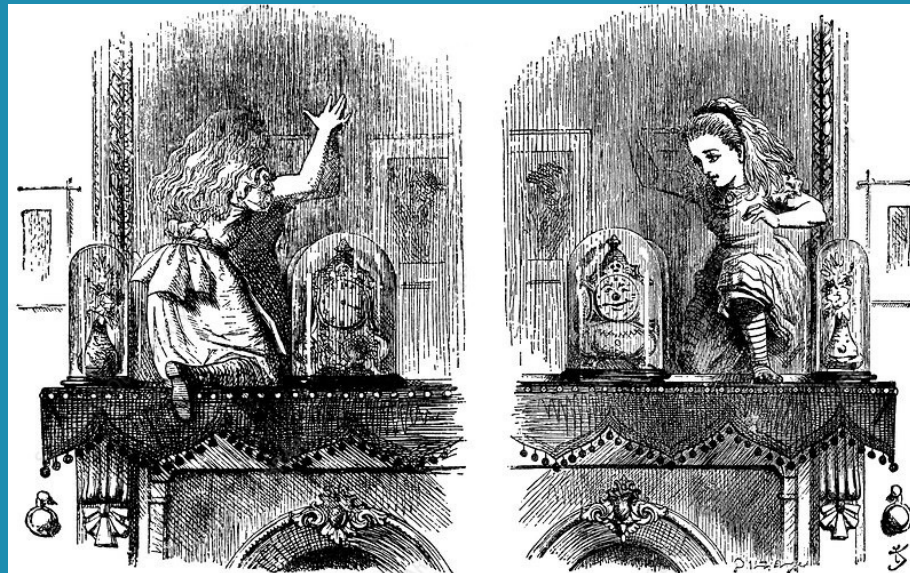


InTraNS 2024 Workshop

Mirror energy differences between ^{43}Ti and ^{43}Sc : a direct insight into the wave-functions

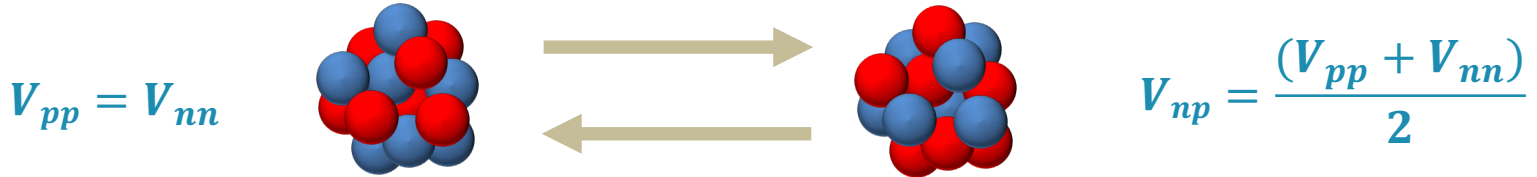
Kseniia Rezyunkina

INFN, Sezione di Padova



Introduction : proton-neutron symmetry

- Exchange symmetry between π and $\nu \rightarrow$ isospin T

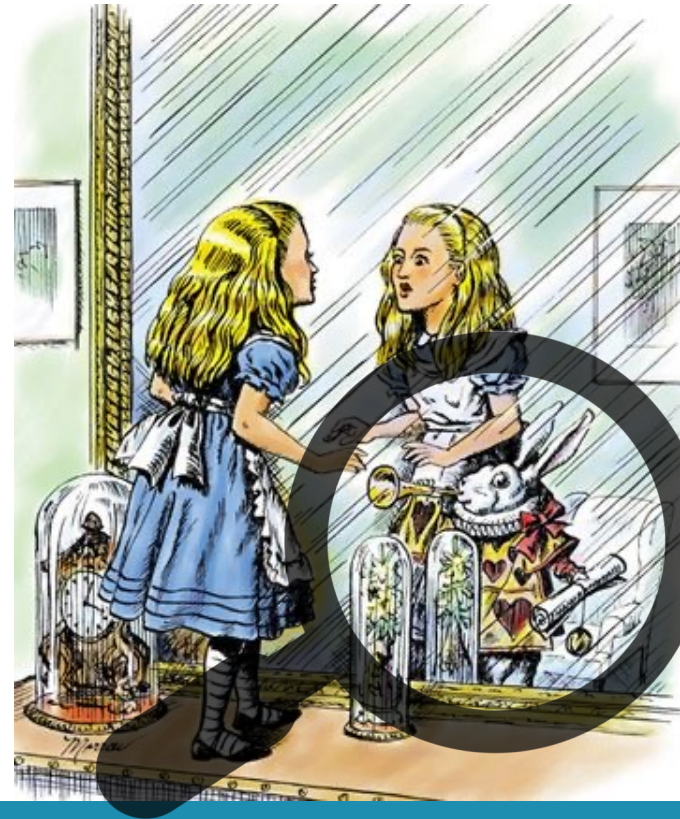


- States with the same T in $N=Z$ **mirror nuclei** \rightarrow Isobaric Analogue States (IAS)

- ΔE_x between same- T states in isobaric doublets \rightarrow **Mirror Energy Differences (MED)**

$$\text{MED}_{J,T} = E_{J,T,T_z=-T}^* - E_{J,T,T_z=T}^*$$

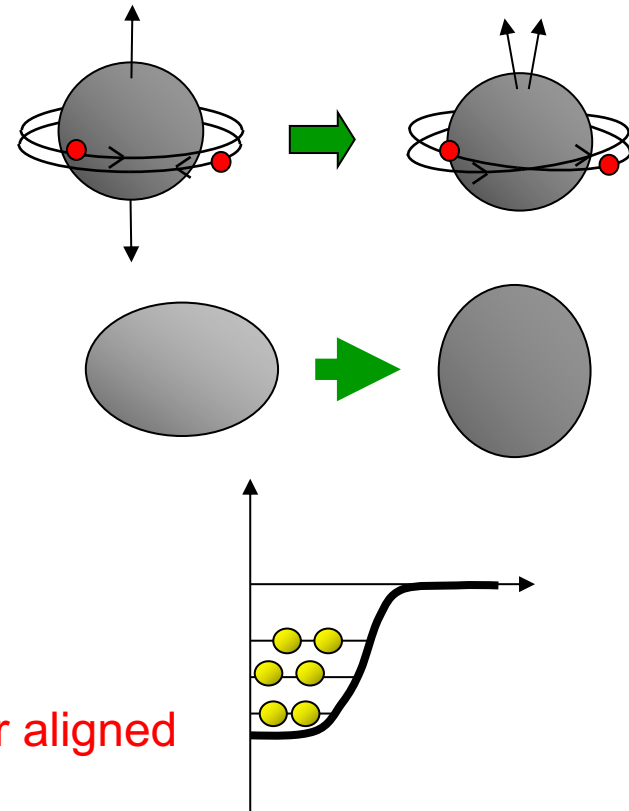
- Differences between IAS magnifies **isospin non-conserving effects**



Shell model interpretation of MED

Coulomb effects:

- **Multipole Coulomb term V_{CM} :**
alignment of the valent protons
- **Monopole term V_{Cm} :**
 1. radius changes with J
 2. $\ell \cdot \ell$ term to account for shell effects
 3. $\ell \cdot s$ **electromagnetic spin-orbit term (EMSO)**
changes in single-particle energies
different on π and ν , and when ℓ and s are parallel or aligned
→ Important in cross-shell excitations

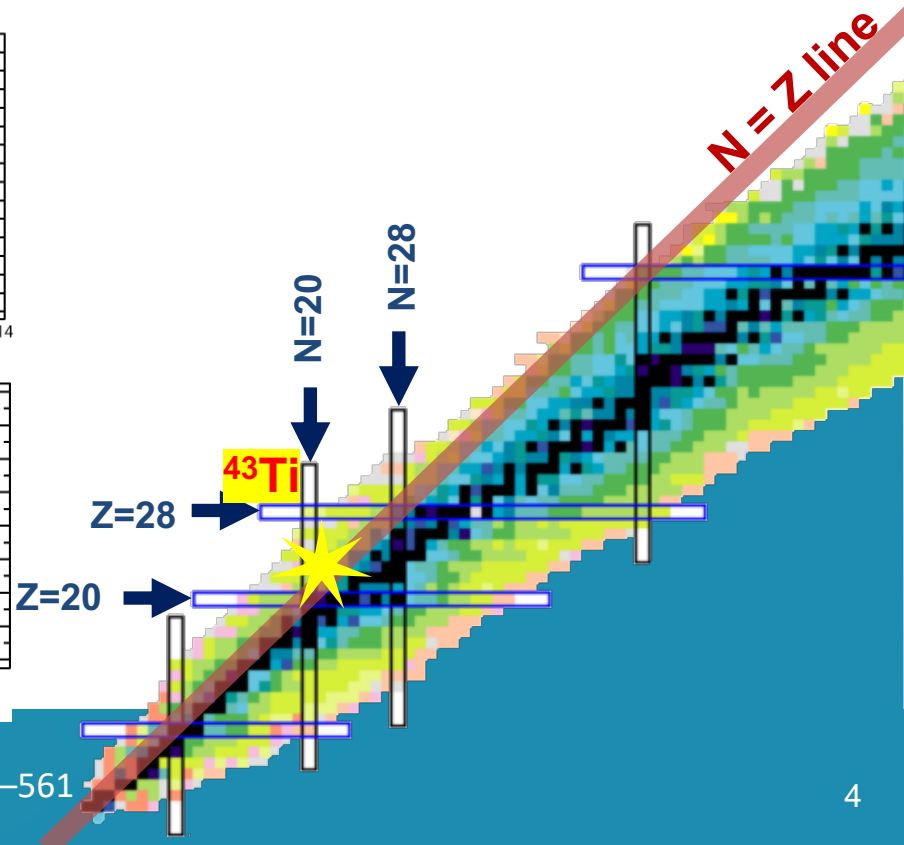
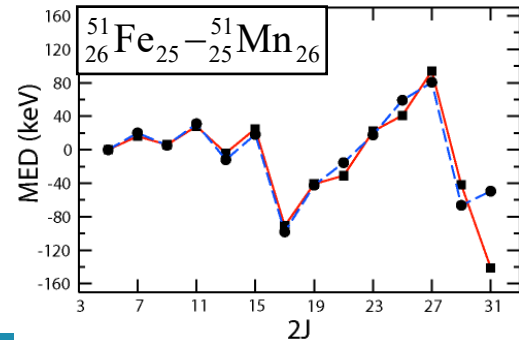
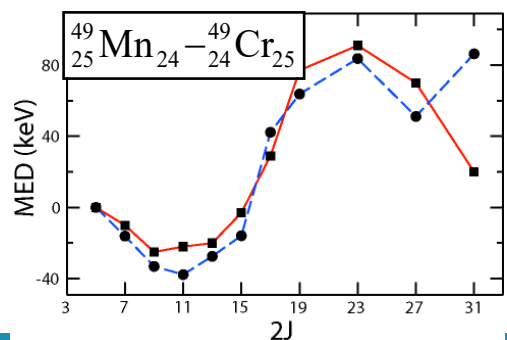
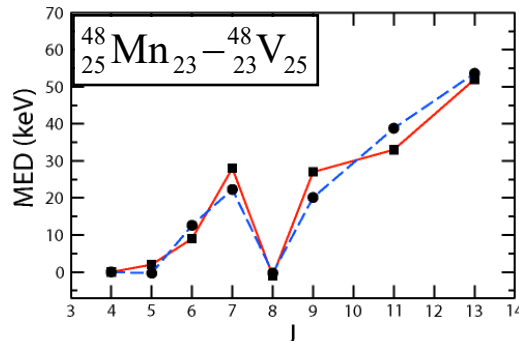
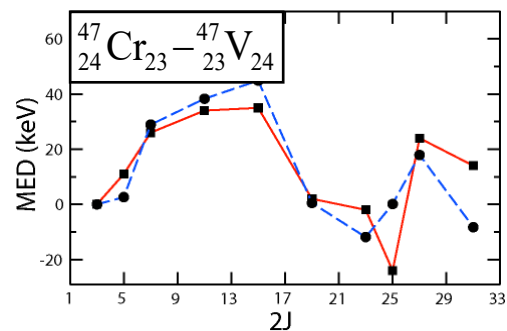
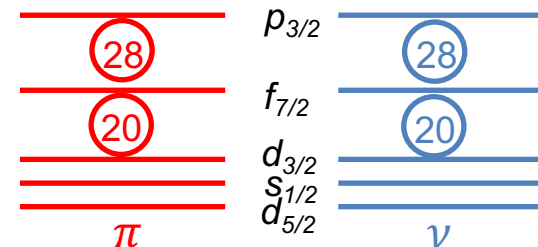


Isospin non-conserving term V_B : charge symmetry breaking

$$MED = V_{CM} + V_{Cm} + V_B$$

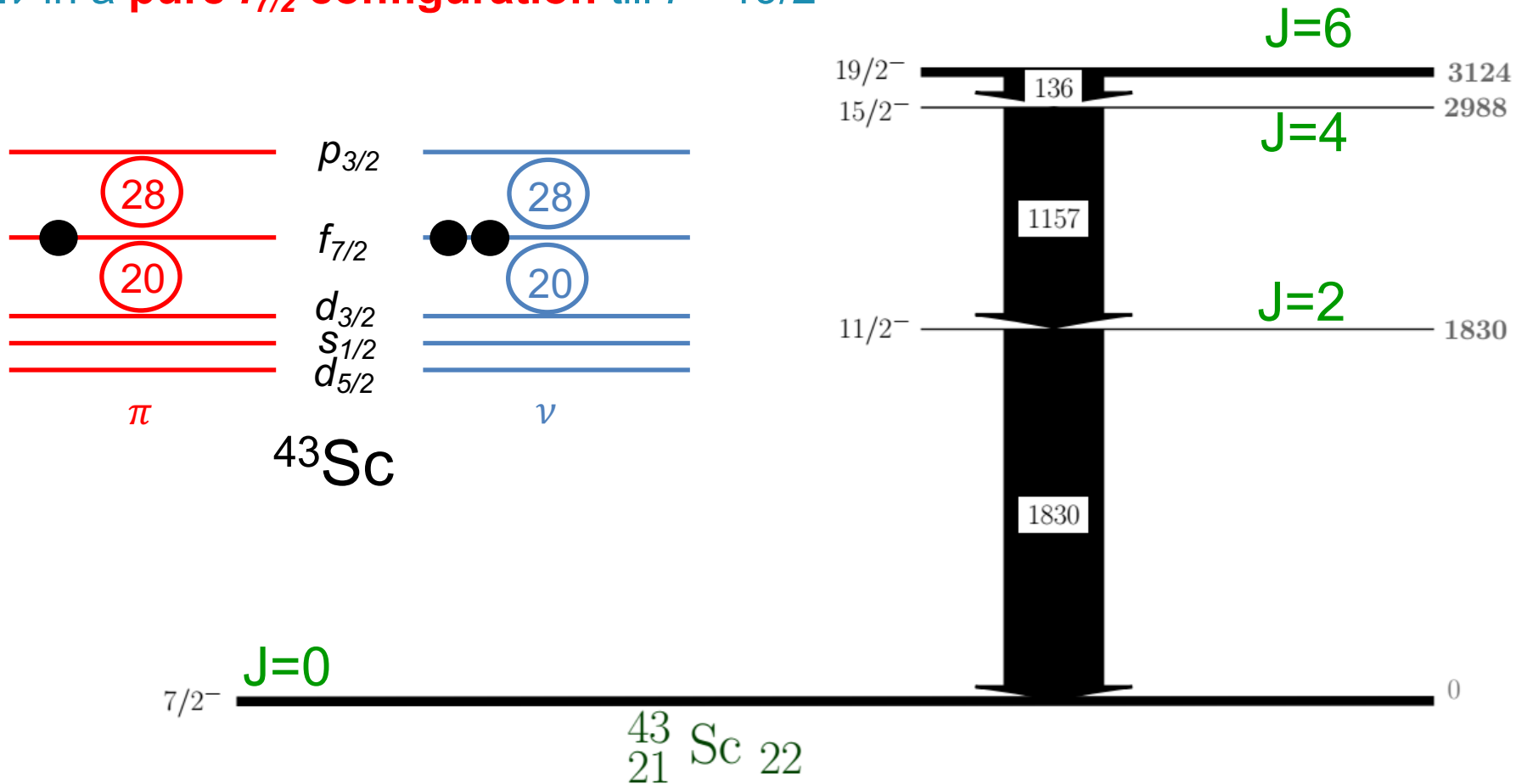
Mirror symmetry in the $f_{7/2}$ shell

- between ^{40}Ca and ^{56}Ni : classic “playground” for isospin symmetry studies:
 - more available experimentally
 - calculations can be limited to few shells (sd and fp)
 - nice way to study the interplay of the ISB effects

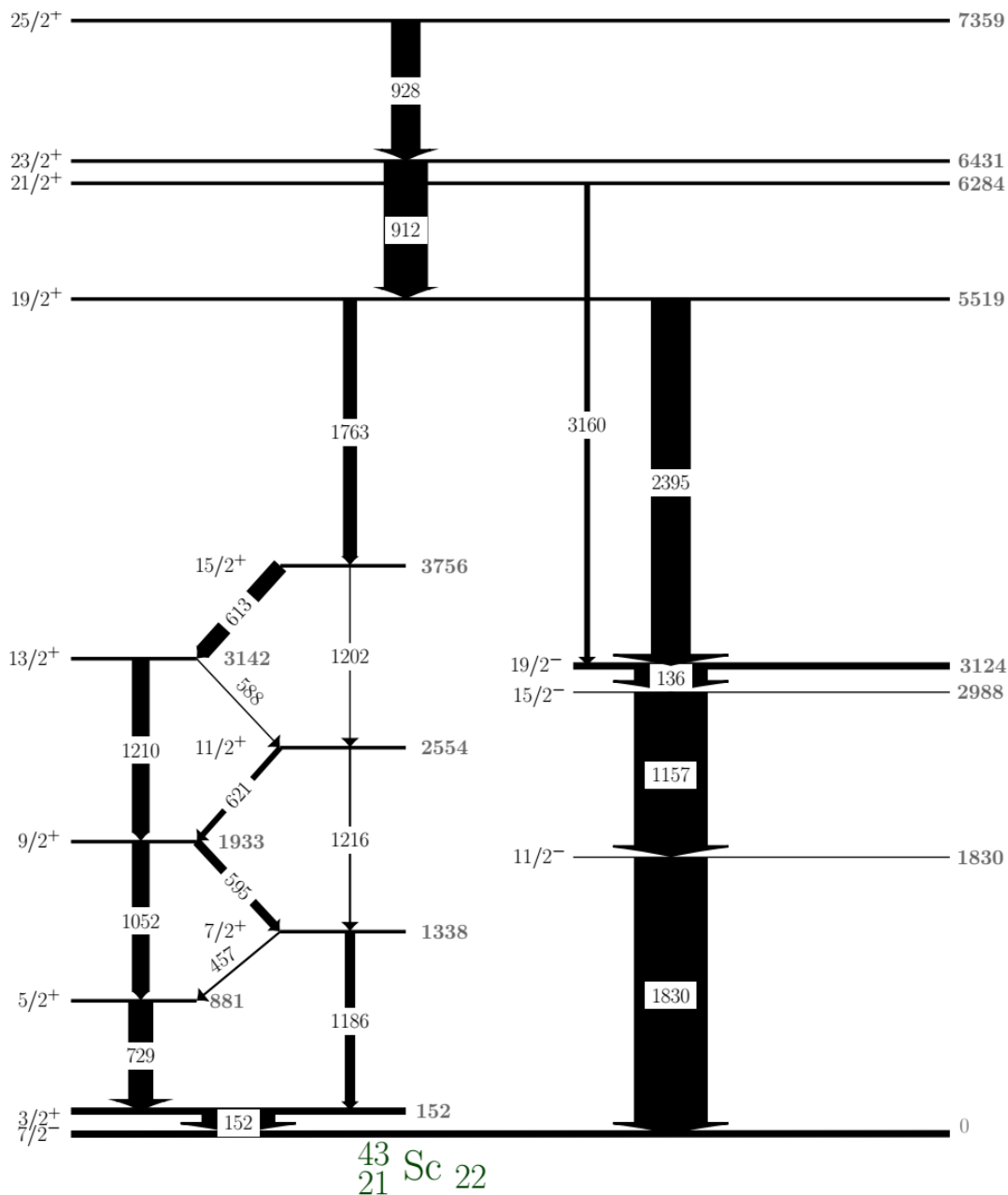


^{43}Sc : negative-parity states

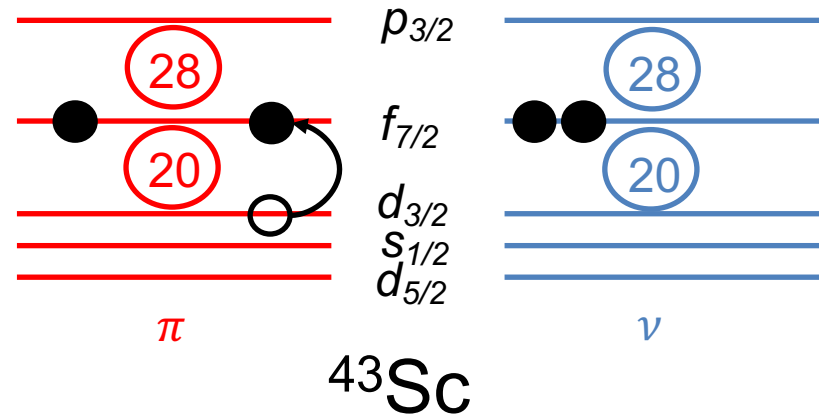
yrast structure, based on the $7/2^-$ g.s., is non-collective
 terminates at the maximum spin that can be generated with one π and
 2ν in a **pure $f_{7/2}$ configuration** till $I = 19/2^-$



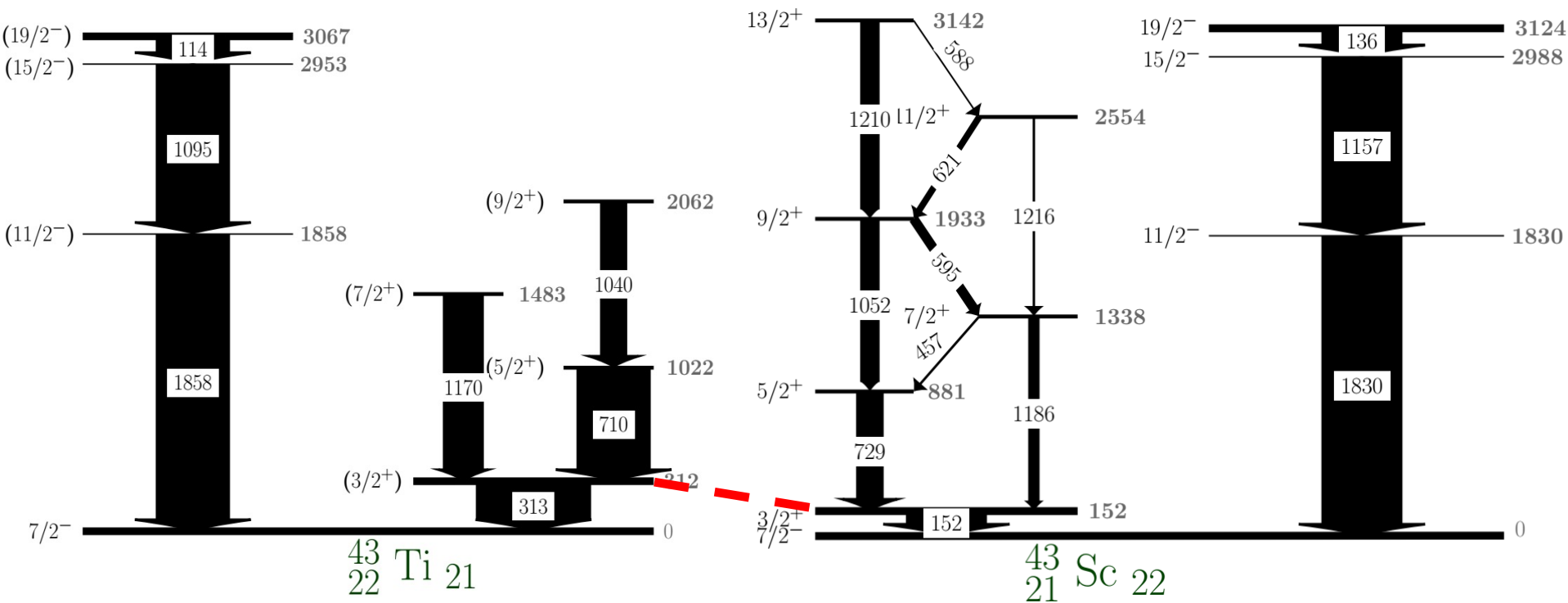
^{43}Sc : positive-parity states



- Rotational band built on the $3/2^+$ IS : **particle-hole cross-shell excitation from the $d_{3/2}$ orbit to the fp shell**
- With increasing spin, the alignment drives the nucleus towards a band termination at $I = 27/2^+$

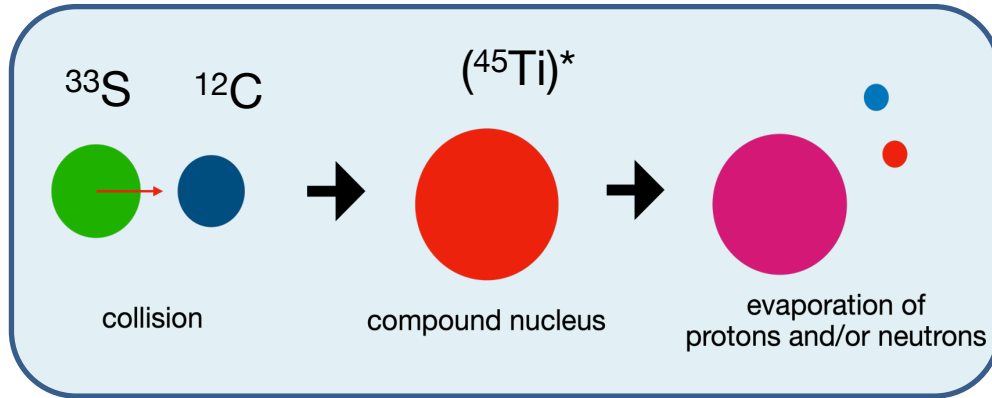


A=43 mirror pair



- Scheme of yrast states in ^{43}Ti known before this work
- The $3/2^+$ appears at **312 keV** instead of **152 keV**
because $N, Z = 20$ gap size is different for π and ν
- **EMSO has a strong effect on MED** → study evolution of wavefunction as a function of the angular momentum

Experiment: spectroscopy of ^{43}Ti



^{43}Ti – 2n evaporation

Stronger channels:

^{43}Sc 1p1n

^{43}Ca 2p

^{40}Ca 1 α 1n

^{40}K 1 α 1p



	p?	p?	p	$\epsilon = 100.00\%$	$\epsilon = 100.00\%$ $\epsilon\alpha$	$\epsilon = 100.00\%$	$\epsilon = 100.00\%$	$\epsilon = 100.00\%$	$\epsilon = 100.00\%$	$\epsilon = 100.00\%$
23										
38Ti	39Ti 31 ms $\epsilon = 100.00\%$ $\epsilon p = 100.00\%$	40Ti 52.4 ms $\epsilon p = 97.50\%$ ϵ	41Ti 81.9 ms $\epsilon = 100.00\%$ $\epsilon p = 100.00\%$	42Ti 208.65 ms $\epsilon = 100.00\%$	43Ti 509 ms $\epsilon = 100.00\%$	44Ti 60.0 y $\epsilon = 100.00\%$	45Ti 184.8 min $\epsilon = 100.00\%$	46Ti STABLE 8.25%	47Ti STABLE 7.6%	48Ti STABLE 73.7%
22										
37Sc	38Sc	39Sc < 300 ns $p = 100.00\%$	40Sc 182.3 ms $\epsilon = 100.00\%$ $\epsilon p = 0.44\%$ $\epsilon\alpha = 0.02\%$	41Sc 596.3 ms $\epsilon = 100.00\%$	42Sc 680.70 ms $\epsilon = 100.00\%$	43Sc 3.891 h $\epsilon = 100.00\%$	44Sc 3.97 h $\epsilon = 100.00\%$	45Sc STABLE 100%	46Sc STABLE 8.2%	47Sc STABLE 73.7%
21	p?	p								
36Ca	37Ca 12 ms $\epsilon = 100.00\%$ $\epsilon p = 82.10\%$	38Ca 440 ms $\epsilon = 100.00\%$	39Ca 859.6 ms $\epsilon = 100.00\%$	40Ca > $3.0E+21$ y 96.94% 2 ϵ	41Ca 9.94E4 y $\epsilon = 100.00\%$	42Ca STABLE 0.647%	43Ca STABLE 0.135%	44Ca STABLE 2.09%	45Ca STABLE 1.91%	46Ca STABLE 16.0%
20										
35K	36K 78 ms $\epsilon = 100.00\%$ $\epsilon p = 0.37\%$	37K 342 ms $\epsilon = 100.00\%$ $\epsilon p = 0.05\%$ $\epsilon\alpha = 3.4E-3\%$	38K 1.226 s $\epsilon = 100.00\%$	39K 7.636 min $\epsilon = 100.00\%$	40K STABLE 93.2581%	41K 1.248E+9 y 0.0117% $\beta = 89.28\%$ $\epsilon = 10.72\%$	42K STABLE 6.7302%	43K 12.355 h $\beta = 100.00\%$	44K 22.3 h $\beta = 100.00\%$	45K STABLE 0.17%
19										
34Ar	35Ar 4.5 ms $\epsilon = 100.00\%$	36Ar 1.7756 s $\epsilon = 100.00\%$	37Ar STABLE 0.3336%	38Ar 35.04 d $\epsilon = 100.00\%$	39Ar STABLE 0.0629%	40Ar 269 y $\beta = 100.00\%$	41Ar STABLE 99.6035%	42Ar 109.61 min $\beta = 100.00\%$	43Ar 32.9 y $\beta = 100.00\%$	44Ar STABLE 5.74%
18										
33Cl	34Cl 511 s $\epsilon = 100.00\%$	35Cl 1.5264 s $\epsilon = 100.00\%$	36Cl STABLE 2.04%	37Cl 3.01E+5 y $\epsilon = 100.00\%$	38Cl STABLE 2.48%	39Cl 37.24 min $\beta = 100.00\%$	40Cl 56.2 min $\beta = 100.00\%$	41Cl 1.35 min $\beta = 100.00\%$	42Cl 38.4 s $\beta = 100.00\%$	43Cl STABLE 5.7%
	16	17	18	19	20	21	22	23	24	25
	Neutron (N) #									

N=Z

JYFL experiment JM11

Reaction: $^{33}\text{S} + ^{12}\text{C} \rightarrow ^{43}\text{Ti} + 2\text{n}$ @ 100 MeV beam energy

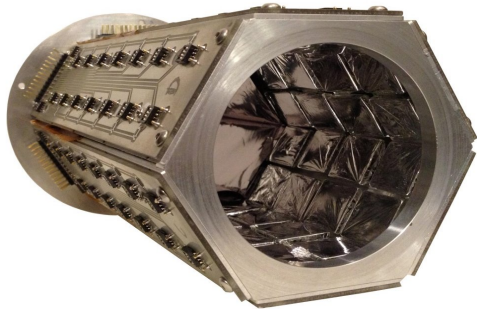
JUROGAM 3
prompt γ -rays

MARA
recoil selection



JYTube: channel ID

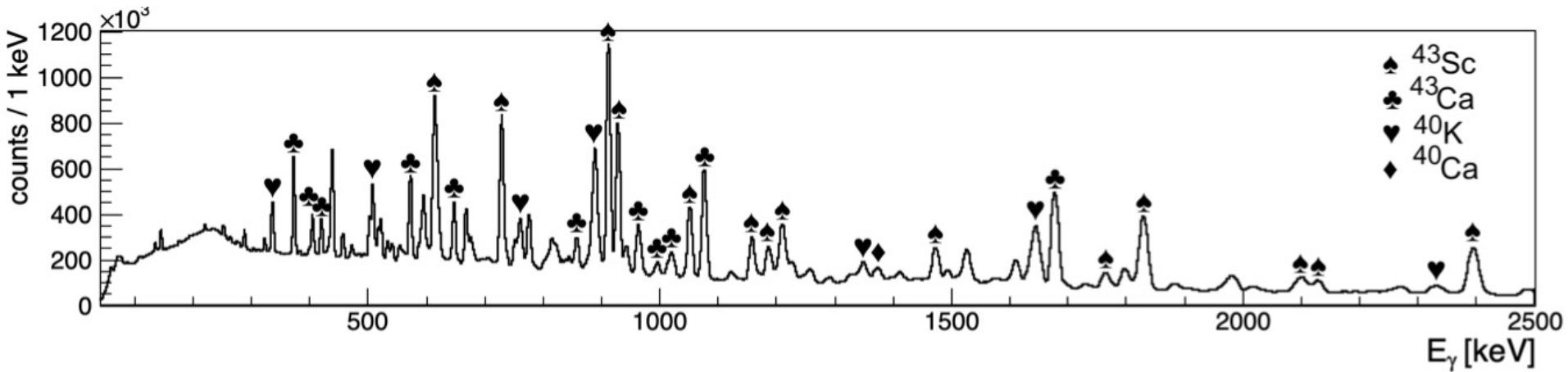
Focal plane:
DSSD, FPGe
isomer tagging



(talk by J. Pakarinen)

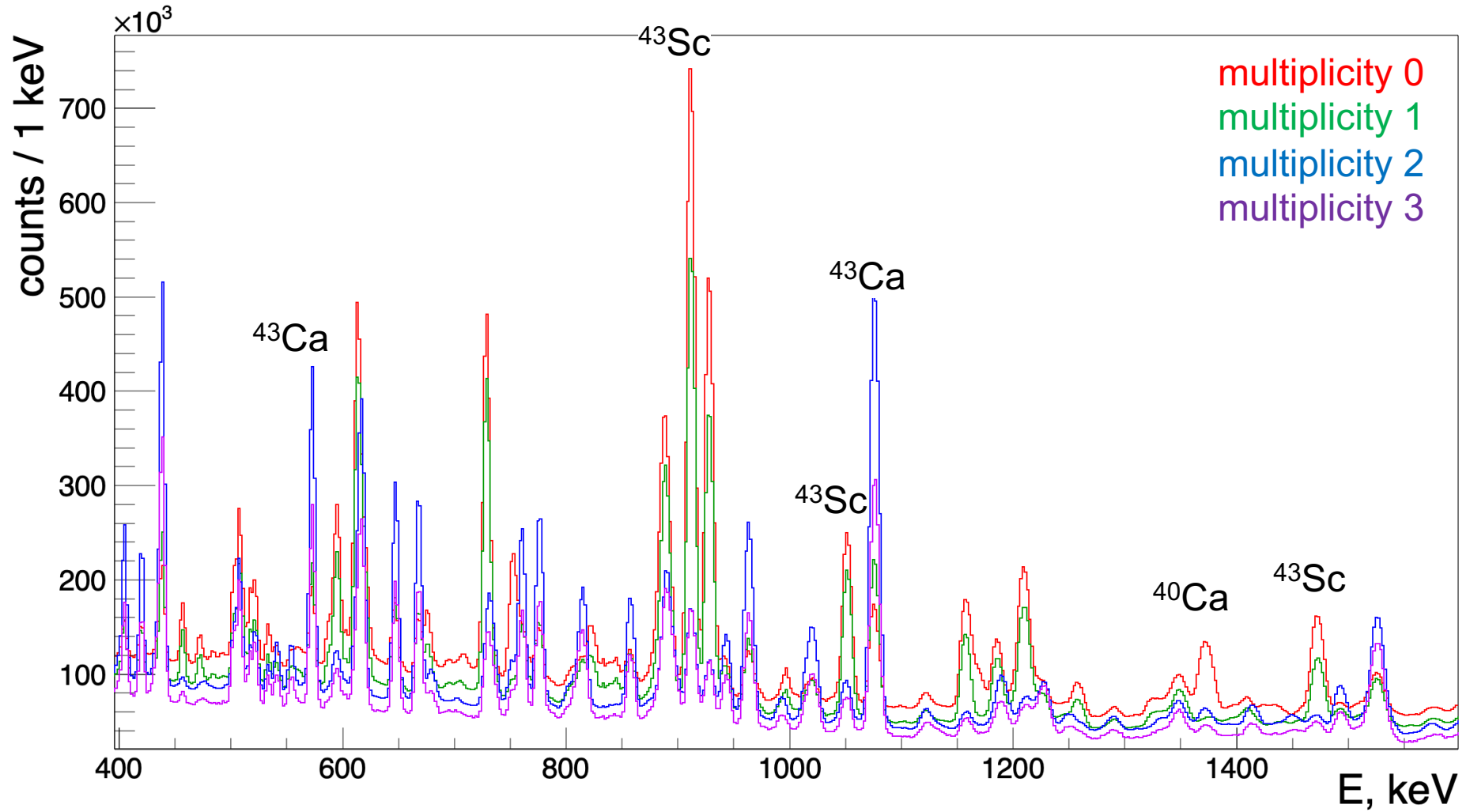
Prompt JUROGAM 3 spectrum

After selection with MARA, still many A/Q “twins” get transported to the focal plane



Additional constraints are needed!

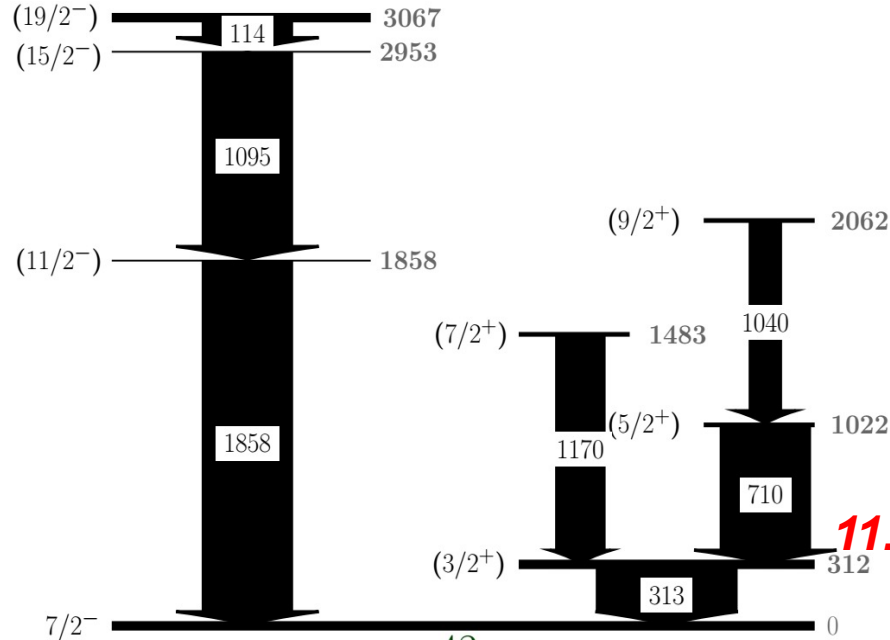
JYTube: charged particle tagging



Tagging on isomers in ^{43}Ti

gate the on fast IS
 → negative-parity
 states

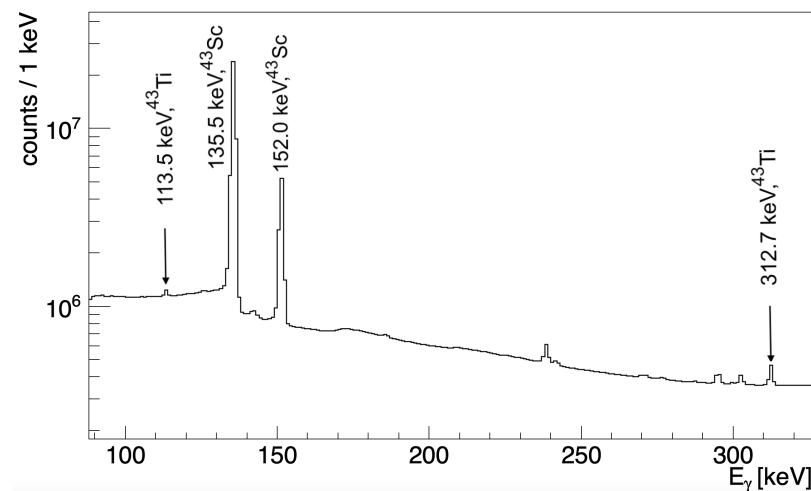
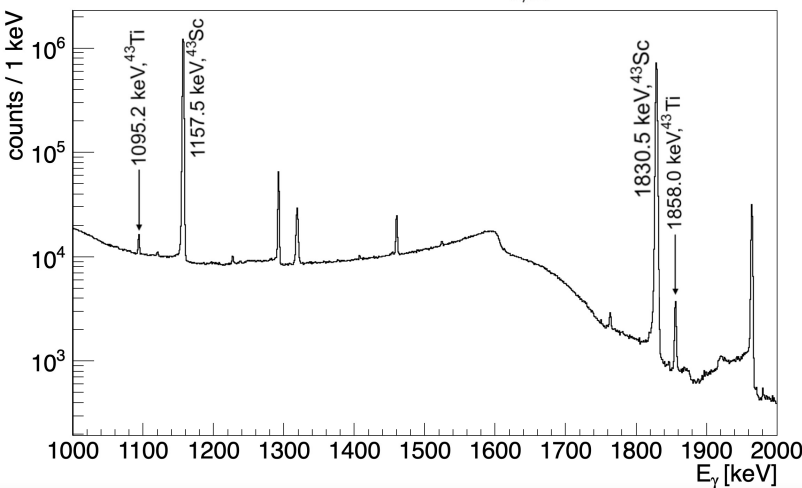
551 ns



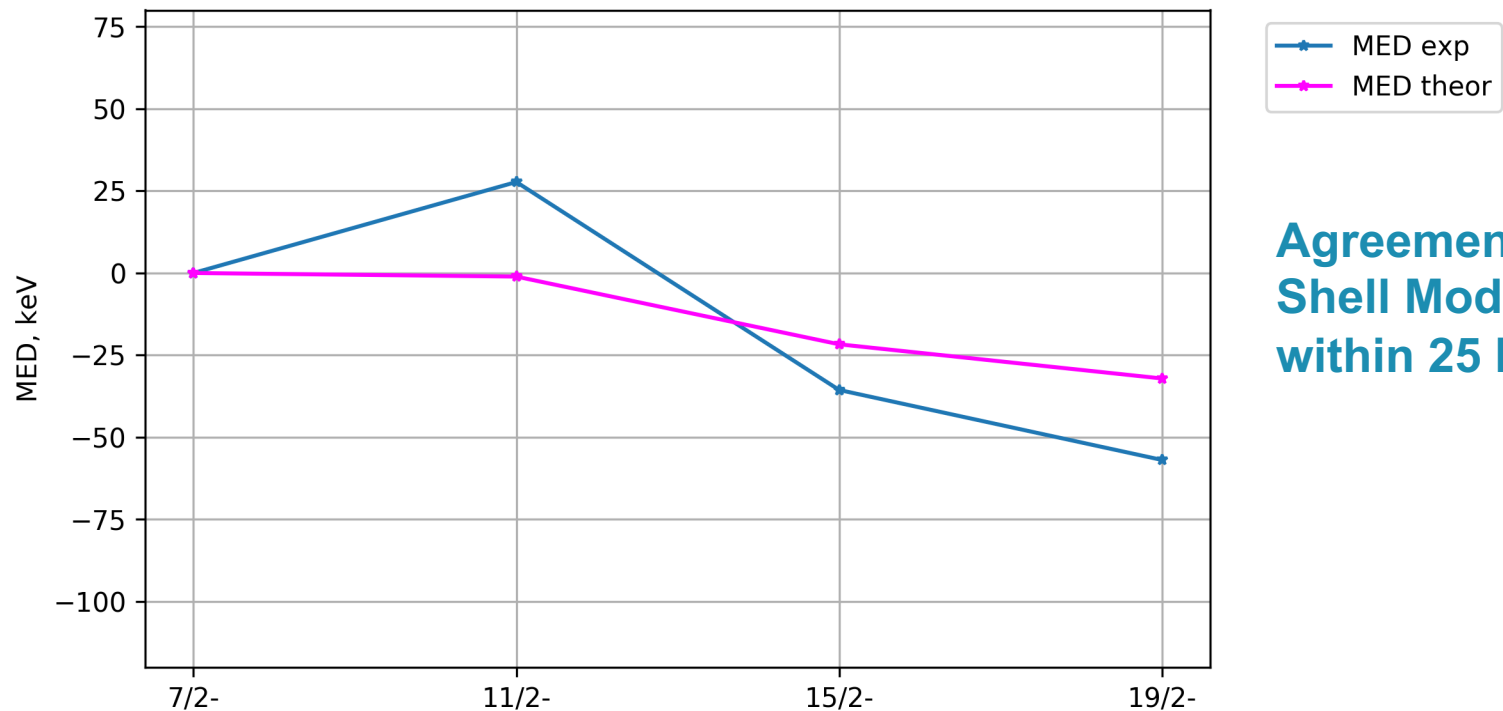
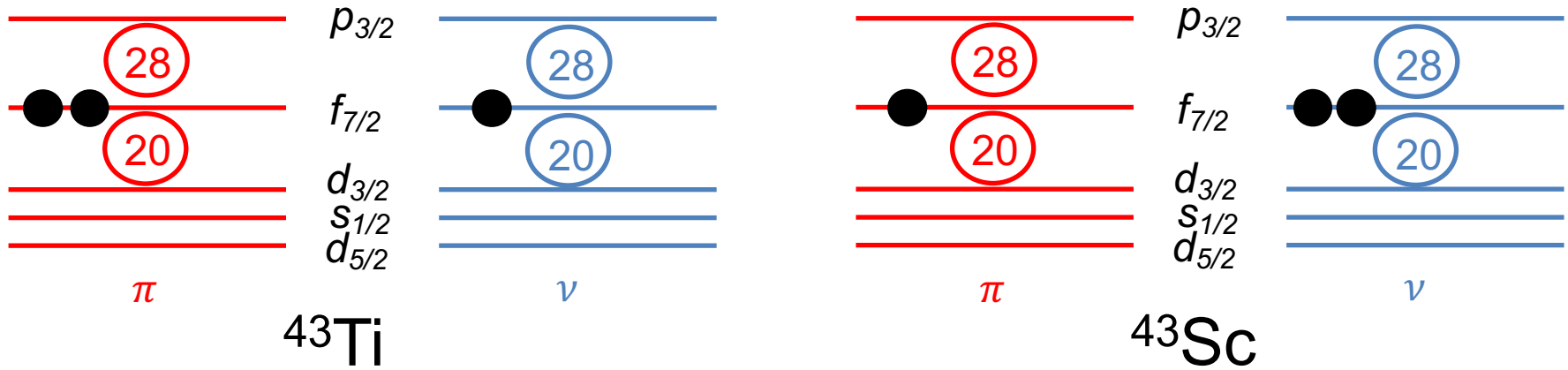
gate on the slow IS
 → positive-parity
 states

11.7 us

$^{43}_{22}\text{Ti}$ $^{21}_{21}$

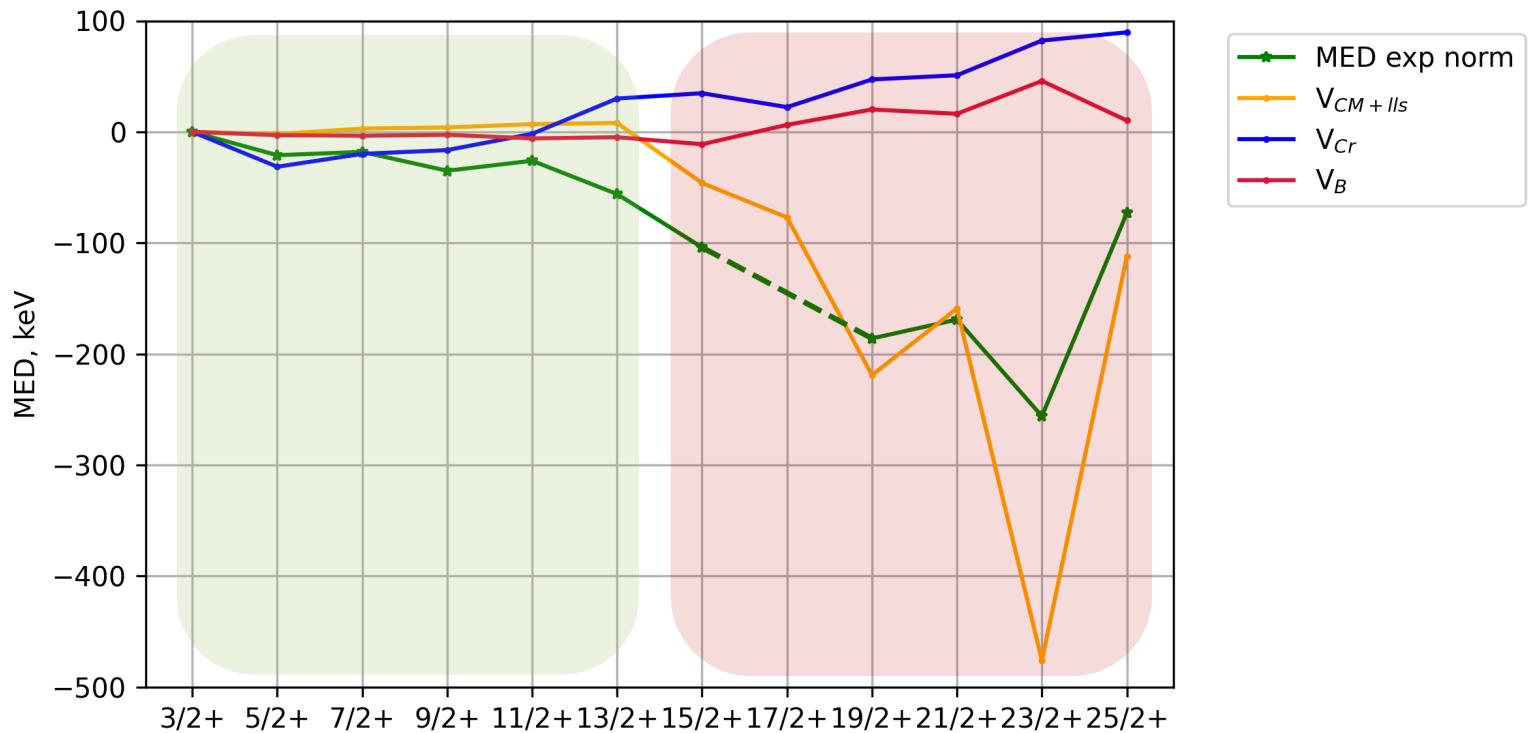
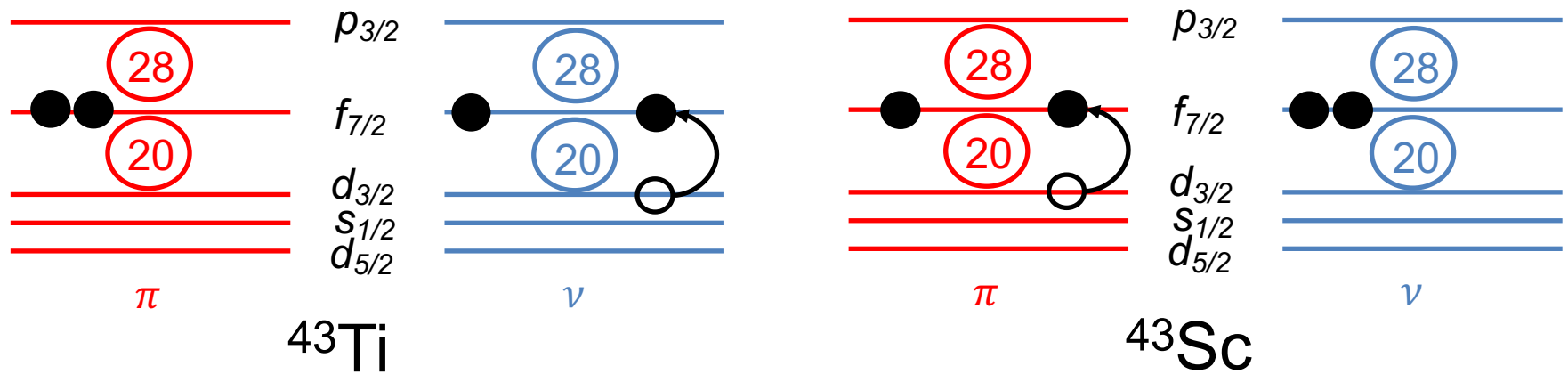


MED: Negative-parity states

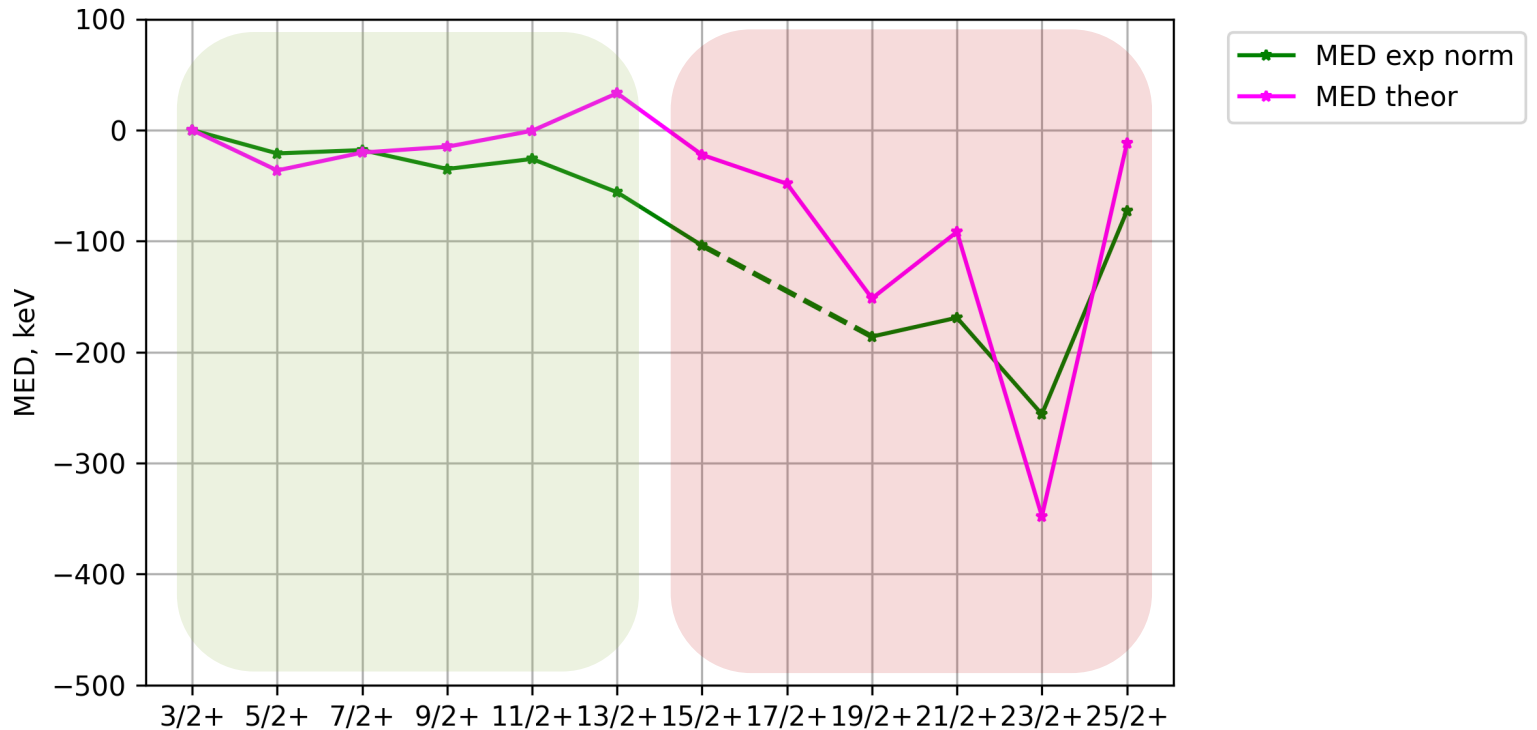
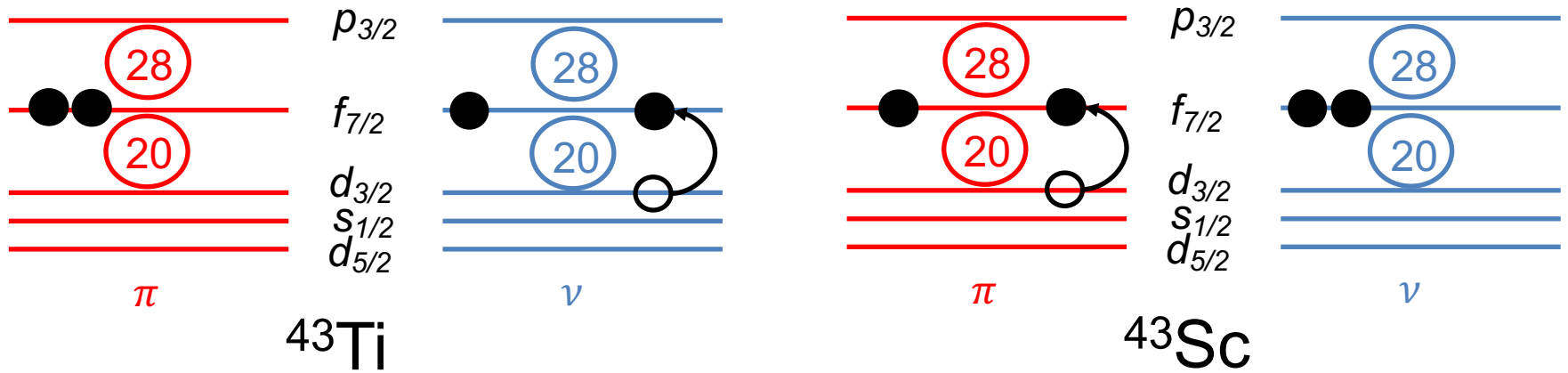


Agreement with Shell Model within 25 keV

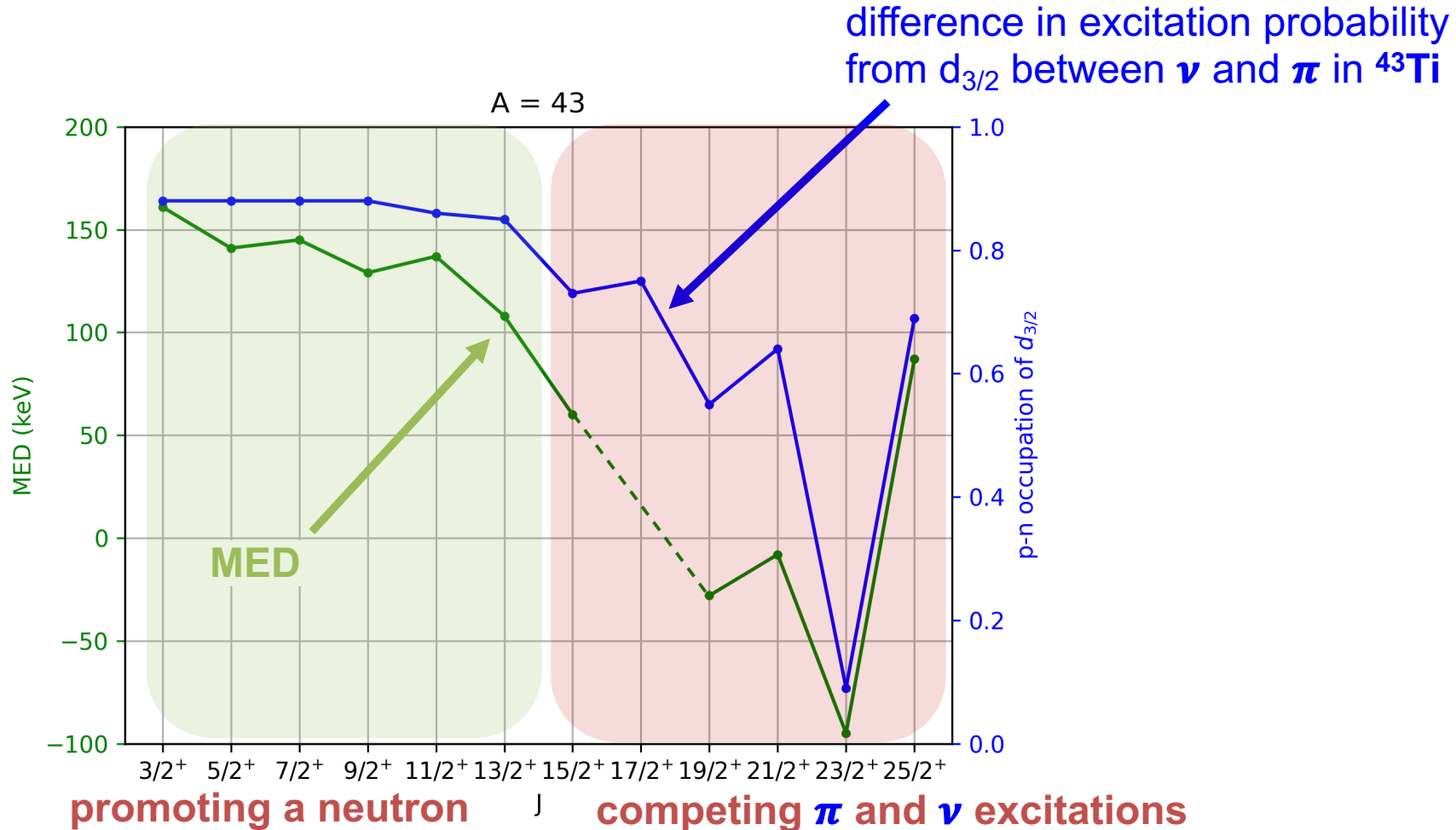
MED: Positive-parity states



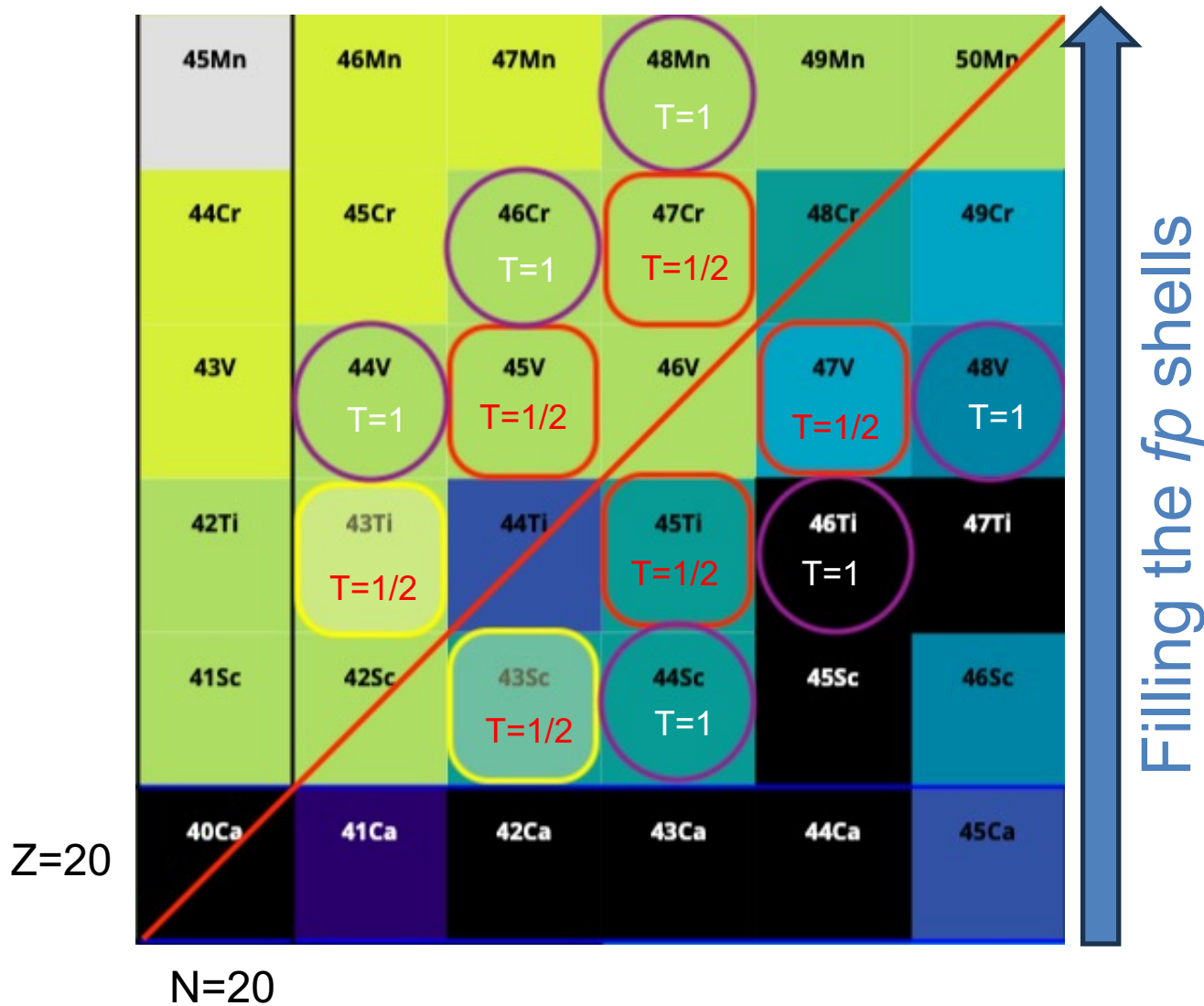
MED: Positive-parity states



Correlation between MED and excitations across the N,Z=20 gap

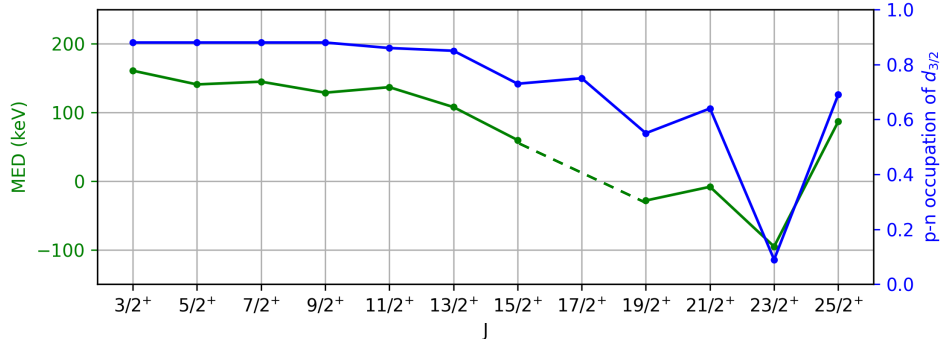


Systematic study of the $d_{3/2}$ occupancy

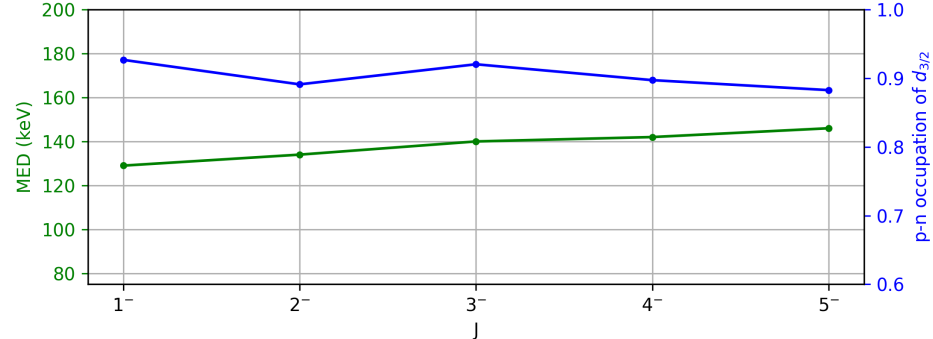


$d_{3/2}$ occupancy compared to MED

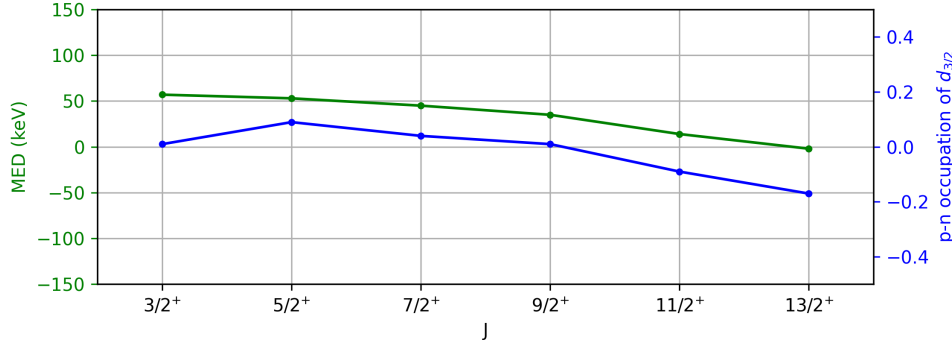
A = 43



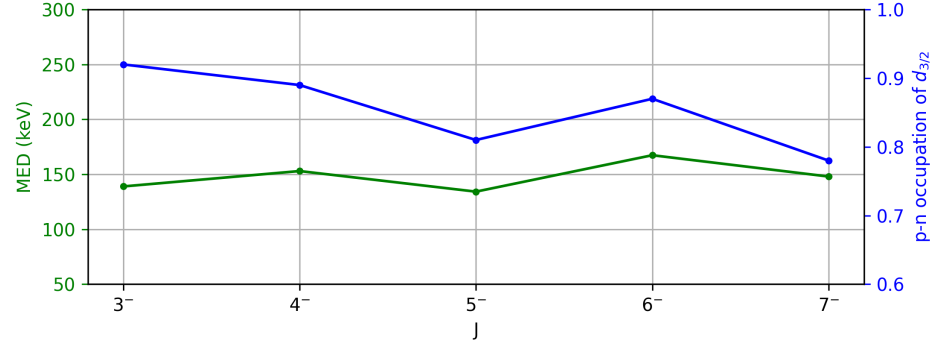
A = 44



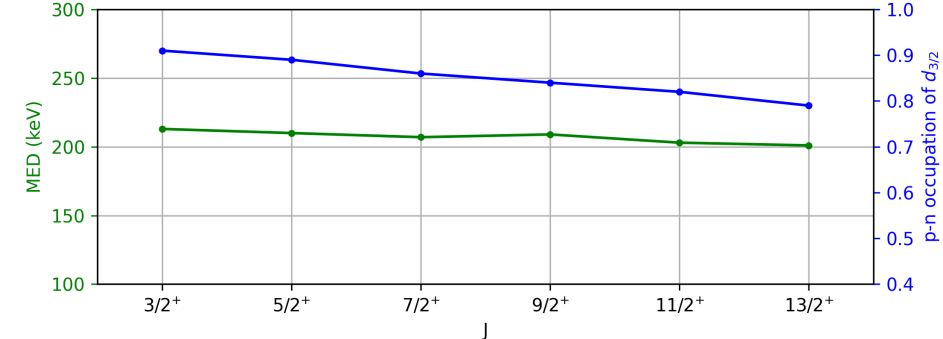
A = 45



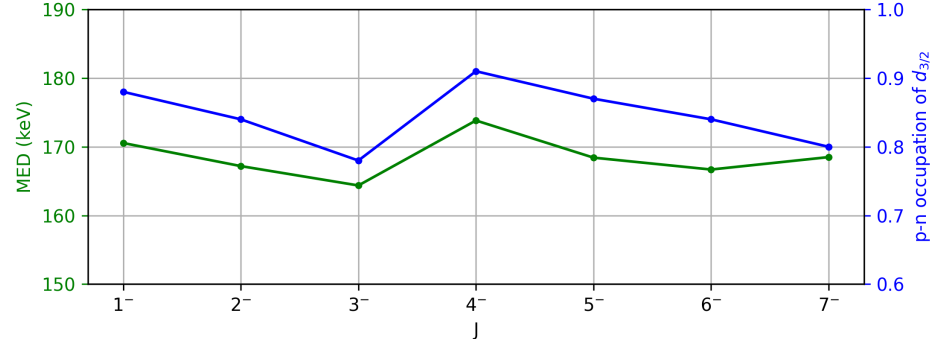
A = 46



A = 47



A = 48



Conclusions

- Extended the level scheme of ^{43}Ti up to $25/2^+$
- For the negative-parity states, good agreement of MED between experiment and Shell Model
- The MED in $A=43$ increase after $15/2^+$ *because the excited nucleon is not always the same*
- This is put in evidence in the EMSO term (difference in the gap π and ν)
- As the calculations are in good agreement with the experiment, we can say that *the experimental MED allow us to probe the wavefunction*

JM11 collaboration

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