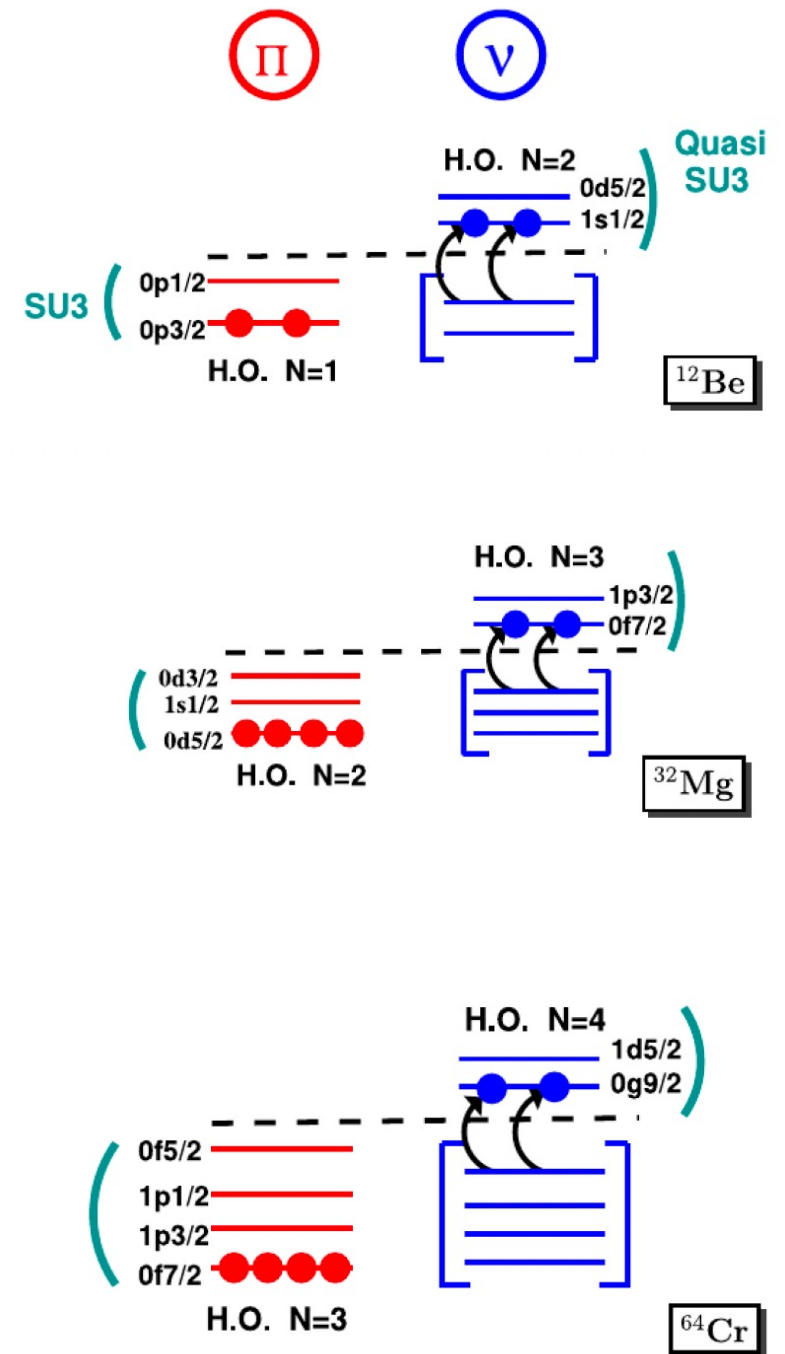


# Probing the island of inversion in heavy $N=Z$ nuclei

Francesco Recchia, Jeongsu Ha  
University and INFN Padova  
and the e19034 Collaboration

# Development of deformation at N=8,20,40

- ▶ Experimental evidence of **shell structure with magic numbers - energy gaps**: to promote particles above the Fermi levels costs energy
- ▶ Some **intruders configurations** can overwhelm their loss of monopole energy with their **huge gain in correlation energy**
  - ▶  $^{12}\text{Be}$ ,  $^{32}\text{Mg}$ ,  $^{64}\text{Cr}$ : center of islands of inversion
- ▶ In exotic nuclei the effective nuclear interaction weight very differently proton and neutron interaction than they do at the stability line. Therefore leading in some cases to **the vanishing of established shell closures or to the appearance of new ones**



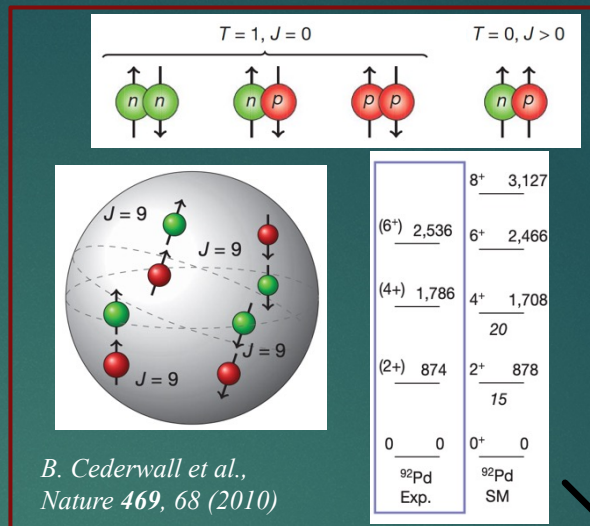
# Physics Motivation

- ▶  $N = Z$  nuclei play a special role
  - ▶ **(np) collectivity** by the proton-neutron interaction
  - ▶ **spatial overlap** of their respective wave functions at the Fermi surface
  - ▶ proton and neutrons act coherently.
- ▶ Competing **isoscalar np pairing** and normal isovector ( $T = 1, I = 0$ ) pairing modes
  - ▶ a nuclear superfluid **analogous to “Cooper Pairs”** may exist in nuclei
  - ▶ Isoscalar correlations are predicted to be prominent in the ground states of heavier ( $A > 76$ )  $N = Z$  nuclei
  - ▶ Difficult to find a smoking gun signature
  - ▶ shell-model predicts that **isoscalar pairing enhances collectivity** → **measurements of  $B(E2)$**

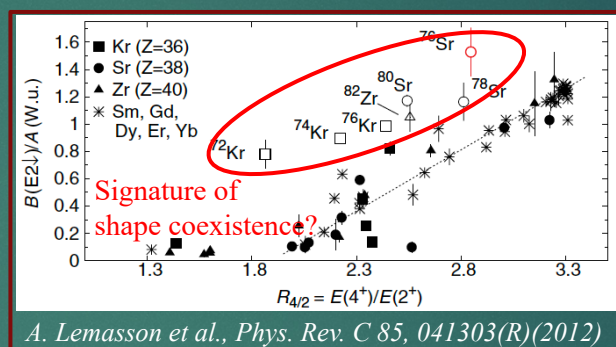
# Physics Motivation

- The self-conjugate  $N = Z$  nuclei
  - Proton-neutron correlations: role of np-pairing, ...
  - Schematic way to understand the phenomena: Nilsson SU3 scheme, ...

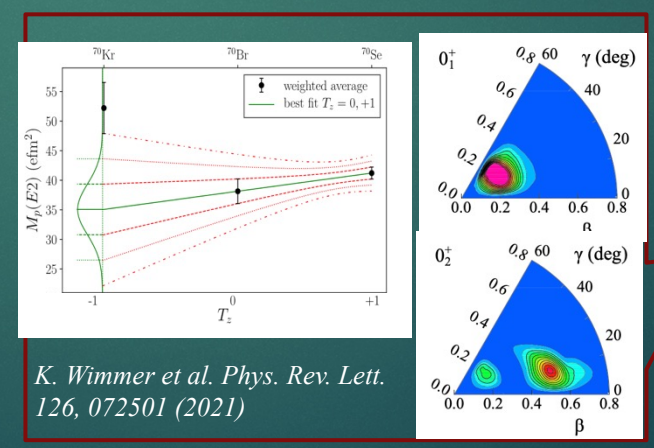
- A significant shape change has been anticipated among the medium-mass nuclides  
 → **Competition between shapes is expected**



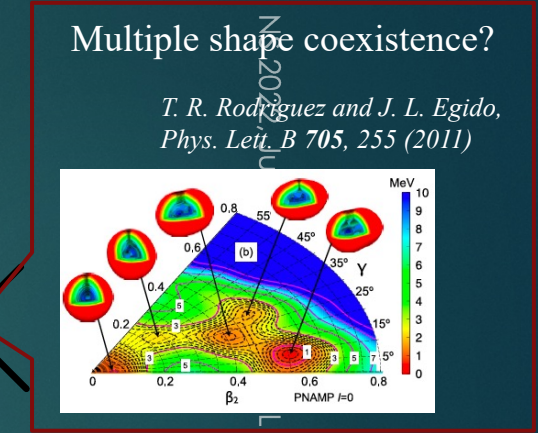
B. Cederwall et al., Nature 469, 68 (2010)



A. Lemasson et al., Phys. Rev. C 85, 041303(R)(2012)



K. Wimmer et al. Phys. Rev. Lett. 126, 072501 (2021)



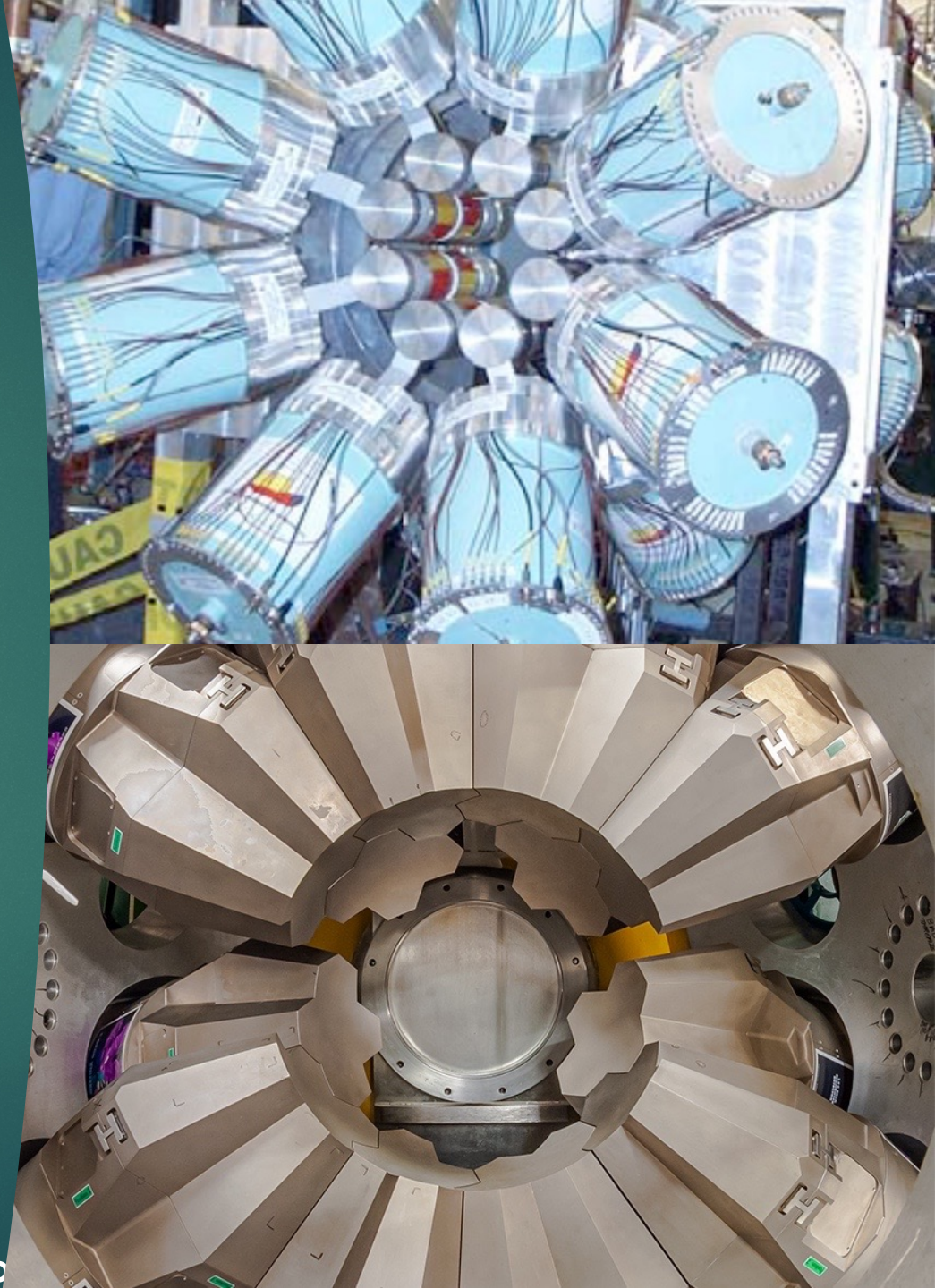
Maximum (prolate) deformation

Prolate-oblate shape coexistence

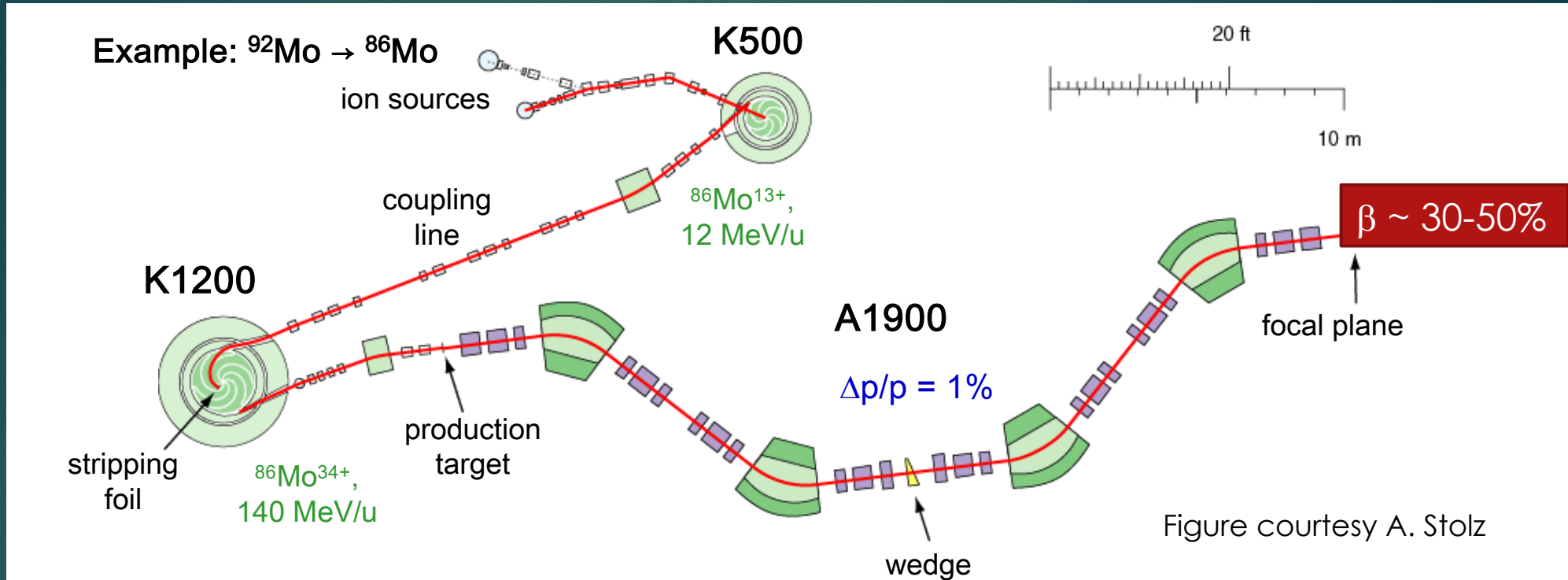
Oblate collectivity

# Along $N=Z$ at the NSCL facility

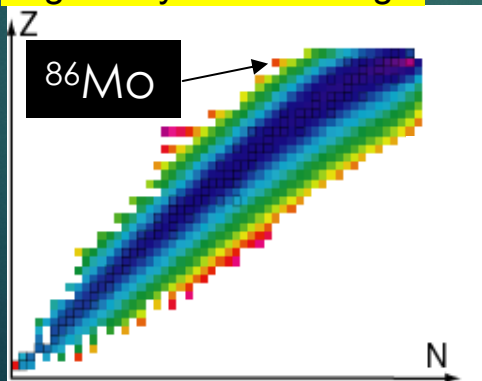
- ▶  $^{72}\text{Kr}$ 
  - ▶ **First GRETINA campaign 2013-14**
  - ▶ **H. Iwasaki et al. Phys. Rev. Lett. 112, 142502 (2014)**
- ▶  $^{74}\text{Rb}$ : A. Lemasson
- ▶  $^{76}\text{Sr}$ 
  - ▶ **Last SEGA campaign ~2010**
  - ▶ **A. Lemasson Phys Rev C 85, 0041303(R) (2012)**
- ▶  $^{78}\text{Y}$ : R. D. O. Llewellyn
- ▶  $^{80}\text{Zr}$ 
  - ▶ **Last GRETINA campaign at NSCL 2019-20**
  - ▶ **R. D. O. Llewellyn et al. Phys. Rev. Lett. 124, 152501 (2020)**



# Secondary beams: fragmentation

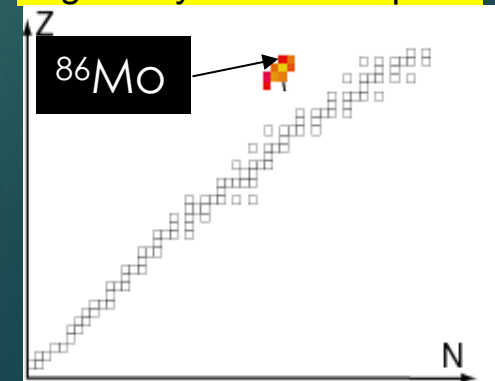


fragment yield after target



- ▶ Identification event-by-event
  - ▶ B – Rho
  - ▶ TOF

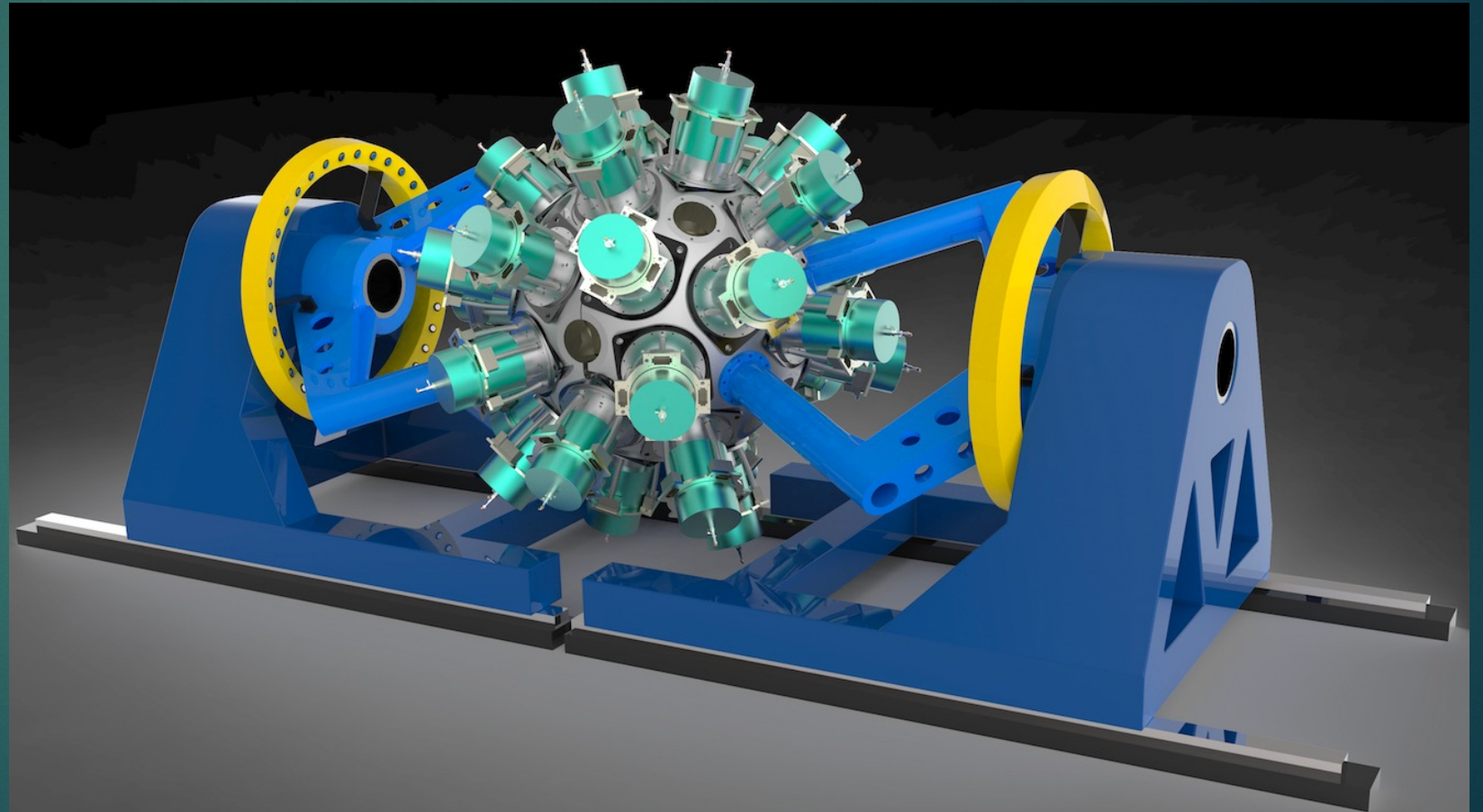
fragment yield at focal plane



# Gamma Ray Energy Tracking Array

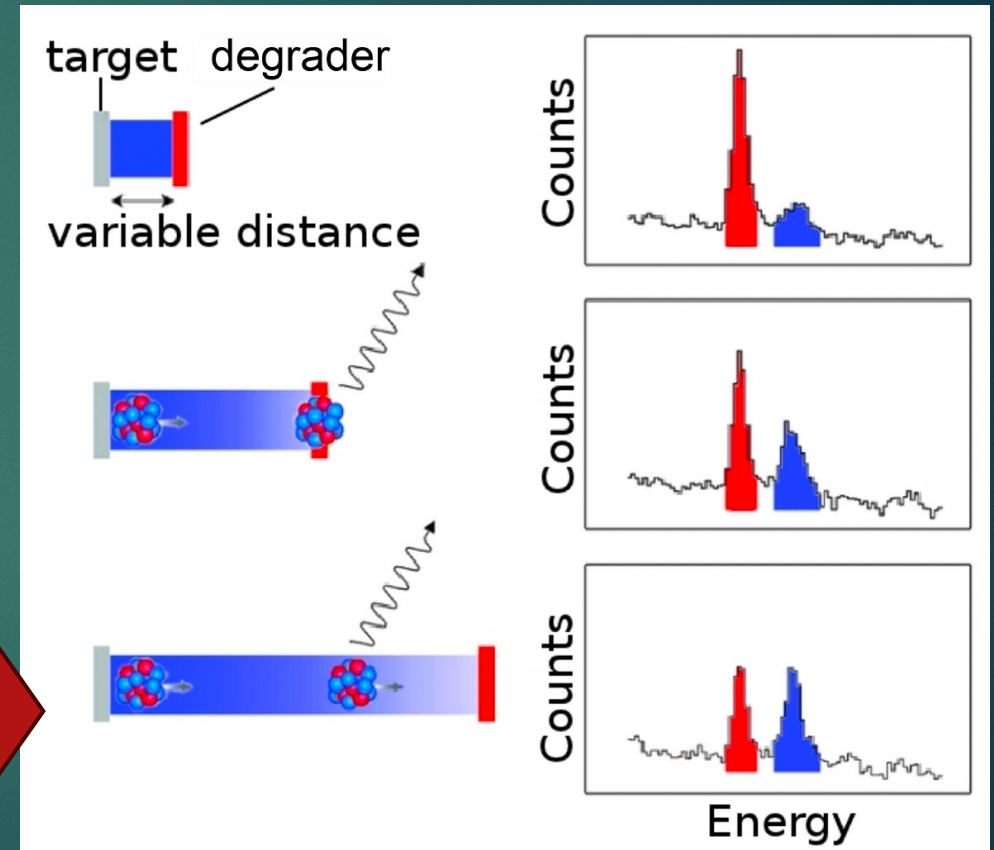
7

- ▶ **GRETA**:  $4\pi$  array of 120 HPGe detectors with 36 segments each (USA)
- ▶ **AGATA**: Advanced Gamma Tracking Array in Europe



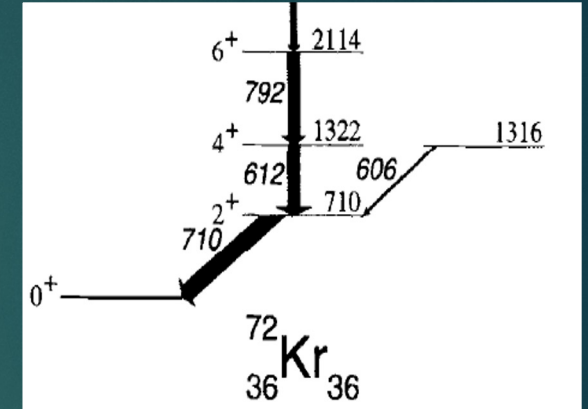
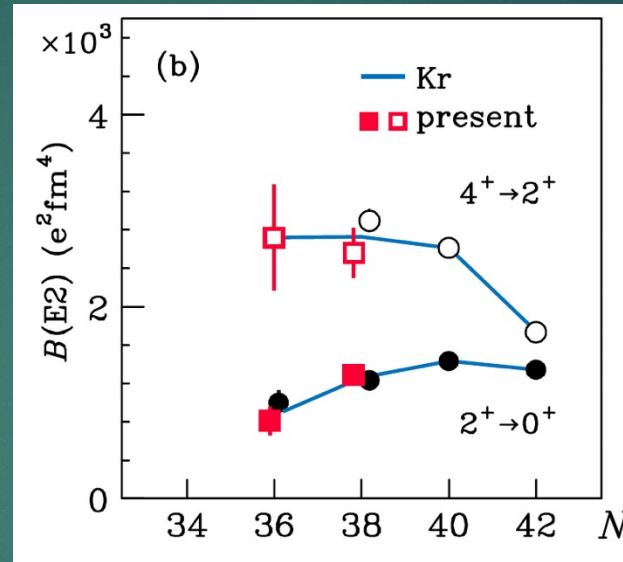
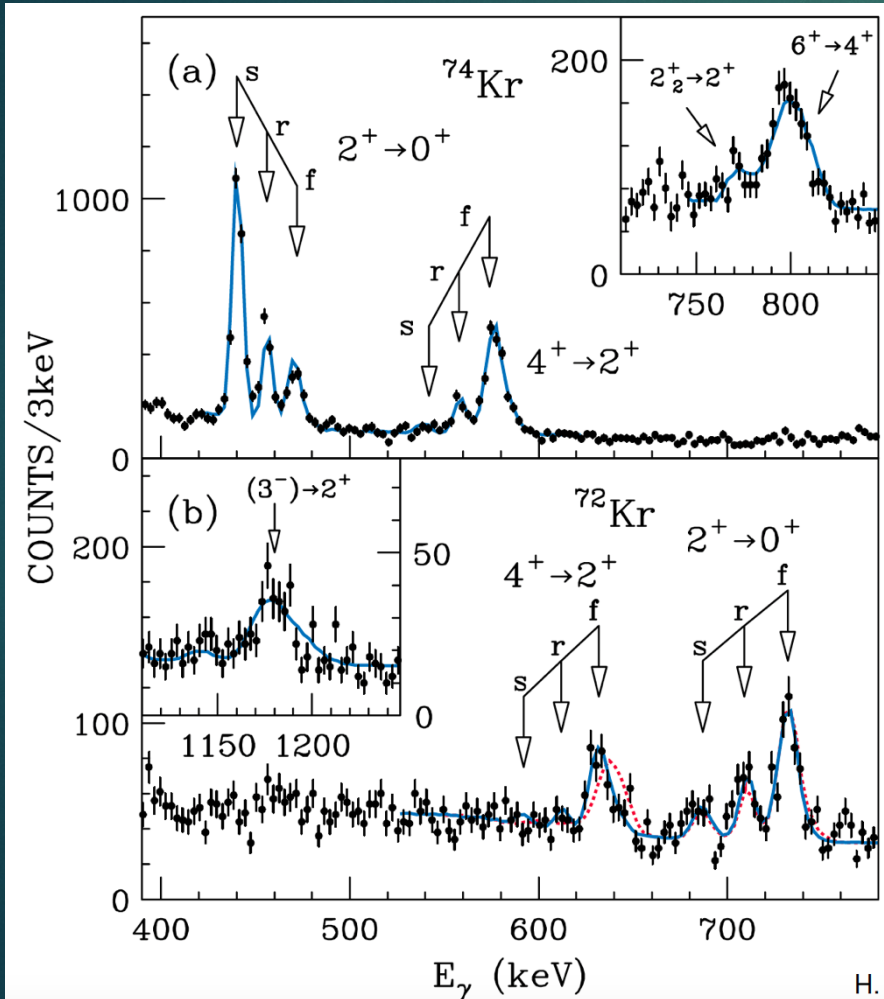
# In-beam lifetime measurements .. with radioactive beams

- ▶ the beam **intensity is low**, beam time is scarce
- ▶ use a **degrader instead of a stopper** → residual nucleus can be identified event by event
- ▶ two different emission velocities, **two peaks** in spectrum
- ▶ Variations over distances to adapt to the lifetime(s) of interest





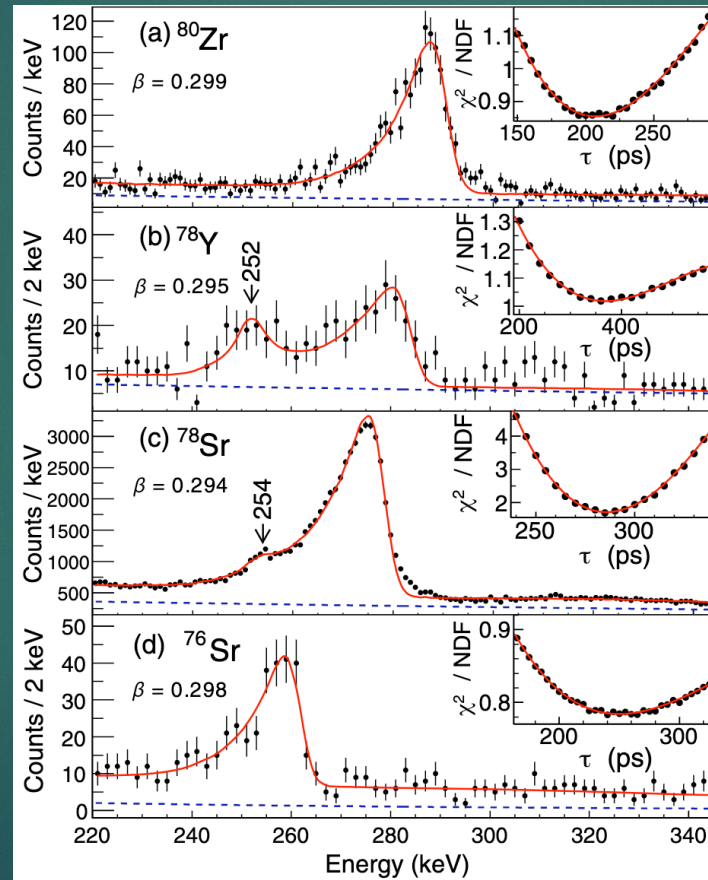
# Lifetimes in $^{72}\text{Kr}$ : competition of deformations



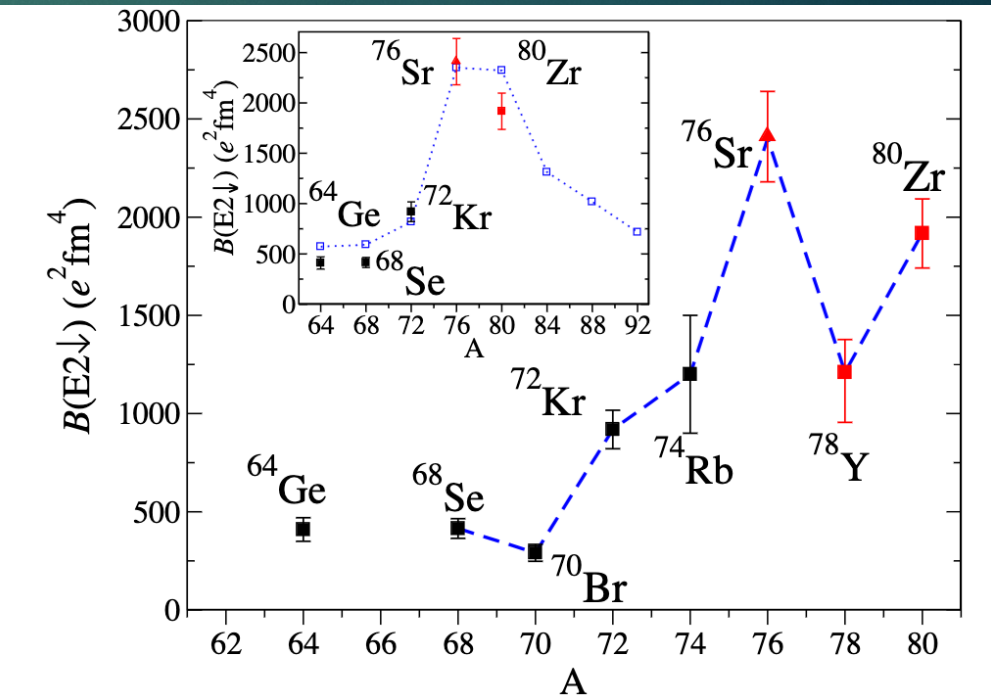
- short lifetime of  $4^+$  state in  $^{72}\text{Kr}$ 
  - large  $B(E2; 4^+ \rightarrow 2^+)$
- **shape transition next to the g.s.**
  - oblate ground state,
  - prolate for higher spins as suggested by LNL experiment that measured level spacing in 1997

# Lifetimes extracted from lineshapes for $^{80}\text{Zr}$ and $^{78}\text{Y}$

- Very large quadrupole deformation
- Maximum along N=Z



	$E(2^+)$	$\tau$	$\tau_{\text{prev},1}$	$\tau_{\text{prev},2}$	$\tau_{\text{avg}}$	$B(E2\downarrow)$
$^{80}\text{Zr}$	290.4(4)	207(19)				1910(180)
$^{78}\text{Y}$	283.6(8)	$369^{+77}_{-54}$				$1200^{+180}_{-250}$
$^{78}\text{Sr}$	278.1(3)	286(20)	276(39) <sup>a</sup>	224(27) <sup>b</sup>	266(15)	1840(100)
$^{76}\text{Sr}$	261.6(5)	250(44)	296(36) <sup>a</sup>		278(28)	2390(240)



# Physics Motivation

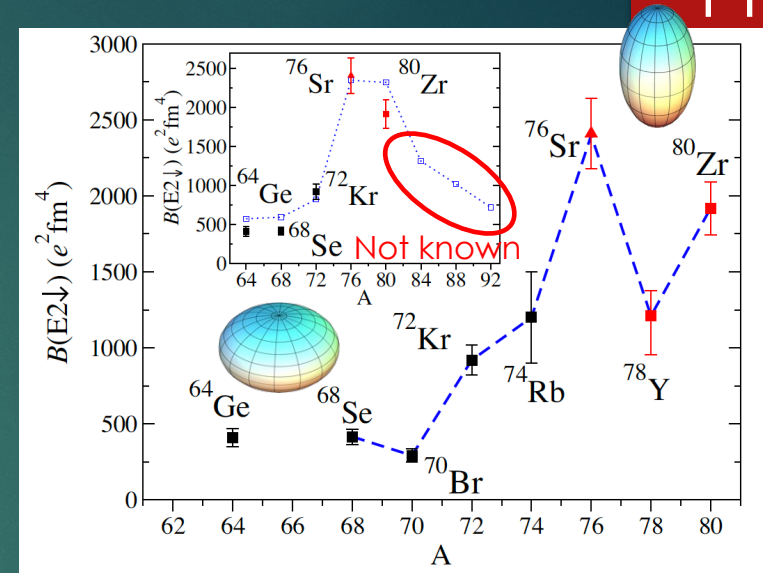
▶ Along  $N = Z$ : shape change **from oblate** ( $^{64}\text{Ge}$ ,  $^{68}\text{Se}$ ) **to prolate** around  $^{72}\text{Kr}$

▶ Large deformation continues up to  $^{80}\text{Zr}$

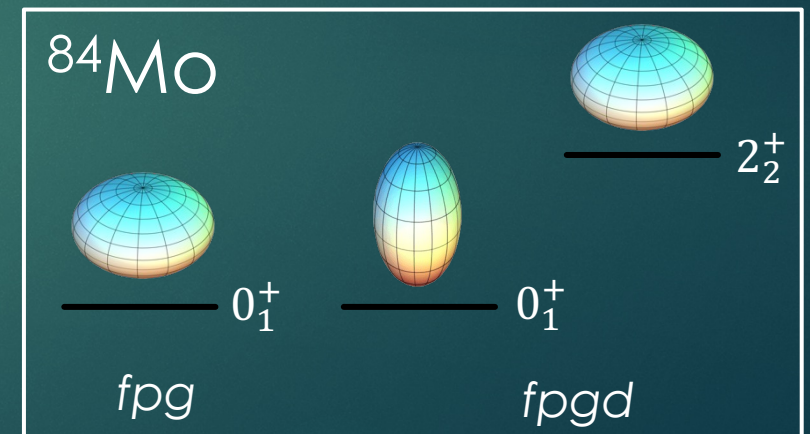
▶ Then prolate or oblate??

▶ Shell model predictions for  $^{84}\text{Mo}$ :

- oblate,  $\tau(2_1^+) = 75$  ps
- prolate,  $\tau(2_1^+) = 43$  ps



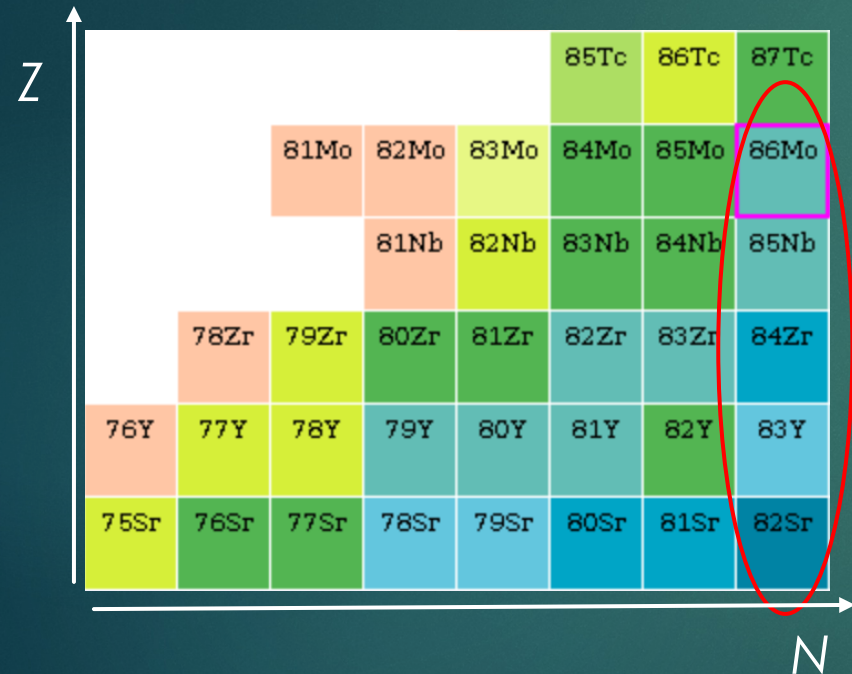
R. D. O. Llewellyn et al., *Phys. Rev. Lett.* **124**, 152501 (2020)



# Incoming PID

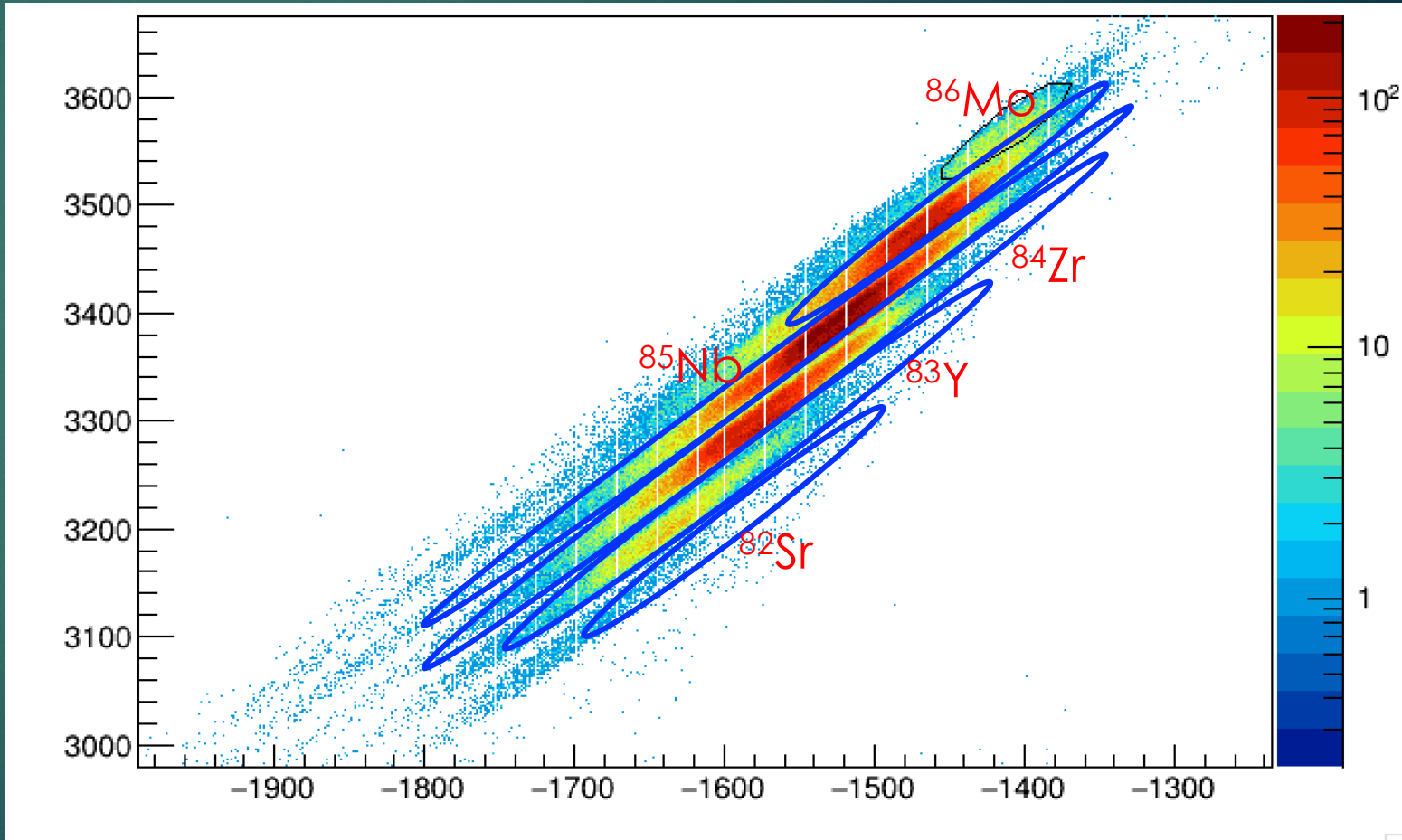
12

[Selection of the incoming beam]



XFP - E1 Time of flight (arb.)

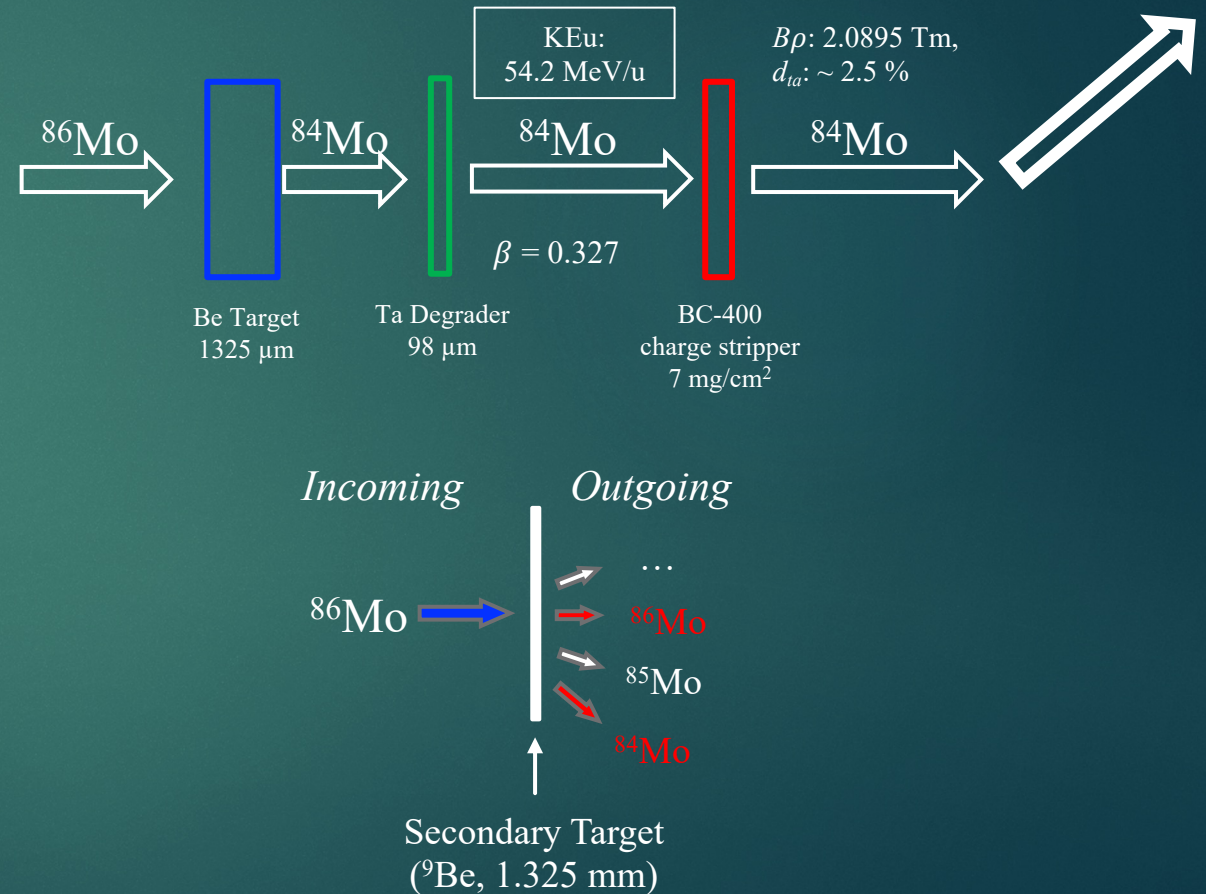
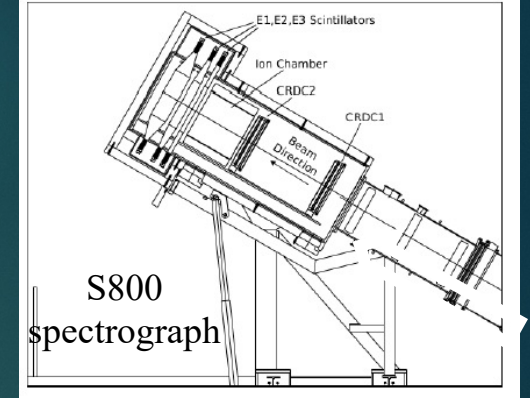
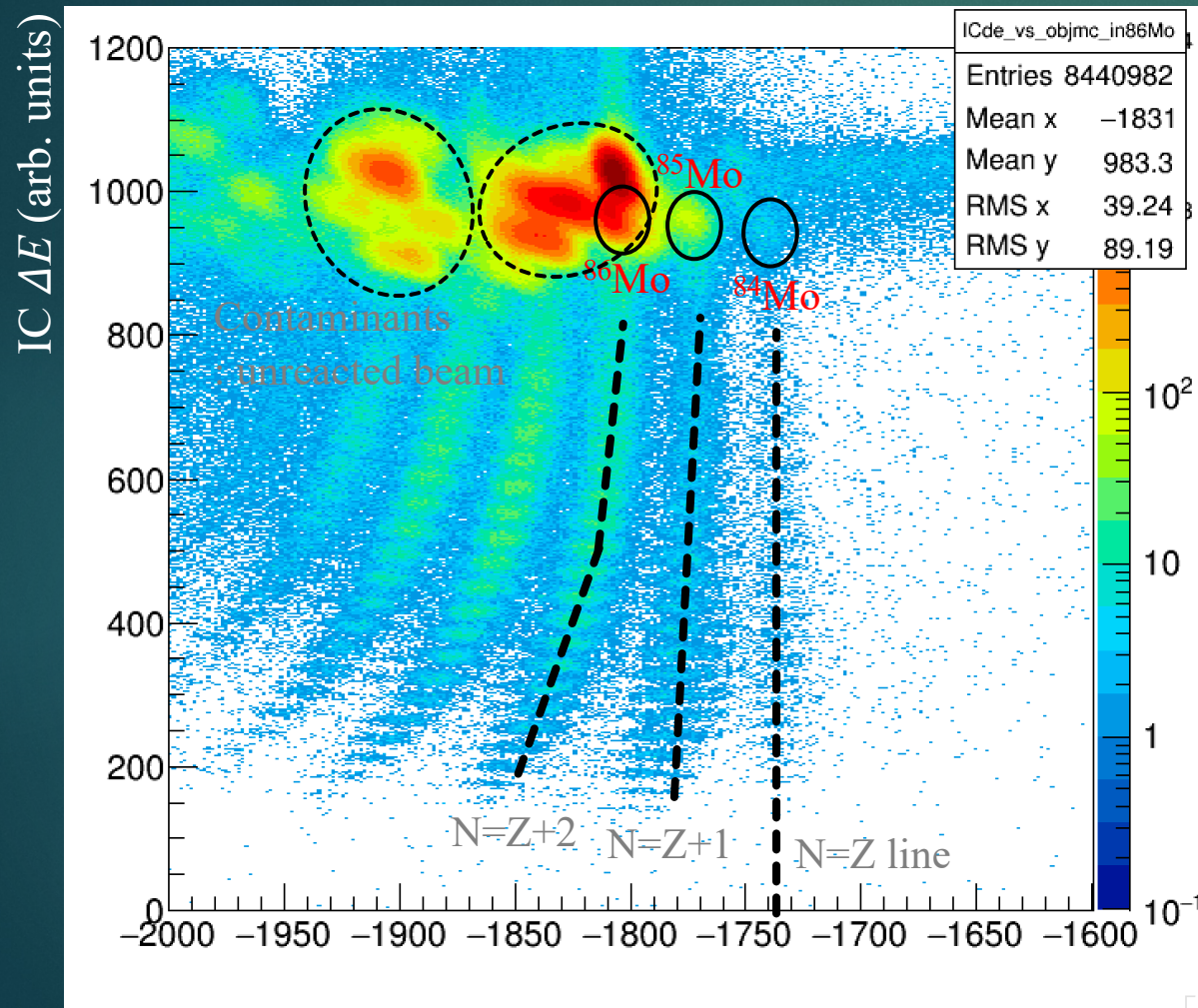
86Mo was 0.8% of incoming beam



OBJ - E1 Time of flight (arb.)

# Analysis

[Outgoing beam PID plot for incoming  $^{86}\text{Mo}$  beam]



# Comparison to full Monte Carlo

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- The spatial and energy distribution of the secondary beam are reproduced in the **simulation**
- Strong **direct** population to  $2^+$ 
  - Residual population to  $4^+$  states that decays by a fast transition

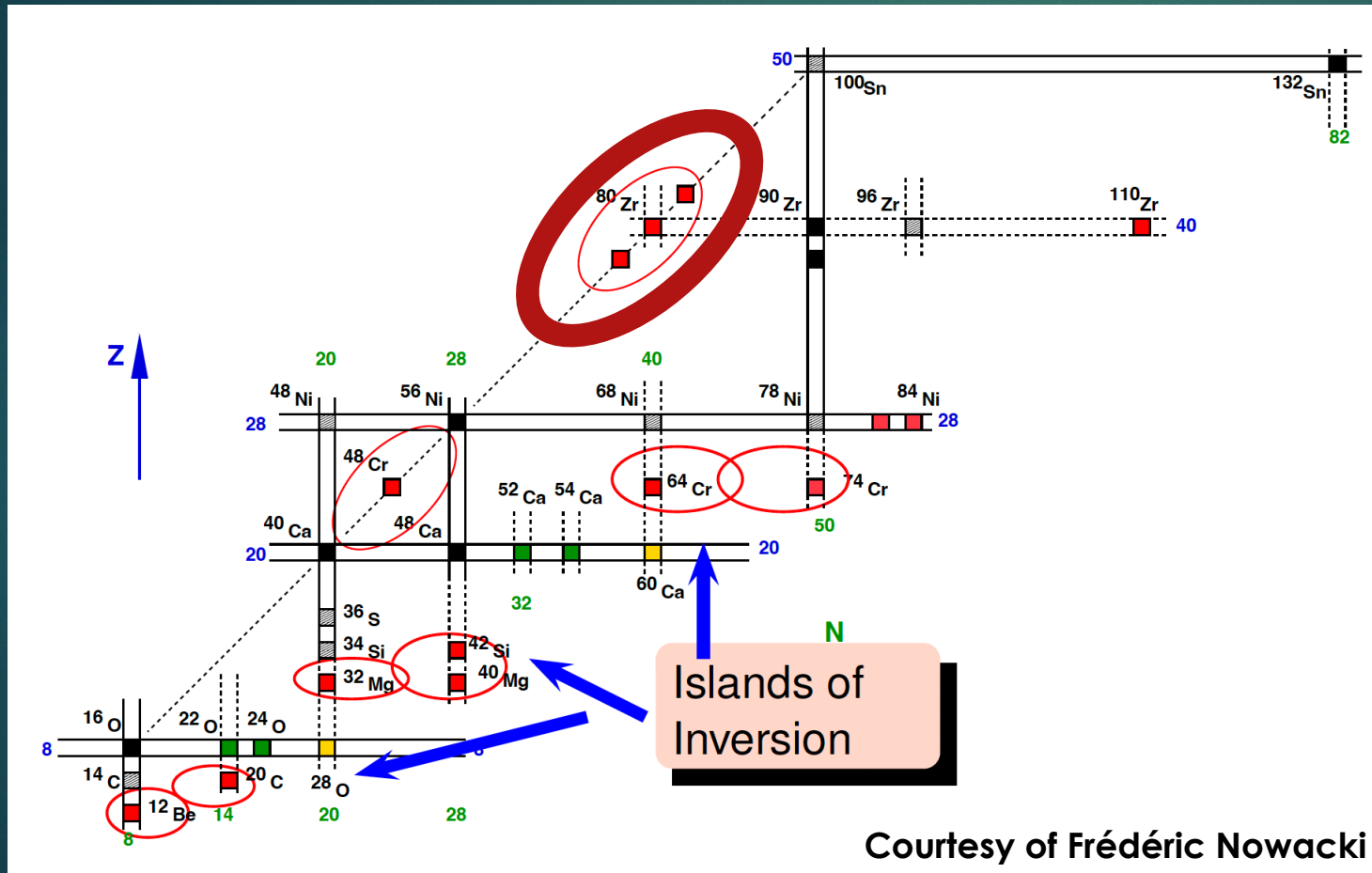
# Conclusion 1/2

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- ▶ Advanced RIB Facilities and instrumentation allow progress
  - ▶ Measure collectivity by  $B(E2)$  along  $N=Z$
  - ▶ New challenges for theoretical description of the  $B(E2)$  measured in the center of the  $g_{9/2}$  shell
  - ▶ **Quadrupole correlations beyond expectations; possible triaxiality...** calculation still in progress
  - ▶ Shell model description: new region of deformation and **sharp transition between  $^{84}\text{Mo}$  and  $^{86}\text{Mo}$**



# Conclusion 2/2



- **Limit of past facilities is reached.** Looking forward for the new ones, FRIB
- Heavier nuclei along  $N=Z$ :  $^{88}\text{Ru}$ ,  $^{92}\text{Pd}$ ,  $^{96}\text{Cd}$
- odd-odd nuclides ( $^{82}\text{Nb}$ ,  $^{86}\text{Tc}$ , ...) shape competition and coexistence



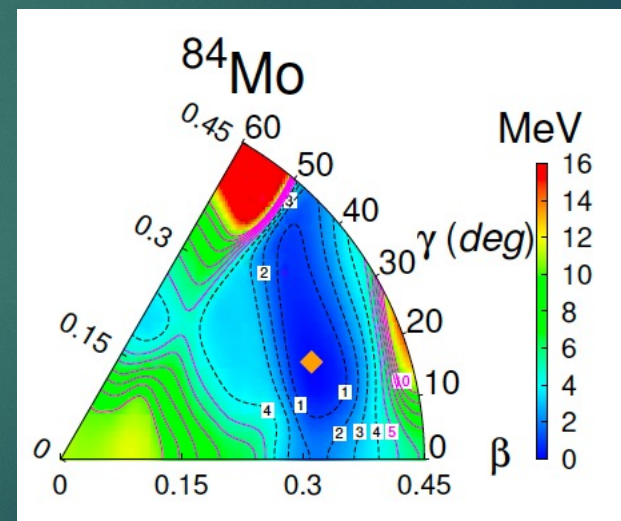
ONLY POSSIBLE THANKS TO:

Jeongsu Ha  
Pablo Aguilera  
Sara Carollo



WITH CALCULATIONS BY:

F. Nowacki  
D. D. Dao  
S. Lenzi  
A. Poves



THE FULL NSCL COLLABORATION IS ACKNOWLEDGED



## Generator Coordinate Method: $|\Psi_{\text{eff}}\rangle = \sum_i f_i |\Phi_i\rangle$

- 1) Deformed Hartree-Fock (HF) Slater determinants
- 2) Restoration of rotational symmetry
- 3) Mixing of shapes:

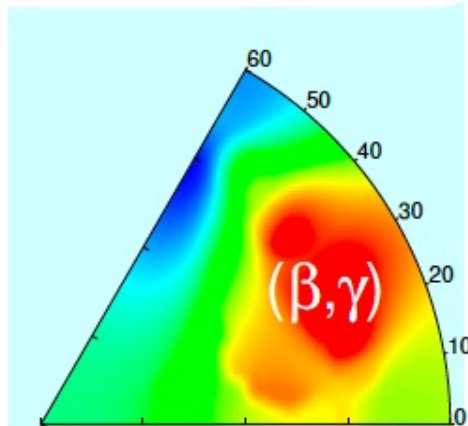
$$|\Psi_{\text{eff}}\rangle = \text{[deformed shape 1]} + \text{[deformed shape 2]} + \text{[deformed shape 3]} \dots$$

## Basis Truncation Method

**?** *choice of relevant deformed Hartree-Fock states*

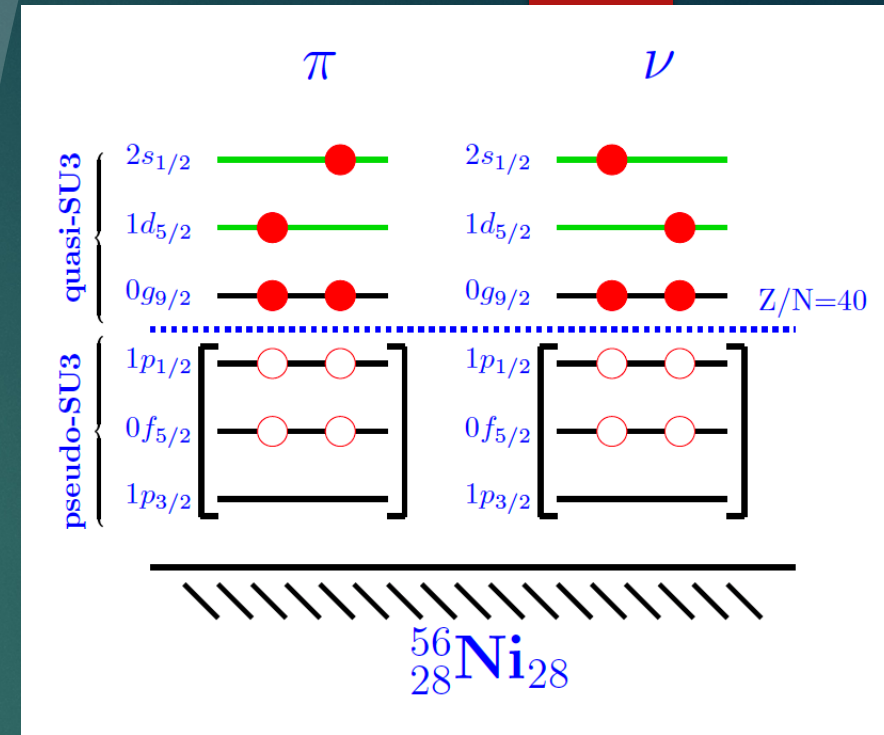
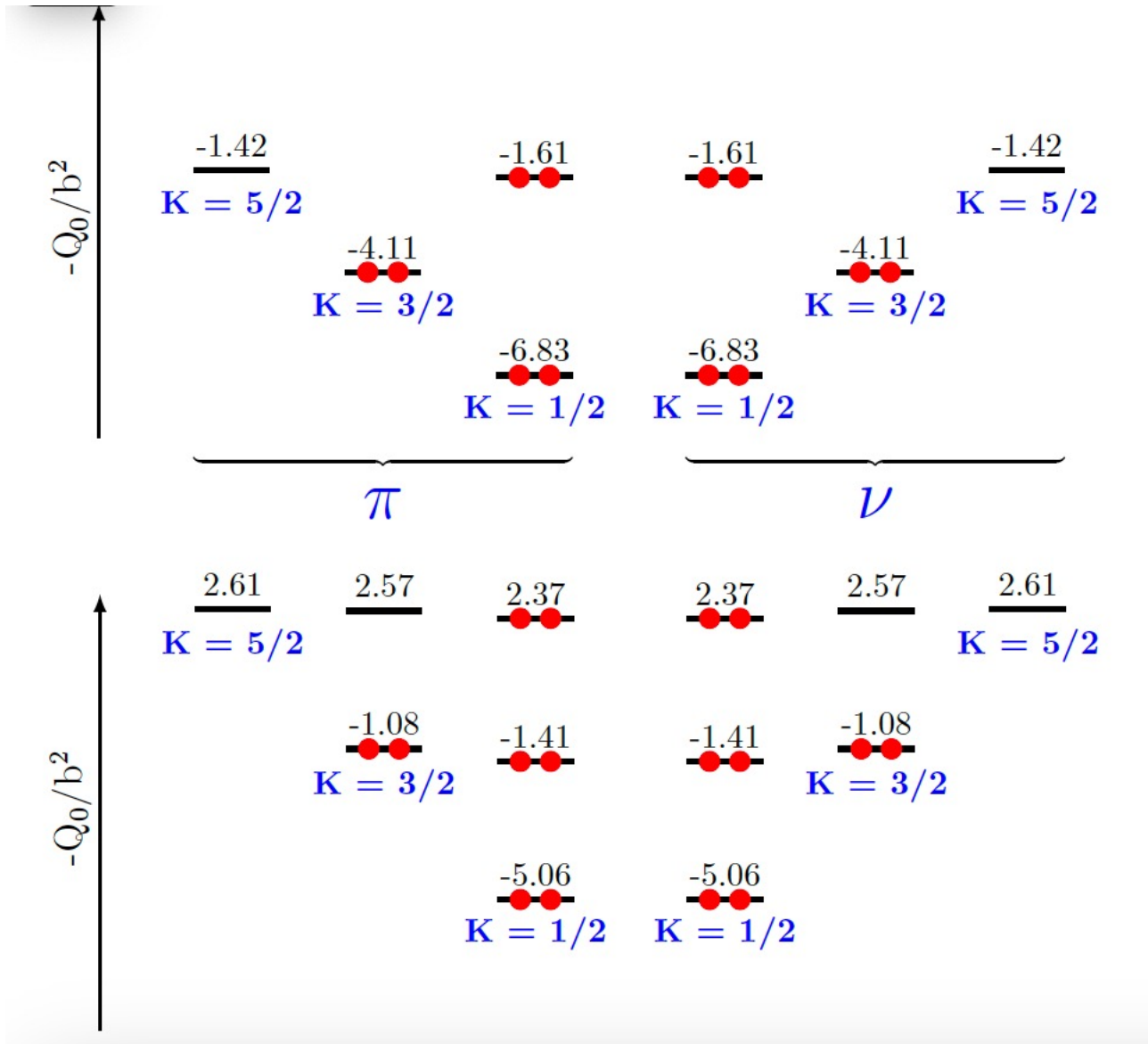
- **E. Caurier's Minimization Technique:**

(E. Caurier, Proc. on GCM, BLG report **484** (1975))



- ◇ Based on the variational principle
- ◇ Minimization of the energy of given states  $\{J^\pi\}$

Courtesy of F. Nowacki



## ZRP w/ ZBM interaction

A. P. ZUKER, B. BUCK, AND J. B. MCGRORY, PHYS. REV. LETT. 21, 39 (1968);