

A conclusive test of the cold dark matter model

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Institute for Computational Cosmology,
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The standard model of cosmology

The new Ogden
Centre at Durham



The Λ CDM model of cosmogony

Cosmological constant Cold dark matter



- Proposed in 1980s, it is an *ab initio*, **fully specified** model of **cosmic evolution** and the formation of cosmic structure
- Has strong **predictive** power and can, in principle, be **ruled out**
- Has made a number of **predictions** that were subsequently **verified** empirically (e.g. CMB, LSS, galaxy formation)

Three Nobel Prizes in Physics since 2006

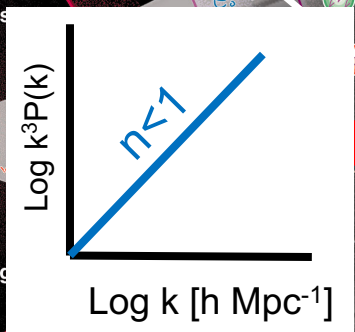
The big Bang



The cosmic microwave background is emitted
($t \sim 350,000$ yrs)

Production of particle dark matter
($t \sim 10^{-10}$ s)

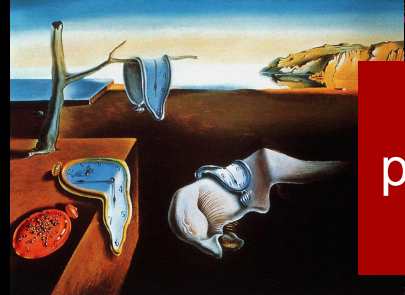
Cosmic inflation (initial conditions)
($t \sim 10^{-35}$ s)



The first light in our Universe

$t = 13.7$ billion yrs

- ⋯ radiation
- particles
- W⁺ heavy particles carrying the weak force
- W⁻ heavy particles carrying the weak force
- Z heavy particles carrying the weak force
- q quark
- q̄ anti-quark
- e⁻ electron
- e⁺ positron (anti-proton)
- p proton
- n neutron
- meson
- H hydrogen
- D deuterium
- He helium
- Li lithium



300 tho
3 minutes

15 thousand million years

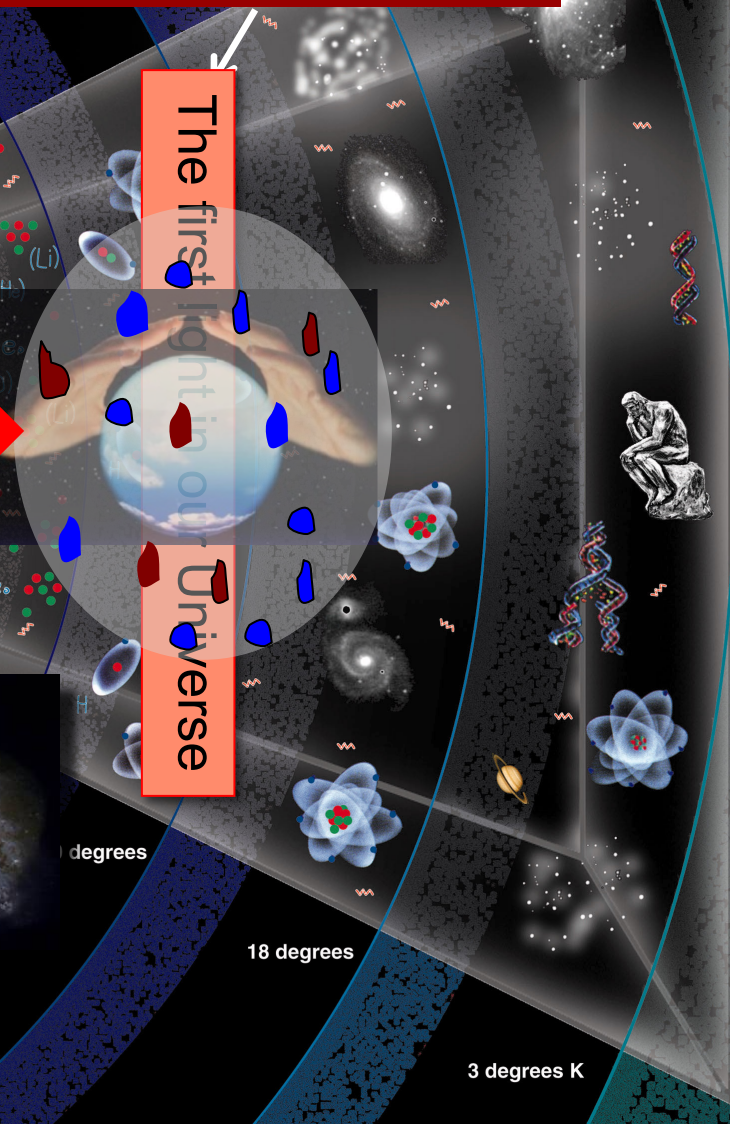
10^{-43} s
 10^{32} deg

10^{-35} degrees
 10^{15} degr

degrees

18 degrees

3 degrees K



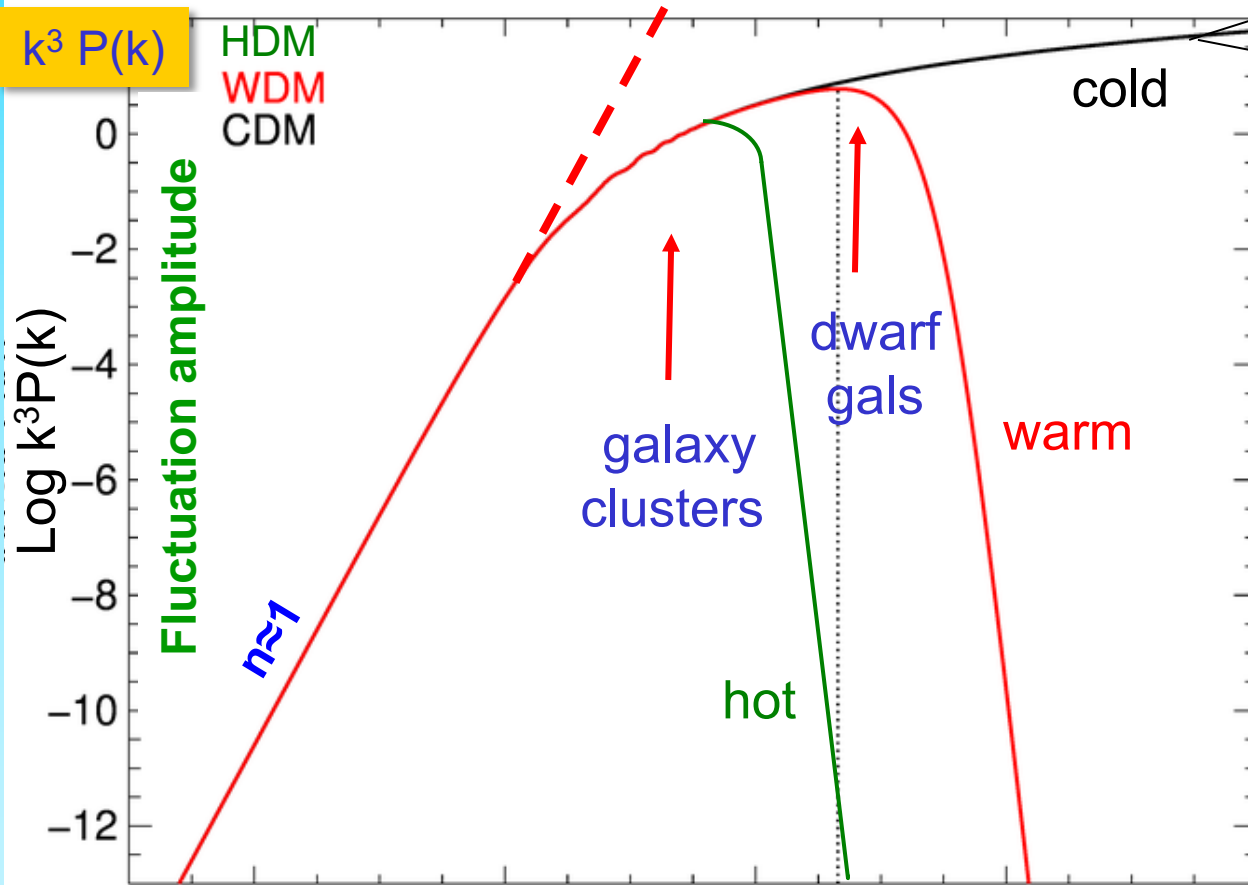
Non-baryonic dark matter candidates

From the early 1980s:

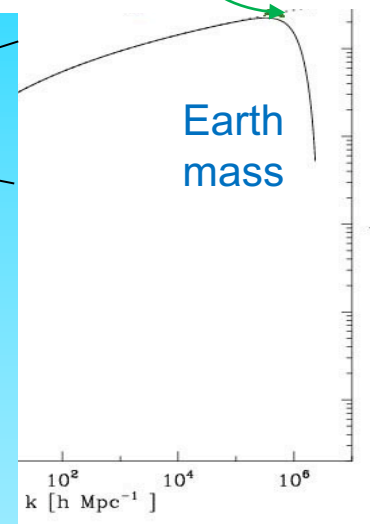
Type	example	mass
hot	neutrino	few tens of eV
warm	sterile ν	keV-MeV
cold	axion neutralino	10^{-5} eV - 100 GeV

The dark matter power spectrum

The linear power spectrum ("power per octave")



Free-streaming cutoff



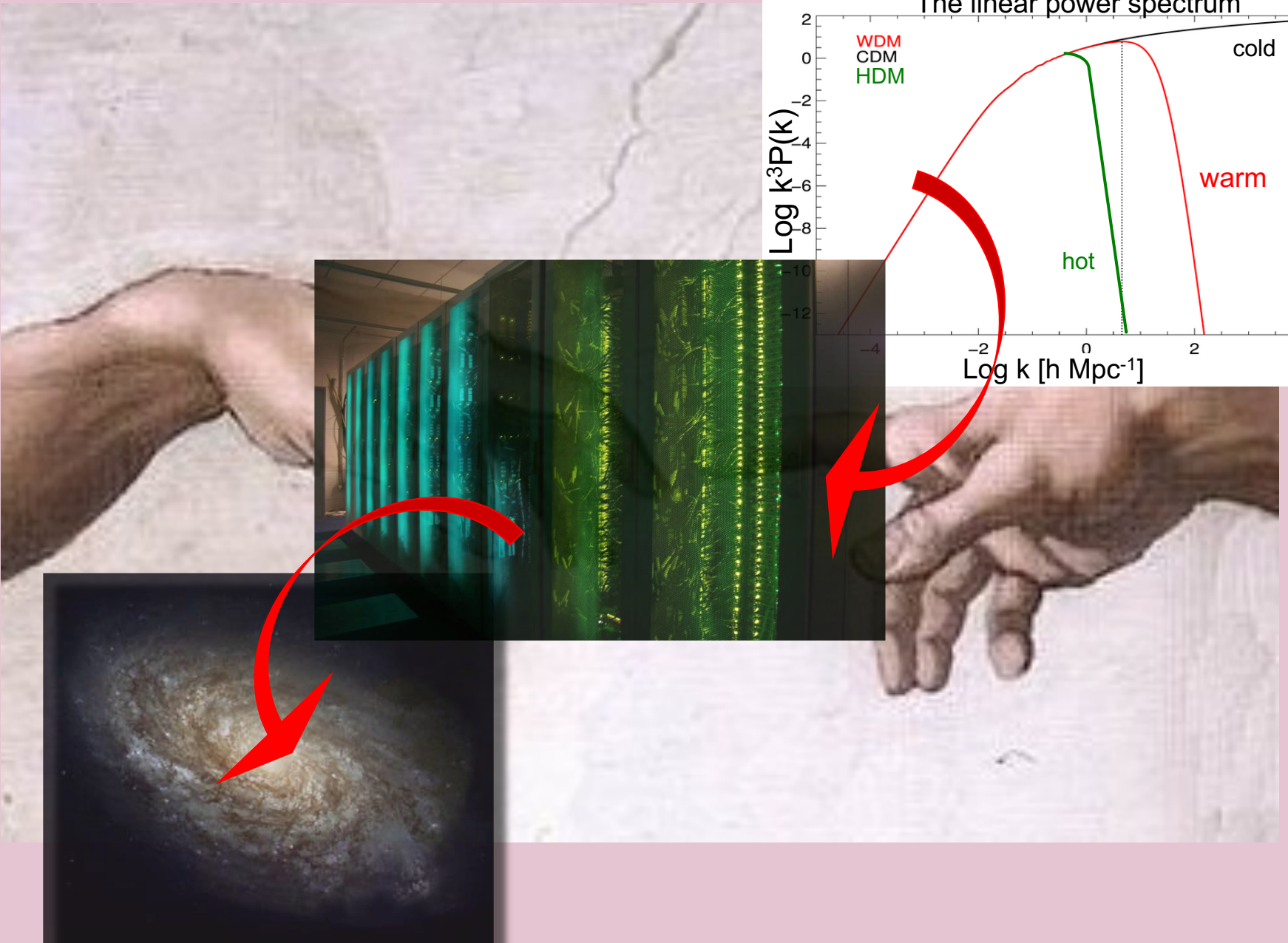
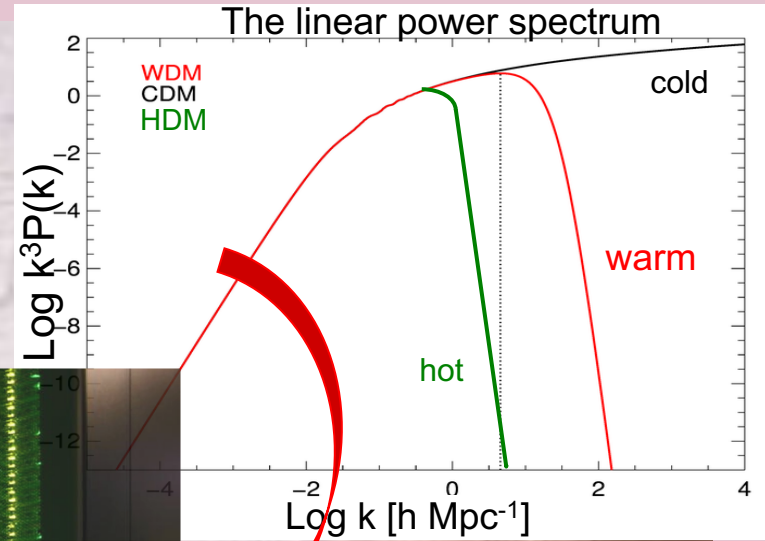
Free streaming →

$$\lambda_{\text{cut}} \propto m_x^{-1}$$

for a thermal relic

These possibilities can be tested with astrophysics

Non-linear evolution



Non-linear evolution: simulations

Assumption about content of Universe → Initial conditions

Relevant equations:

Collisionless Boltzmann;
 Poisson; Friedmann eqns;
 Radiative hydrodynamics
 Subgrid astrophysics



How to make a virtual universe

Hot dark matter

$$m_\nu = 30 \text{ eV} \rightarrow \Omega_m = 1$$

1981

HAS THE NEUTRINO A NON-ZERO REST MASS?
(Tritium β -Spectrum Measurement)

V. Lubimov, E. Novikov, V. Nozik, E. Tretyakov
Institute for Theoretical and Experimental Physics, Moscow, U.S.S.R.

V. Kosik
Institute of Molecular Genetics, Moscow, U.S.S.R.

ABSTRACT

The high energy part of the β -spectrum of tritium in the molecule was measured with high precision by a toroidal β -spectrometer. The results give evidence for a non-zero electron anti-neutrino mass.

Fifty years ago Pauli introduced the neutrino to explain the β -spectrum shape. Pauli made the first estimate of the neutrino mass ($E_{\beta \text{ max}} \approx$ nuclei mass defect): it should be very small or maybe zero. Up to now the study of the β -spectrum shape is the most sensitive, direct method of neutrino mass measurement. For allowed β -transitions, if $M_\nu = 0$, then $S \approx (E - E_0)^2$. The Kurie plot is then a straight line with the only kinematic parameter being $E_k = E_0$ (total β -transition energy). If $M_\nu \neq 0$, then $S \approx (E_0 - E) \sqrt{(E_0 - E)^2 - M_\nu^2}$. The Kurie plot is then distorted, especially near the endpoint.

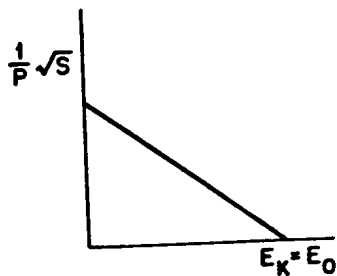


Fig. 1. Kurie plot for $M_\nu = 0$.

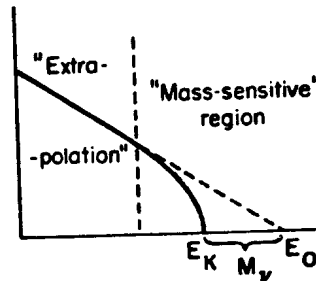


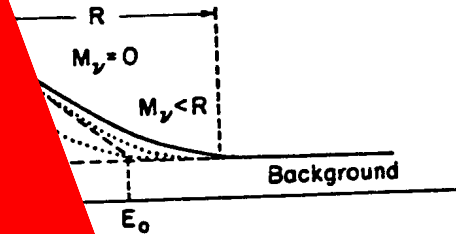
Fig. 2. Kurie plot for $M_\nu \neq 0$.

The method for the neutrino mass measurement is to obtain E_0 from the extrapolation and obtain E_k from the spectrum intercept. Then $M_\nu = E_0 - E_k$. Qualitatively, $M_\nu \neq 0$ if the β -spectrum near the endpoint runs below the extrapolated curve.

* Paper presented by Oleg Egorov.



things are more complicated. The apparatus resolution strongly affects the spectrum endpoint and rather the spectrum slope.



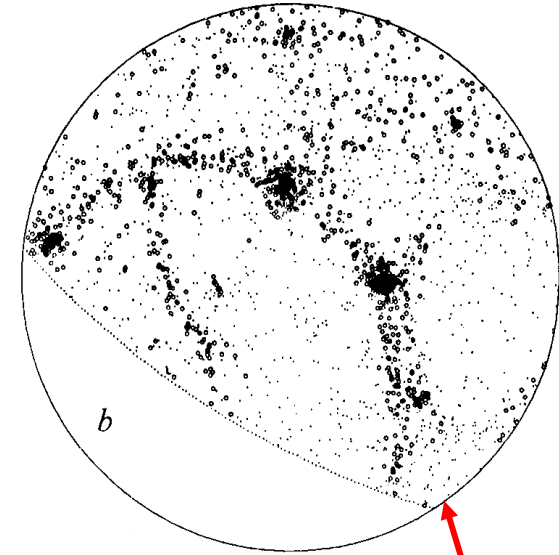
Realistic Kurie plot.

extrapolation. However, we are unable to determine M_ν , then once again the lack of counts near the endpoint indicate that $M_\nu \neq 0$. If $M_\nu \leq R$, the changes due to M_ν and the influence of R are indistinguishable. For M_ν determination the knowledge of R is compulsory. The background determines the statistical accuracy near the endpoint, i.e., in the region of the highest sensitivity to the ν mass. So: 1) R should be $\sim M_\nu$, 2) the smaller M_ν is, the smaller the background ($\sim M_\nu^2$) must be and the higher the statistics ($\sim M_\nu^{-3}$) must be. For example, suppose that for $M_\nu = 100$ eV we need resolution R , background Q , and statistics N . If $M_\nu = 30$ eV, to achieve the same $\Delta M/M$ they should be $R/3$, $Q/10$, and $N \times 30$, respectively.

The shorter the β -spectrum, the less it is spread due to R (as $R \sim \Delta p/p = \text{const.}$). A classical example is ^3H β -decay, which has 1) the smallest $E_0 \sim 18.6$ keV, 2) an allowed β -transition, simple nucleus, and simple theoretical interpretation, 3) highly reduced radioactivity. The first experiments with ^3H were by S. Curran et al. (1948) and G. Hanna, B. Pontecorvo (1949). Using ^3H gas in a proportional counter, they obtained $M_\nu \leq 1$ keV. Further progress required magnetic spectrometer development. This allowed the resolution to be improved considerably, and L. Langer and R. Moffat (1952) obtained $M_\nu \leq 250$ eV. The best value was obtained by K. Bergkvist (1972): $R \sim 50$ eV and $M_\nu \leq 55$ eV.

The ITEP spectrometer is of a new type: ironless, with toroidal magnetic field (E. Tretyakov, 1973). The principle of the toroidal magnetic field focusing systems was proposed by V. Vladimirovsky et al. (An example is a "Horn" of ν -beams.) It turns out that a rectilinear conductor (current) has a focusing ability for particles emitted perpendicular to the rotation axis. This system has infinite periodical focusing structure. The ITEP spectrometer is based on this principle.

Non-baryonic dark matter cosmologies



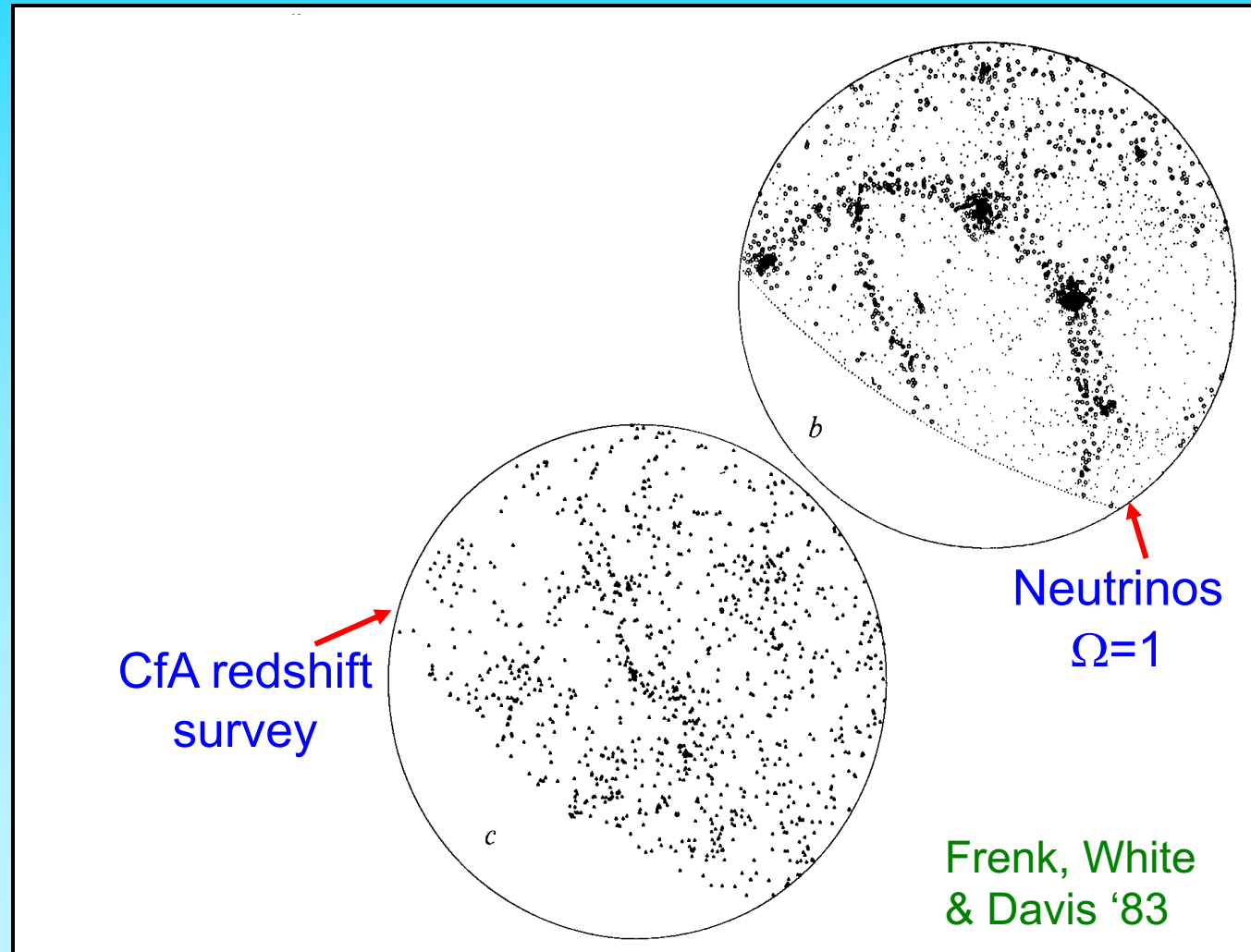
Neutrinos
 $\Omega=1$

Frenk, White
& Davis '83

Non-baryonic dark matter cosmologies

Neutrino DM \rightarrow
wrong clustering

Neutrinos cannot
make appreciable
contribution to Ω
 $\rightarrow m_\nu \ll 30 \text{ eV}$



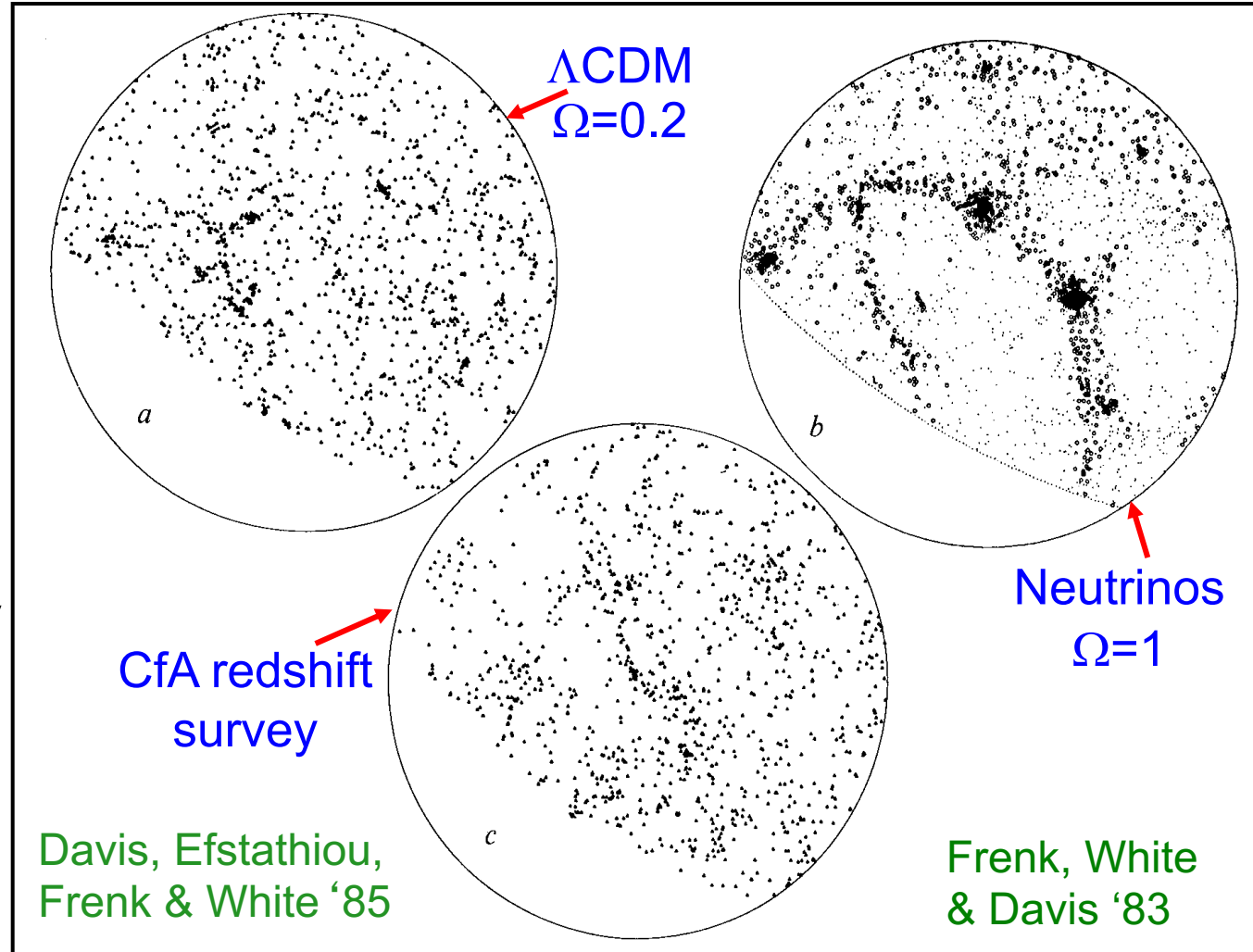
Non-baryonic dark matter cosmologies

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make appreciable
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Early CDM N-body
simulations gave
promising results

In CDM structure
forms hierarchically



The big Bang



300 tho

3 minutes

15 thousand million years

The temperature of this radiation should show small irregularities

Production of particle dark matter
($t \sim 10^{-10}$ s)

10^{-43} seconds

10^{32} degrees

10^{27} degrees

10^{15} degr

1 degrees

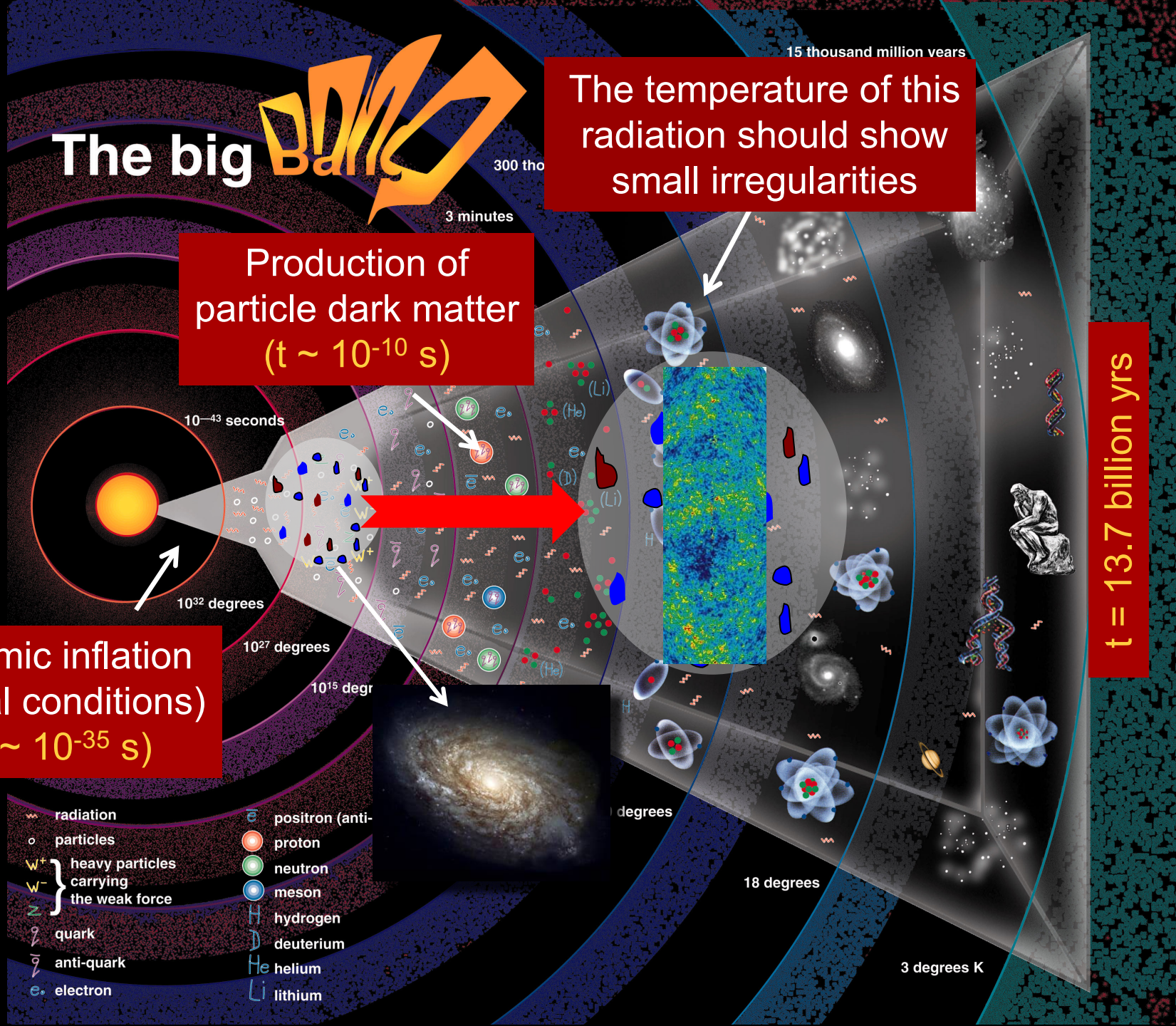
18 degrees

3 degrees K

t = 13.7 billion yrs

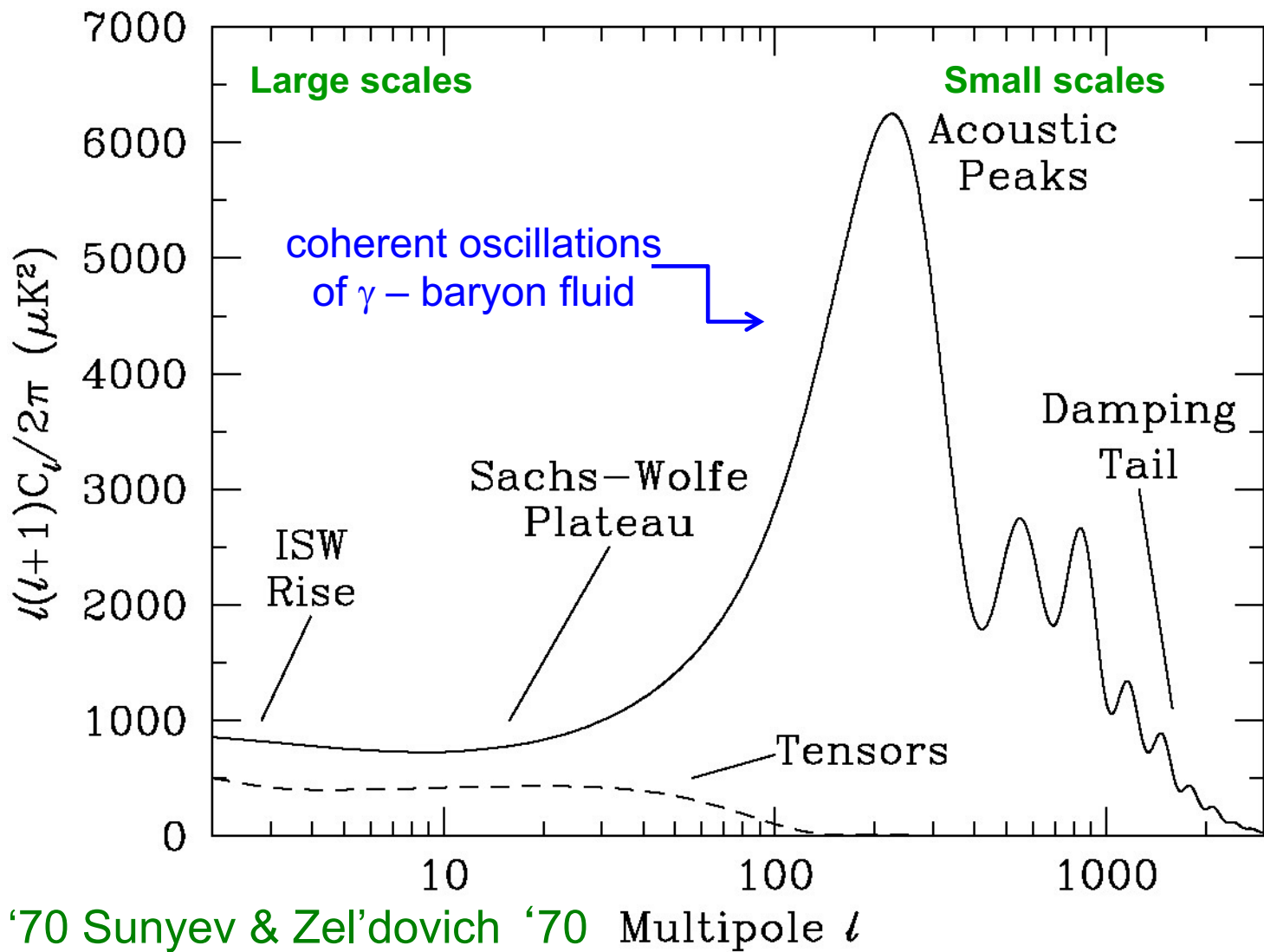
Cosmic inflation
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Temperature anisotropies in CMB

2D power spectrum



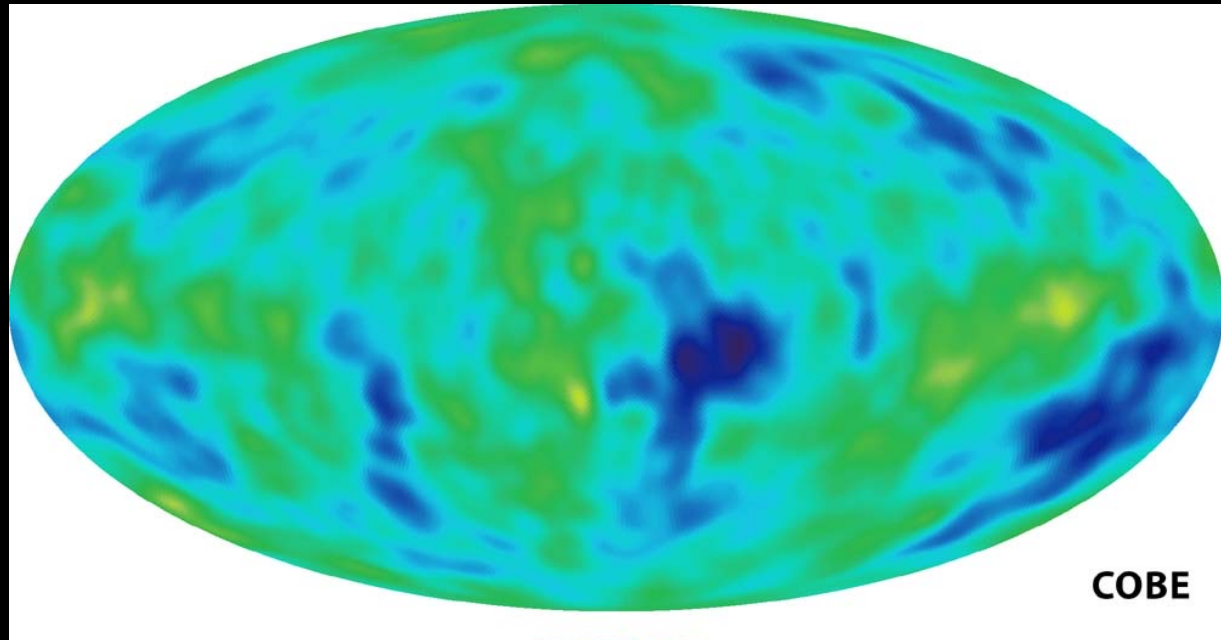
Peebles & Yu '70 Sunyev & Zel'dovich '70

For CDM: Peebles '82; Bond & Efstathiou '84

Jim Peebles
Nobel prize 2019



1992



The cosmic microwave background radiation (CMB) provides a window to the universe at $t \sim 3 \times 10^5$ yrs

In 1992 COBE discovered temperature fluctuations ($\Delta T/T \sim 10^{-5}$) consistent with inflation predictions



THE INDEPENDENT

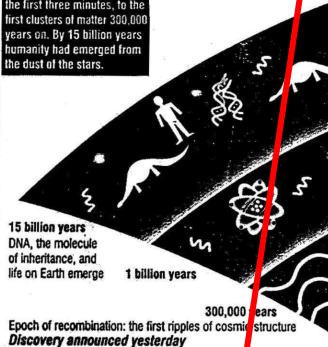
No 1,722

A Nasa spacecraft has detected the stars after the Big Bang has

How

BACK TO CREATION

How the universe evolved from the Big Bang, through the first three minutes, to the first clusters of matter 300,000 years on. By 15 billion years humanity had emerged from the dust of the stars.



FOURTEEN thousand million years ago the universe hiccuped. Yesterday, American scientists announced that they have heard the echo.

A Nasa spacecraft has detected ripples at the edge of the Cosmos which are the fossilised imprint of the birth of the stars and galaxies around us today.

According to Michael Rowan-Robinson, a leading British cosmologist, "What we are seeing here is the moment when the structures we are part of - the stars and galaxies of the universe - first began to form."

The ripples were spotted by the Cosmic Background Explorer (Cobe) satellite and presented to excited astronomers at a meeting of the American Physical Society in Washington yesterday. "Oh wow... you can have no idea how exciting this is," Carlos Frenk, an astronomer at Durham University, said yesterday. "All the world's cosmologists are on the telephone to each other at the moment trying to work out what these numbers mean."

Cobe has provided the answer to a question that has baffled scientists for the past three decades in their attempts to understand the structure of the Cosmos. In the 1960s two American researchers found definitive evidence that Big Bang had started the whole thing off about 15 billion years ago. But the Big Bang would have spread matter like thin gruel evenly throughout the universe. The problem was to work out how

the lumps (stars, planets and galaxies) got into the porridge.

"What we have found is evidence for the birth of the universe," said Dr George Smoot, an astrophysicist at the University of California, Berkeley, and the leader of the Cobe team.

Dr Smoot and colleagues at Berkeley joined researchers from several American research organisations to form the Cobe team. This included the

Space Flight Center, Nasa's Jet Propulsion Laboratory, the Massachusetts Institute of Technology and Princeton University. Joel Primack, a physicist at the University of California at Santa Cruz, said that if the research is confirmed, "it's one of the major discoveries of the century. In fact, it's one of the major discoveries of the century."

Turner, a University of Chicago physicist, called the discovery "unbelievably important... the significance of this cannot be overstated. They have found the Holy Grail of cosmology... it is indeed correct, this would have to be considered for a Nobel Prize." Since the ripples were created almost 15 billion years ago, their radiation has been travelling toward Earth at the speed of light. By detecting the radiation, Cobe is "a wonderful time machine"

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3 minutes

1 second

Stable subnuclear particles, neutrons and protons, are formed

10⁻¹⁰ second

10⁻³ The quark bare particle

able to view the young universe, Dr Smoot said.

A remnant glow from the Big Bang is still around today, in the form of microwave radiation that has bathed the universe for the billions of years since the explosion. Galaxies must have formed by growing gravitational forces bringing matter together. To produce a "lumpy" universe, radiation from the Big Bang should itself show signs of being lumpy.

Cobe, which has been orbiting 500 miles above the Earth since the end of 1989, has instruments on board that are sensitive to this extremely old radiation. The ripples Cobe has found are the first hard evidence of the long-sought lumpiness in the radiation.

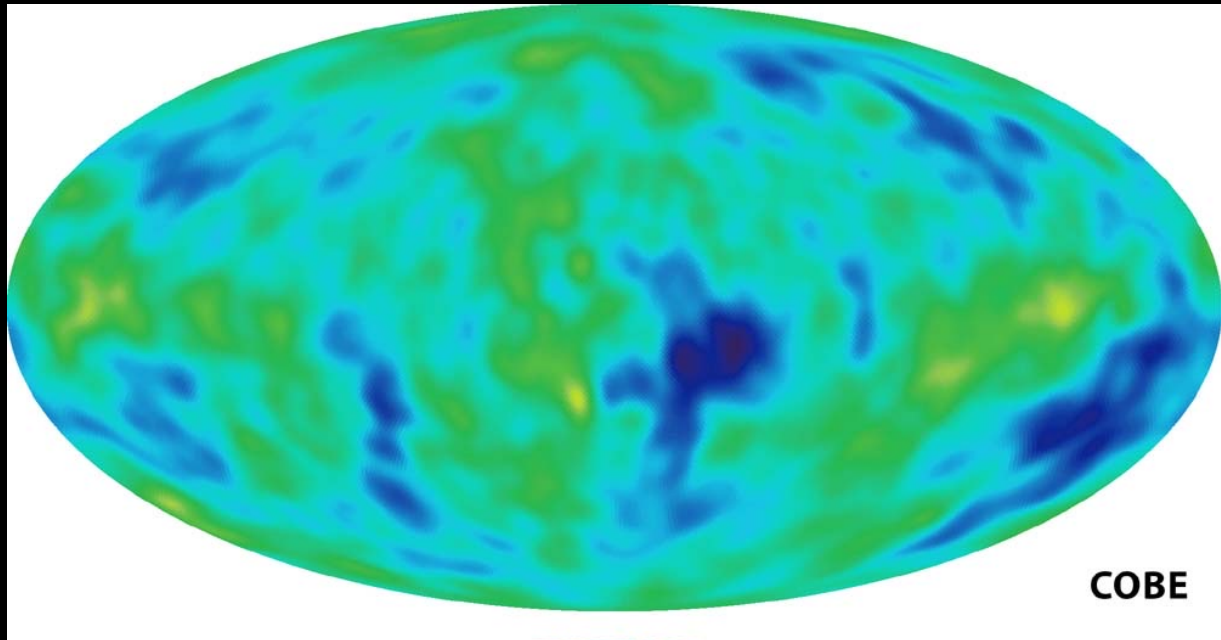
Cobe detected almost imperceptible variations in the tem-

ceptible variations in the temperature... surrounded by slightly less dense matter... time when the foggy fireball of radiation... and light from these galaxies, re-emitted... predictions about what the size of the original fog looked like.

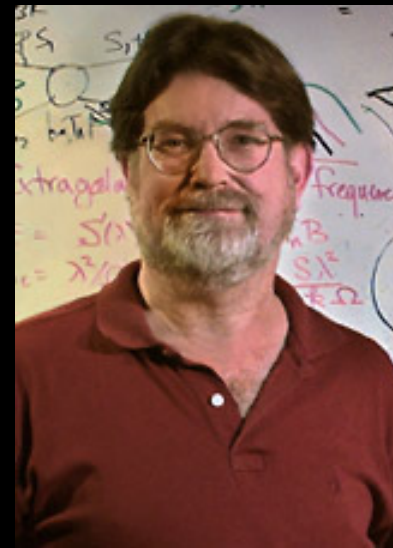


The CMB

1992



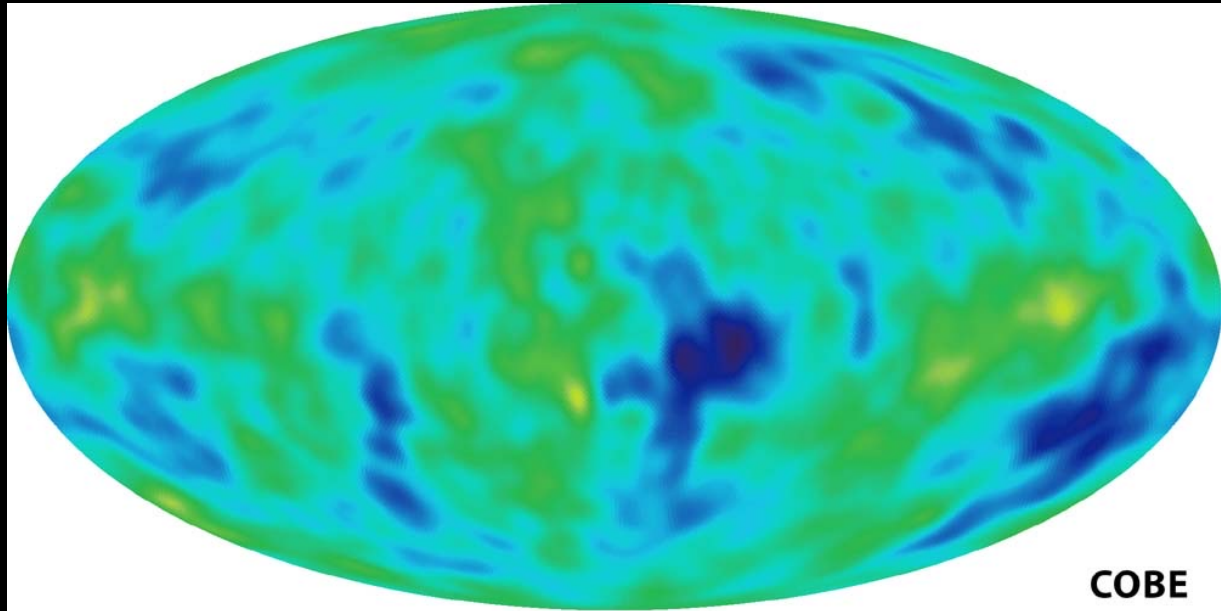
George Smoot - Nobel Prize 2006



ICC

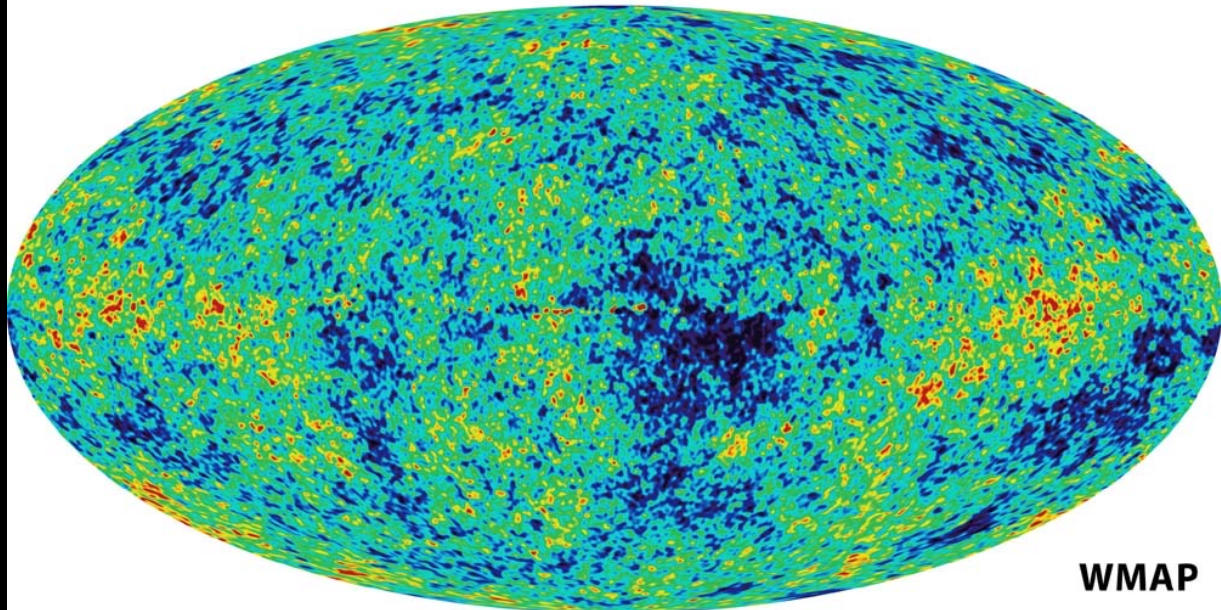
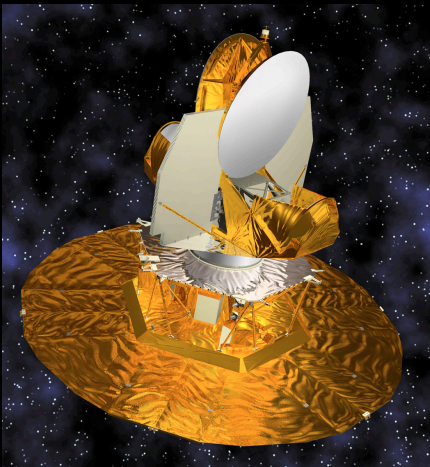
The CMB

1992



COBE

2003

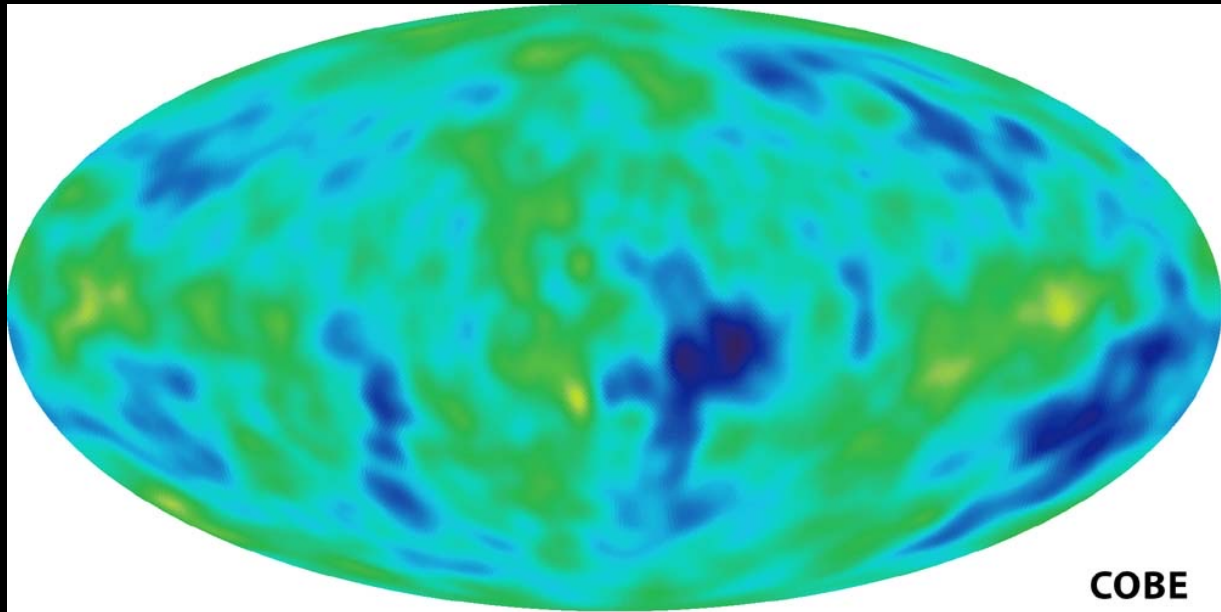


WMAP

ICC

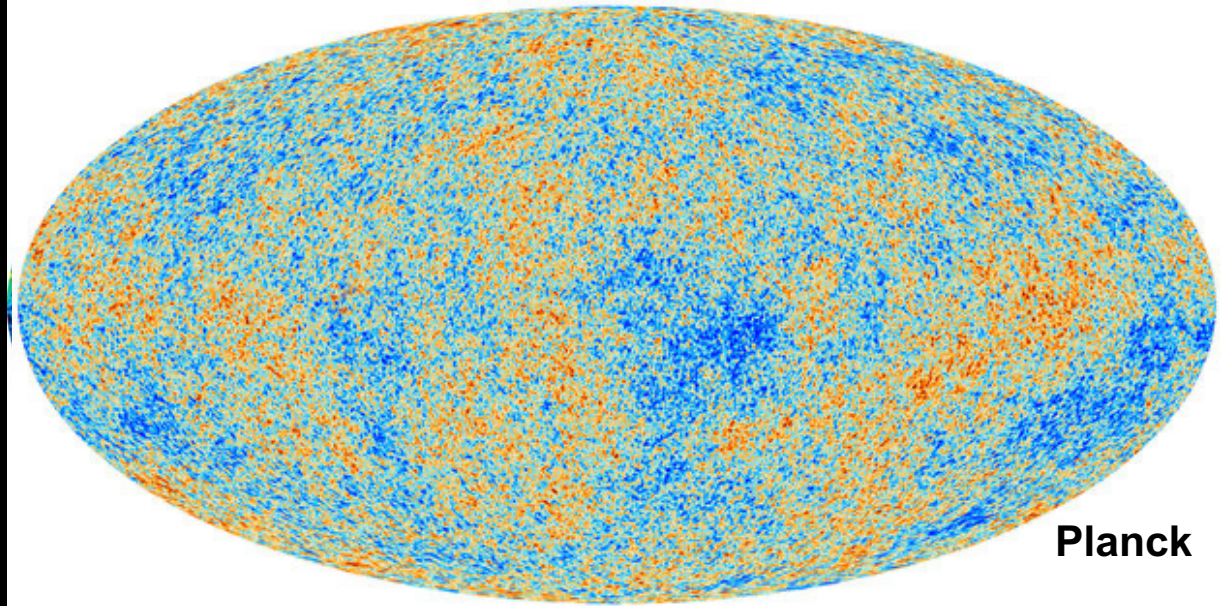
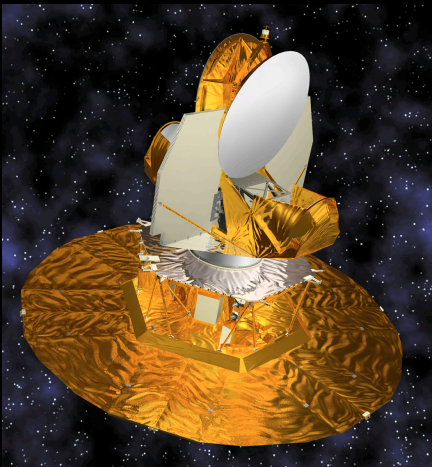
The CMB

1992



COBE

2012



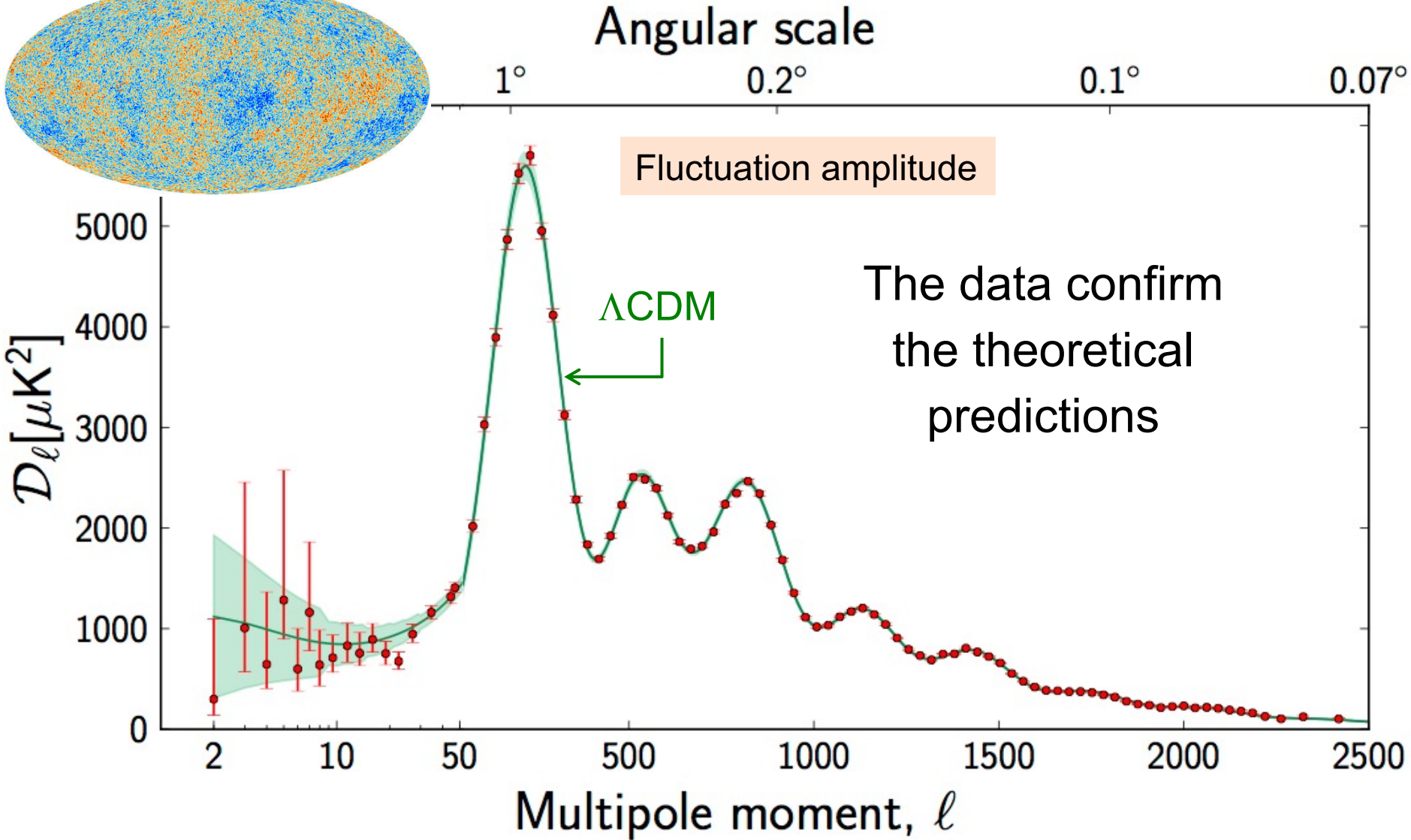
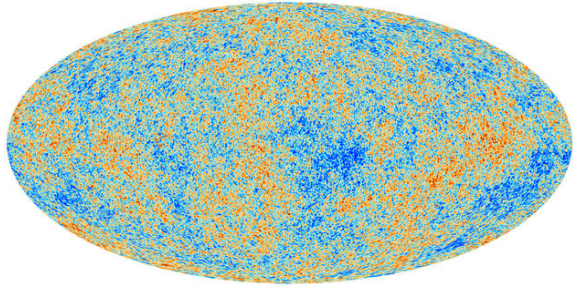
Planck

The initial conditions for galaxy formation



Quantum fluctuations from inflation

Planck: CMB temperature anisotropies



		<i>Planck+WP</i>	
Parameter		Best fit	68% limits
$\Omega_b h^2$	density of baryons	0.022032	0.02205 ± 0.00028
$\Omega_c h^2$	density of CDM	0.12038	0.1199 ± 0.0027
$100\theta_{MC}$		1.04119	1.04131 ± 0.00063
τ		0.0925	0.089 ^{+0.012} _{-0.014}
n_s		0.9619	0.9603 ± 0.0073
$\ln(10^{10} A_s)$		3.0980	3.089 ^{+0.024} _{-0.027}

A 40 σ detection of non-baryonic dark matter!

The curvature of the Universe

The Planck power spectra (temperature and polarization) (positions of acoustic peaks) \rightarrow the Universe is spatially flat

Combined with LSS data, Planck $\rightarrow \Omega_k = 0.0004 \pm 0.0018$

$$\rightarrow \Omega_{\text{tot}} = \Omega_m + \Omega_\Lambda + \Omega_k = 1$$

Since $\Omega_{\text{matter}} = 0.28 \pm 0.005 \rightarrow$ “dark energy”, e.g. $\Omega_\Lambda = 0.72$

Λ anticipated from galaxy distribution in 1991;

inferred from accelerated expansion \rightarrow 2011 Nobel prize

Observational tests of Λ CDM

Fundamental prediction of Λ CDM

→ Primordial PS of density perturbations + random phases

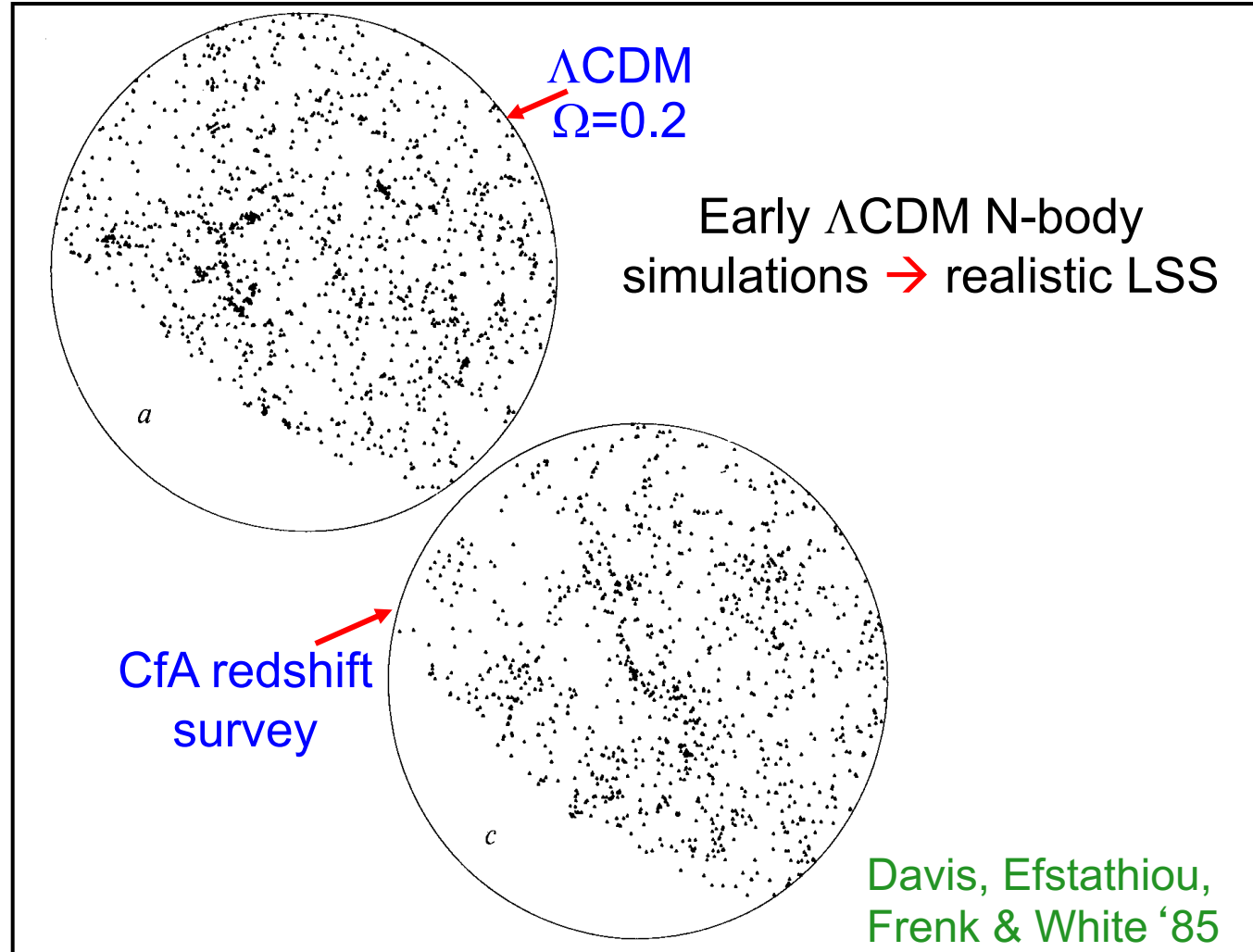
Can test this in **two regimes**:

Linear regime: cosmic microwave background ✓
large-scale structure

Evolved non-linear regime: dark matter halos →

- abundance
- structure
- clustering

The Λ CDM cosmology



VIRGO

The Millennium/Aquarius/Phoenix simulation series

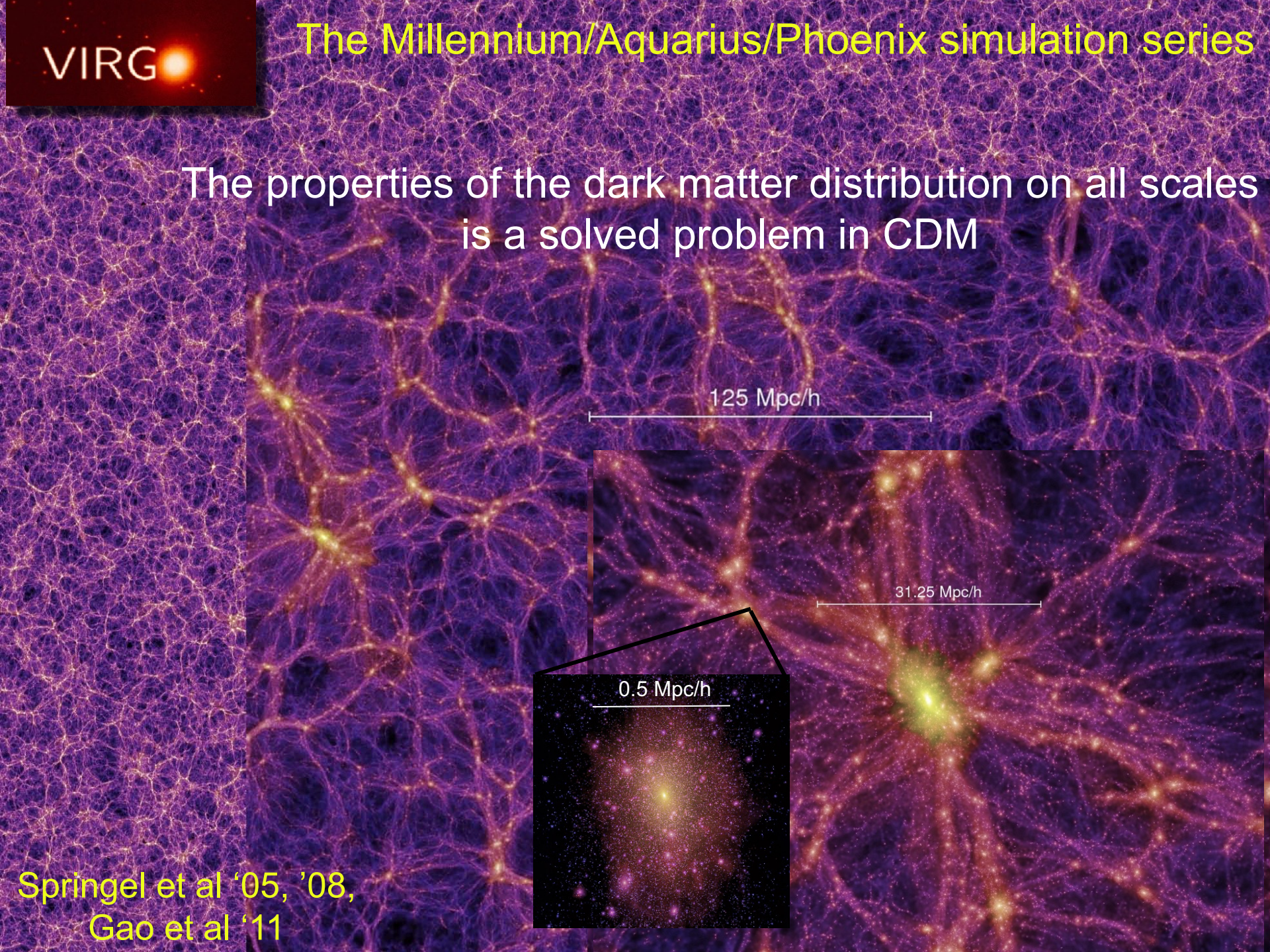
The properties of the dark matter distribution on all scales is a solved problem in CDM

125 Mpc/h

31.25 Mpc/h

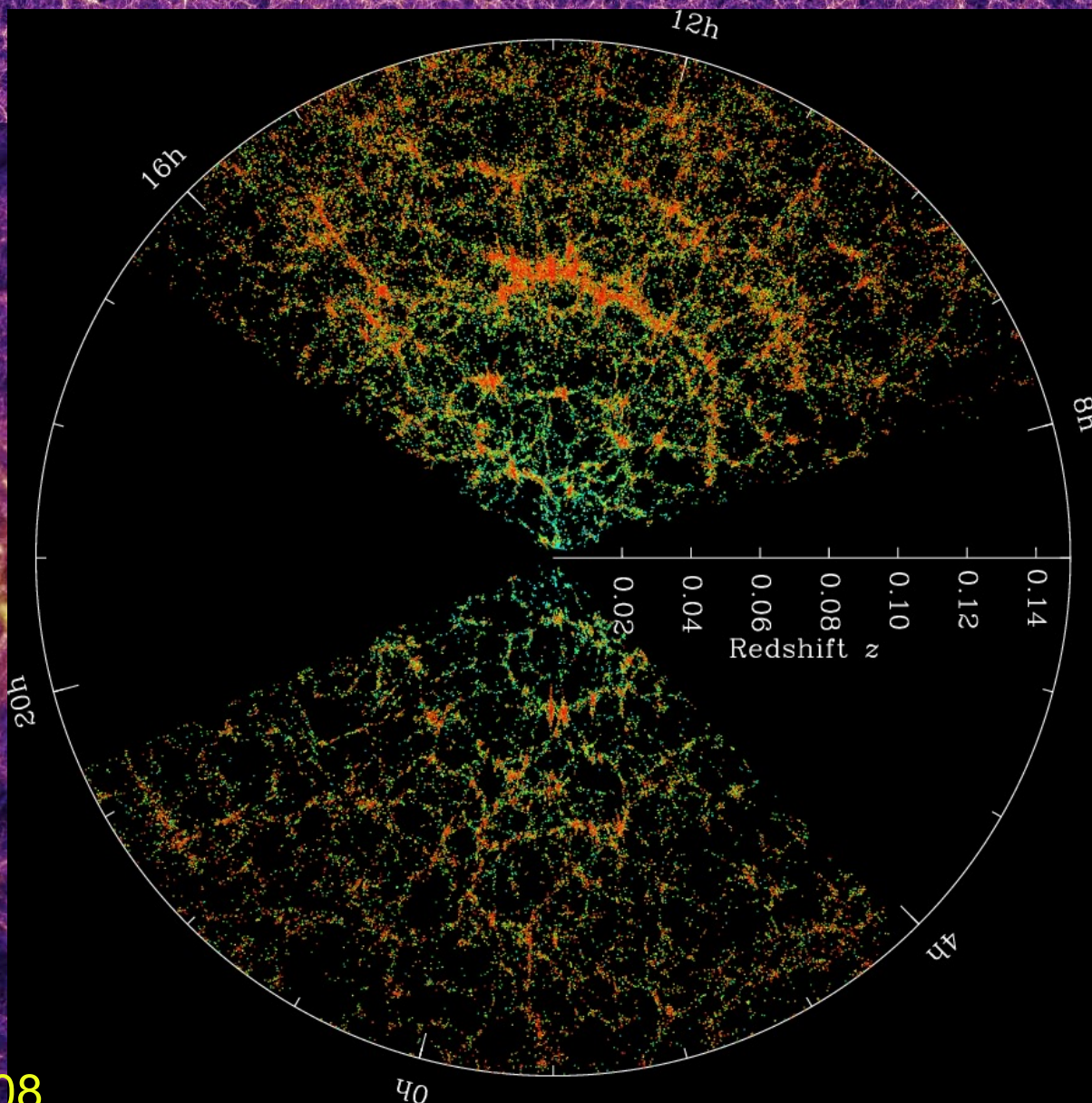
0.5 Mpc/h

Springel et al '05, '08,
Gao et al '11



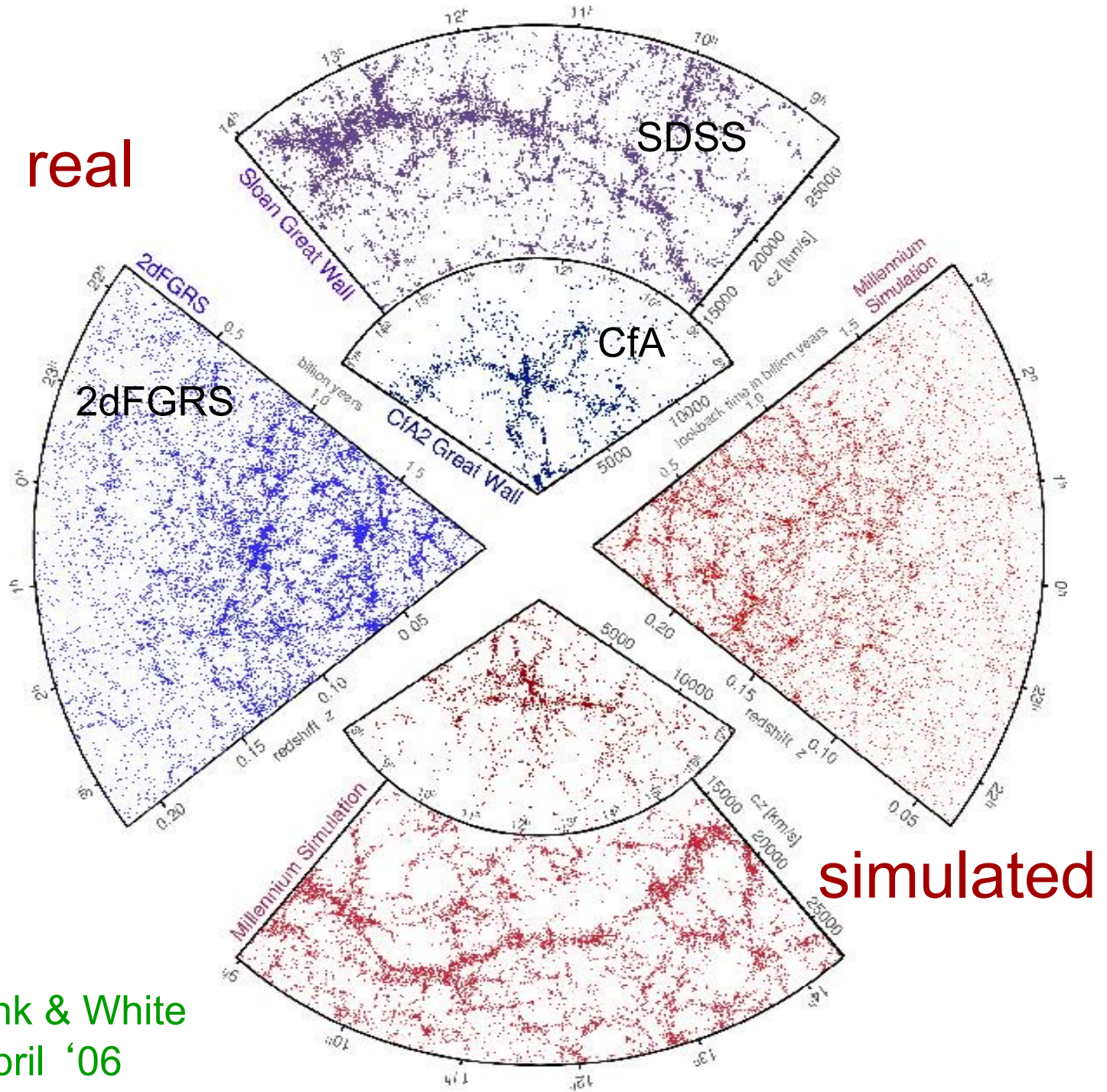
VIRGO

The Millennium/Aquarius/Phoenix simulation series



Springel et al '05, '08,
Gao et al '11

real



simulated

Galaxy distribution encodes info about dark matter and dark energy

5 billion yrs

DESI already has > 10 million spectra

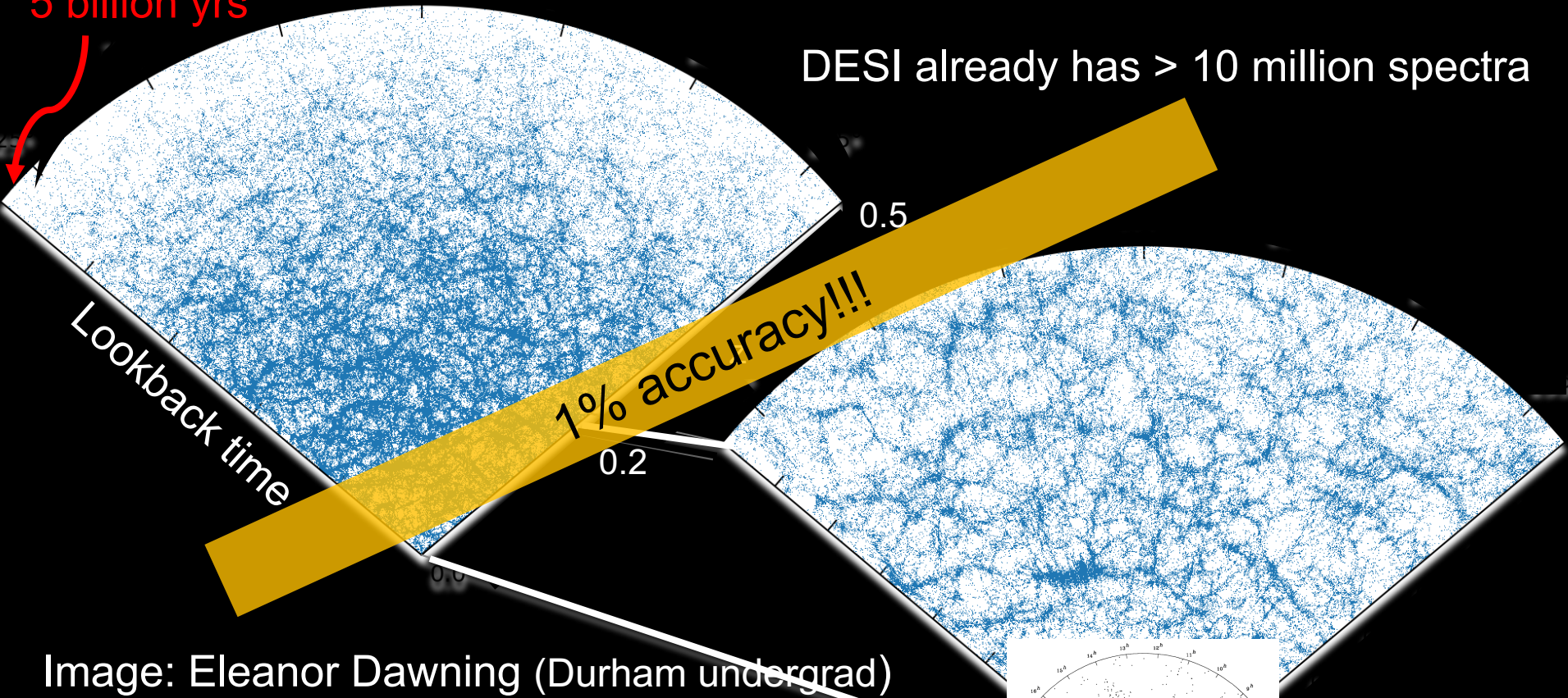


Image: Eleanor Dawning (Durham undergrad)





STARS

NEUTRINOS

Neutrinos make up $< 1\%$ of total dark matter

Can simulate their distribution with 1% accuracy

DESI may be able to measure the mass of the neutrino

200 Mpc

GAS

CDM

Elbers, Frink, Jenkins, Li, Pascoli '23

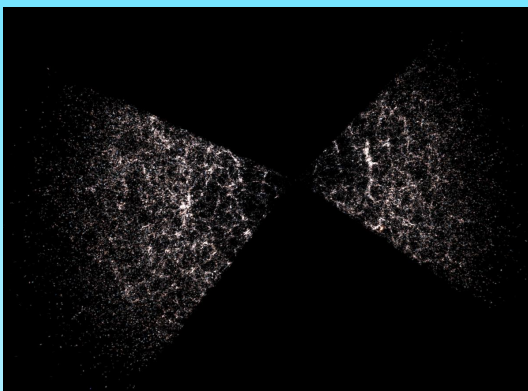
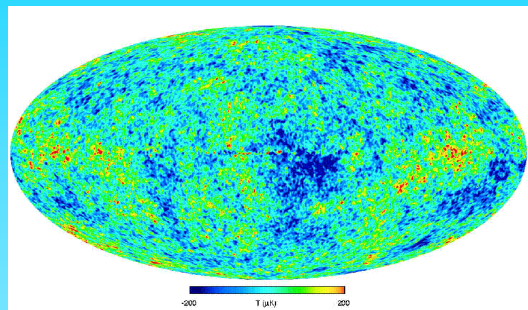


Λ CDM

Basic ideas proposed in 1980s

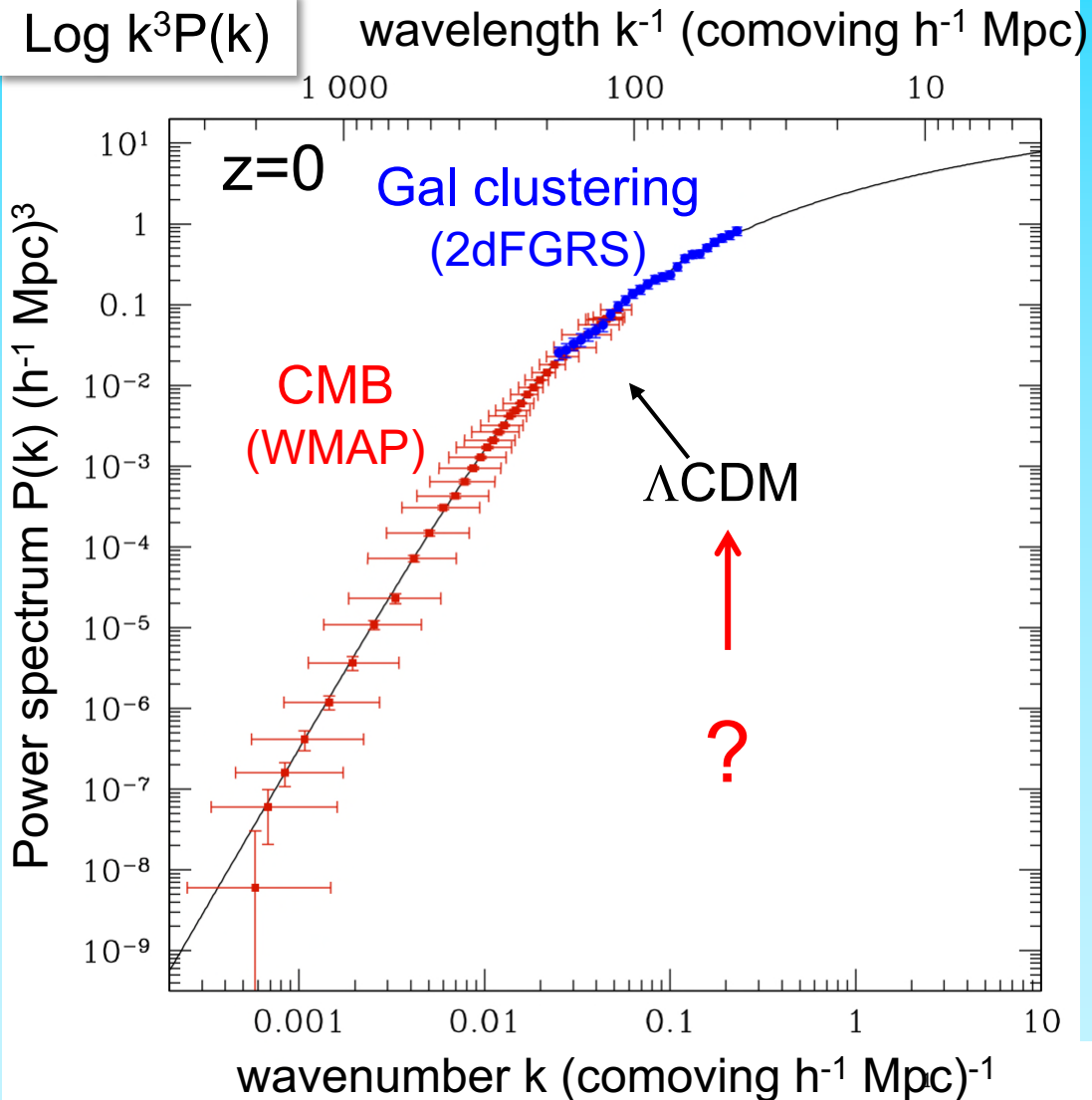
- Cosmic structure forms from primordial **quantum fluctuations** from inflation amplified by gravity of **dark matter (DM)**
- N-body simulations compared to large-scale structure data
 - **neutrinos** are **not** bulk of DM
 - **CDM** promising
- $\delta T/T$ -fluctuations in **CMB** (→ **DM**, Flatness → Λ) → **Λ CDM**
- Impressive **agreement**: modern **simulations** & **galaxy surveys**
- Λ first appeared in '90s for CDM to agree **galaxy distribution**
- Era of **1% accuracy** is here: test **Λ CDM** + measure ν **mass**

The cosmic power spectrum: from the CMB to the 2dFGRS



⇒ Λ CDM provides an excellent description of mass power spectrum from 10-1000 Mpc

Sanchez et al 06



The cosmic power spectrum: from the CMB to the 2dFGRS

Free streaming \rightarrow

$$\lambda_{\text{cut}} \propto m_x^{-1}$$

for thermal relic

$$m_{\text{CDM}} \sim 100 \text{ GeV}$$

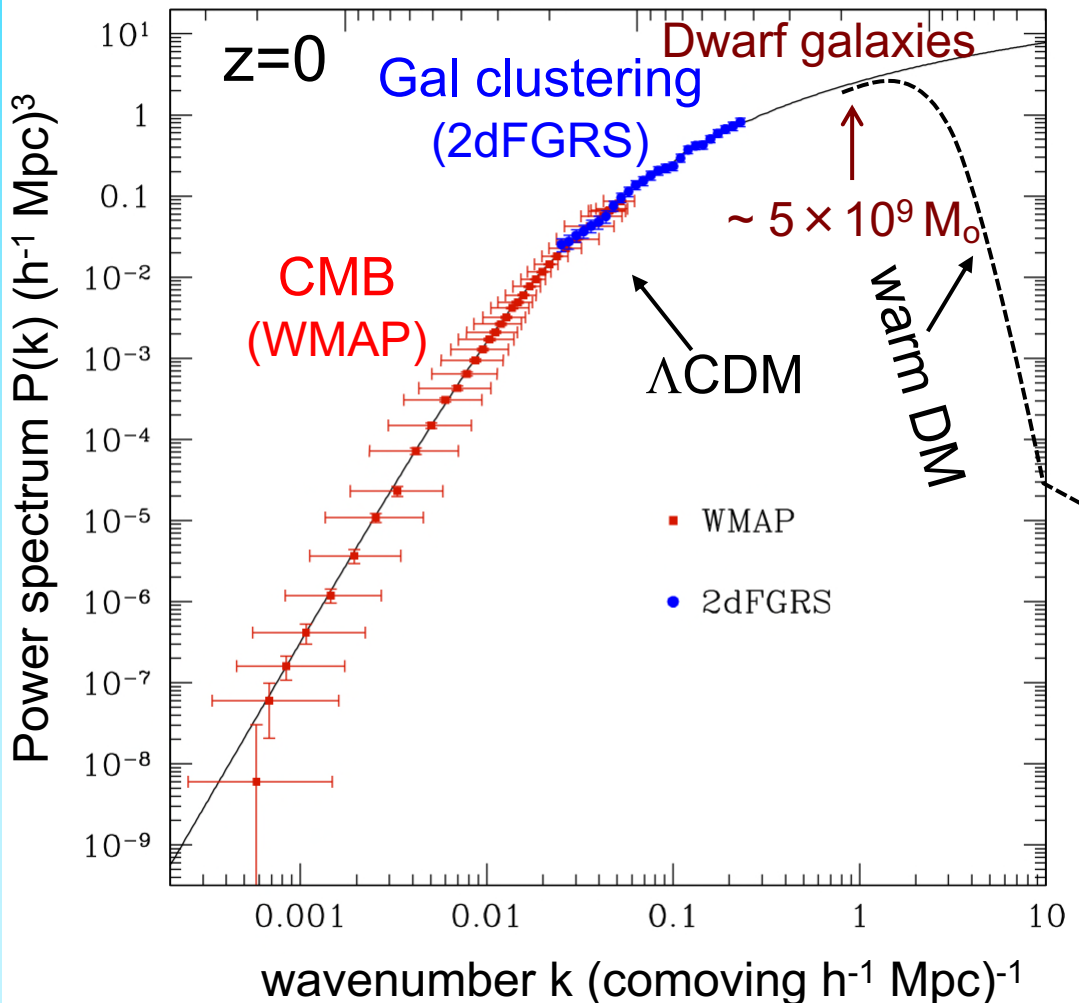
$$\text{susy}; M_{\text{cut}} \sim 10^{-6} M_{\odot}$$

$$m_{\text{WDM}} \sim \text{few keV}$$

$$\text{sterile } \nu; M_{\text{cut}} \sim 10^9 M_{\odot}$$

Log $k^3 P(k)$ wavelength k^{-1} (comoving h^{-1} Mpc)

1 000 100 10



Explain:

- Neutrino oscillations and masses
- Baryogenesis
- Absence of right-handed neutrinos in standard model
- Dark matter

Sterile neutrino minimal standard model (ν MSM; Boyarski+ 09):

- Extension of SM w. 3 sterile neutrinos: 2 of GeV; 1 of keV mass
- If $\Omega_N = \Omega_{DM}$, 2 parameters: mass, lepton asymmetry/mixing angle
- GeV particles may be detected at CERN (SHiP)
- Dark matter candidate can be detected by X-ray decay

Observational tests of Λ CDM

Fundamental prediction of Λ CDM

→ Primordial PS of density perturbations + random phases

Can test this in **two regimes**:

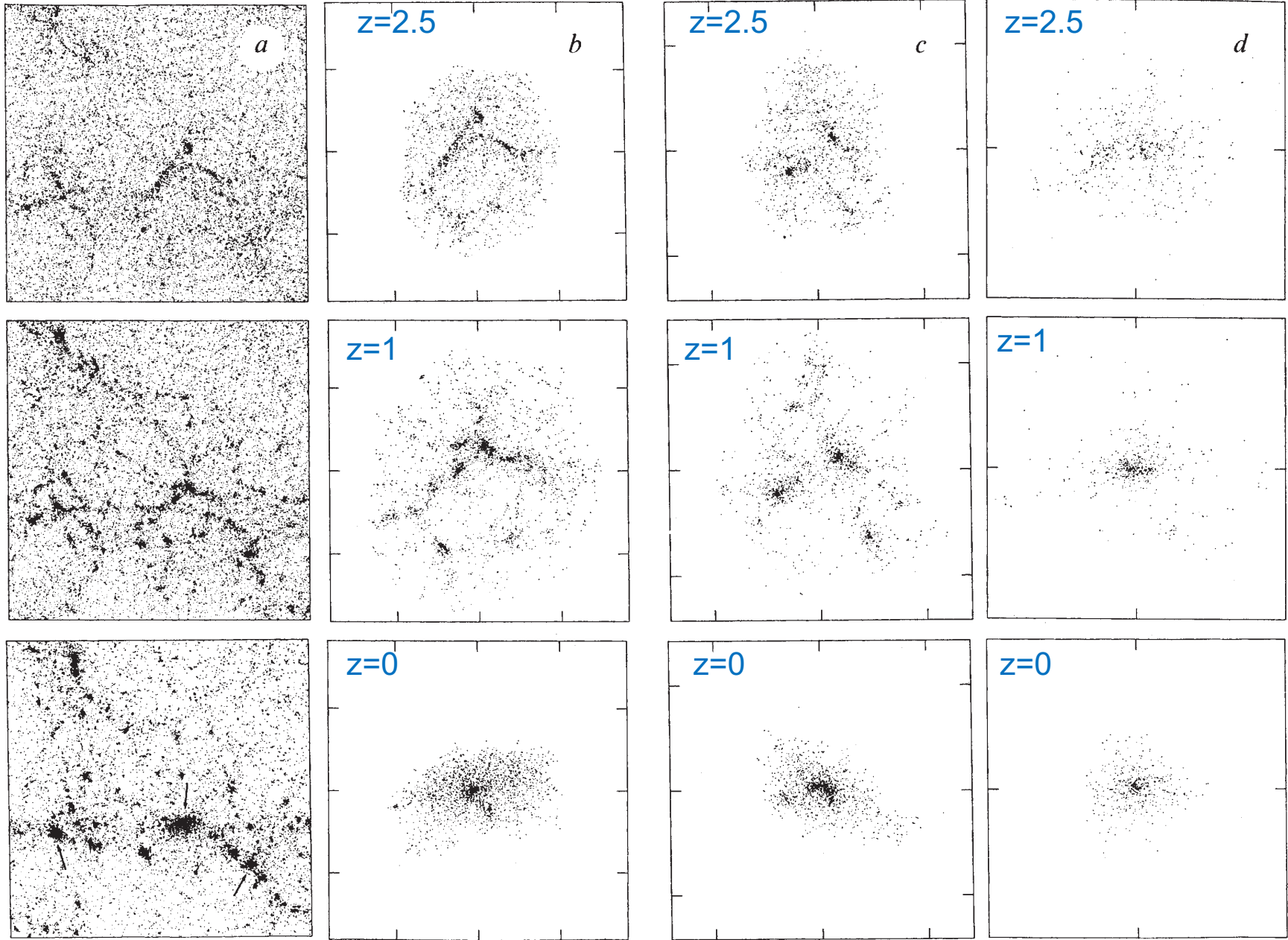
Linear regime: cosmic microwave background ✓
large-scale structure ✓

Evolved non-linear regime: dark matter halos →

Nature of the dark matter

- abundance
- structure
- clustering

Formation of CDM halos



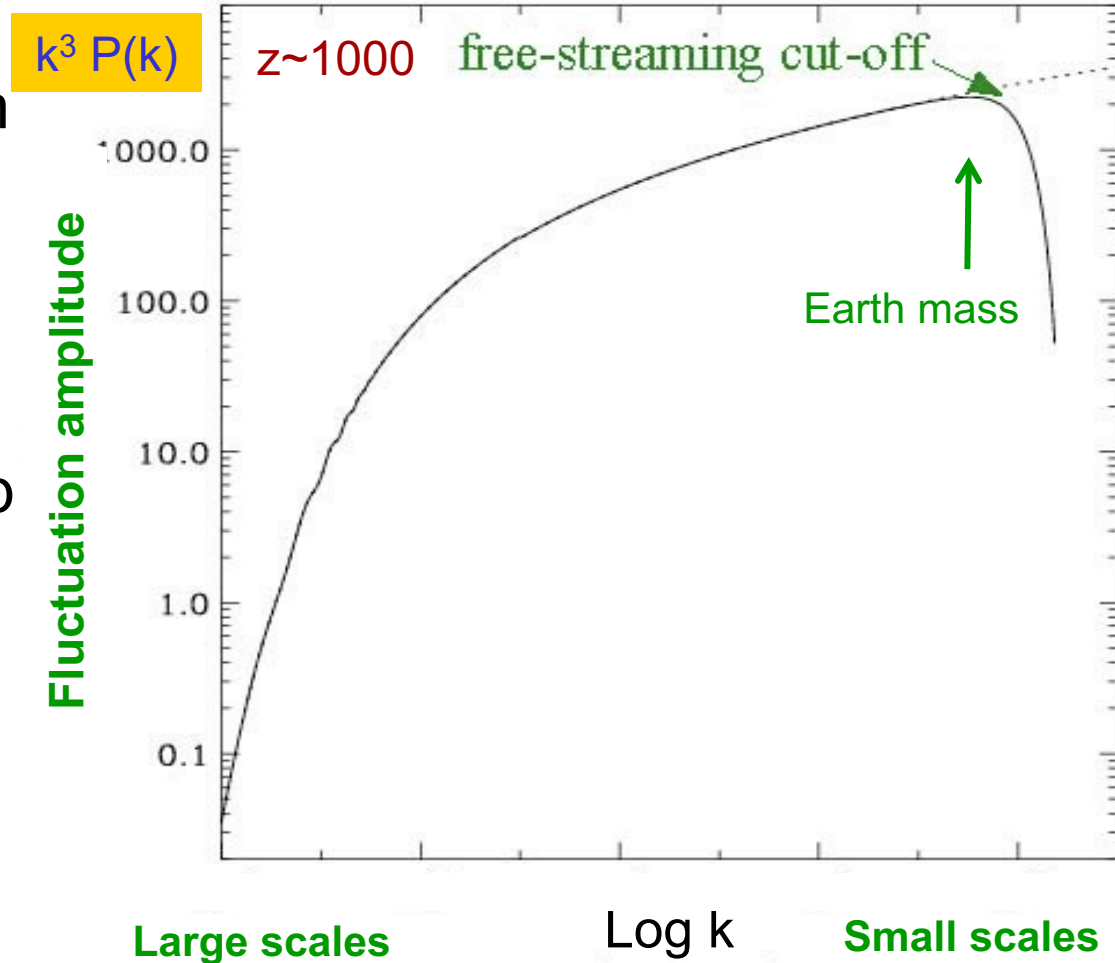
We now know:

- halo mass function down to cutoff mass
- the internal structure of halos of all mass

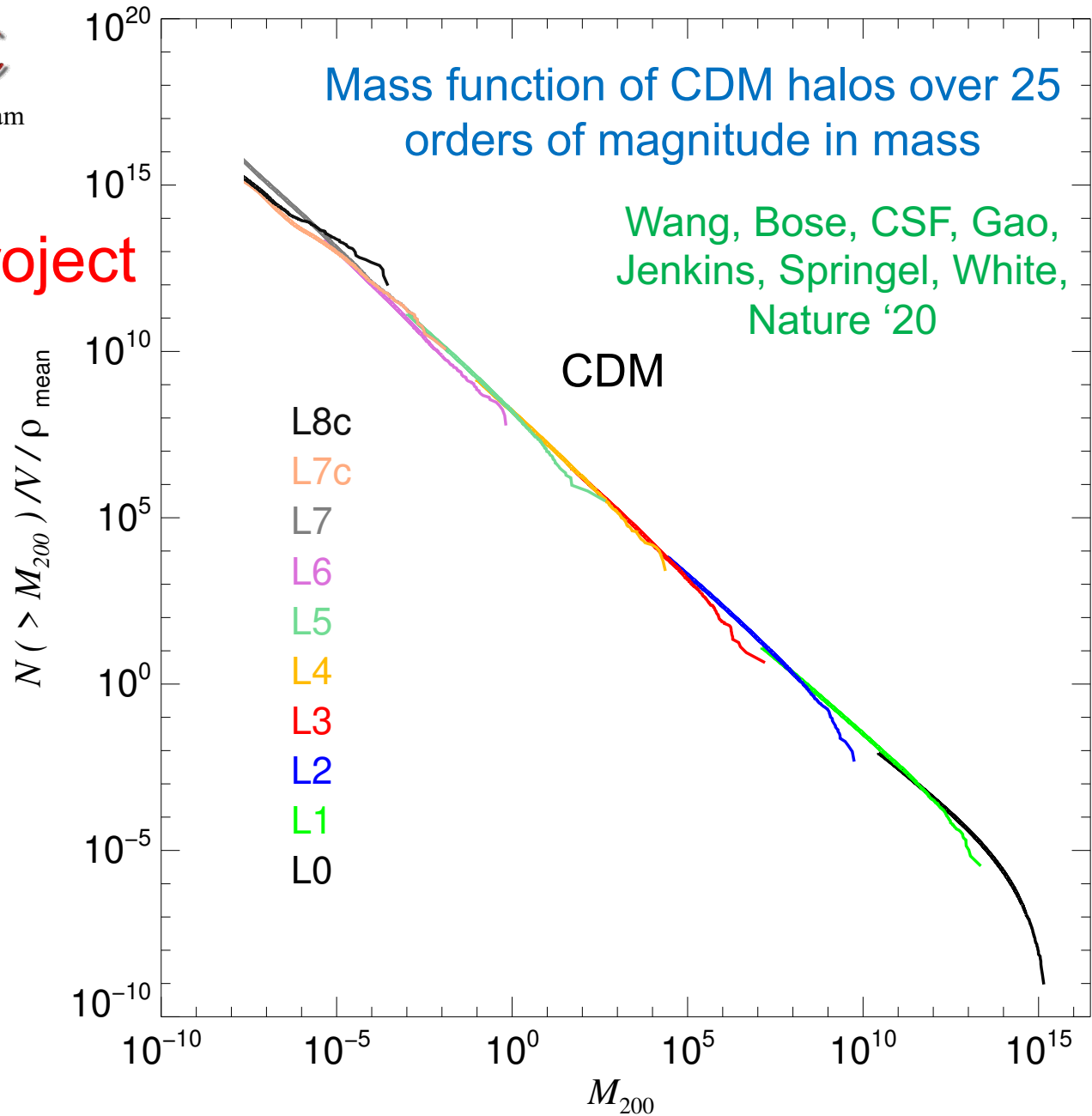
The cold dark matter power spectrum

The linear power spectrum
("power per octave")

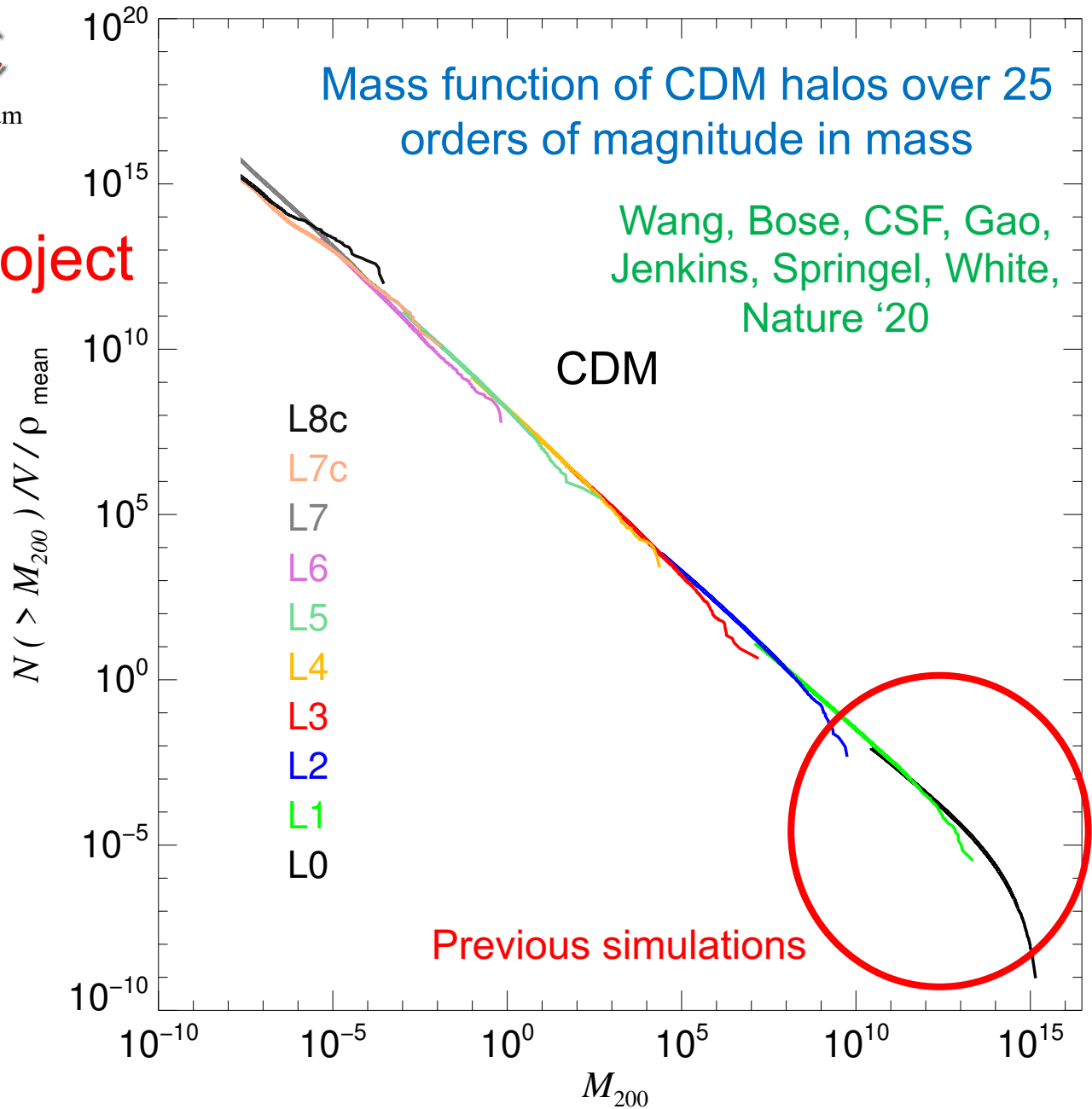
Assumes a 100GeV wimp
Green et al '04



The VVV project



The VVV project



The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

$$M_{\text{char}} = 10^{14} M_{\odot}$$

Base Level

L0

150 Mpc

The VVV simulation

Planck cosmology

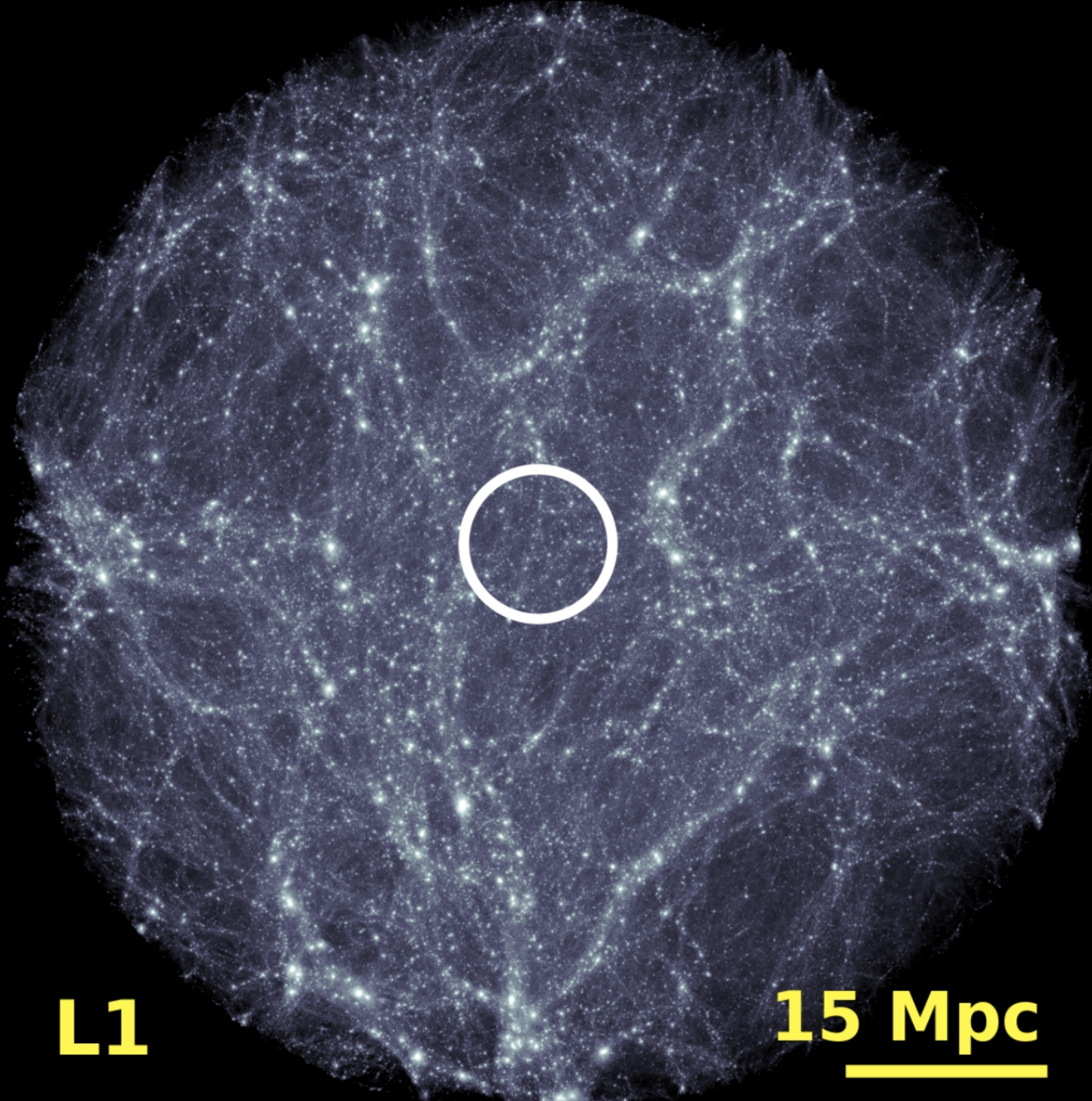
Dark matter only

Dynamic range of
30 orders of
magnitude in mass

$$M_{\text{char}} = 10^{12} M_{\odot}$$

Zoom Level 1

Wang, Bose et al 2020



L1

15 Mpc

The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

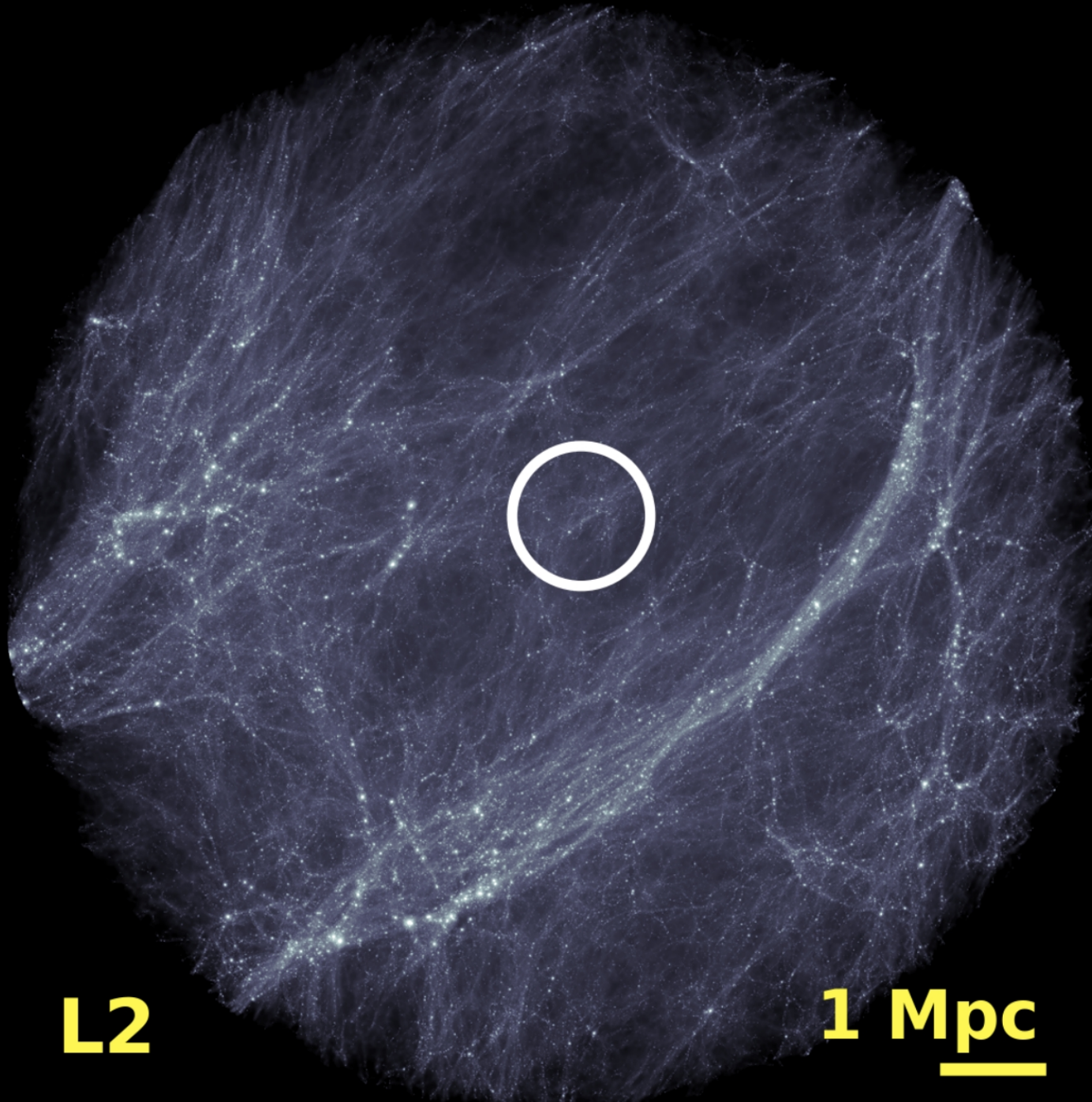
$$M_{\text{char}} = 10^9 M_{\odot}$$

Zoom Level 2

Wang, Bose et al 2020

L2

1 Mpc



The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

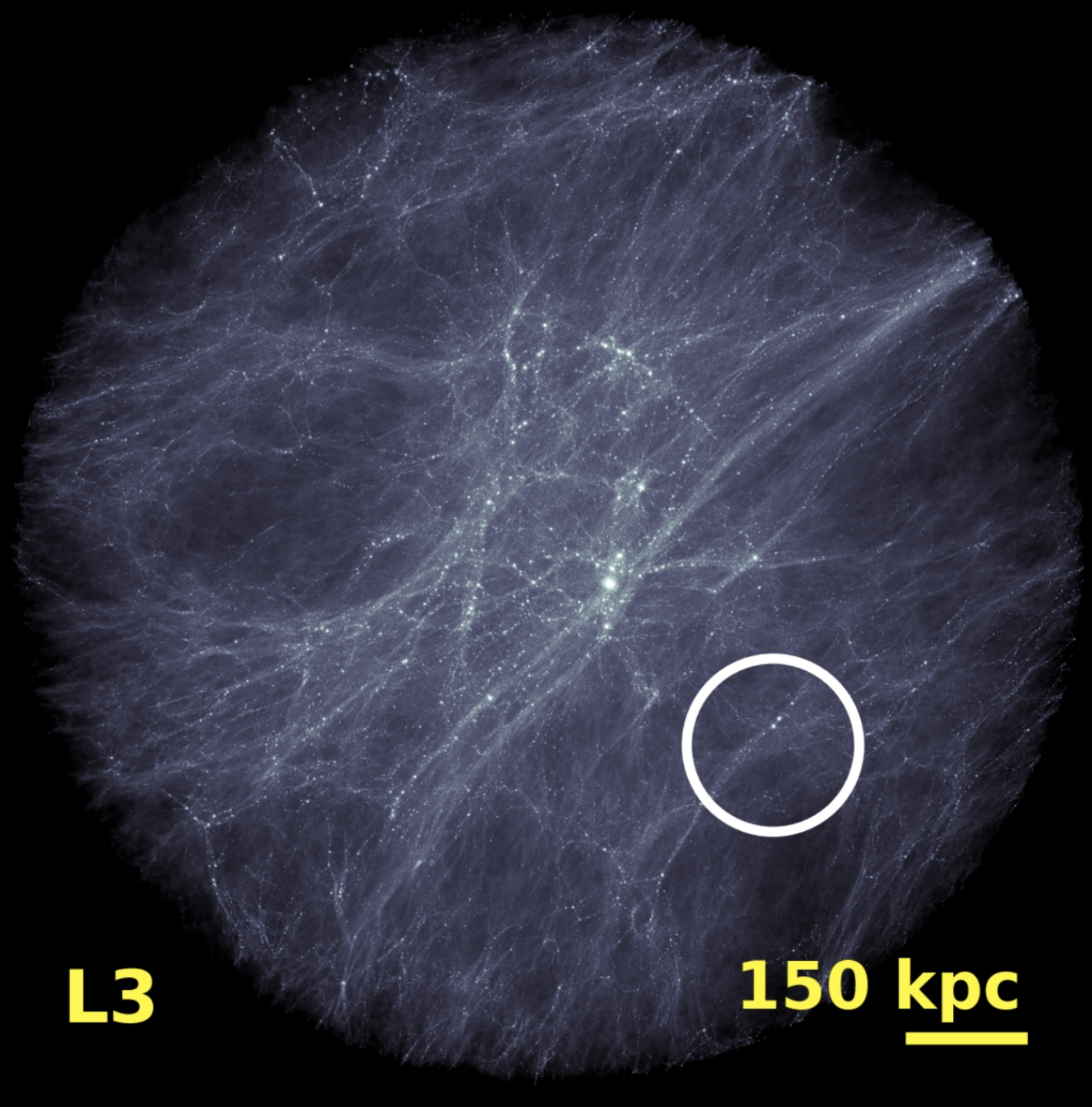
$$M_{\text{char}} = 10^6 M_{\odot}$$

Zoom Level 3

Wang, Bose et al 2020

L3

150 kpc



The VVV simulation

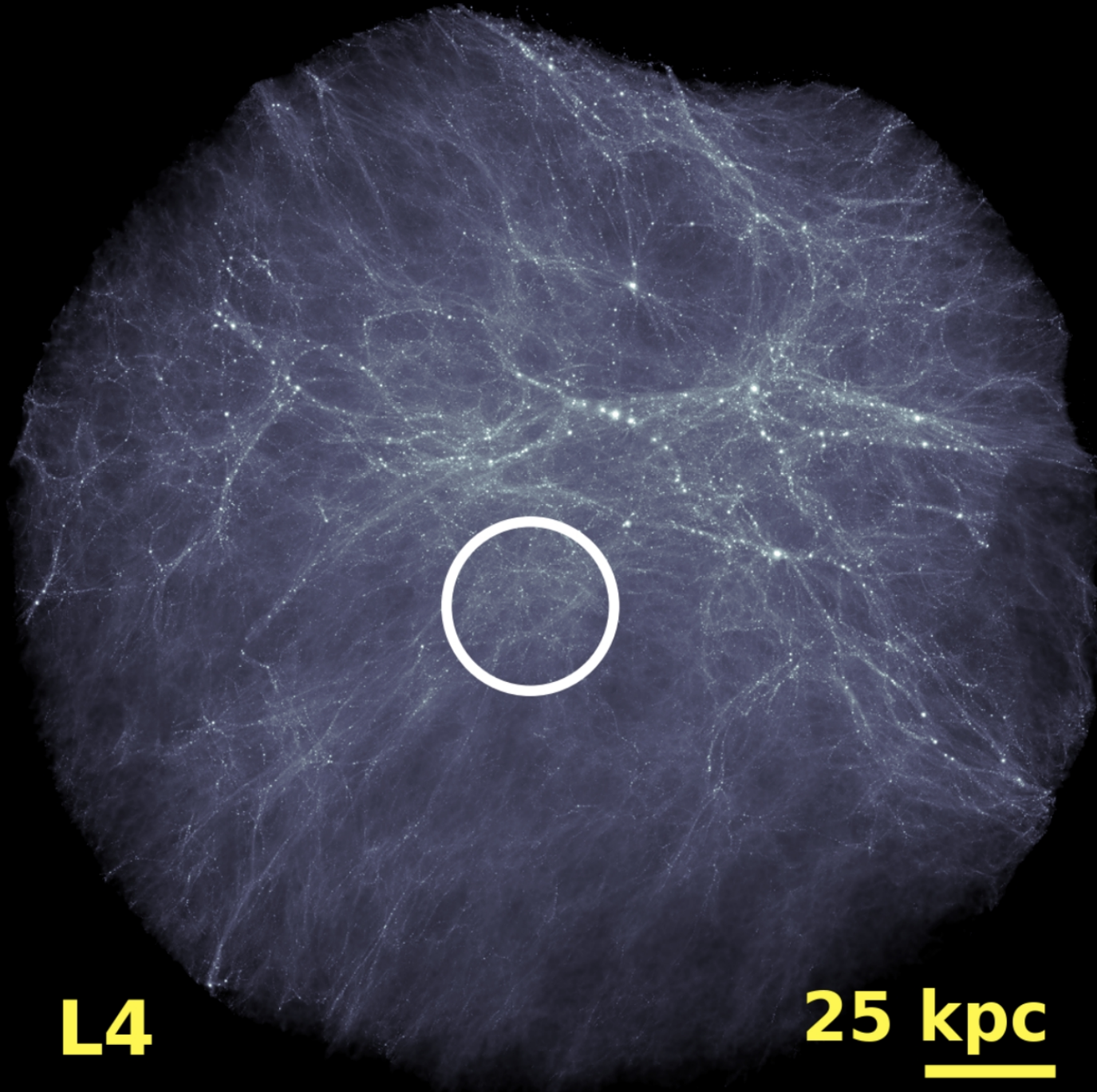
Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

$$M_{\text{char}} = 10^3 M_{\odot}$$

Zoom Level 4



L4

25 kpc

Wang, Bose et al 2020

The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

$$M_{\text{char}} = 10 M_{\odot}$$

Zoom Level 5



L5

5 kpc

Wang, Bose et al 2020

The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

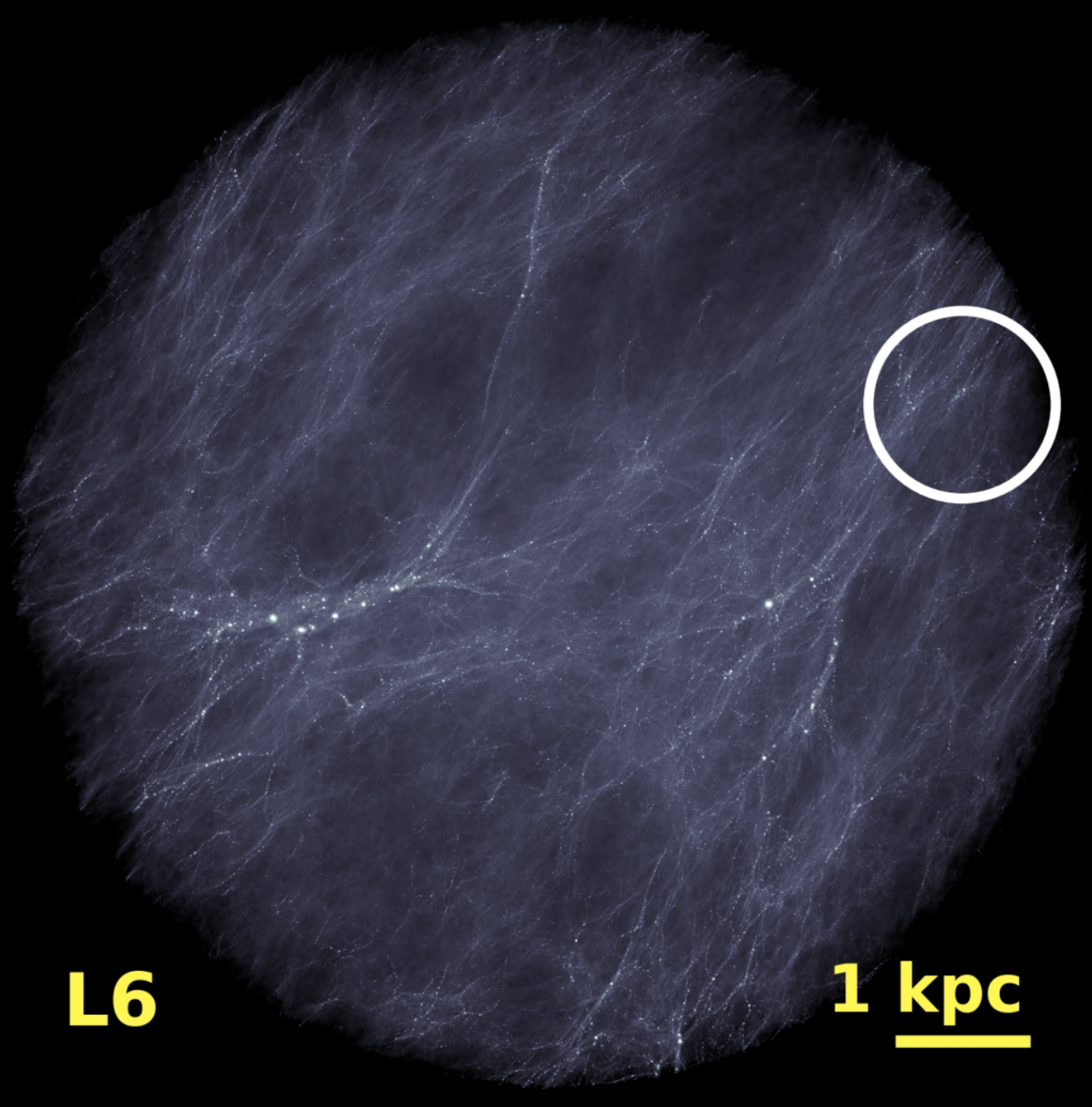
$$M_{\text{char}} = 10^{-1} M_{\odot}$$

Zoom Level 6

L6

1 kpc

Wang, Bose et al 2020



The VVV simulation

Planck cosmology

Dark matter only

Dynamic range of
30 orders of
magnitude in mass

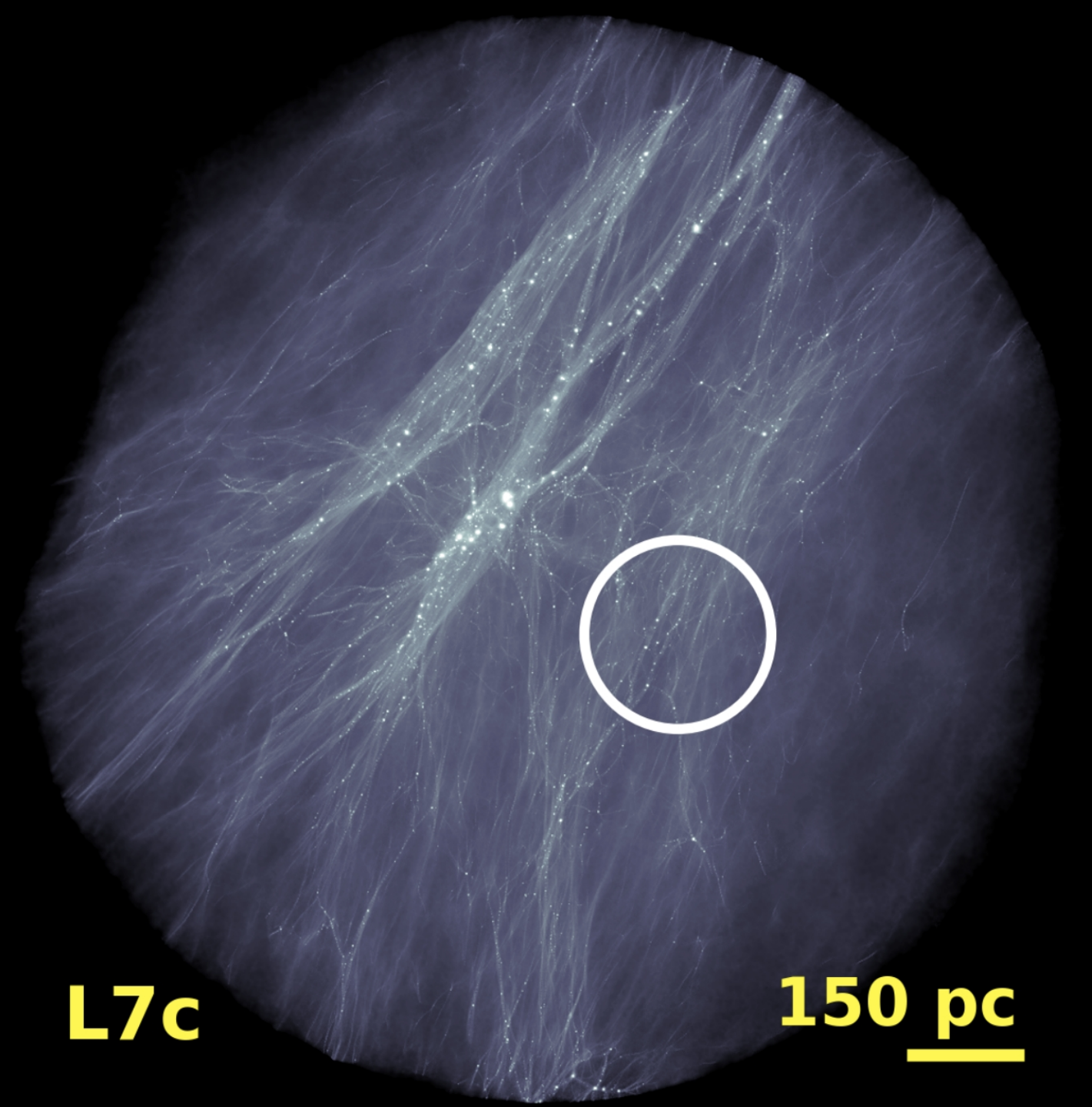
$$M_{\text{char}} = 10^{-4} M_{\odot}$$

Zoom Level 7

Wang, Bose et al 2020

L7c

150 pc



The VVV simulation

Planck cosmology

Dark matter only

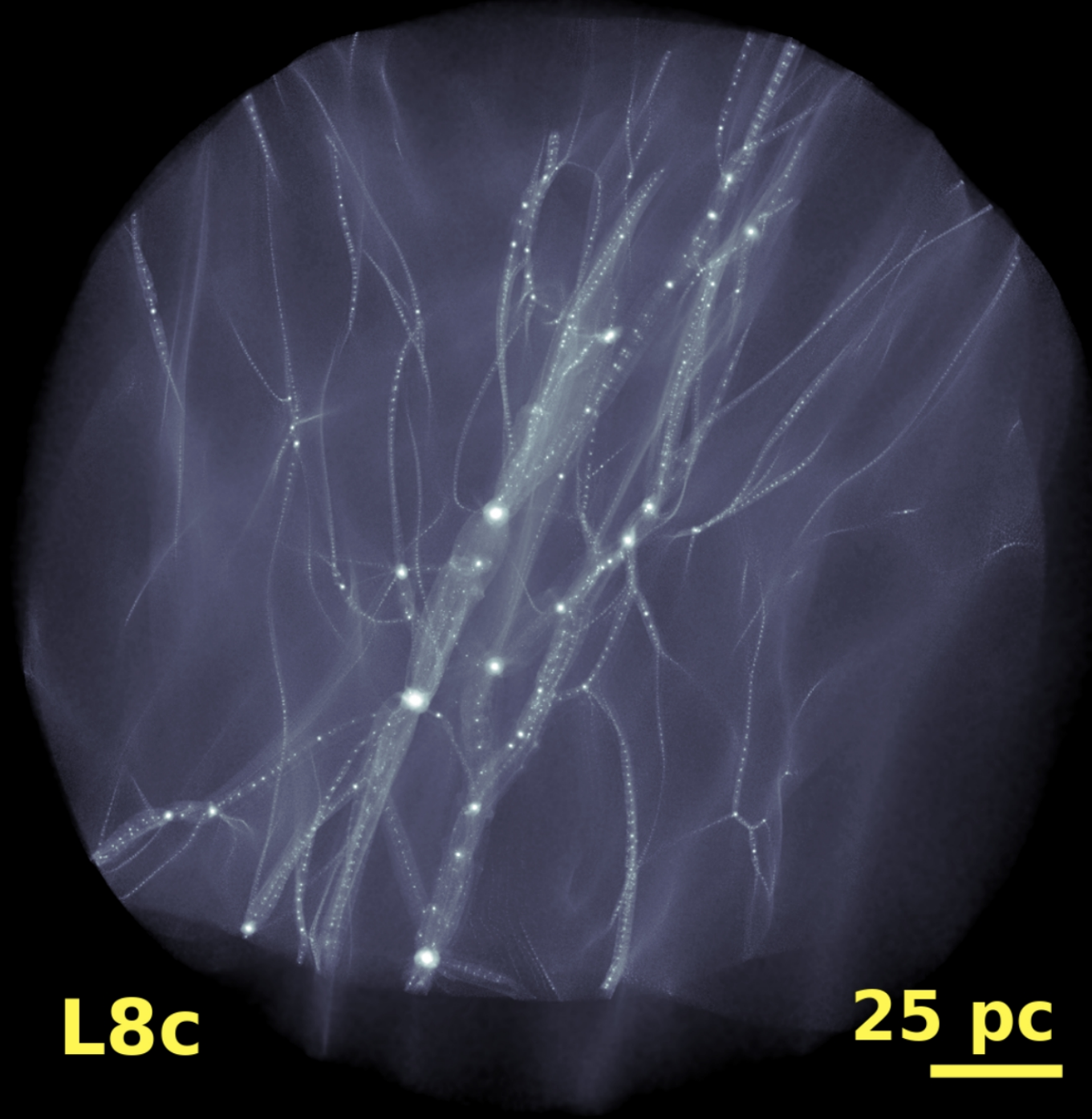
Dynamic range of
30 orders of
magnitude in mass

$$M_{\text{char}} = 10^{-6} M_{\odot}$$

Zoom Level 8

The density of
this region is
only $\sim 3\%$ of the
cosmic mean

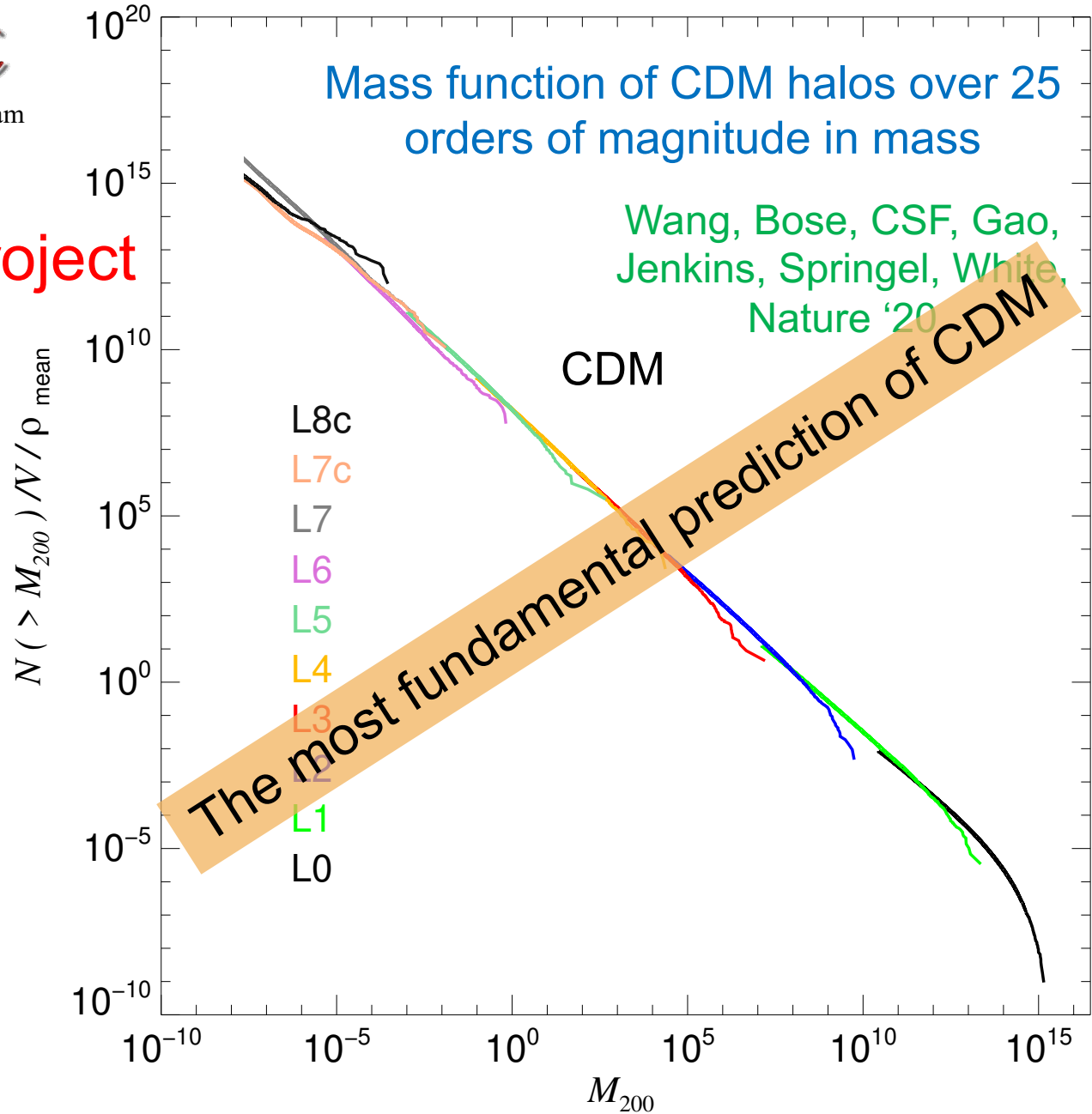
Wang, Bose et al 2020



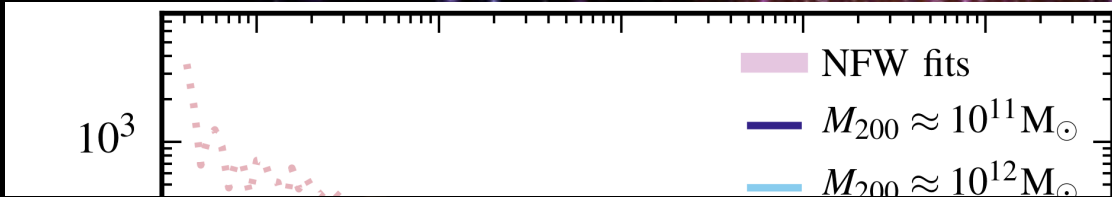
L8c

25 pc

The VVV project



The density profile of cold dark matter halos



Shape of halo profiles
~independent of halo mass & parameters

are “cuspy” -
the centre

formula:

$$\frac{\delta_c}{(1+r/r_s)^2}$$

White '97)

halos and
earlier have
higher densities (bigger δ)

Universal halo density profiles

$$\frac{\rho(r)}{\rho_{crit}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

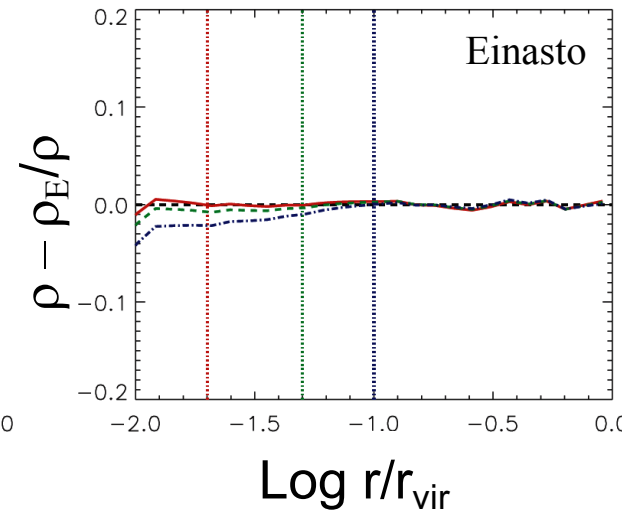
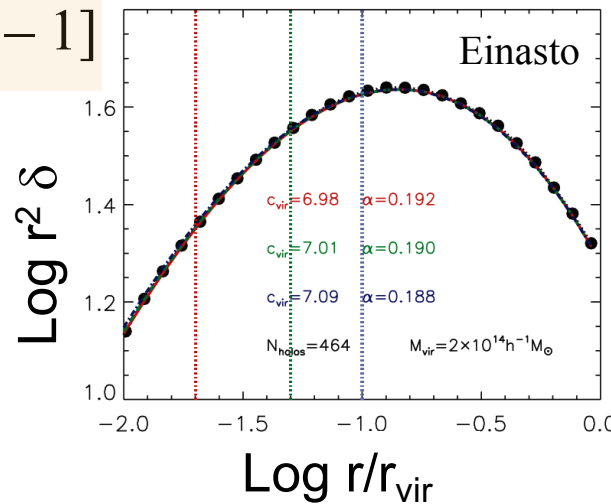
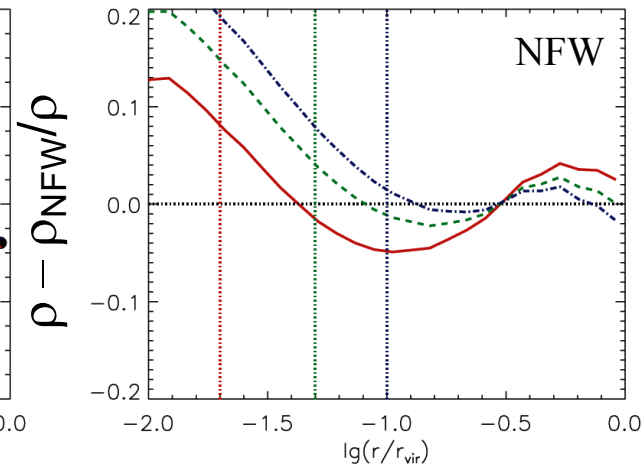
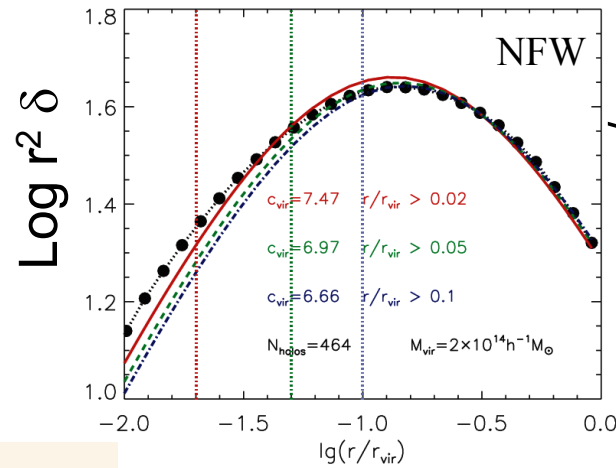
The “Einasto” formula

$$\ln(\rho(r)/\rho_{-2}) = (-2/\alpha) [(r/r_{-2})^\alpha - 1]$$

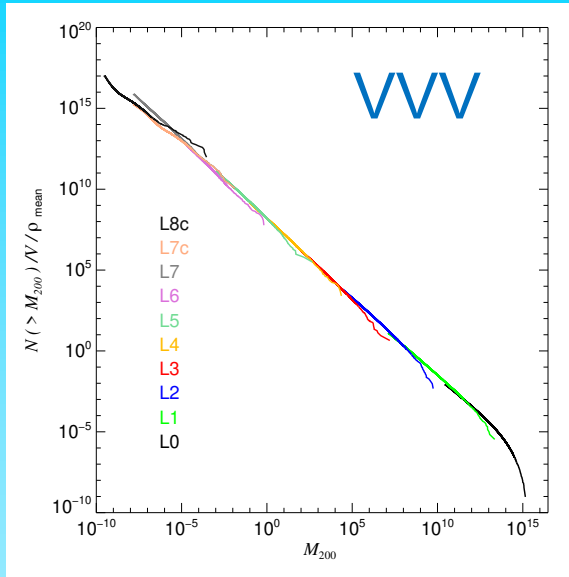
Fits mean profiles even better

Gao, N, F, W + 2008

Averaged cluster mass halos fit with NFW and Einasto

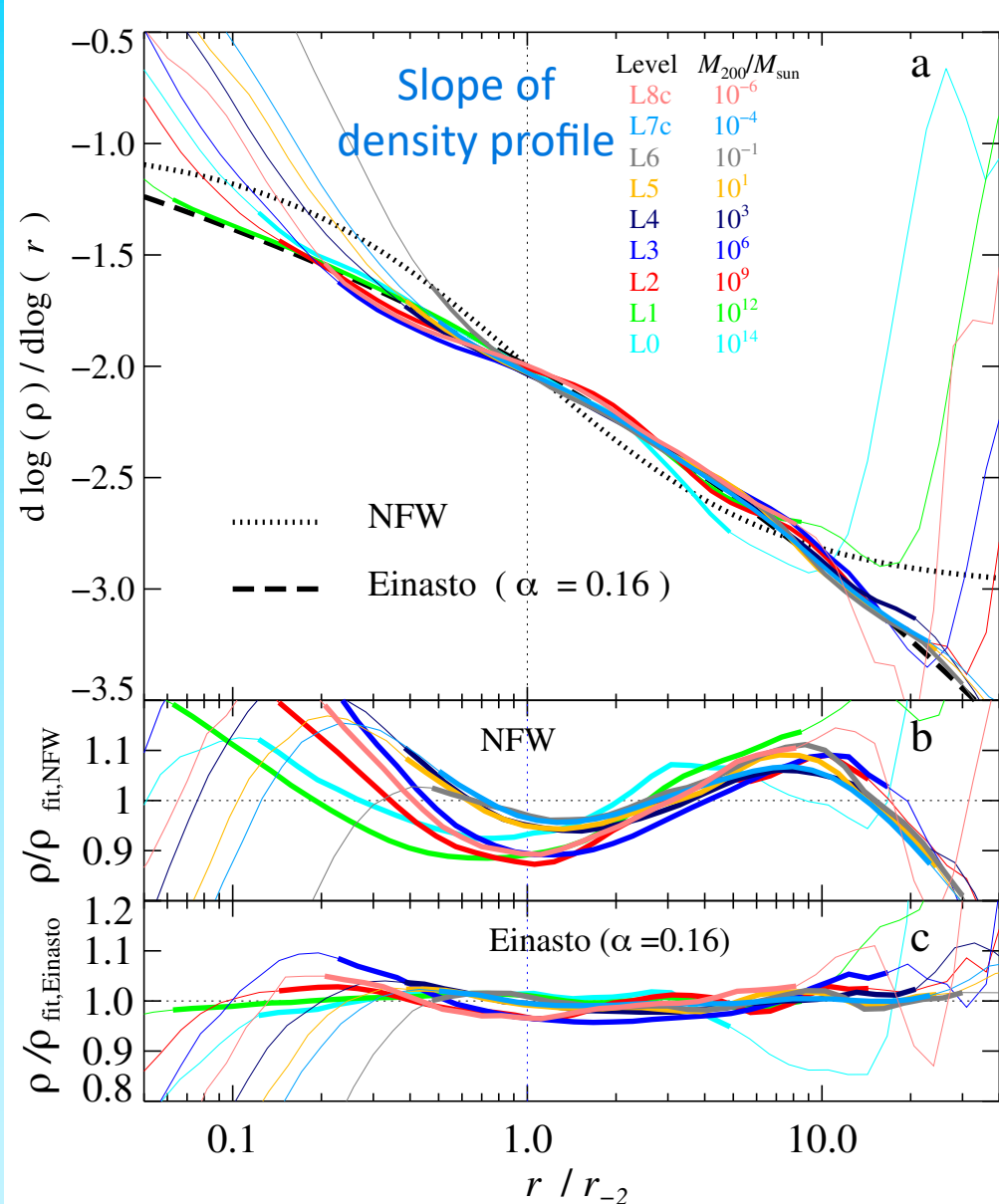


Density profiles of ALL halos



Over **25 orders** of magnitude in halo **mass** and 4 orders of magnitude in density, the mean density **profiles** of halos are **fit** by **NFW** to within **20%** and by **Einasto** ($\alpha = 0.16$) to within **7%**

Wang, Bose, CSF + '20





Observational tests of Λ CDM

Fundamental prediction of Λ CDM

→ Primordial PS of density perturbations + random phases

Can test this in **two regimes**:

Linear regime: cosmic microwave background
large-scale structure

Evolved non-linear regime: dark matter halos →

Nature of the dark matter

- abundance
- structure
- clustering

A galaxy formation primer

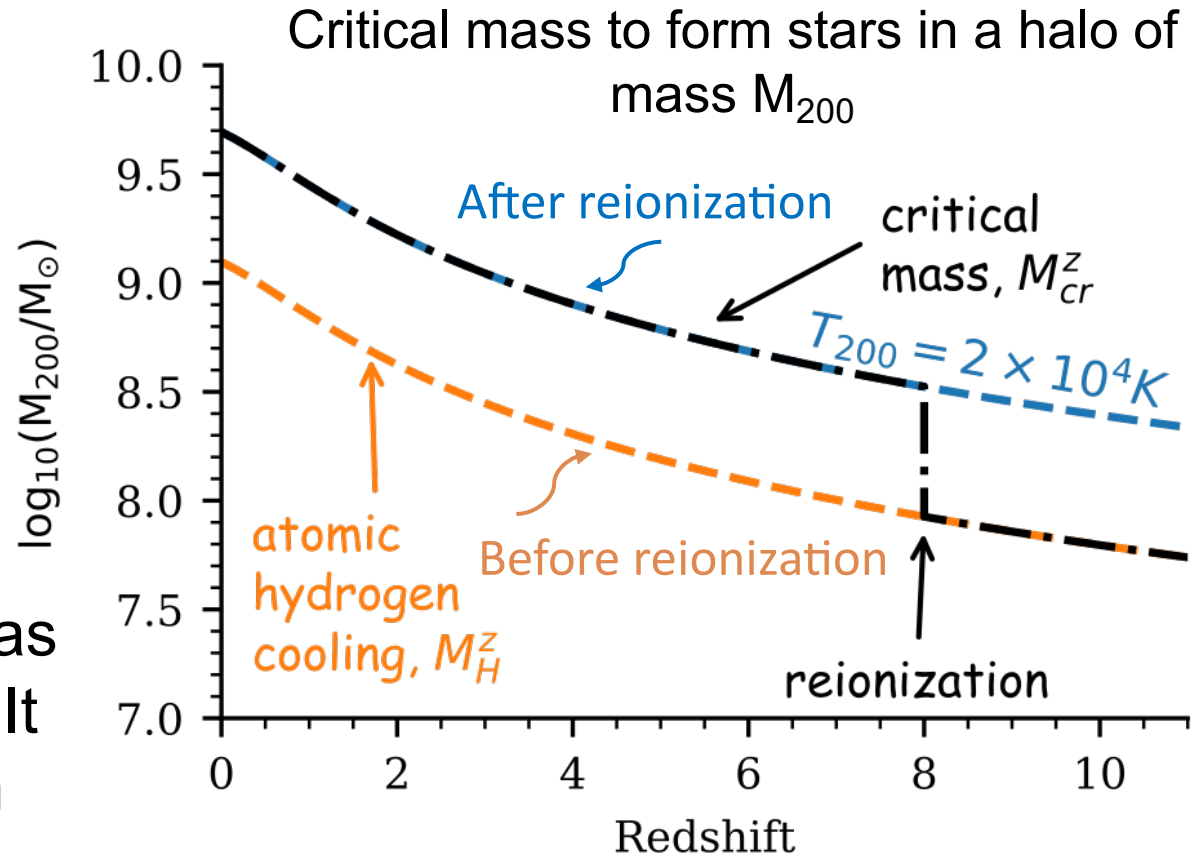
In which halos do galaxy form?

1. Before reionization, stars can only form if atomic H cooling is effective: $\rightarrow T > 7000 \text{ K}$

$$M_H^z \sim (4 \times 10^7 M_\odot) \left(\frac{1+z}{11} \right)^{-3/2}$$

2. After H reionization, gas is heated to $T = 2 \times 10^4 \text{ K}$. It can only cool and form stars in halos with:

$$T_{\text{vir}} > T_{\text{IGM}} = 2 \times 10^4 \text{ K}$$



A galaxy formation primer

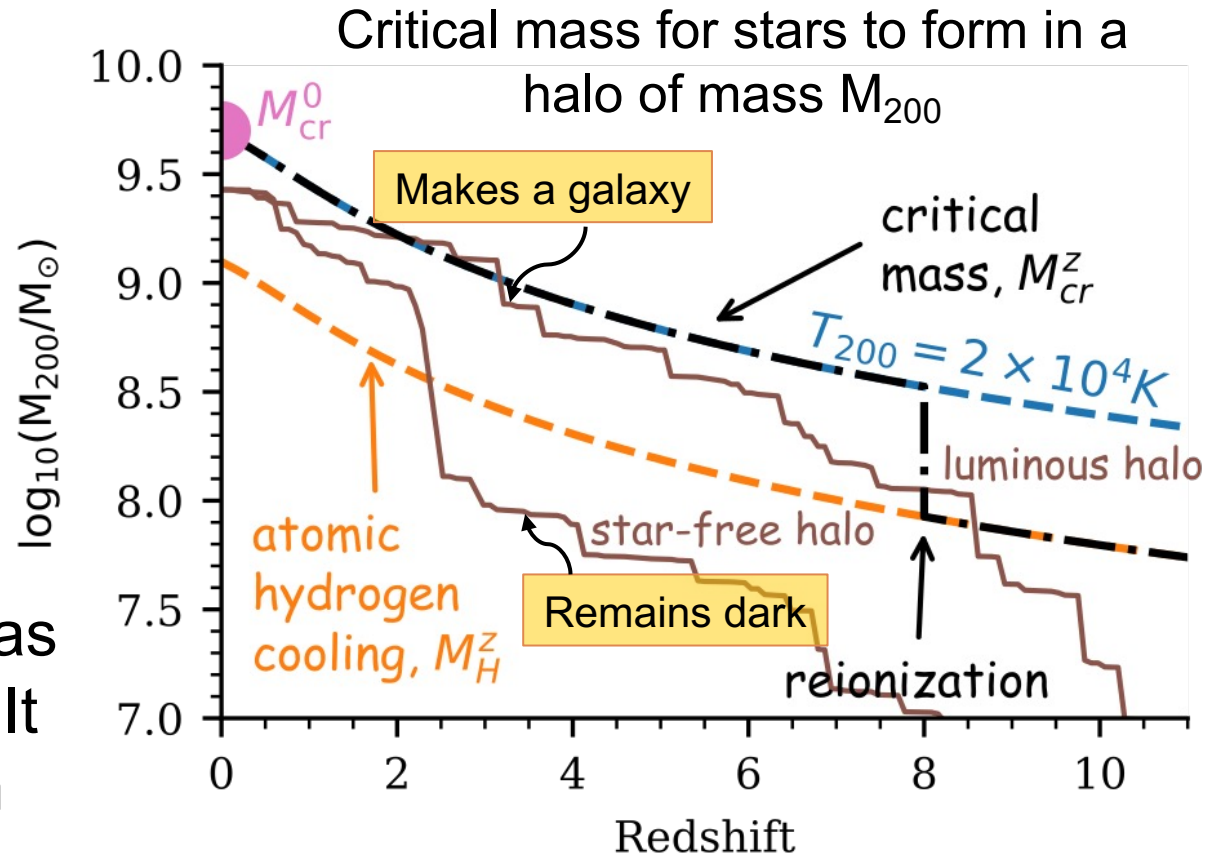
1. Before reionization, stars can only form if gas can cool for which

→ $T > 7000 \text{ K}$

$$M_H^z \sim (4 \times 10^7 M_\odot) \left(\frac{1+z}{11} \right)^{-3/2}$$

2. After H reionization, gas is heated to $T = 2 \times 10^4 \text{ K}$. It can only cool and form stars in halos with:

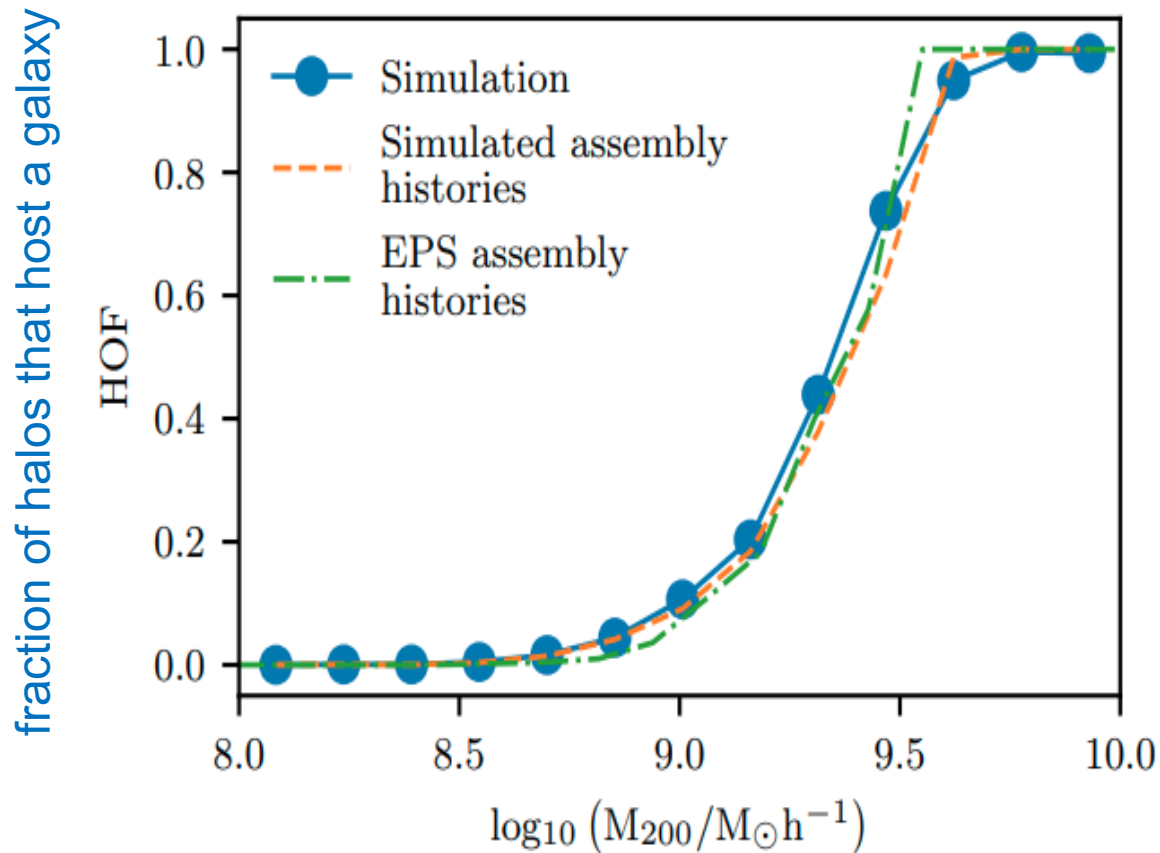
$$T_{\text{vir}} > T_{\text{IGM}} = 2 \times 10^4 \text{ K}$$



Benitez-Llambay & CSF '20

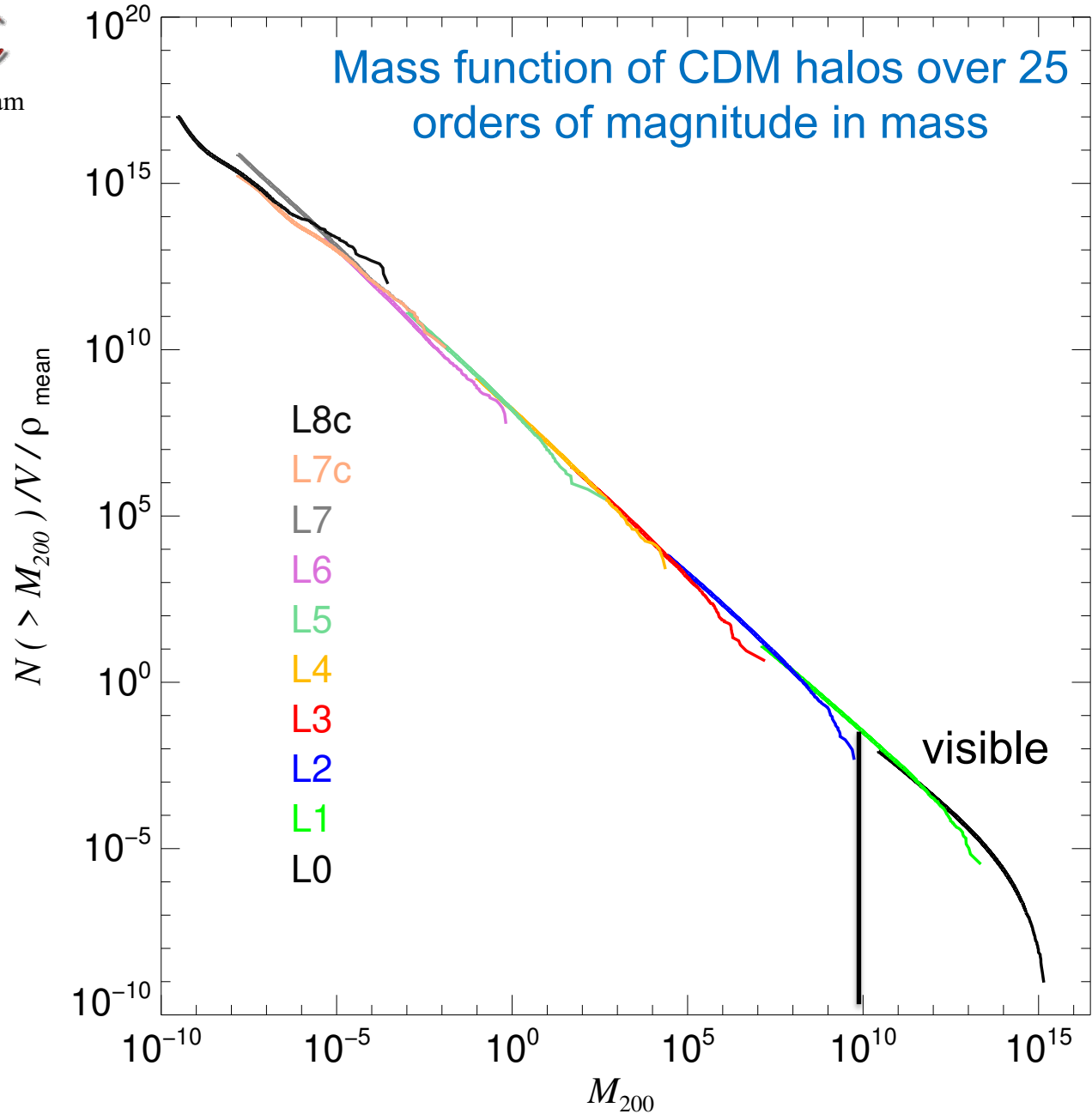
A galaxy formation primer

Halo Occupation Fraction (HOF): fraction of halos of a given mass today that host a galaxy



$M < 3 \times 10^8 M_{\odot}$
 → dark

$M > 3 \times 10^9 M_{\odot}$
 → visible



The small-scale “crisis”: four problems

“Solved” in:

- | | | | |
|--------------------------|------|---|----------------|
| 1. “Missing satellites” | 2002 | } | Baryon effects |
| 2. “Too-big-to-fail” | 2015 | | |
| 3. “Core-cusp” | 1996 | | |
| 4. “Plane of satellites” | 2023 | | |

CDM

DM-only CDM simulations predict many more subhalos in the Milky Way than there are observed satellites

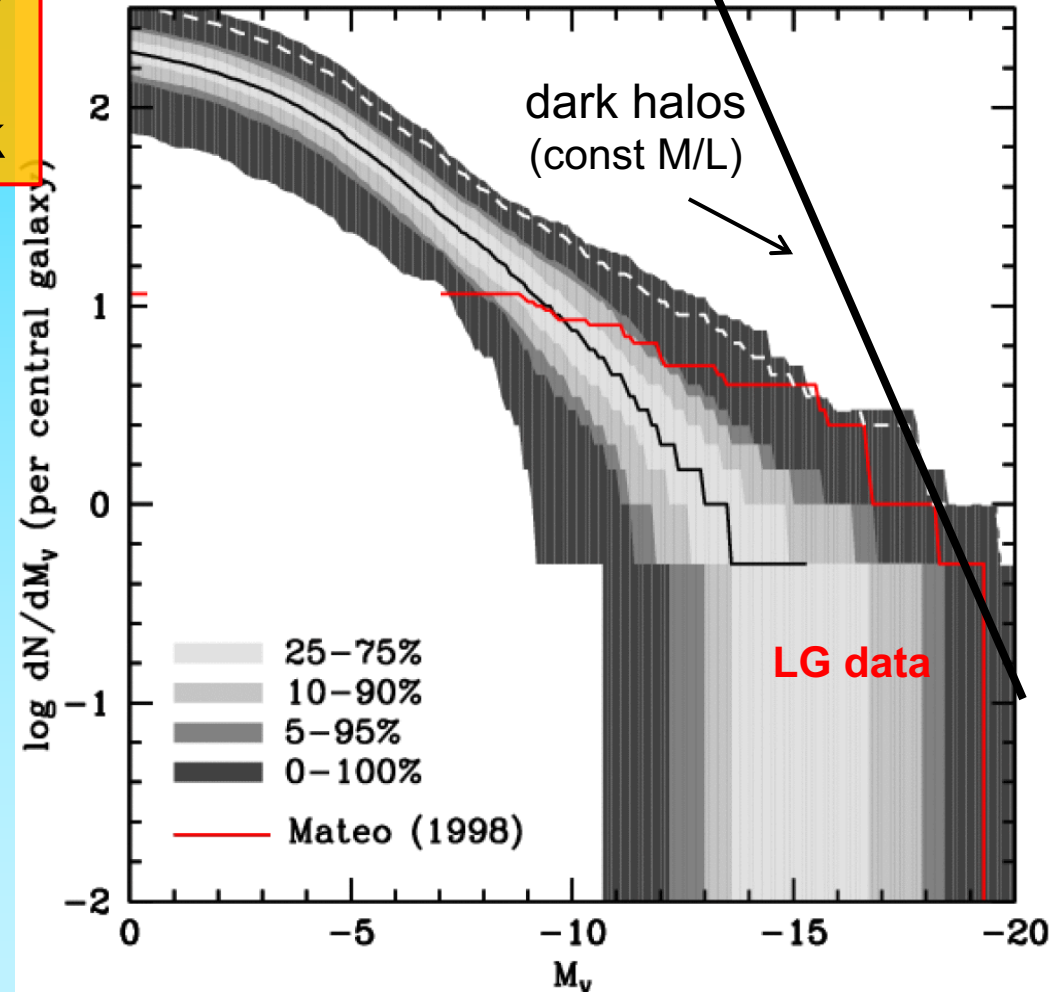
“Missing satellites” problem

Most subhalos never make a galaxy!

Luminosity Function of Local Group Satellites

Semi-analytic model of galaxy formation including effects of reionization and SN feedback

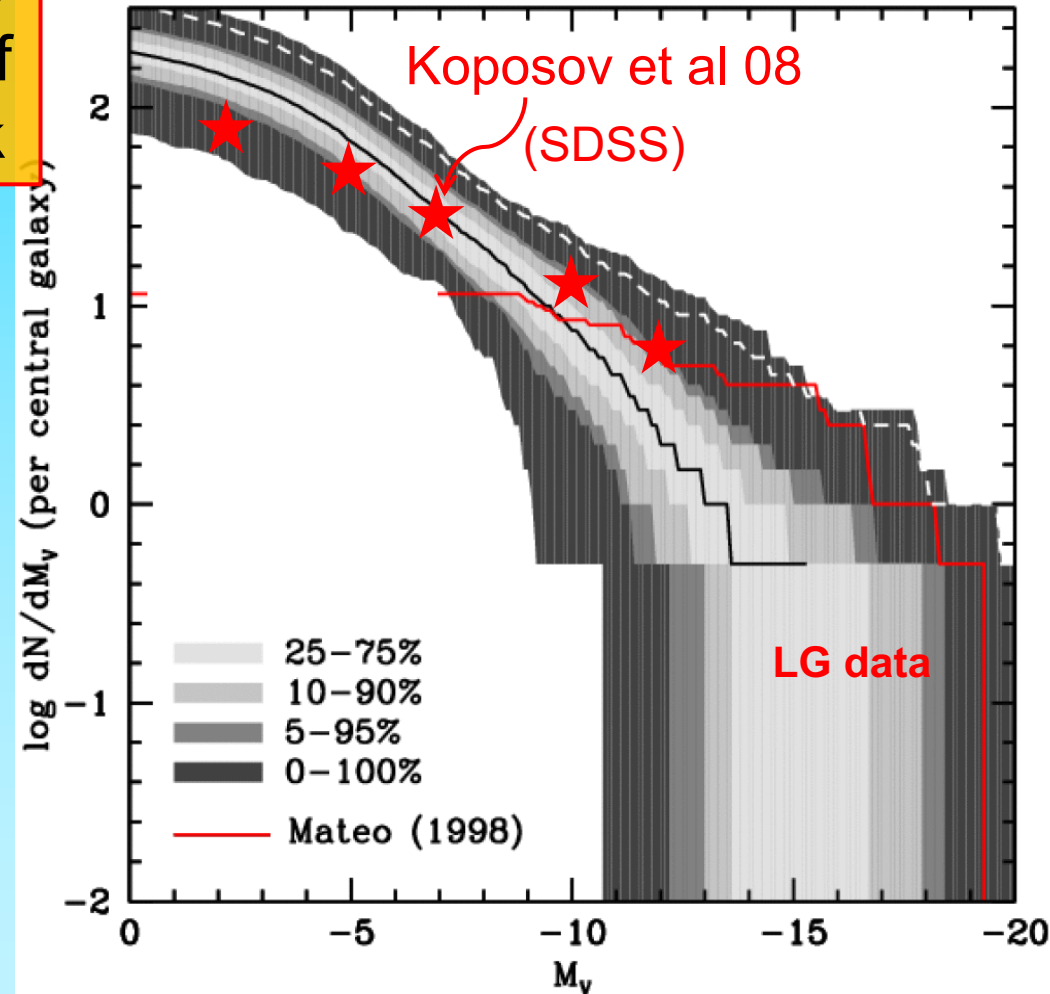
- Median model \rightarrow correct abundance of sats brighter than $M_V = -9$ ($V_{\text{cir}} > 12$ km/s)
- Model predicts many, as yet undiscovered, faint satellites



Luminosity Function of Local Group Satellites

Semi-analytic model of galaxy formation including effects of reionization and SN feedback

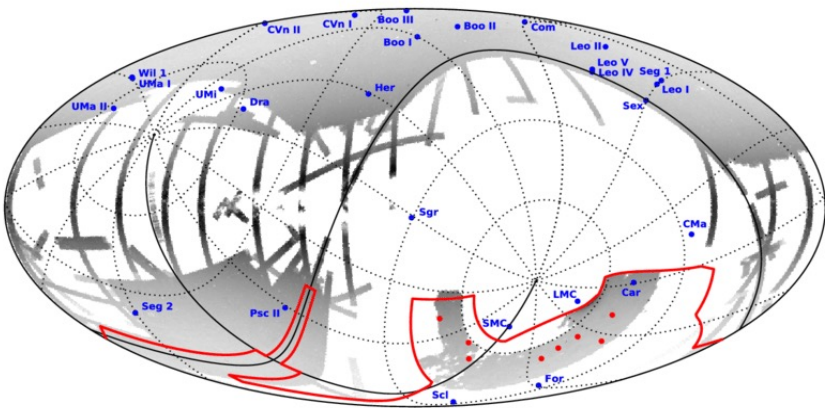
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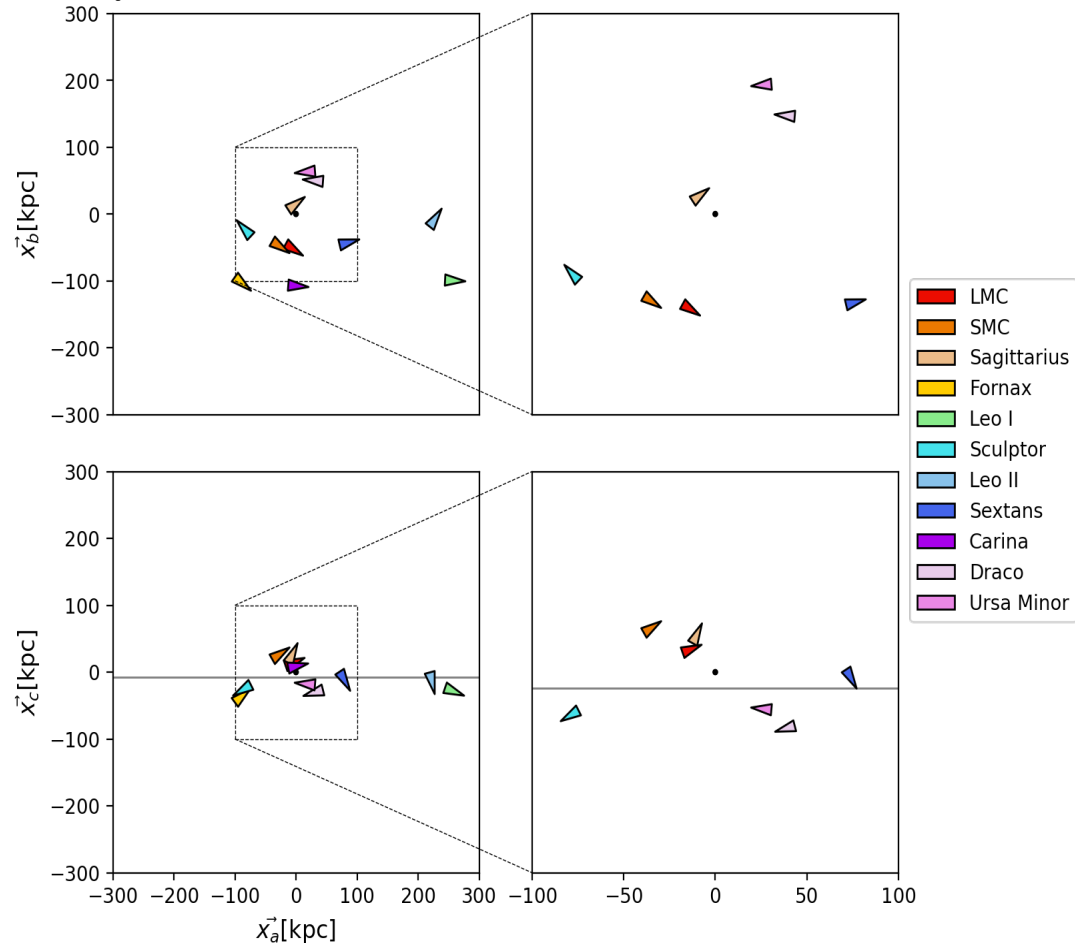
The plane of satellites in the MW

The plane of satellites in the MW

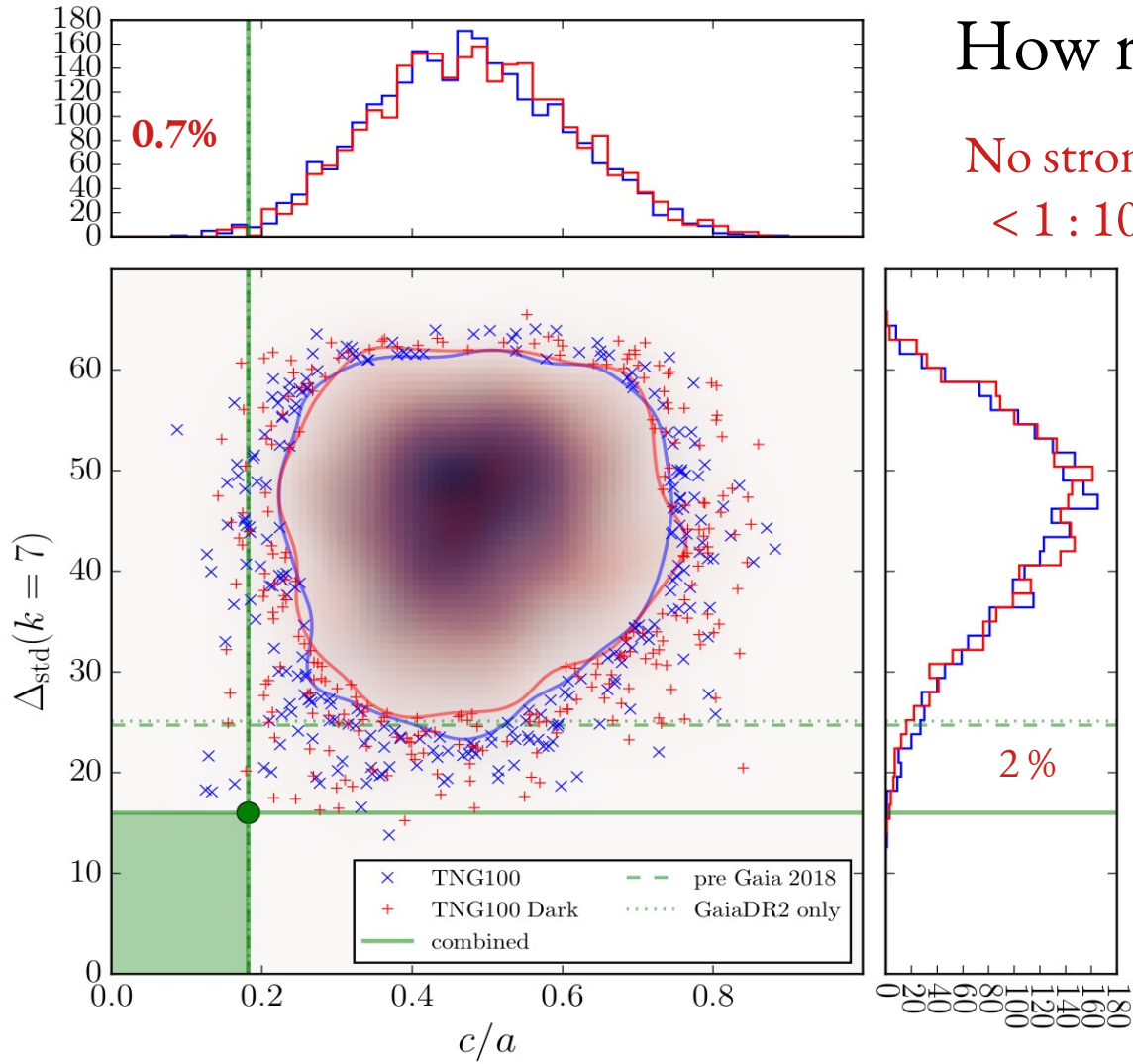
Problem: the 11 “classical” Milky Way satellites are in a thin, possibly rotating plane (Lynden-Bell 1976)



Bechtol+ 2015



The plane of satellites in the MW



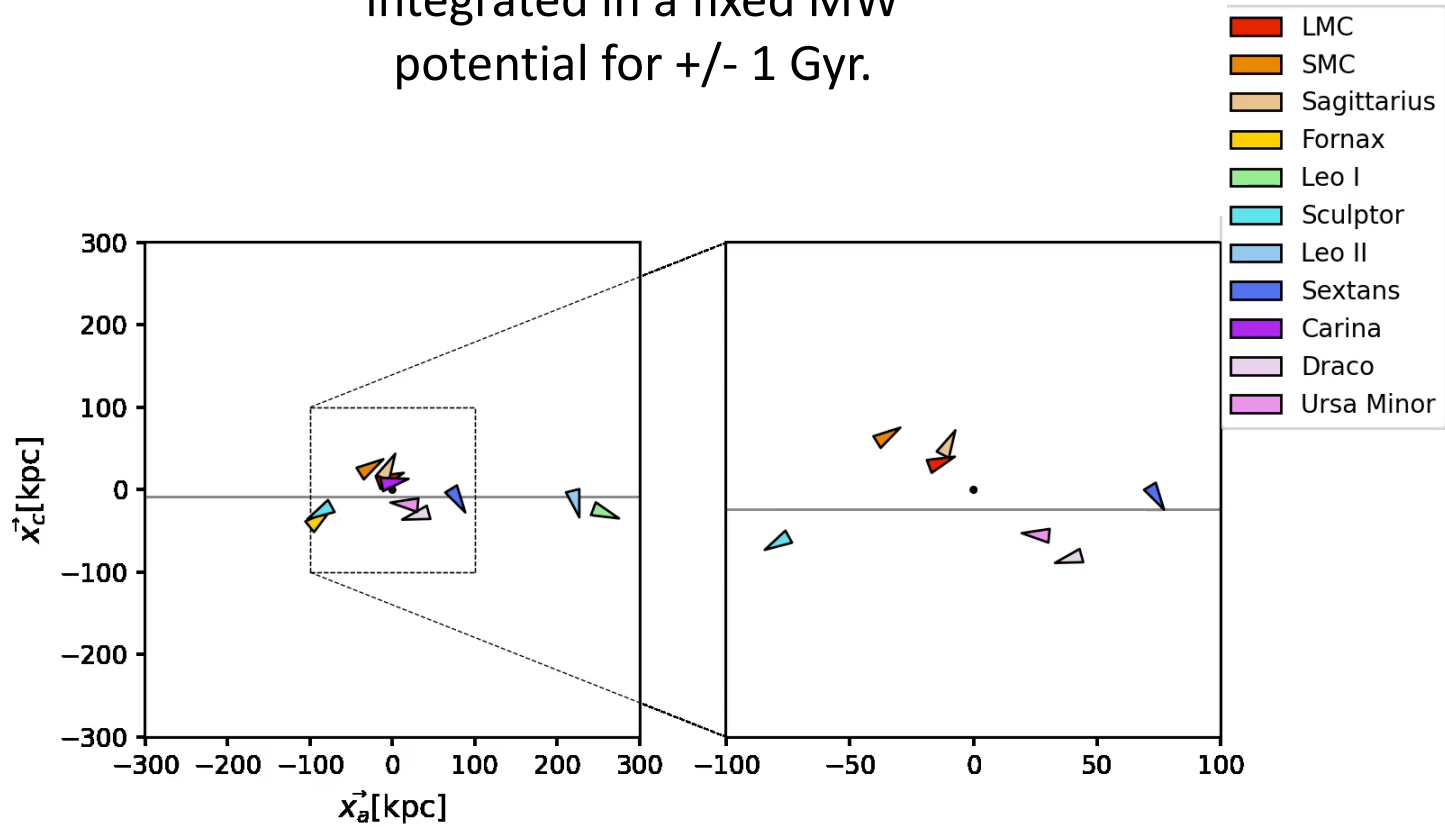
How rare is it?

No strong correlation –
 < 1 : 100,000 chance?

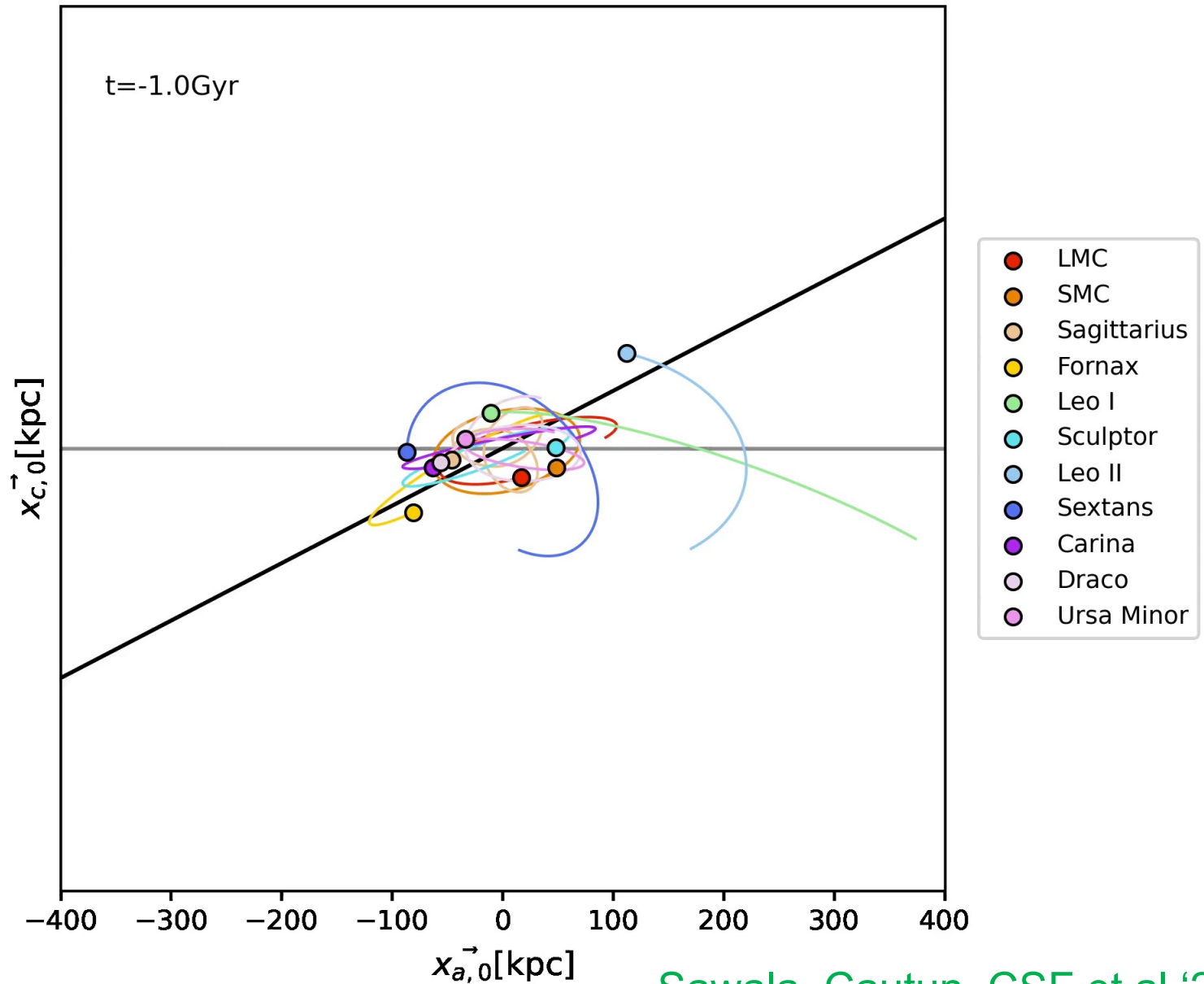
Eigenvalues
 of inertia
 tensor
 $a > b > c$

Pawlowski & Kroupa (2020)

Gaia EDR3 proper motions,
integrated in a fixed MW
potential for +/- 1 Gyr.



The MW plane of satellites is transient

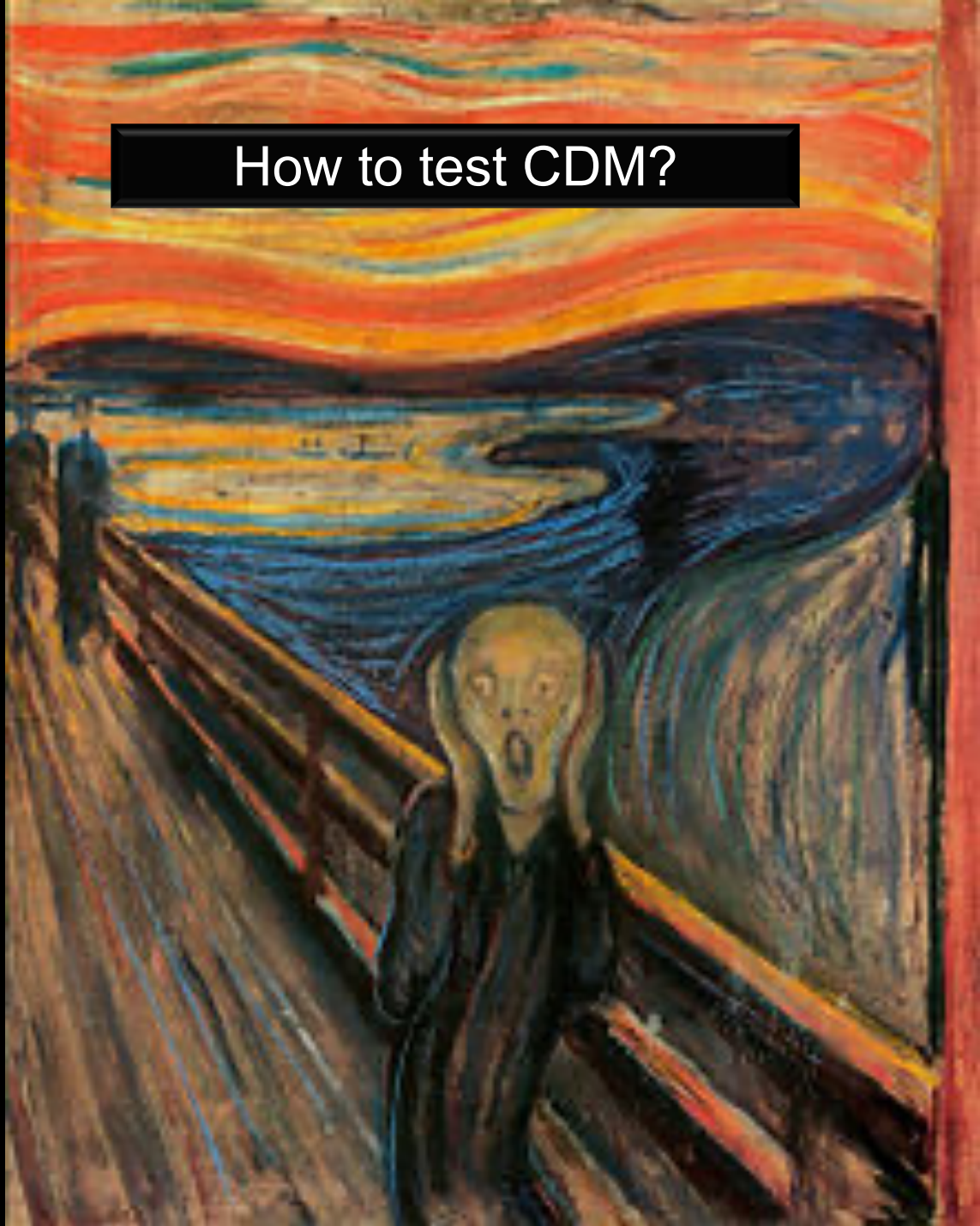


The rotating plane of satellites

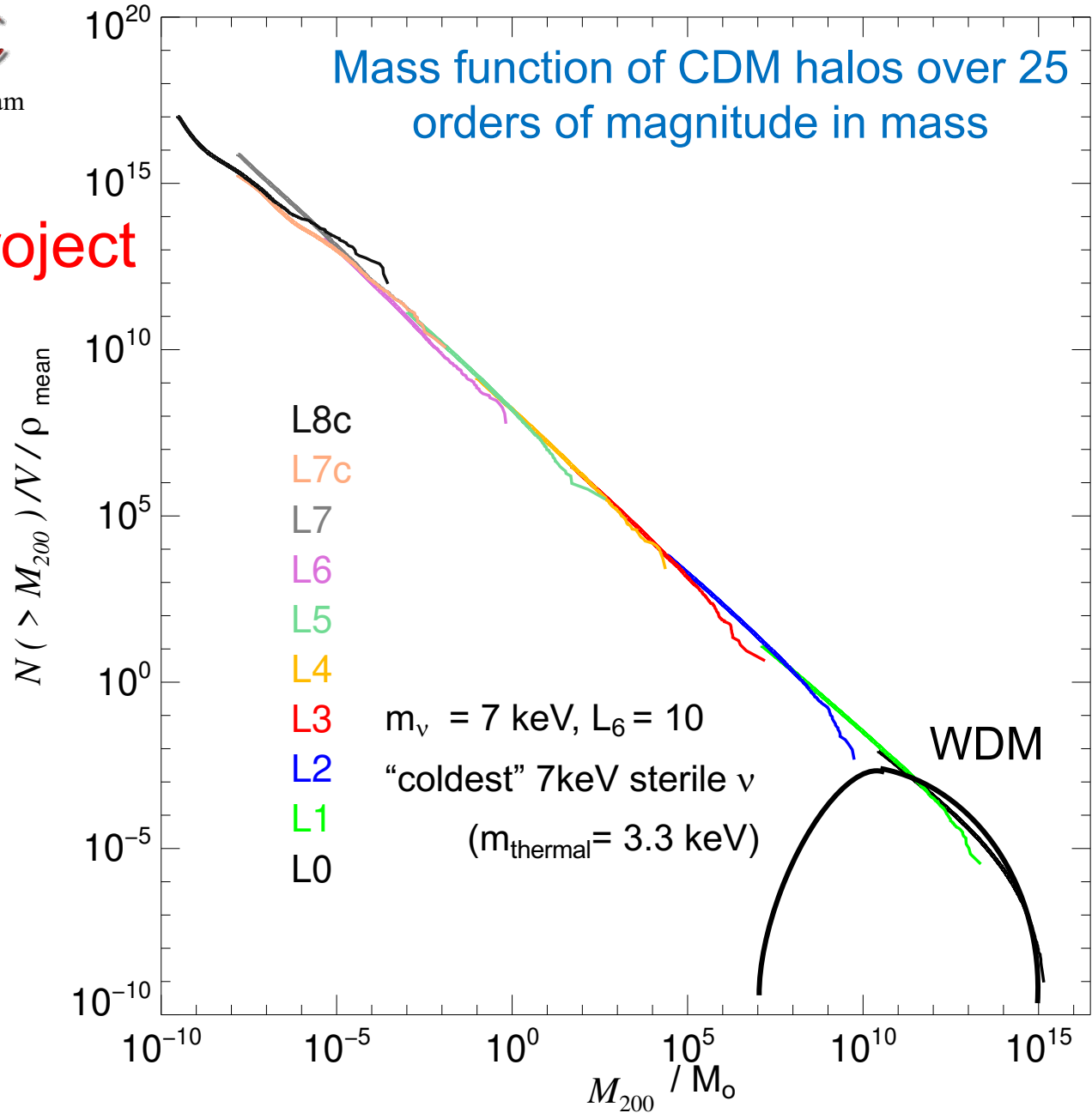
200 Λ CDM N-body
simulations of Local Group
analogues: $m_p = 1 \times 10^6 M_\odot$

We have 5/200 (2.5%) more clustered than the MW (compared to 0.04%)
Still rare, but *not astronomically unlikely*

How to test CDM?



The VVV project



cold dark matter

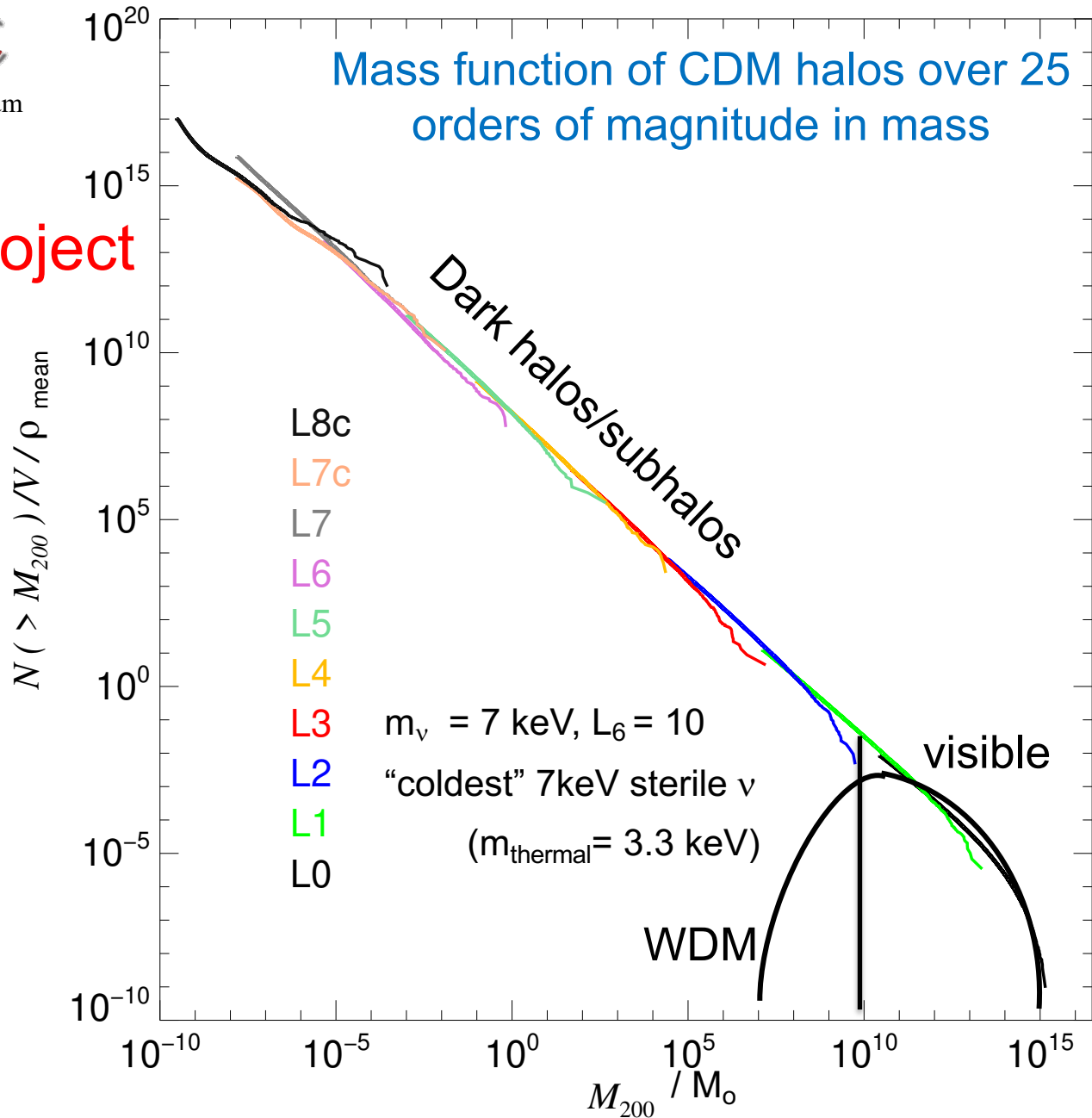


warm dark matter

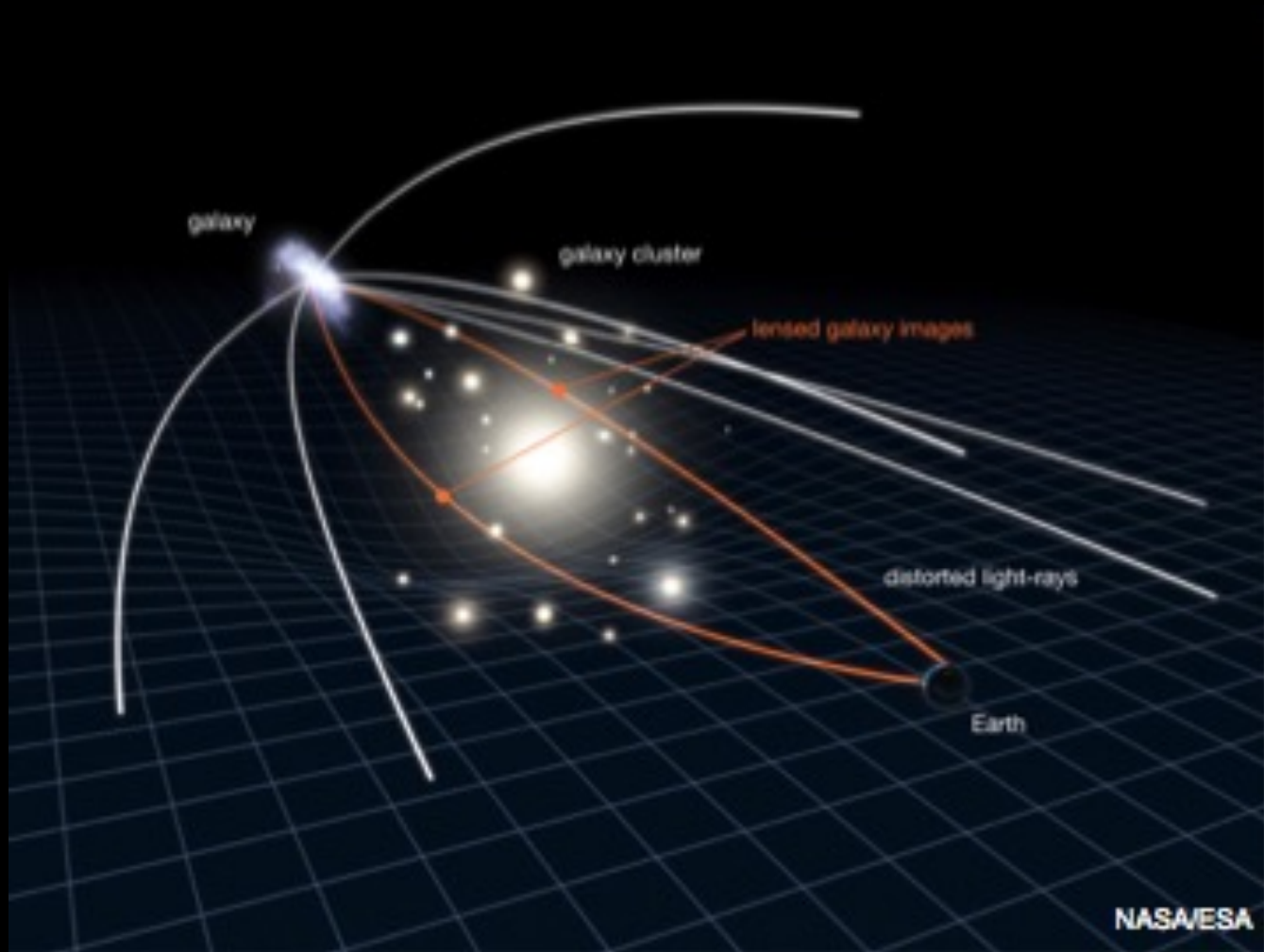


Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,
Boyarski & Ruchayskiy '12

The VVV project



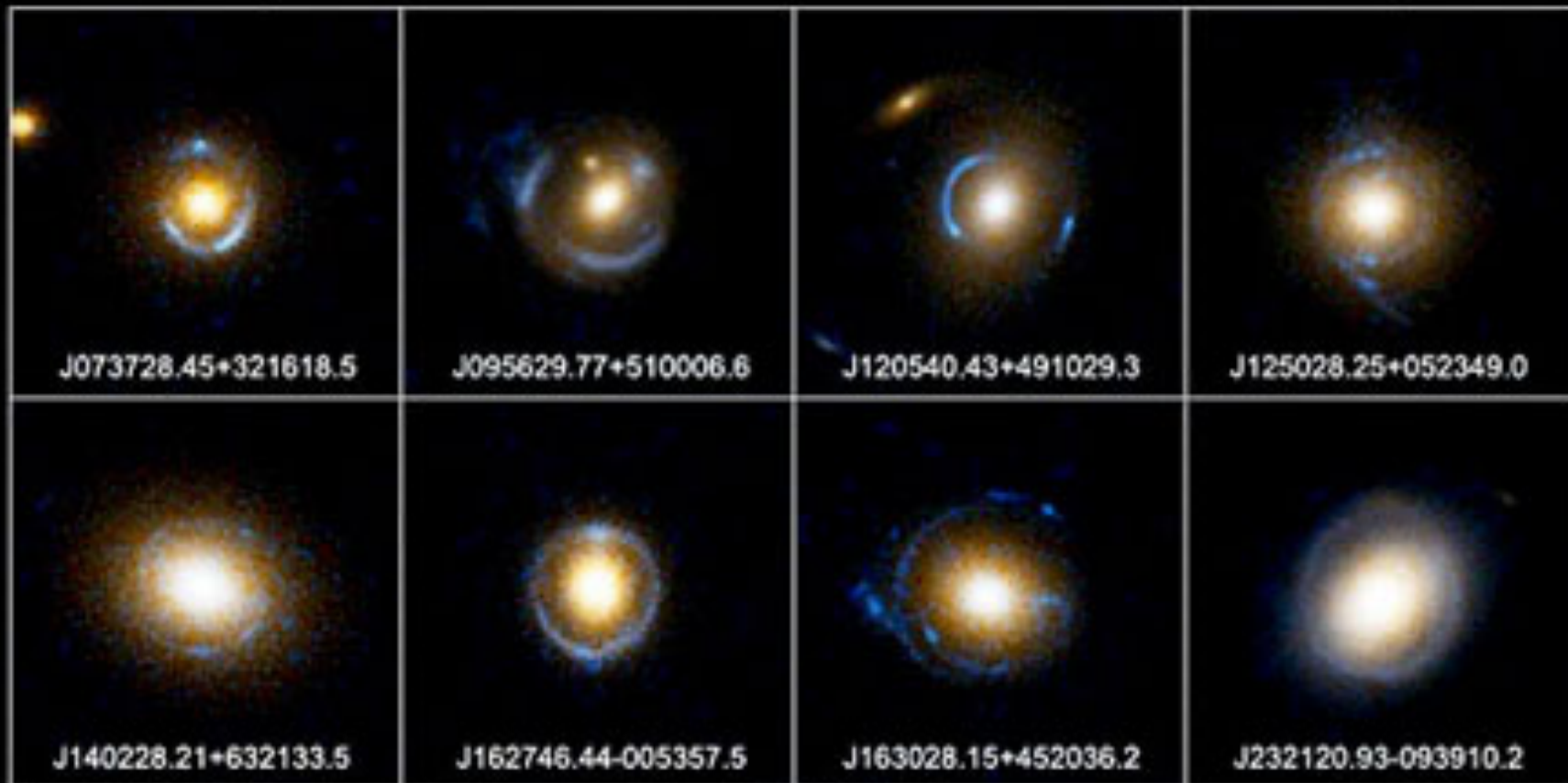
Gravitational lensing: Einstein rings



When the source and the lens are well aligned → strong arc or an Einstein ring

Einstein Ring Gravitational Lenses

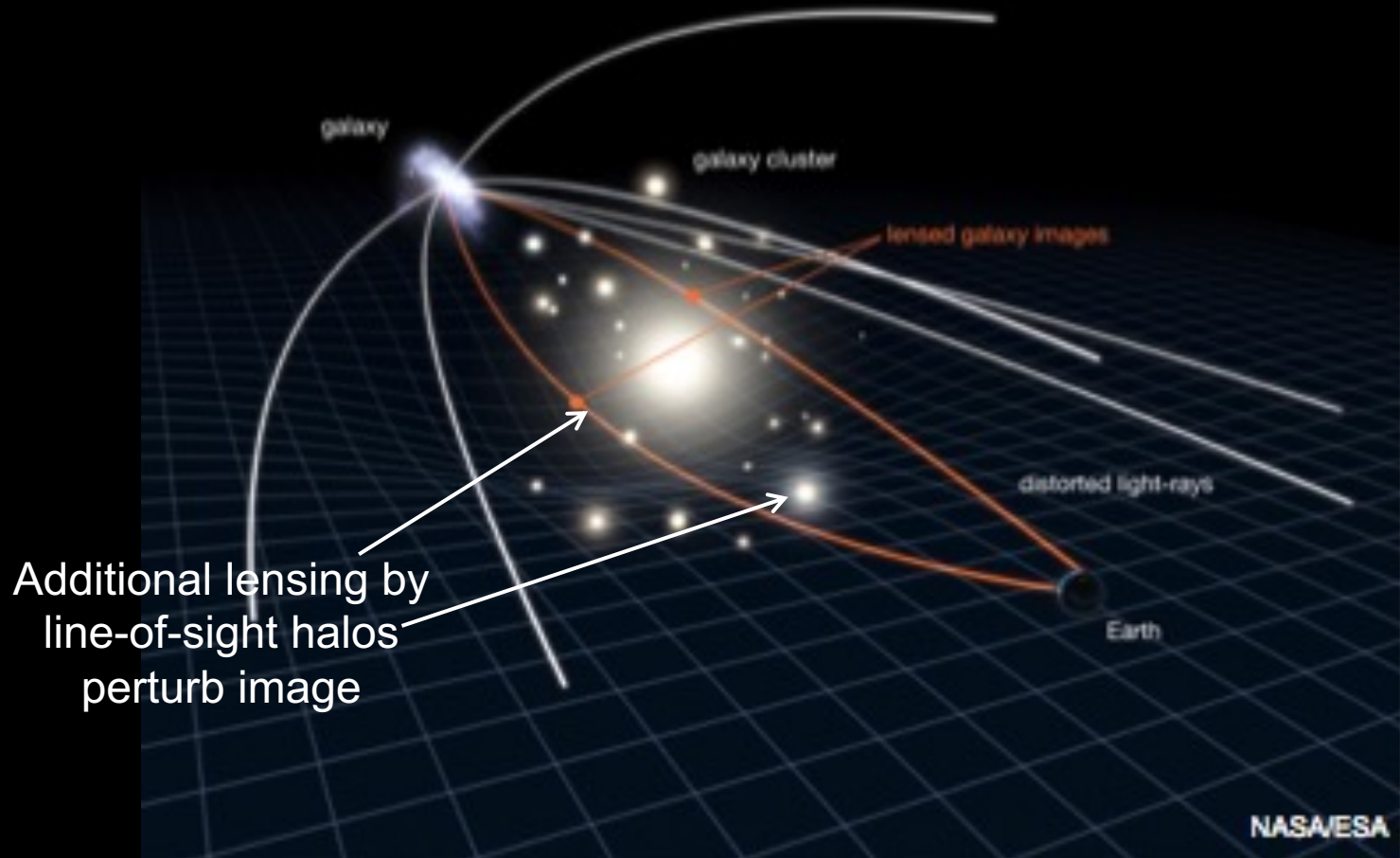
Hubble Space Telescope • ACS



NASA, ESA, A. Bolton (Harvard-Smithsonian CfA), and the SLACS Team

STScI-PRC05-32

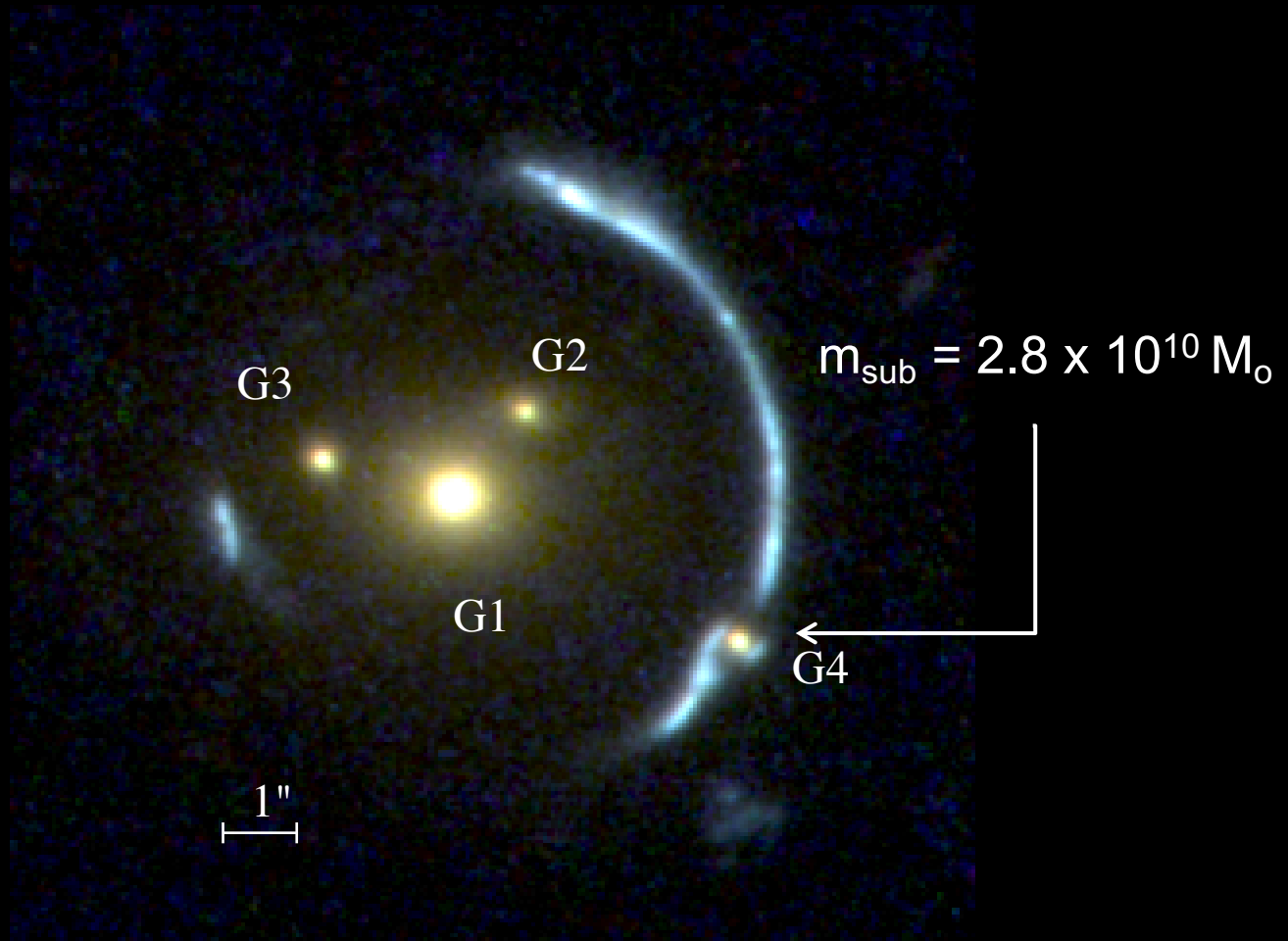
Gravitational lensing: Einstein rings



When the source and the lens are well aligned → strong arc or an Einstein ring

Gravitational lensing: Einstein rings

Halos projected onto an Einstein ring distort the image



Searched for substructure in 55 lenses with good HST imaging

→ 2 detections: G3 G2

SLACS0946+1006 → $\text{Log } M_{\text{sub}} = 11.59^{+0.18 - 0.34}$

BELLS1226+5457 → $\text{Log } M_{\text{sub}} = 11.80^{+0.16 - 0.30}$

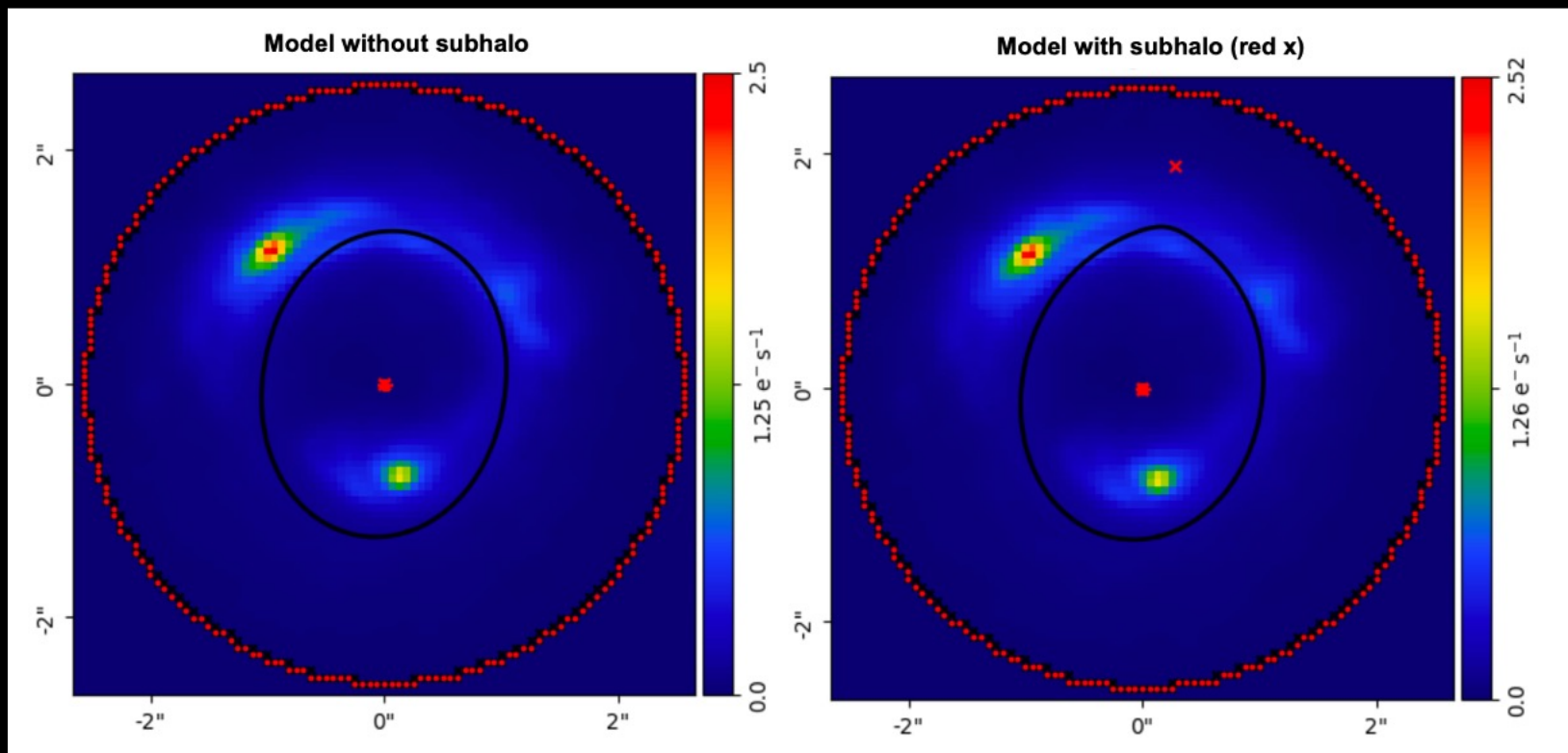
G1

Nightingale + '22

G4

1"
|-----|

JWST



And another one in JWST data:

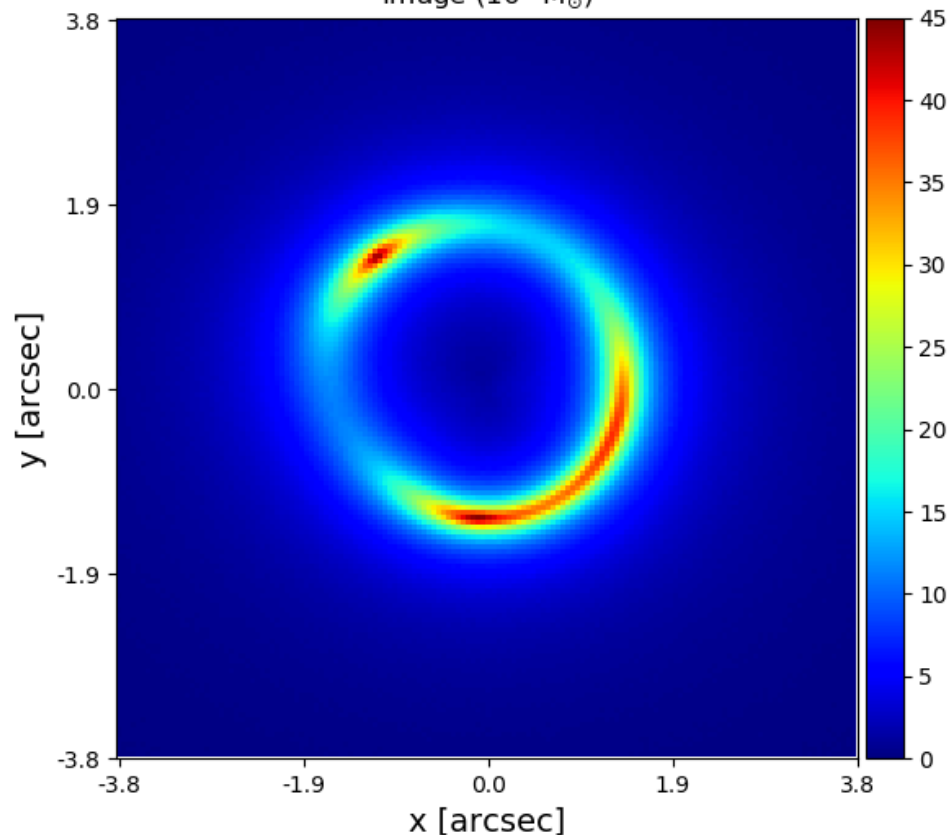
$$\rightarrow \text{Log } M_{\text{sub}} = 11.59^{+0.18}_{-0.34}$$

Lange, Nightingale, CSF+ '23

HST “data”: $z_{\text{source}}=1$; $z_{\text{lens}}=0.2$ $10^7 M_{\odot}$ halo – **NOT** so easy to spot

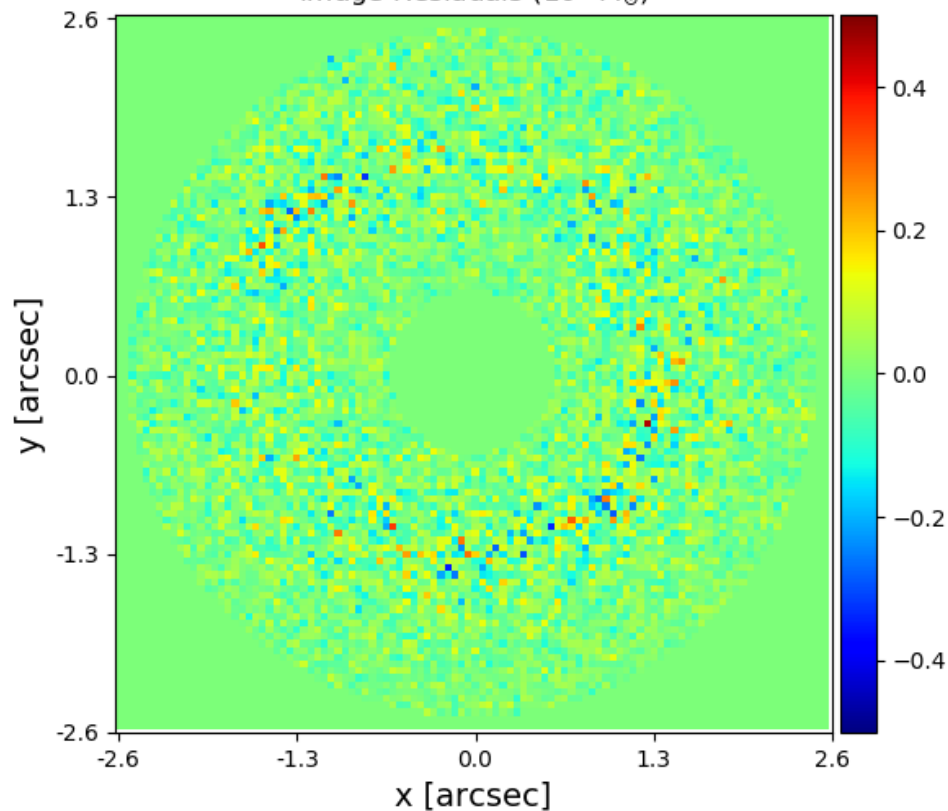
Image

Image ($10^7 M_{\odot}$)



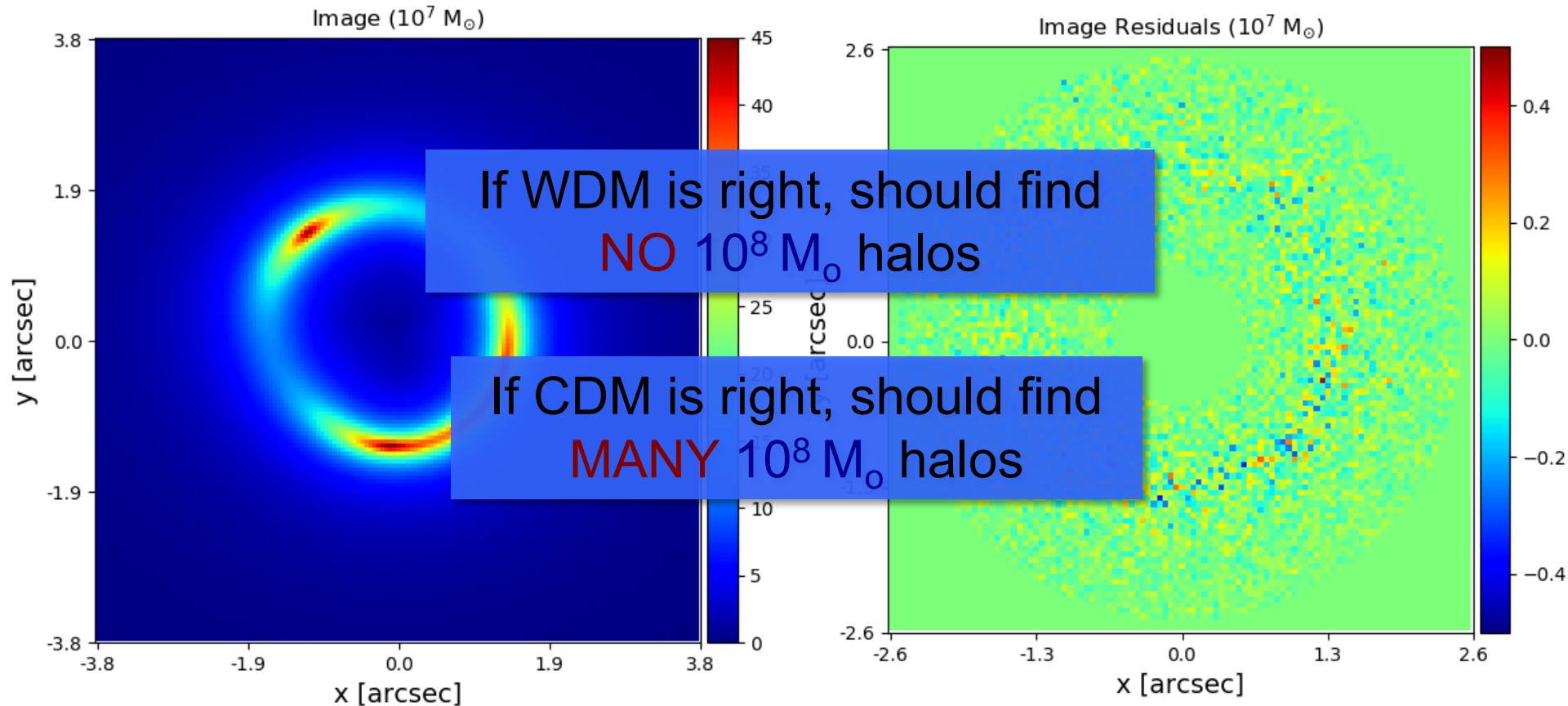
Residuals (image – smooth model)

Image Residuals ($10^7 M_{\odot}$)



Detecting halos w. strong lensing

Can detect halos as small as $10^7 M_\odot$





Conclusions

- Λ CDM: great **success** on scales $> 1\text{Mpc}$: CMB, LSS, gal evolution
- But on these scales Λ CDM cannot be distinguished from **WDM**
- Need to test Λ CDM on **non-linear scales**
- Non-linear **DM** problem **solved**: halo abundance, structure, distr.
- Halos of $M < 5 \cdot 10^8 M_\odot$ are dark; halos of $> 5 \cdot 10^9 M_\odot$ have a galaxy
- Satellite , TBTF, core/cusp “**problems**” in CDM \rightarrow baryon effects
- Distortions of **strong** gravitational **lenses** \rightarrow detect **small haloes**
 - \rightarrow offer a **clean test** of CDM vs WDM
 - \rightarrow can potentially **rule out** CDM!