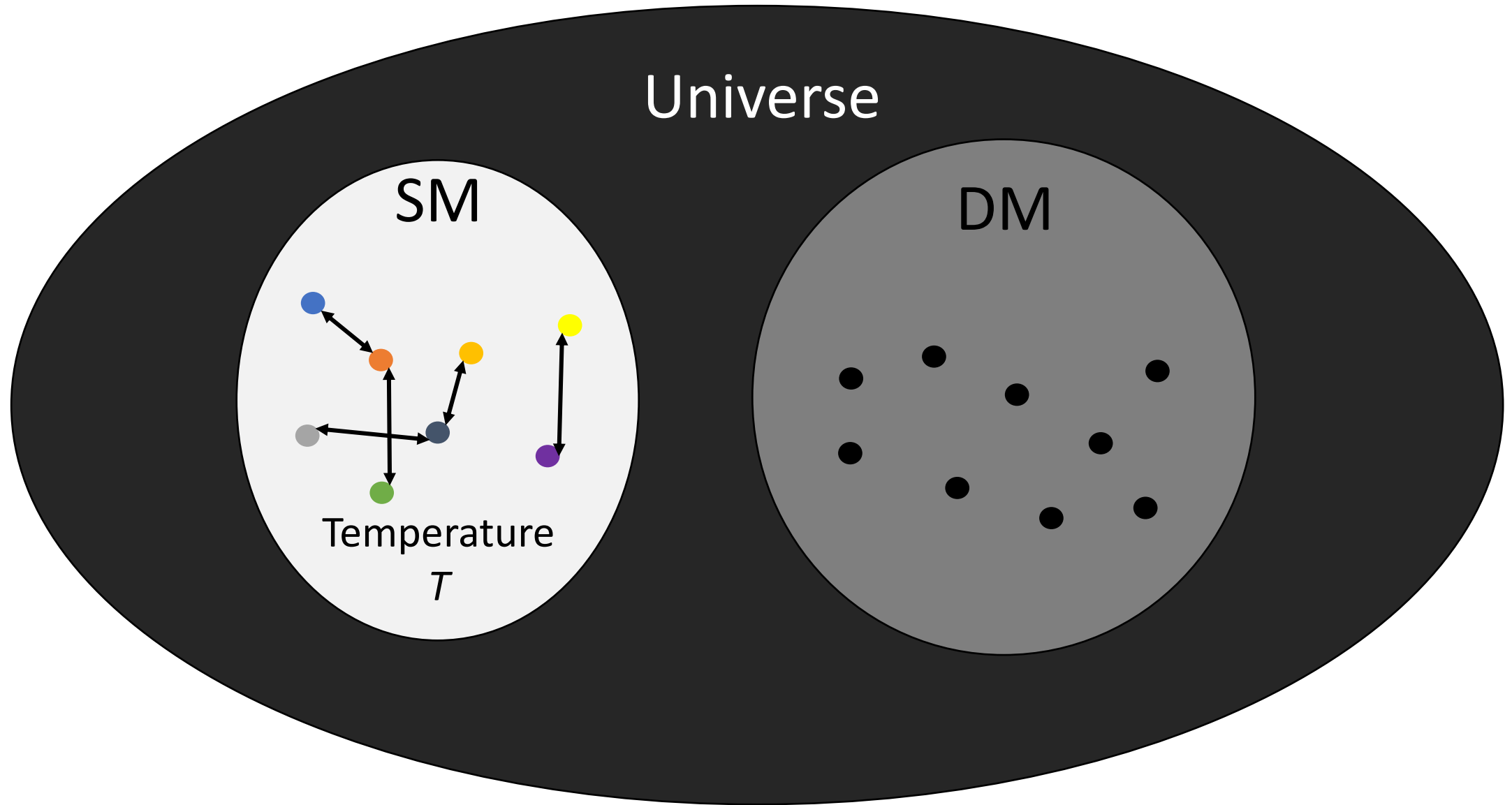
Introduction



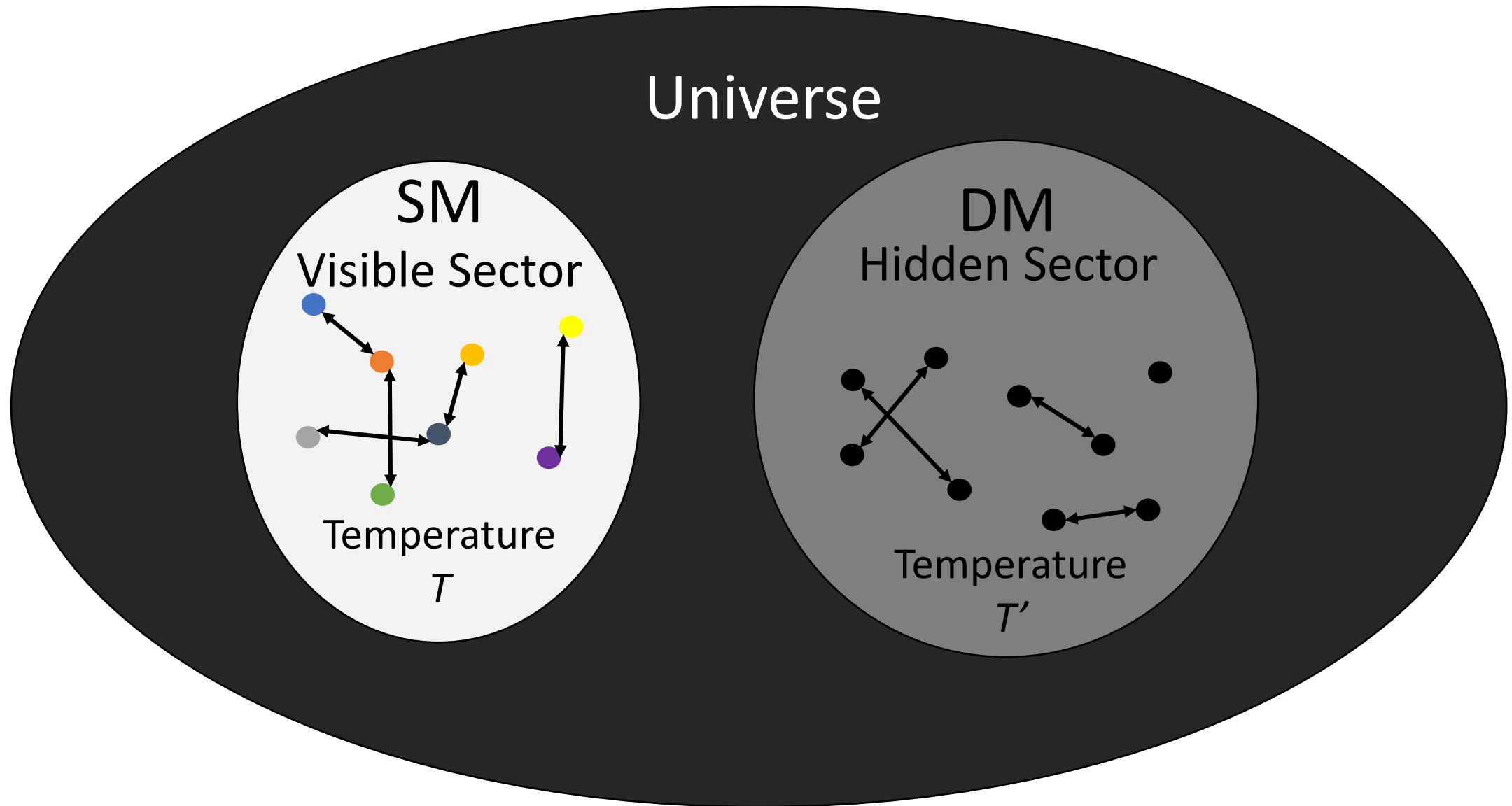
Introduction



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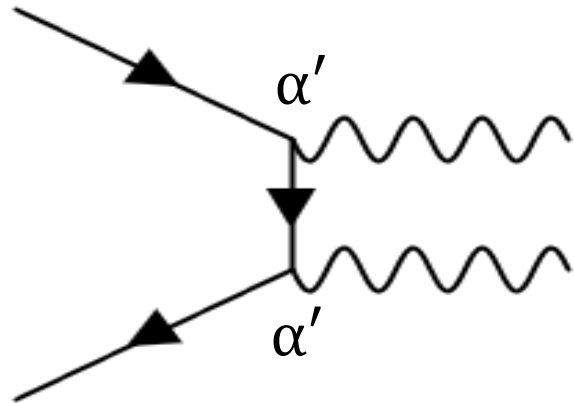
Introduction



Dark QED

$$\mathcal{L} \supset \bar{\chi}(i\not{D}-m_{\text{dm}})\chi - \frac{1}{4}F'_{\mu\nu}F'^{\mu\nu} + \frac{1}{2}m'^2 A'_\mu A'^\mu - \frac{\varepsilon}{2}B_{\mu\nu}F'^{\mu\nu}$$

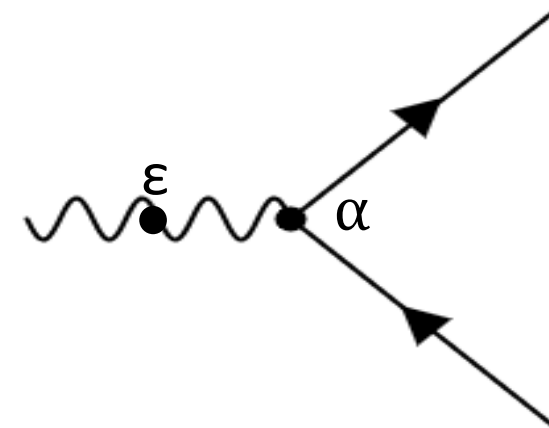
DM annihilation into DP:



Leading process for **dark matter Freeze-out**

(1112.0493, Chu et al.)

DP decay into SM fermions



Leading process for **dark photon evolution** after DM freeze-out

(1605.07195, Berger et al.)₆

Boltzmann equations

3 parameters : $(T, T', \mu) \rightarrow$ 3 equations:

- ρ_t : Total energy density
- ρ' : Dark photon energy density
- n' : Dark photon number density

Γ' = Dark photon decay width

H = Hubble parameter

ω = state parameter

$$\frac{d\rho_t}{dt} + 3(1 + \omega_t)H\rho_t = 0$$

Total energy density

$$\frac{dn'}{dt} + 3Hn' = \langle \Gamma' \rangle_T n'_{\text{eq}}(T) - \langle \Gamma' \rangle_{T'} n'$$

Dark Photon number density

$$\frac{d\rho'}{dt} + 3(1 + \omega')H\rho' = m'\Gamma' [n'_{\text{eq}}(T) - n']$$

Dark Photon energy density

Numerical solutions (dominant hidden sector)

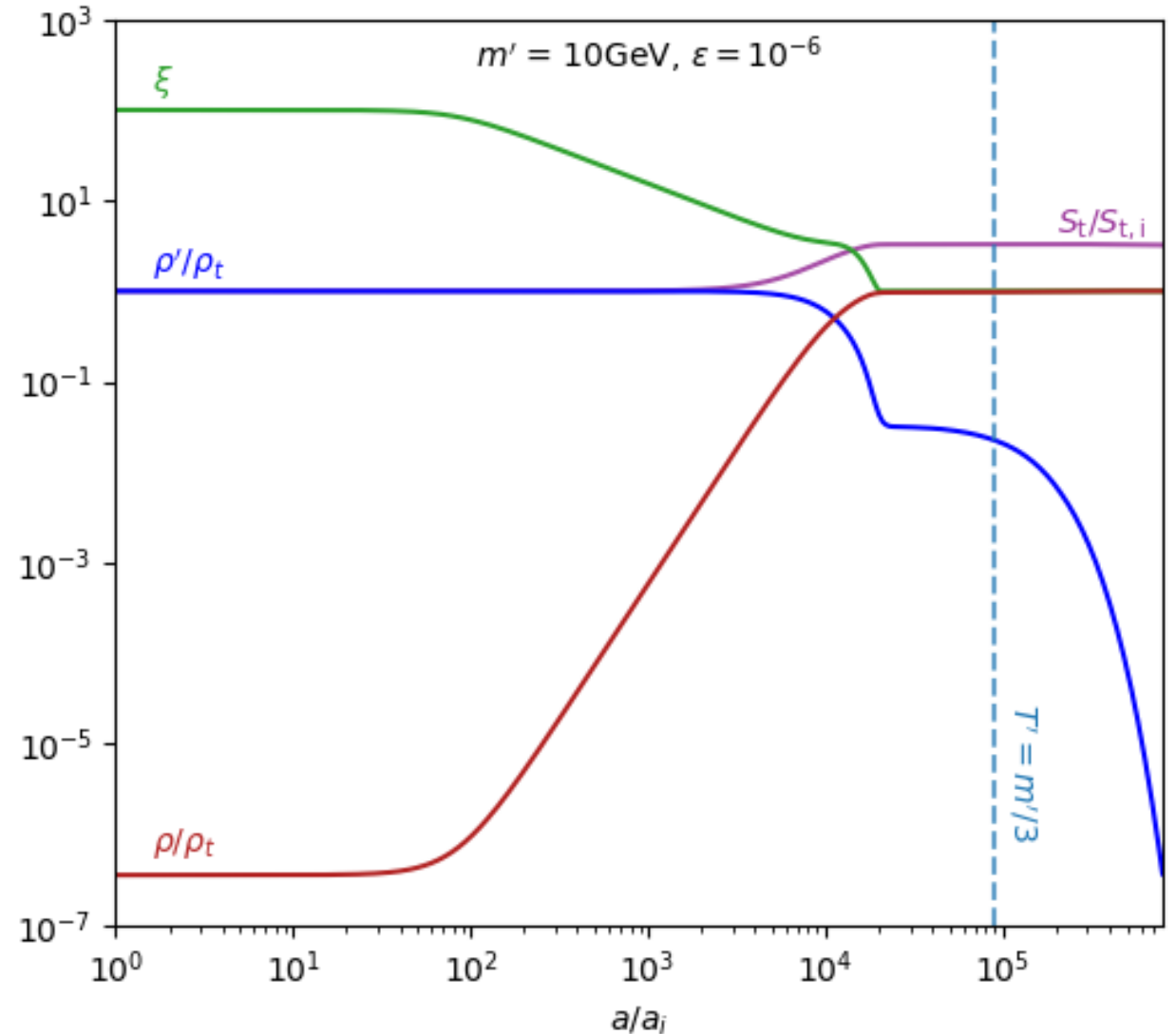
Important parameters to track

- Temperature ratio $\xi = T'/T$
- Energy density fractions ρ'/ρ_t and ρ/ρ_t
- Total entropy production factor $S_t/S_{t,i}$

Relativistic decay:

$$\frac{S_{t,f}}{S_{t,i}} \approx \frac{S_f}{S'_i} \approx \left(\frac{g_*}{g'_*} \right)^{1/4}$$

Decay of a relativistic dark photon



Numerical solutions (dominant hidden sector)

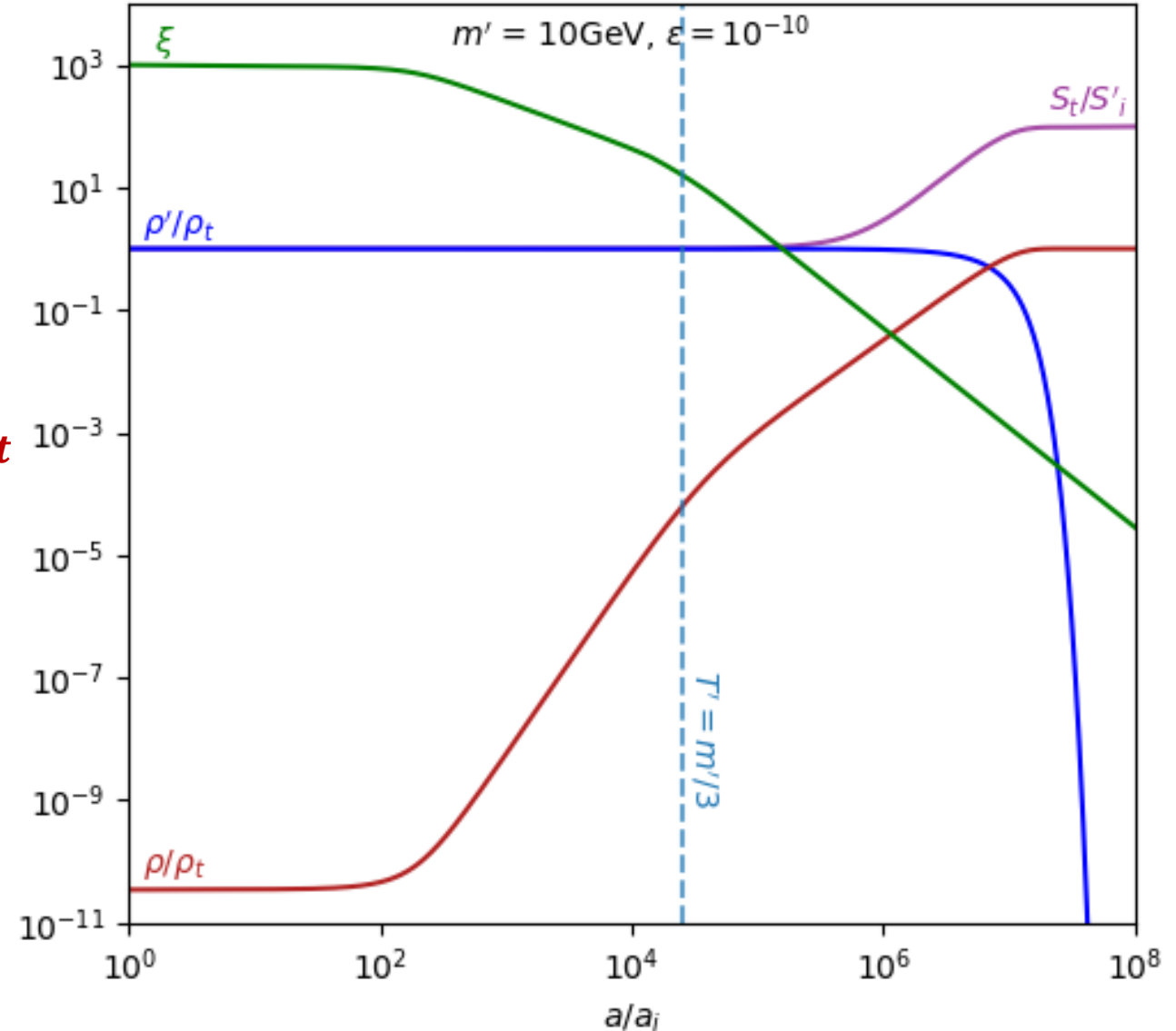
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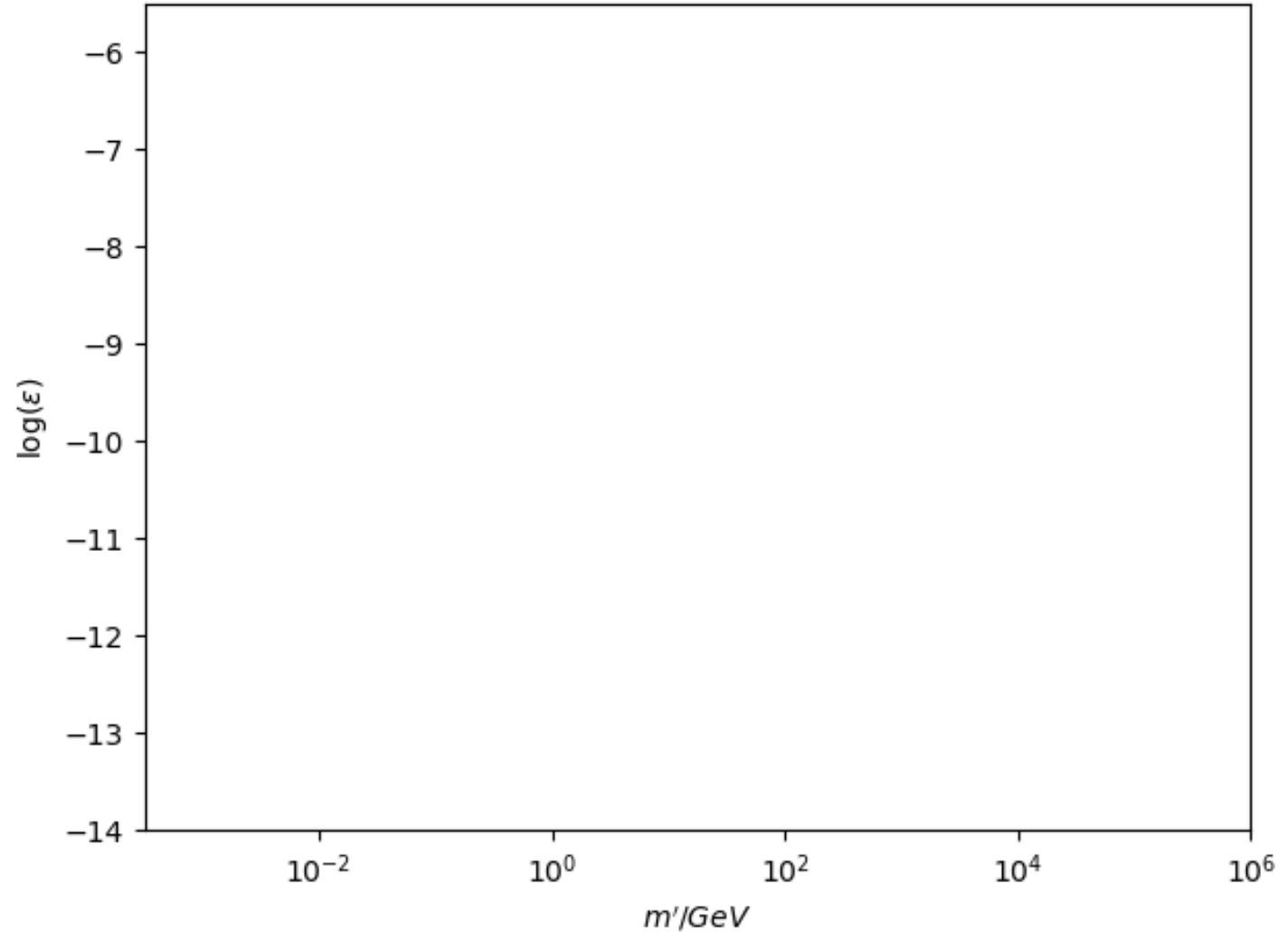
Nonrelativistic decay:

$$\frac{S_{t,f}}{S_{t,i}} \approx \frac{S_f}{S_i} \approx \left(\frac{g_*}{g'_*}\right)^{1/4} \left(\frac{\tau'}{t_{\text{nr}}}\right)^{1/2}$$

Decay of a non-relativistic dark photon



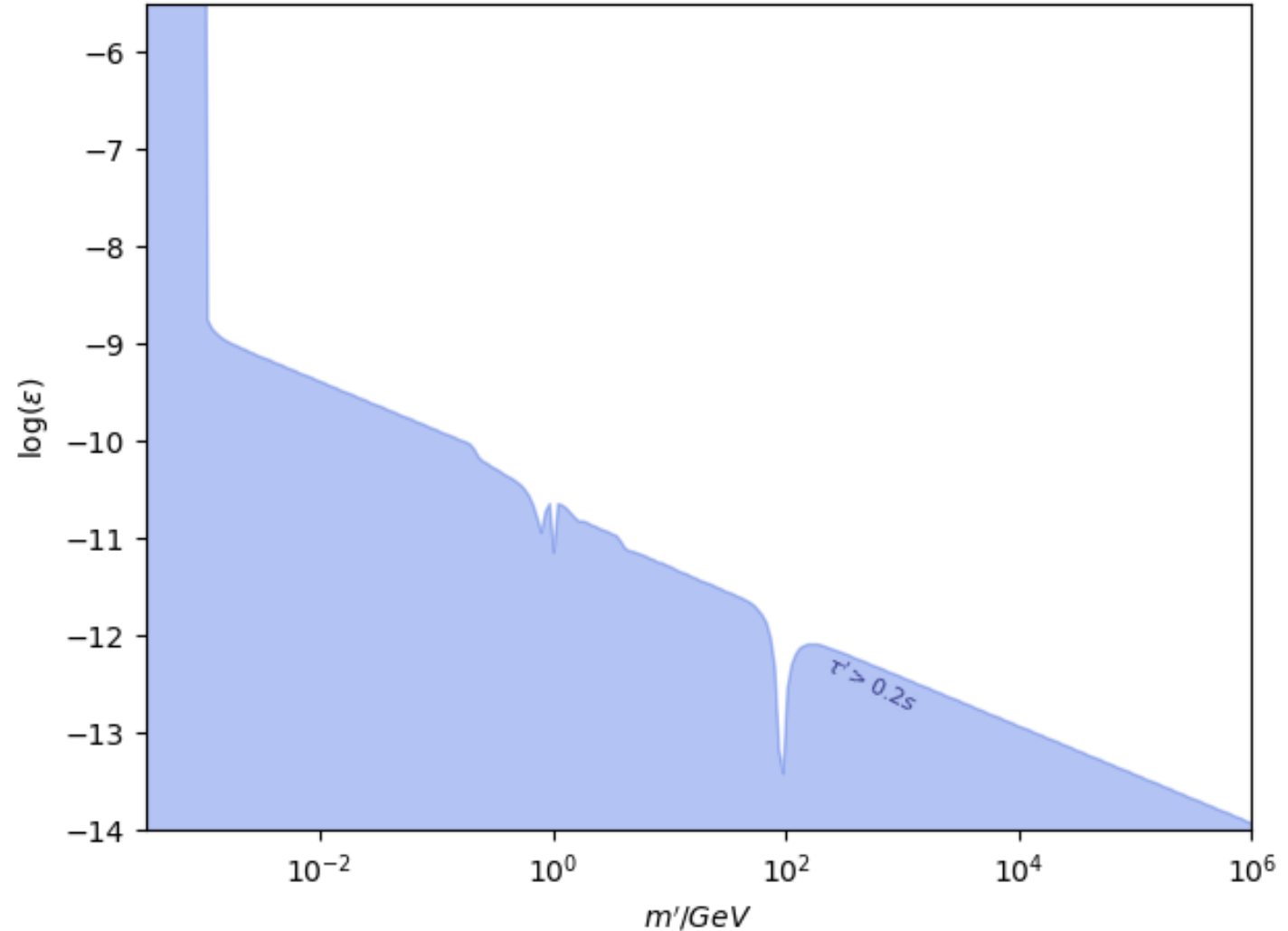
Constraints on the Dark photon characteristics In a dominant Hidden sector ($\xi \gg 1$)



Constraints on the Dark photon characteristics In a dominant Hidden sector ($\xi \gg 1$)

- Decay before BBN :

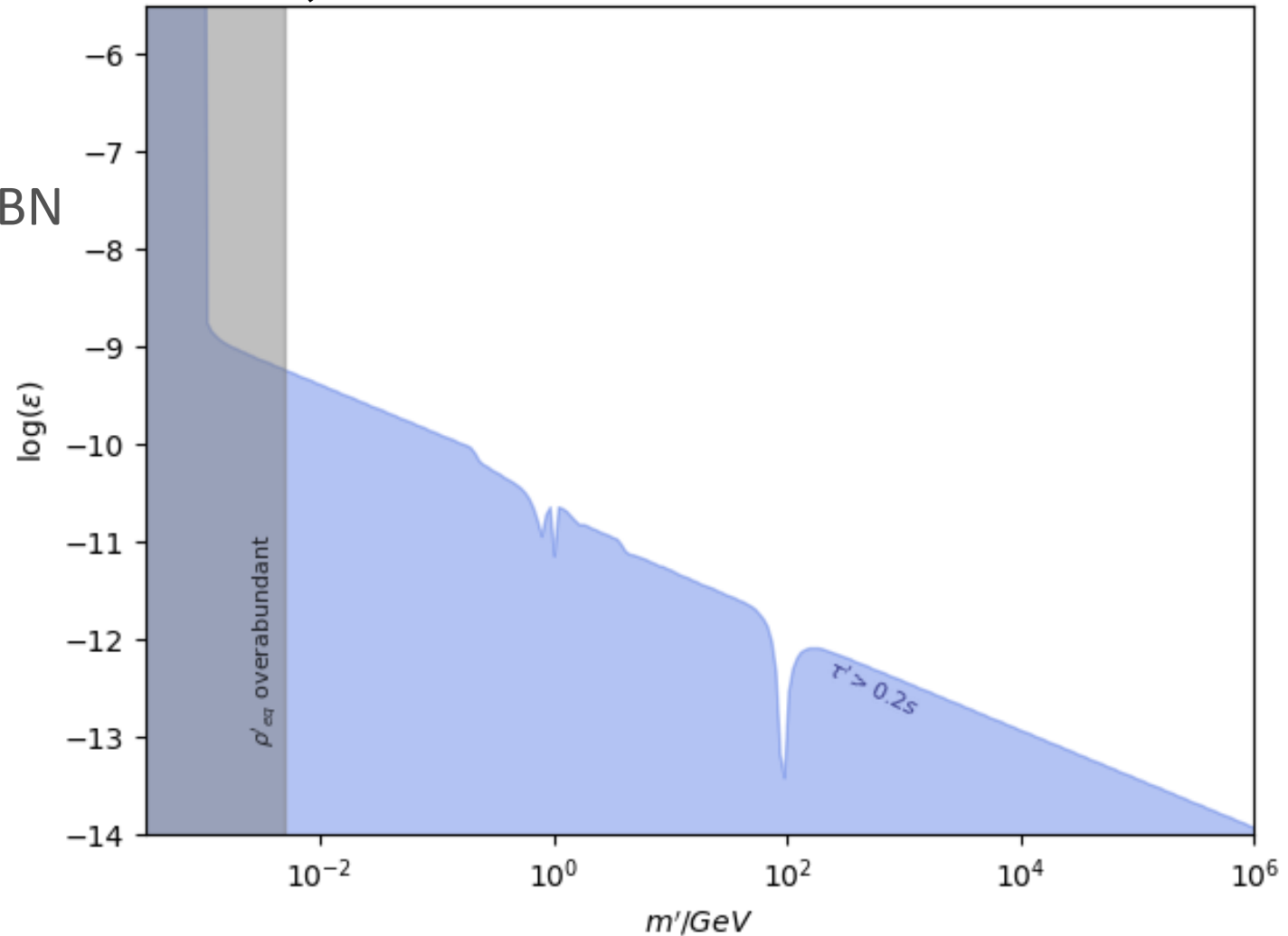
$$\Gamma' \sim \varepsilon^2 m' > \frac{1}{0.2s}$$



Constraints on the Dark photon characteristics In a dominant Hidden sector ($\xi \gg 1$)

- Decay before BBN
- Equilibrium density underabundant at BBN
(1712.03972, Hufnagel et al.):

$$\rho'_{eq}(T_{BBN}) < 0.04 \rho_{eq}(T_{BBN})$$

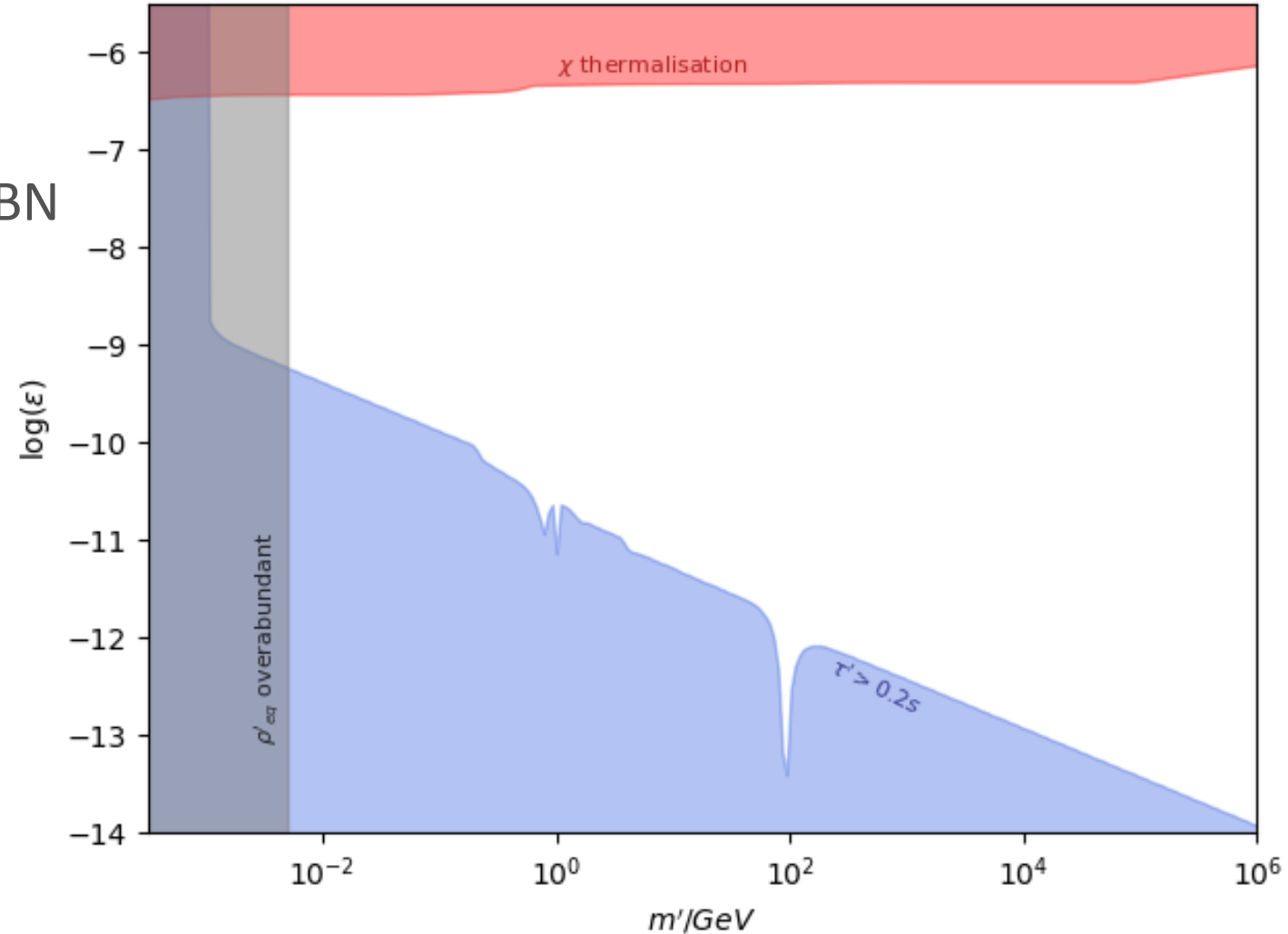


Constraints on the Dark photon characteristics

In a dominant Hidden sector ($\xi \gg 1$)

- Decay before BBN
- Equilibrium density underabundant at BBN (1712.03972, Hufnagel et al.)
- Non thermalisation of DM before FO:

$$\frac{n_\chi \langle \sigma_{\chi\bar{\chi} \rightarrow f\bar{f}\nu} \rangle_{FO}}{H_{FO}} < 1$$

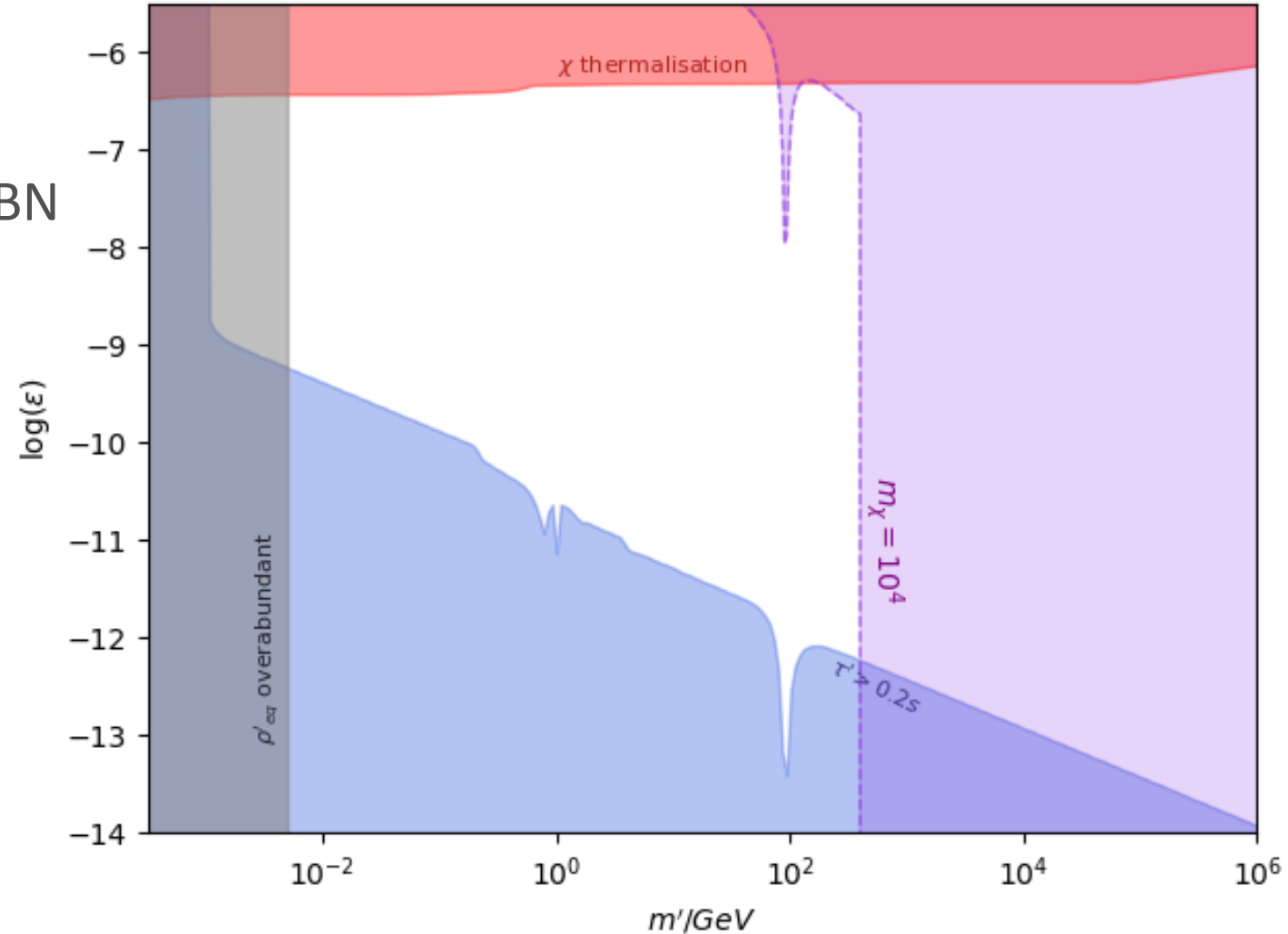


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$$\frac{\langle \Gamma' \rangle_{FO}}{H_{FO}} < 1$$

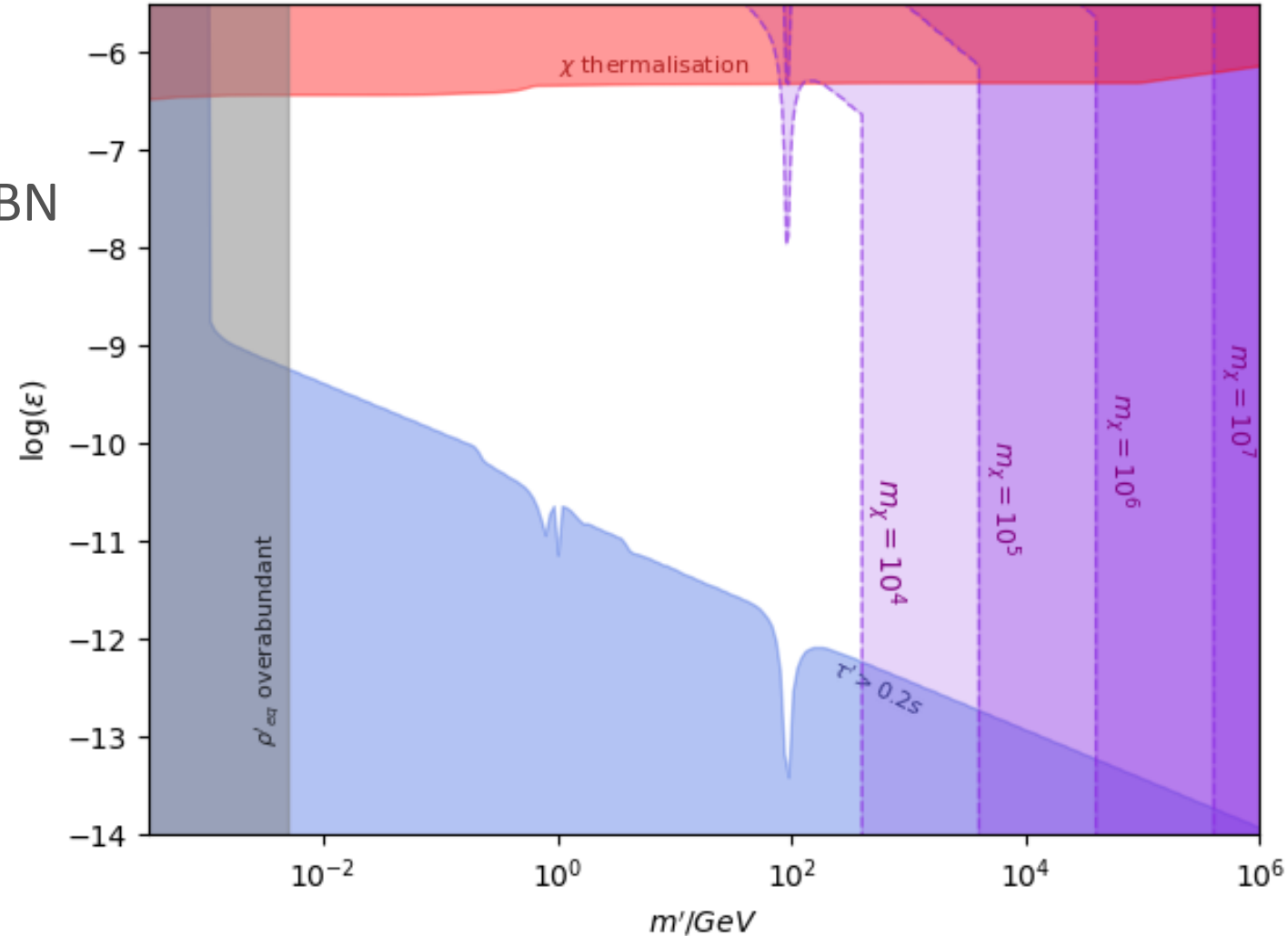


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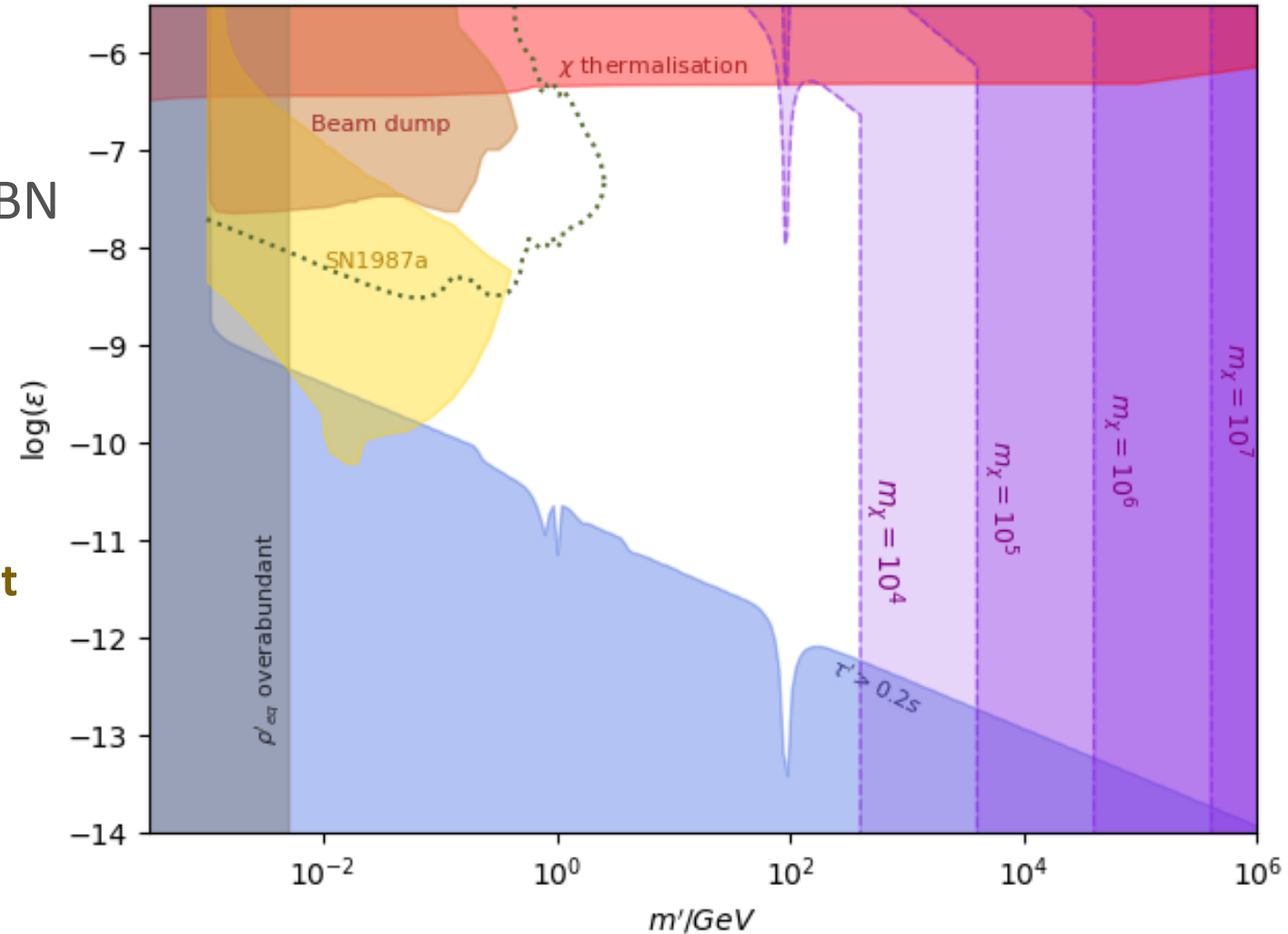
$$\left[\begin{array}{l} \frac{\langle \Gamma' \rangle_{FO}}{H_{FO}} < 1 \\ m_{\gamma'} < m_{\chi} / x'_{FO} \end{array} \right.$$



Constraints on the Dark photon characteristics

In a dominant Hidden sector ($\xi \gg 1$)

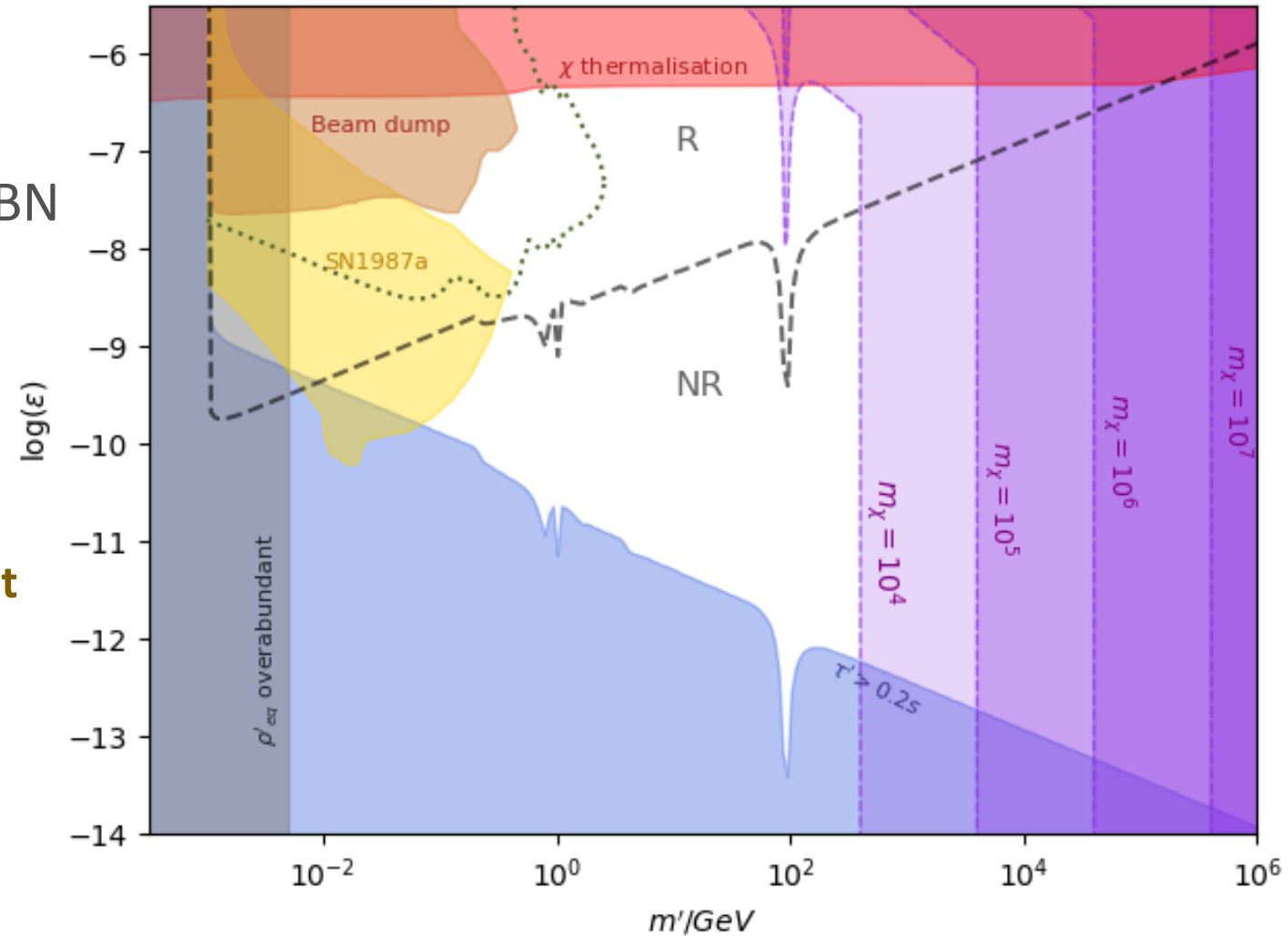
- Decay before BBN
- Equilibrium density underabundant at BBN (1712.03972, Hufnagel et al.)
- Non thermalisation of DM before FO
- Non thermalisation of DP before FO
- Present (and future) experimental and observational bounds (1611.05852, Hardy et al., 1803.05466, Bauer et al.)



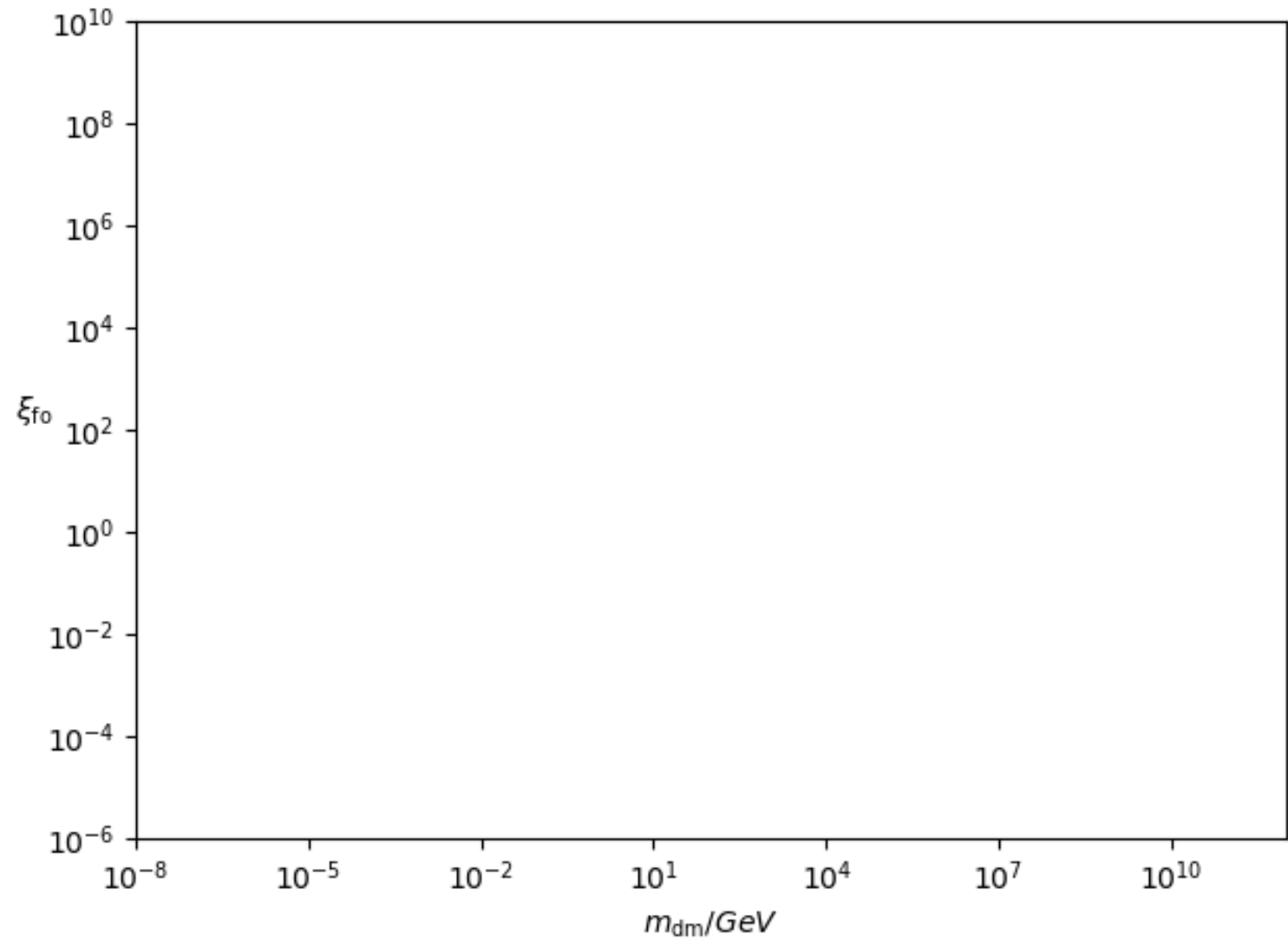
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- Present (and future) experimental and observational bounds (1611.05852, Hardy et al., 1803.05466, Bauer et al.)
- Classification of points corresponding to Relativistic (R) and Non Relativistic (NR) decay



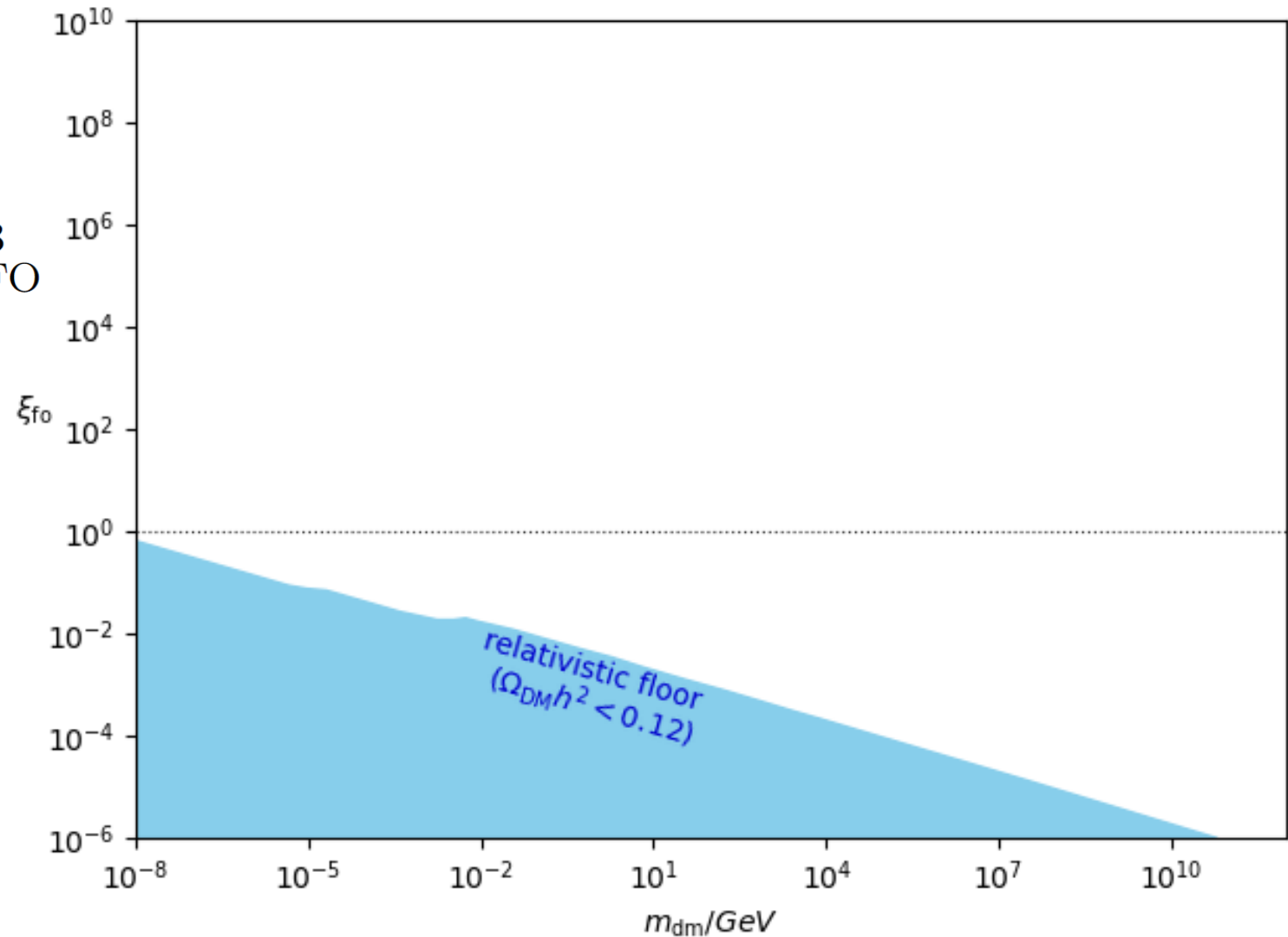
Constraints on the dark matter domain



Constraints on the dark matter domain

- Relativistic freeze-out: maximal relic density

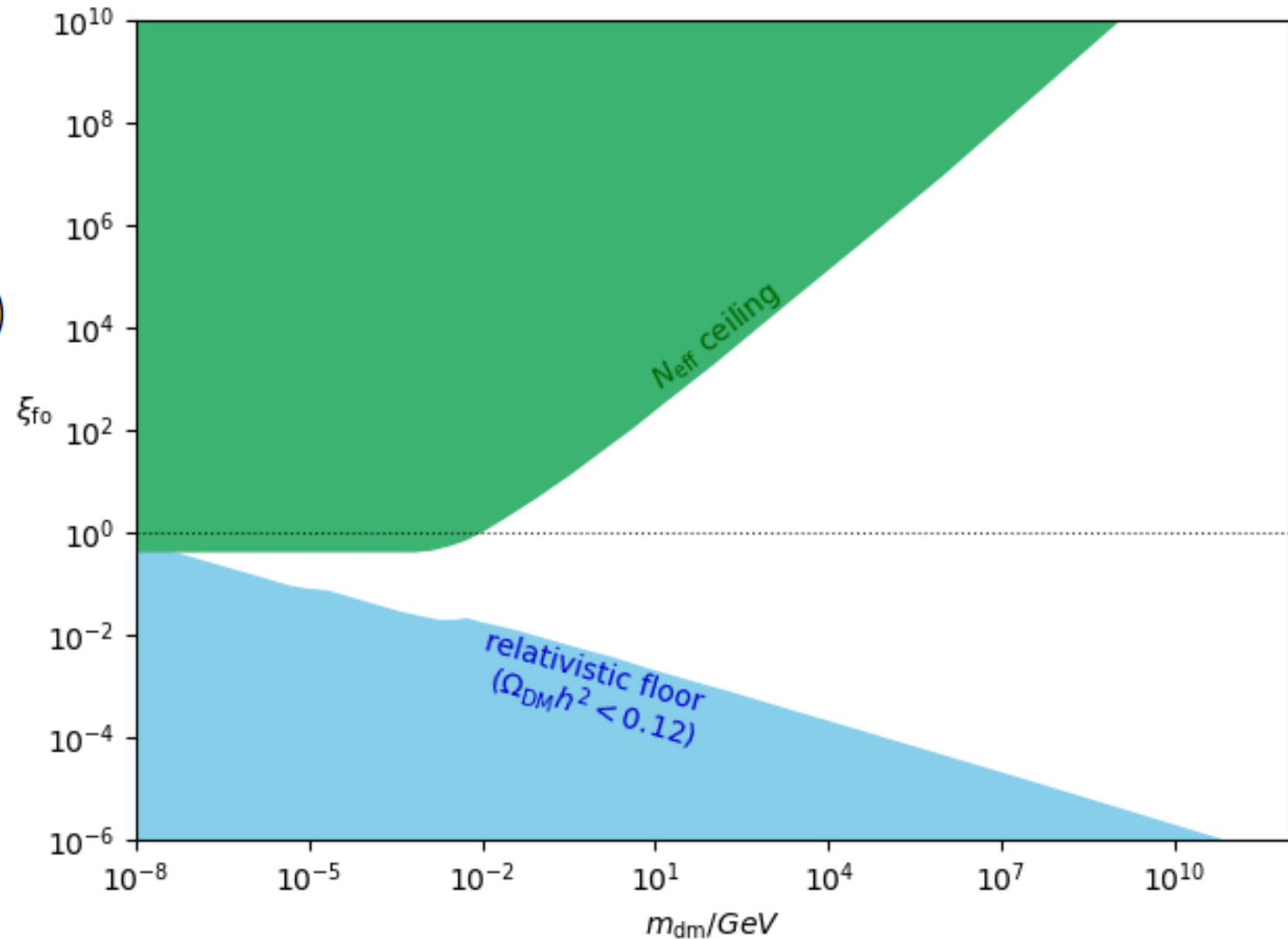
$$\Omega_\chi h^2 = 0.12 \left(\frac{g_{*s,0}}{g_{*s,\text{FO}}} \right) \left(\frac{m_\chi}{6\text{eV}} \right) \xi_{\text{FO}}^3$$



Constraints on the dark matter domain

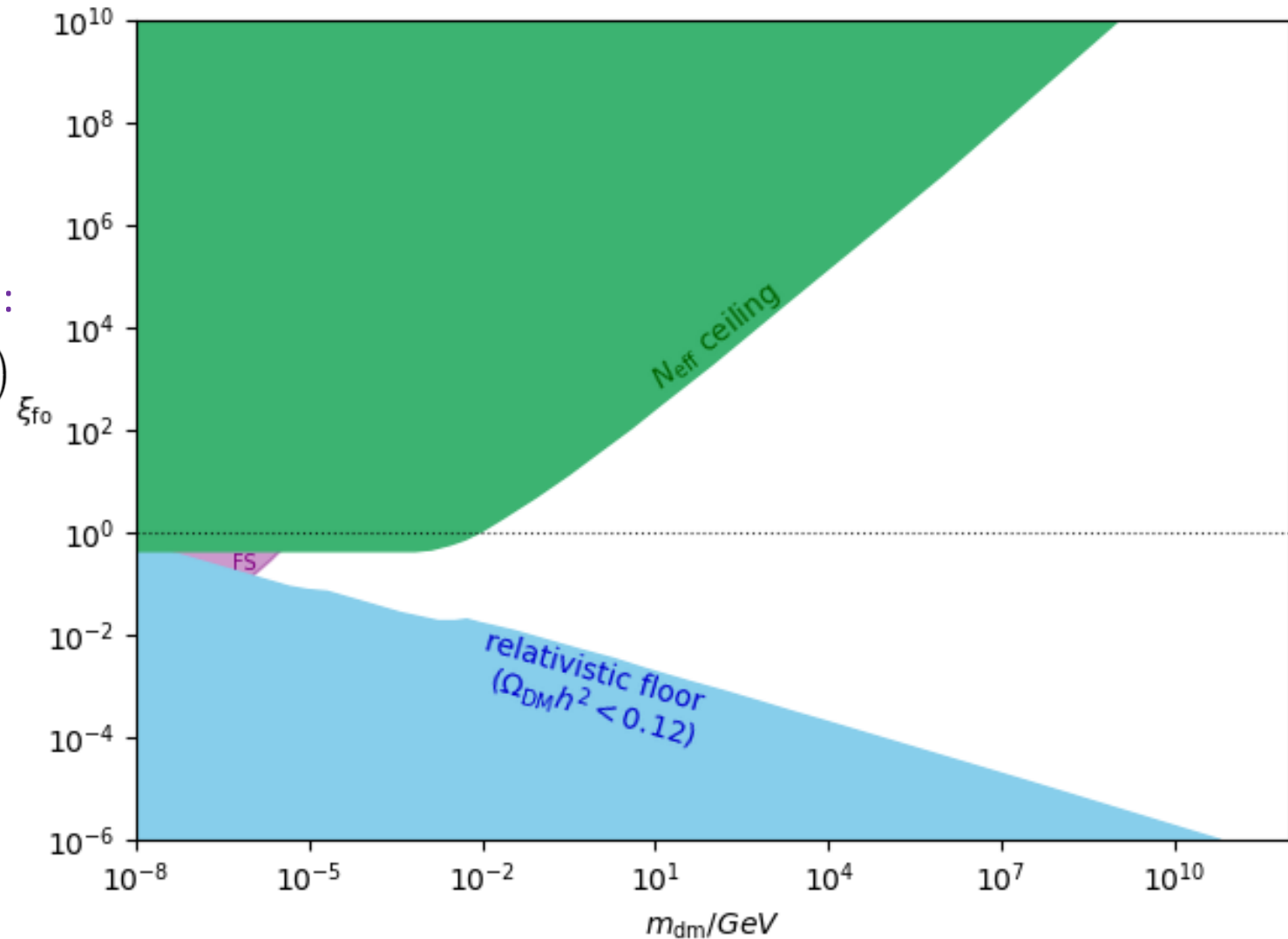
- Relativistic freeze-out: maximal relic density
- Non-dominating DM during BBN

$$\xi \lesssim m_\chi/\text{MeV} \quad (\text{if } m_\chi \geq \text{MeV})$$



Constraints on the dark matter domain

- Relativistic freeze-out: maximal relic density
- Non-dominating DM during BBN
- Upper limit on the free-streaming (FS) length:
 $\lambda_{\text{FS}} \propto \xi/m_\chi \lesssim 0.066\text{Mpc} \quad (\xi < 1)$

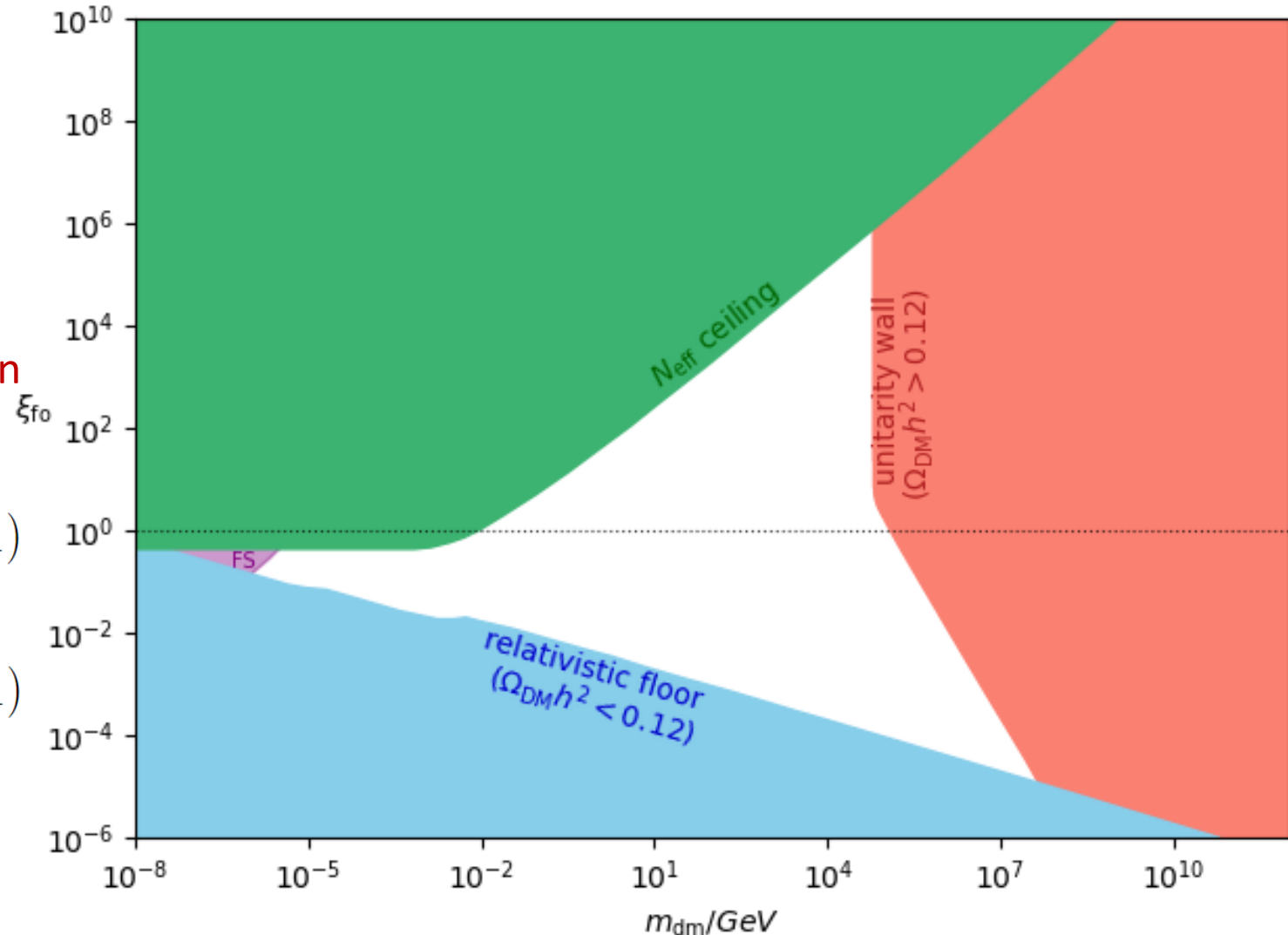


Constraints on the dark matter domain

- Relativistic freeze-out: maximal relic density
- Non-dominating DM during BBN
- Upper limit on the free-streaming (FS) length
- Non-relativistic FO with maximal cross section (unitarity): minimal relic density

$$\Omega_\chi h^2 \simeq 1.6 \times 10^8 \frac{x'_{\text{FO}}{}^{1/2} m_\chi^2}{m_{\text{Pl}} \sqrt{g_*}} \xi_{\text{FO}} \quad (\xi_{\text{FO}} \ll 1)$$

$$\Omega_\chi h^2 \simeq 1.6 \times 10^8 \frac{x'_{\text{FO}}{}^{1/2} m_\chi^2}{m_{\text{Pl}} \sqrt{g_*'}} \quad (\xi_{\text{FO}} \gg 1)$$

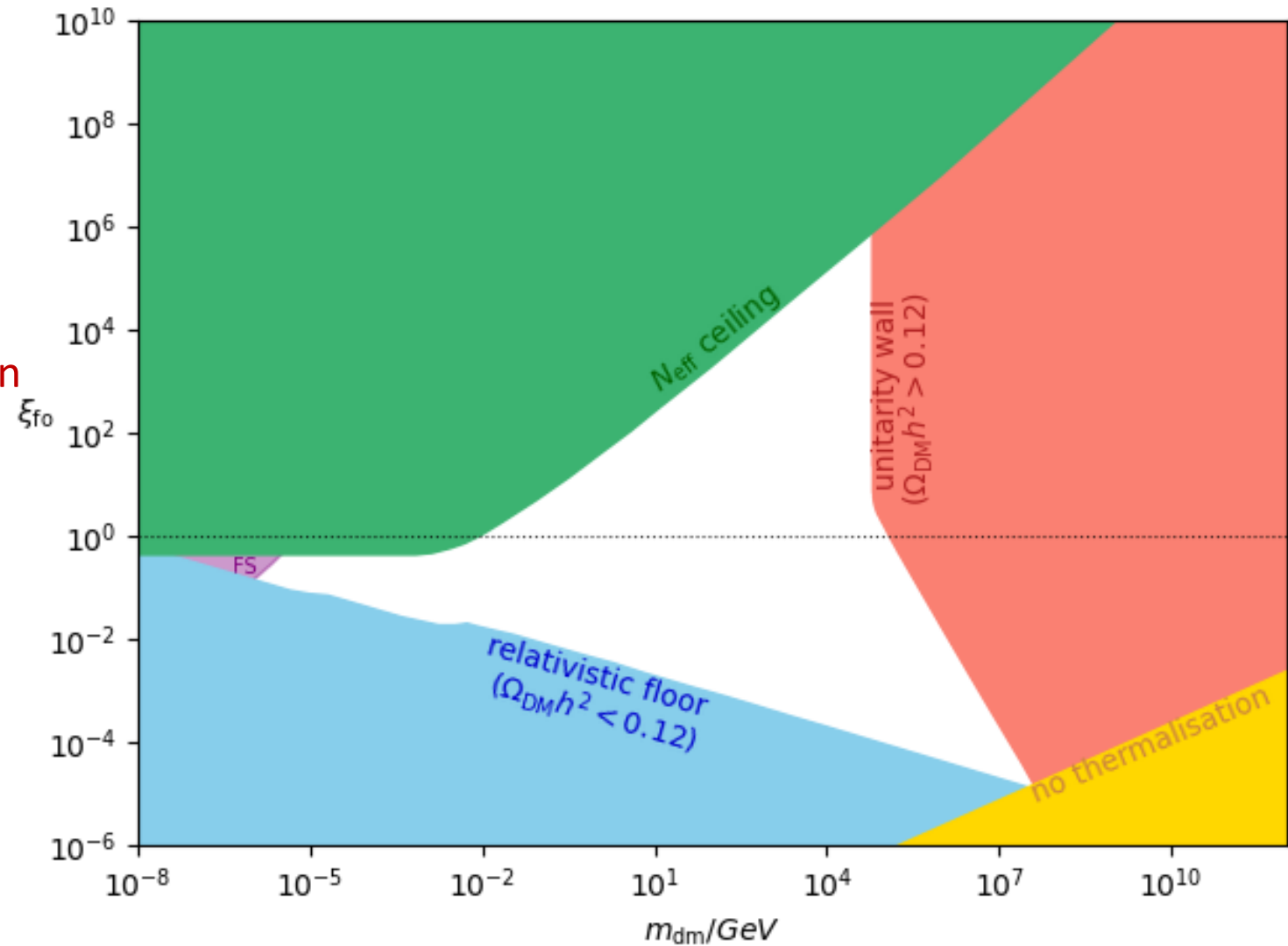


Constraints on the dark matter domain

- Relativistic freeze-out: maximal relic density
- Non-dominating DM during BBN
- Upper limit on the free-streaming (FS) length
- Non-relativistic FO with maximal cross section (unitarity): minimal relic density
- Freeze-out in a subdominant secluded thermalised sector :

$$\frac{n_\chi \langle \sigma v \rangle_{\chi\bar{\chi} \rightarrow \gamma'\gamma'}}{H} \Big|_{T'=m_\chi} \gtrsim 1$$

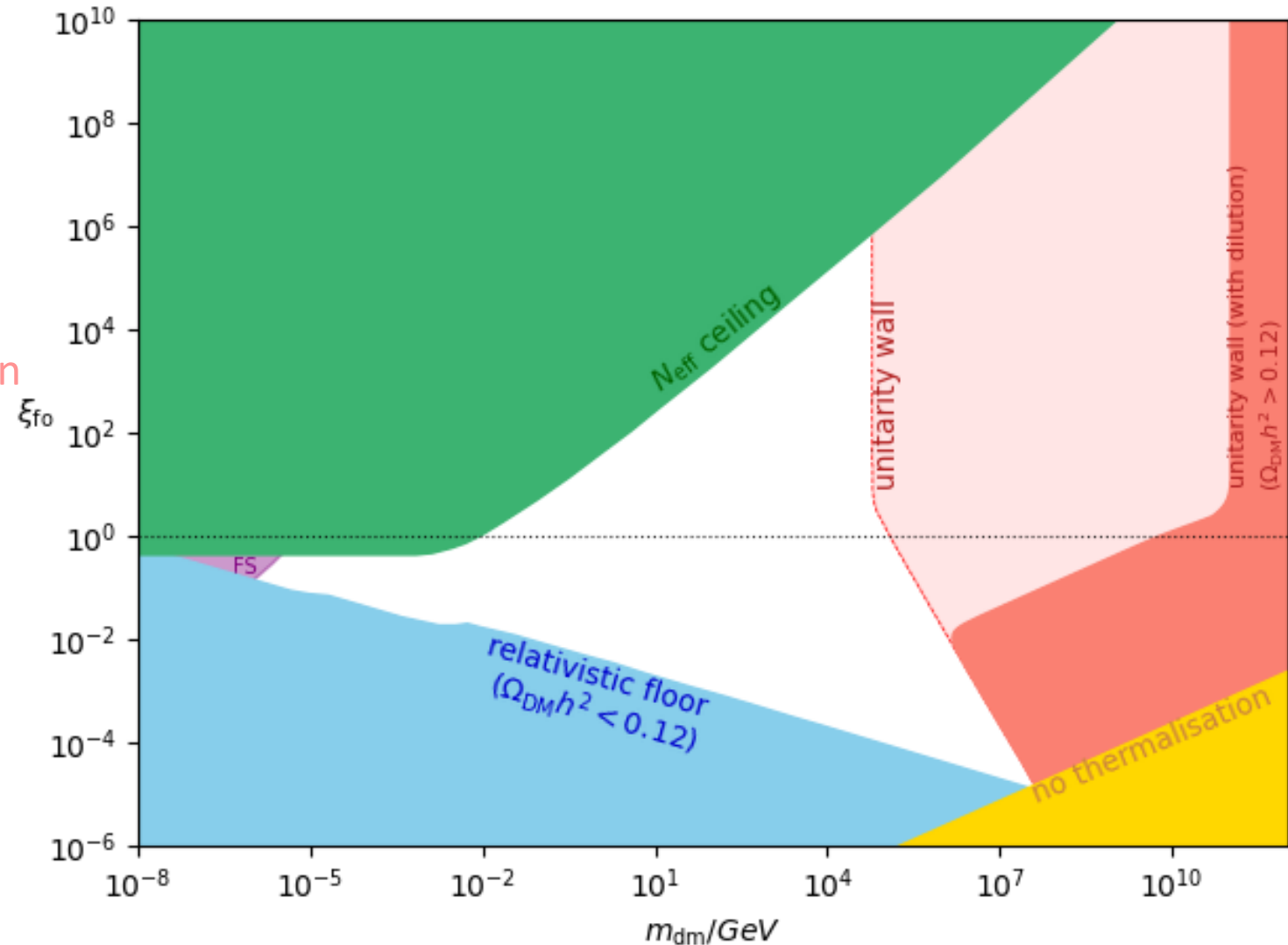
These constraints have been established previously (**2105.01263, Coy et al.**)



Constraints on the dark matter domain

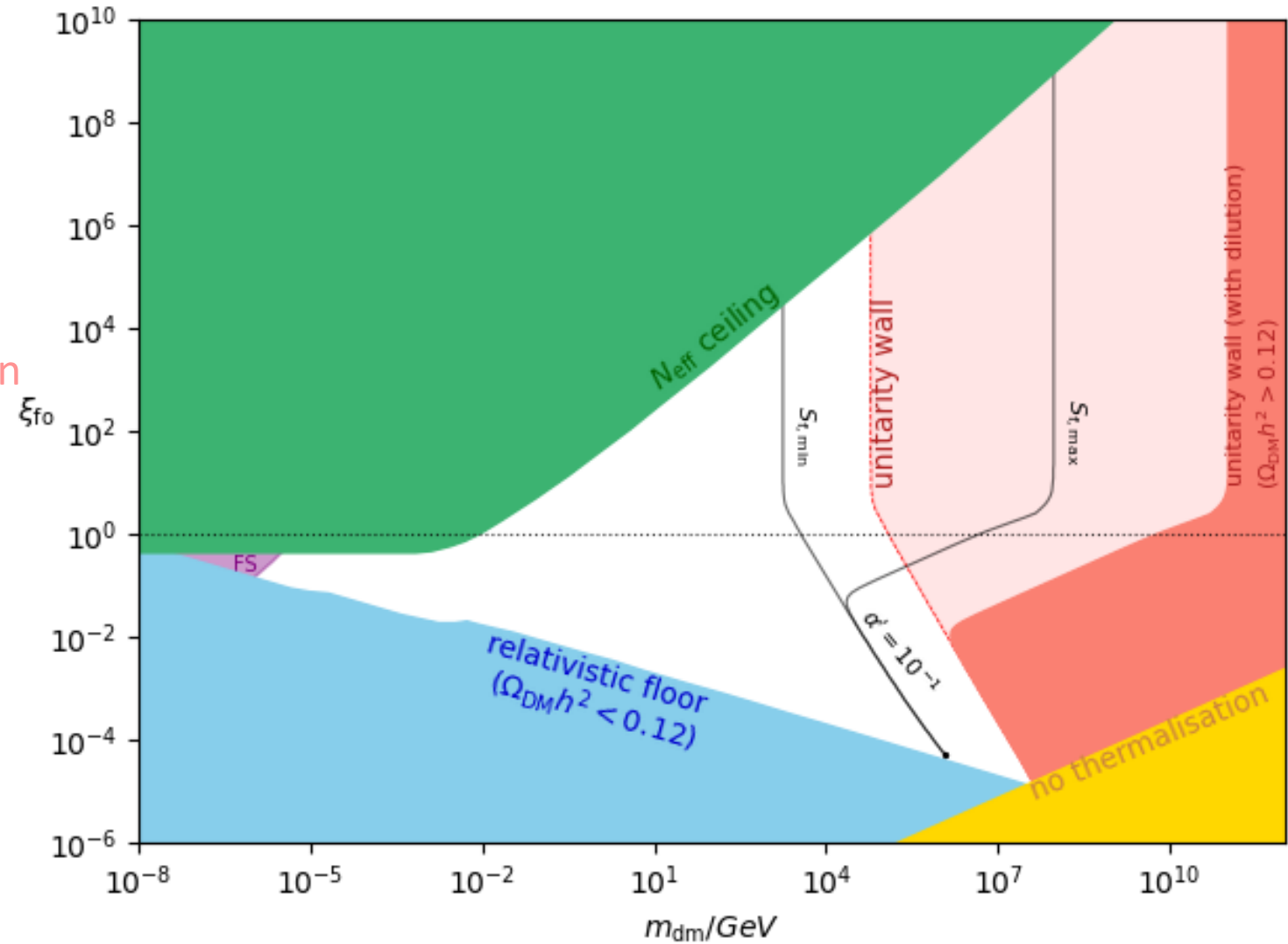
- Relativistic freeze-out: maximal relic density
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- Freeze-out in a secluded thermalised sector (2105.01263, Coy et al.)
- DM relic density entropy dilution

$$\Omega_\chi h^2 \longrightarrow \Omega_\chi h^2 \frac{S_{t,i}}{S_{t,f}}$$



Constraints on the dark matter domain

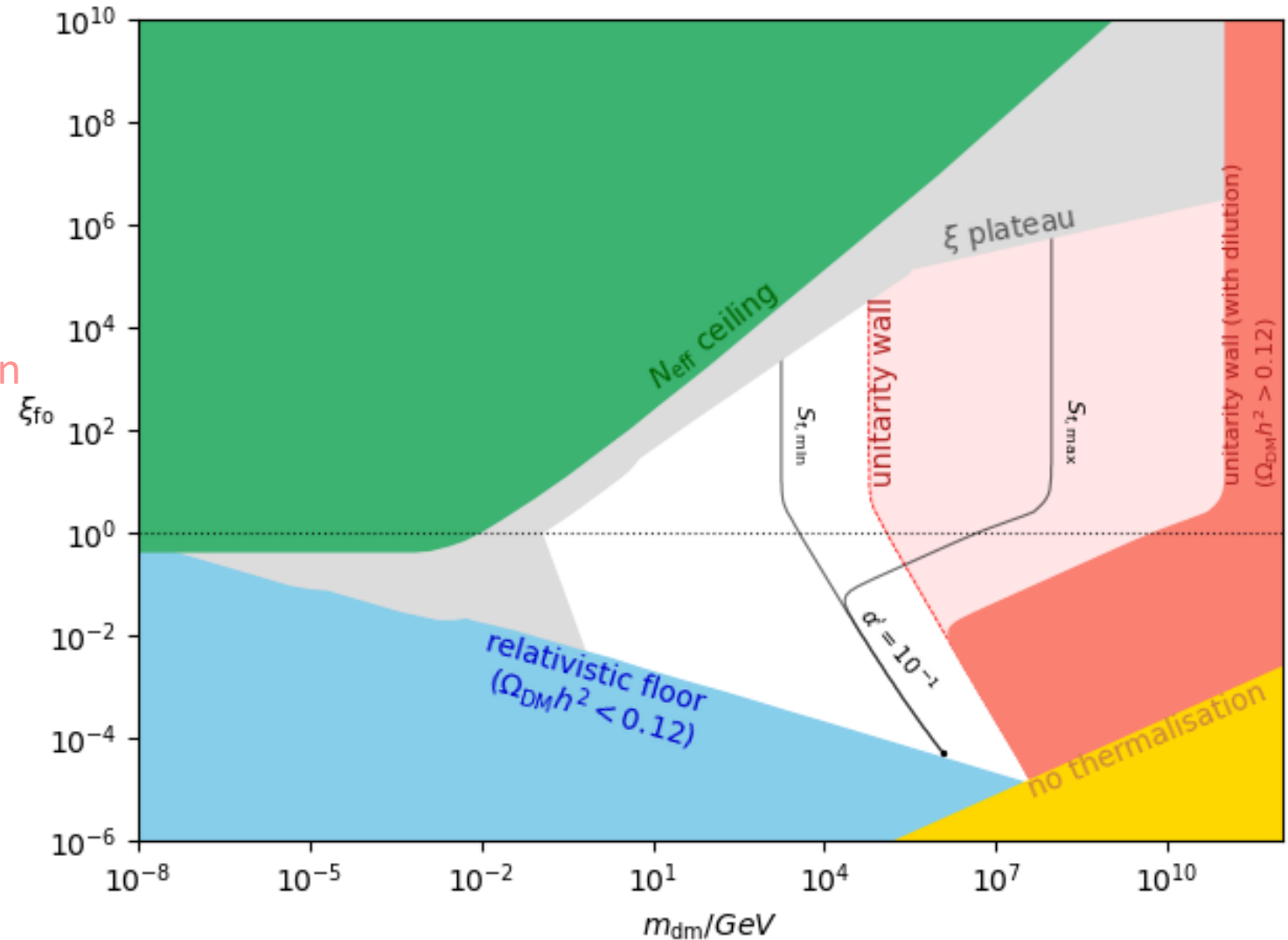
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- DM relic density entropy dilution
- Dark QED candidate : $\alpha' = 0.1$



Constraints on the dark matter domain

- Relativistic freeze-out: maximal relic density
- Non-dominating DM during BBN
- Upper limit on the free-streaming (FS) length
- Non-relativistic FO with maximal cross section (unitarity): minimal relic density
- Freeze-out in a secluded thermalised sector (2105.01263, Coy et al.)
- DM relic density entropy dilution
- Dark QED candidate
- Secluded dark sector at DM freeze-out:

$$\kappa_{\text{FO}} := \frac{1}{3} \xi_{\text{FO}}^4 \frac{\langle \Gamma' \rangle_{T'_{\text{FO}}}}{H_{\text{FO}}} < 1 \quad (\xi_{\text{FO}} > 1)$$



Conclusion

- ❖ Can we live with in a universe early dominated by a hot hidden sector ?
Yes, but only within a given domain of parameters
- ❖ We have now an analytical model of a dark photon population's evolution, confirmed by numerical solutions
- ❖ We can thereby constrain the Dark photon characteristics (ε and $m_{\gamma'}$)
- ❖ With the Dark Photons domain, we can settle new constraints on the Dark Matter mass and temperature

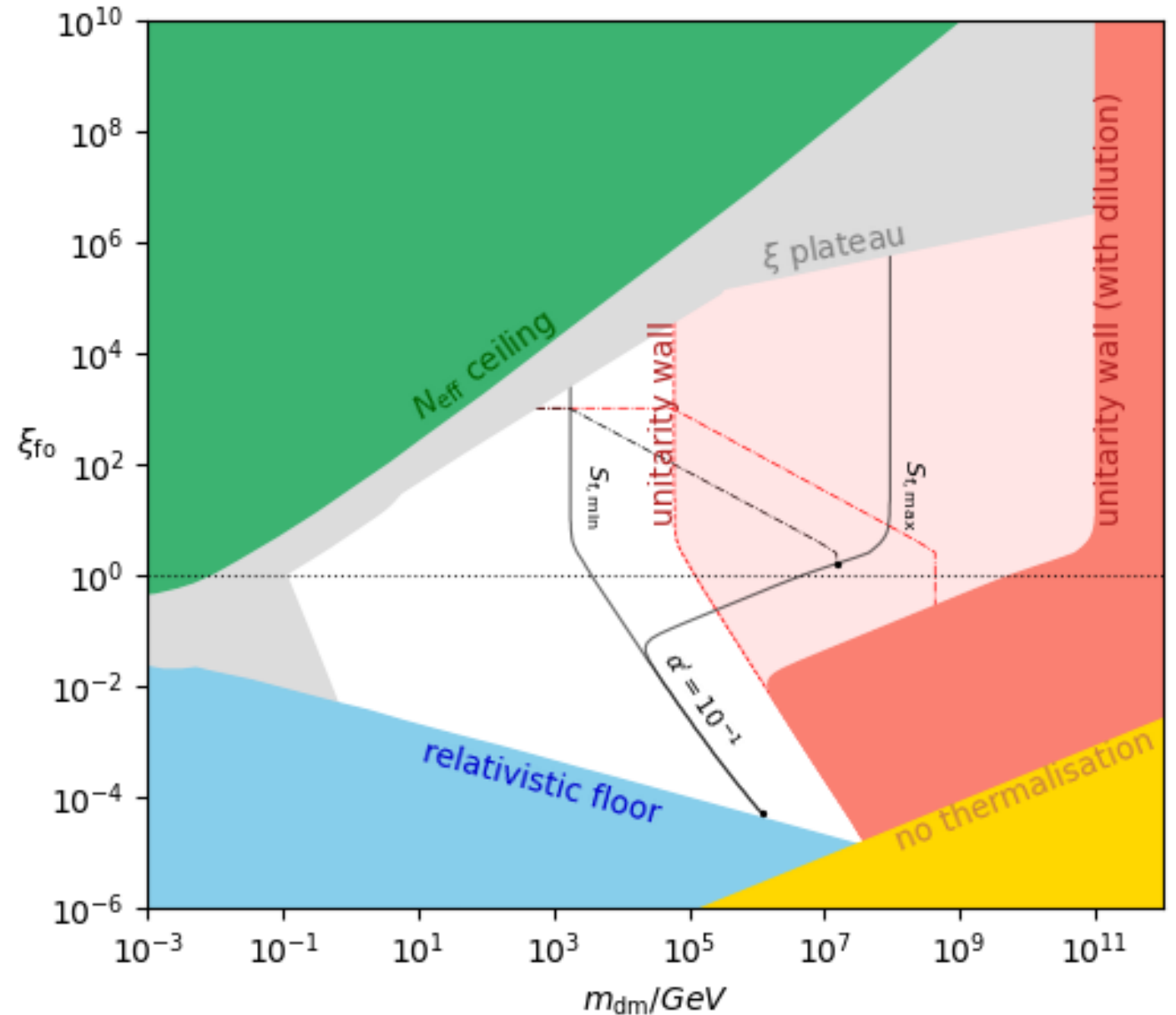
Baryogenesis constraint

The baryon number B in the early universe can be expressed as

$$B \sim 10^{-10} \sim \epsilon_B \frac{n_B}{s_t} \Big|_{T=T_B} \lesssim \frac{n_B}{s_t} \Big|_{T=T_B}$$

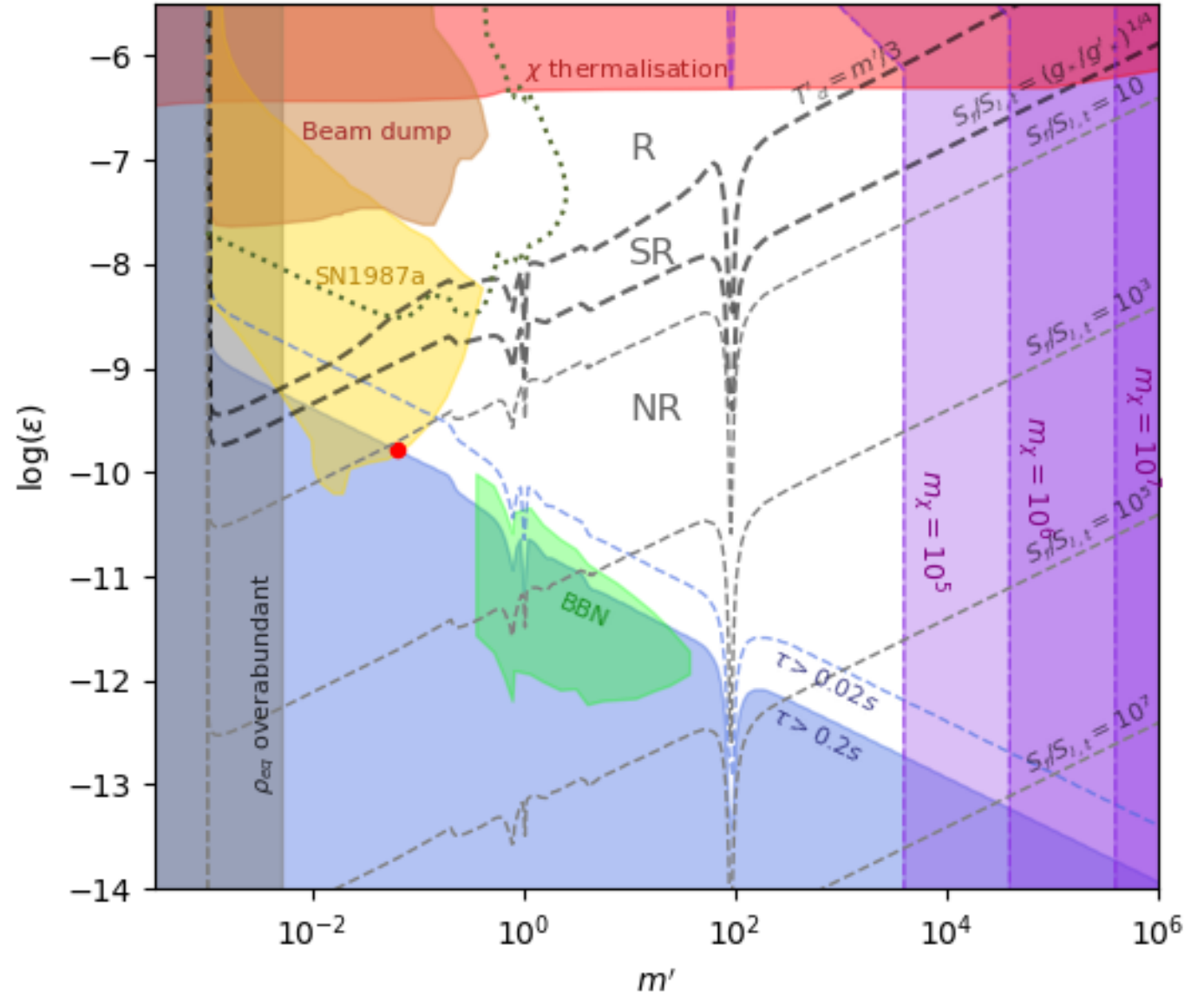
For a dominant dark sector:

$$\xi_B^3 \frac{S_{t,B}}{S_{t,f}} \lesssim B$$



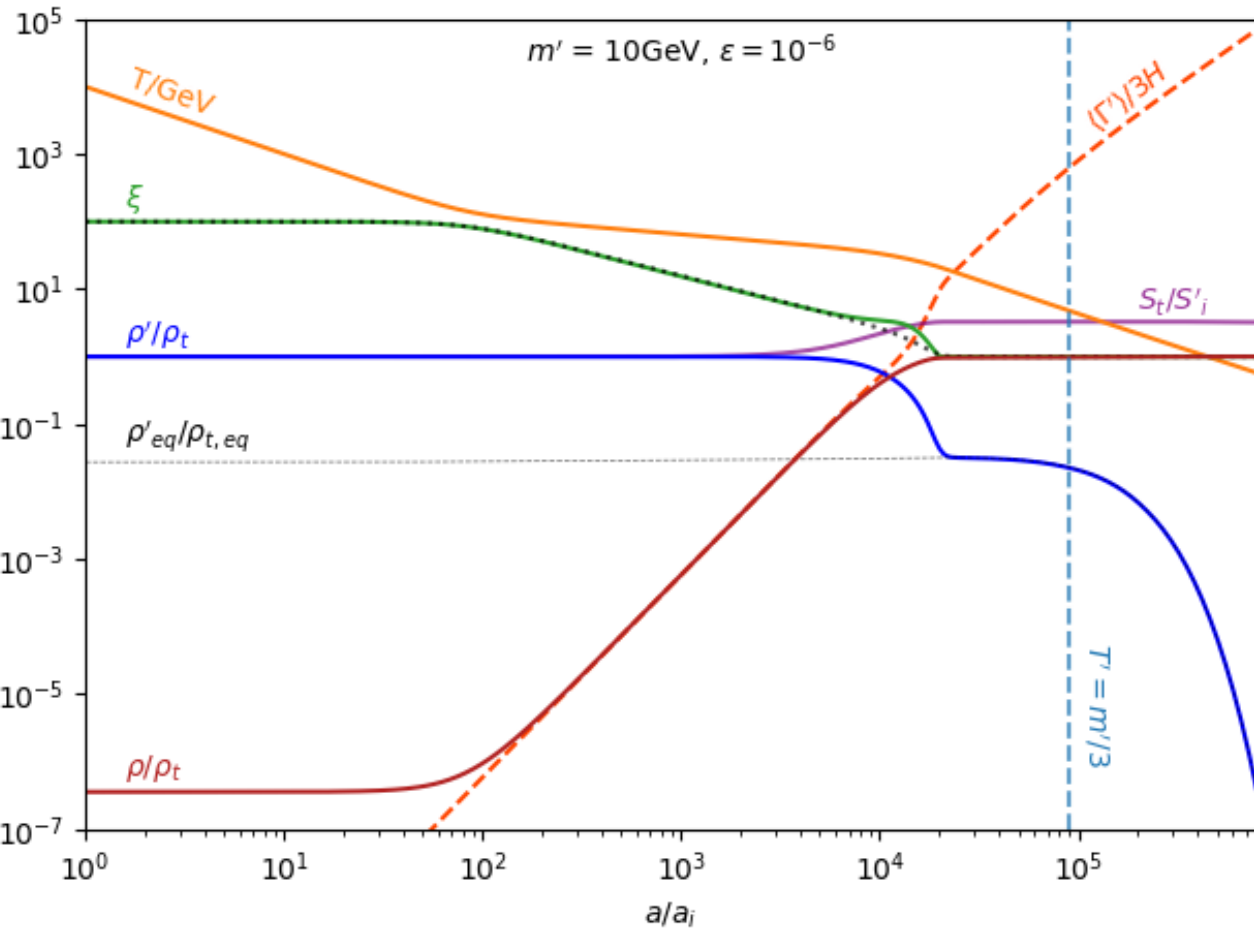
Dark photon domain

- Domains of relativistic (R) and nonrelativistic (NR) decay
- Level curves of entropy production
- Additional theoretical bound (1605.07195, Berger et al.)

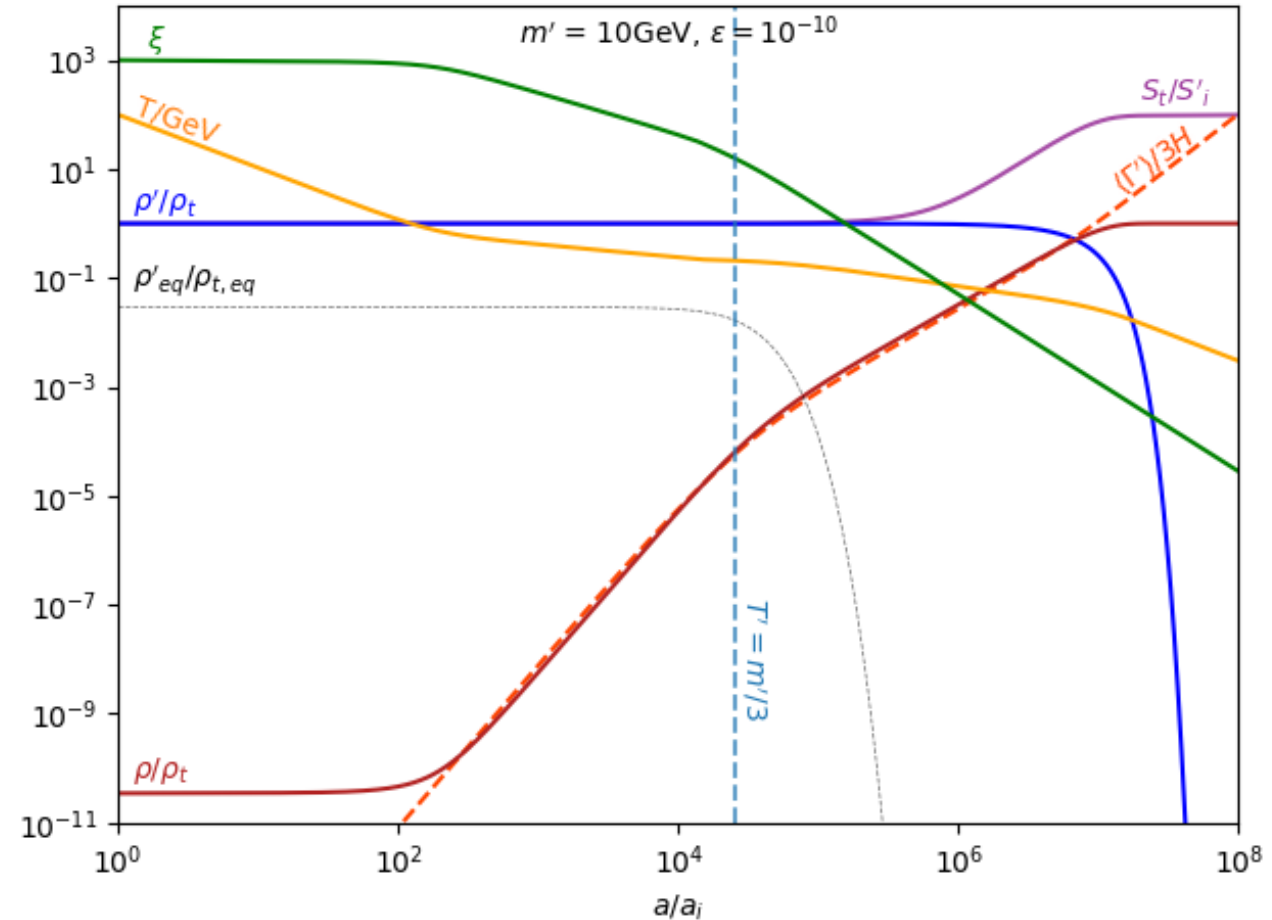


More detailed scenarios

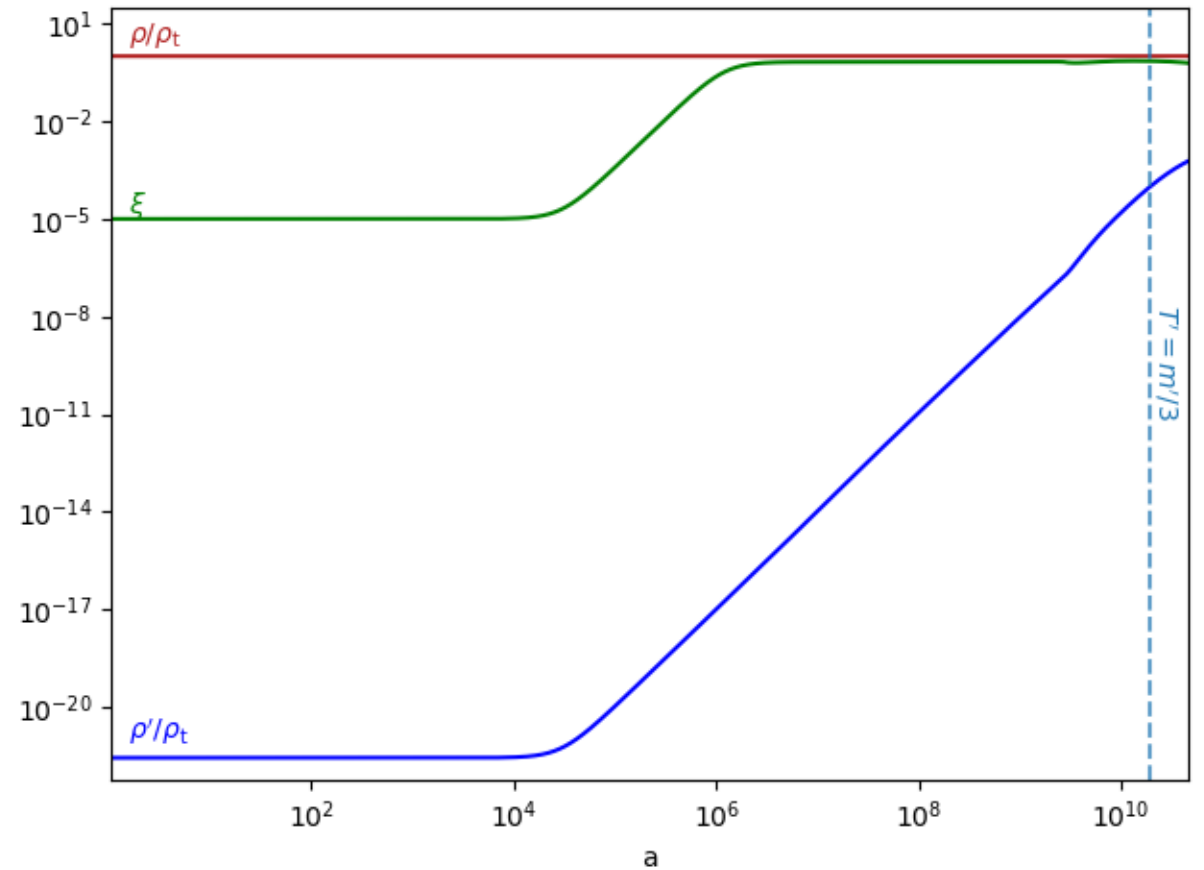
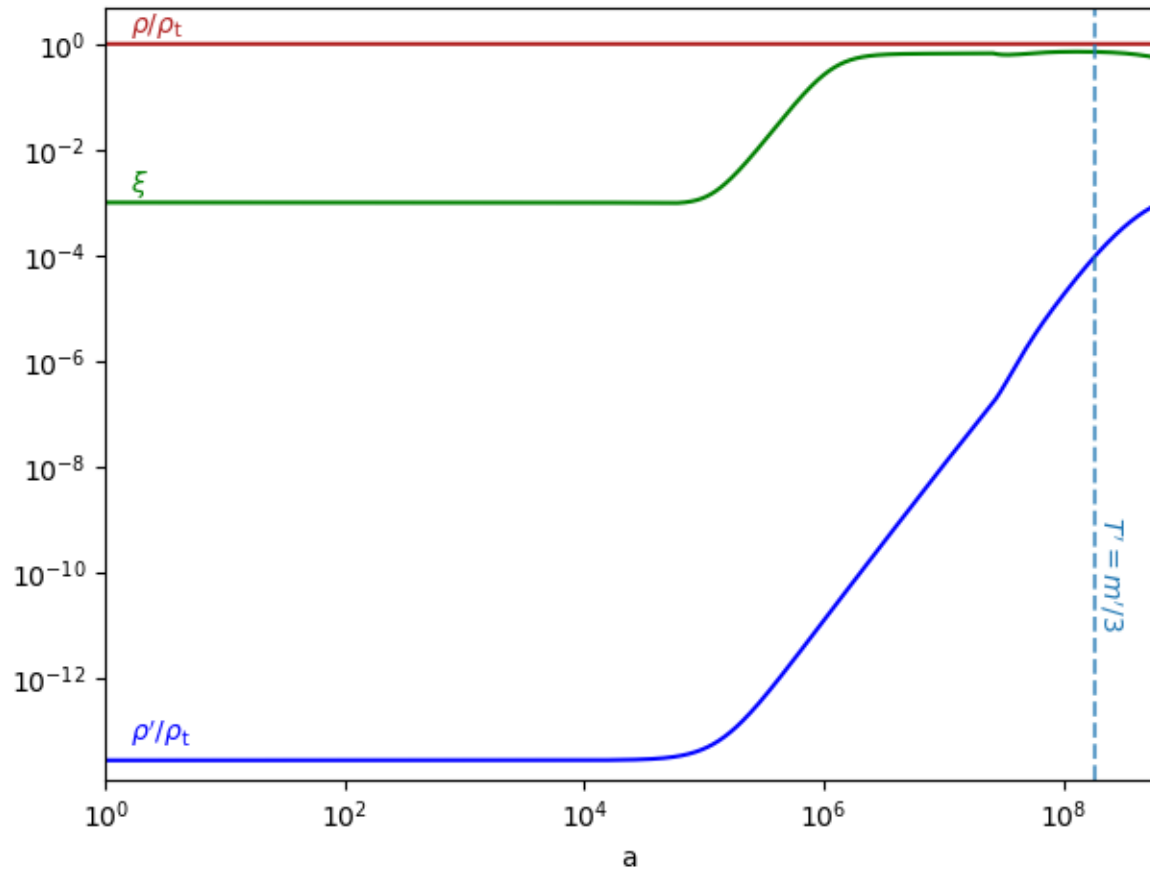
Relativistic thermalisation



Non relativistic thermalisation



Scenarios with a subdominant Dark Photon (Freeze-in)



Parameter κ

$$\frac{d\rho'}{dt} + 3(1 + \omega')H\rho' = m'\Gamma' [n'_{\text{eq}}(T) - n']$$

- **Dominant hidden sector:**

$$\kappa = \frac{1}{3} \frac{\rho'}{\rho} \frac{\langle \Gamma' \rangle}{H}$$

- **Dominant visible sector:**

$$\kappa = \frac{1}{3} \frac{\rho}{\rho'} \frac{\langle \Gamma' \rangle}{H}$$

- Plateau (decoupled sectors) $\rightarrow \kappa \ll 1$
- Attractor (thermalisation) $\rightarrow \kappa = O(1)$
- Thermalised sectors $\rightarrow \kappa > 1$

