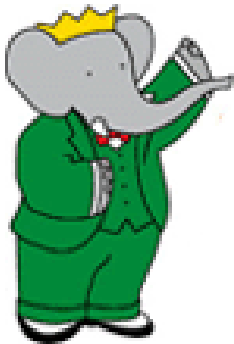


# Precise Measurement of the $e^+e^- \rightarrow \pi^+\pi^-(\gamma)$ Cross Section with BaBar and the Muon $g-2$

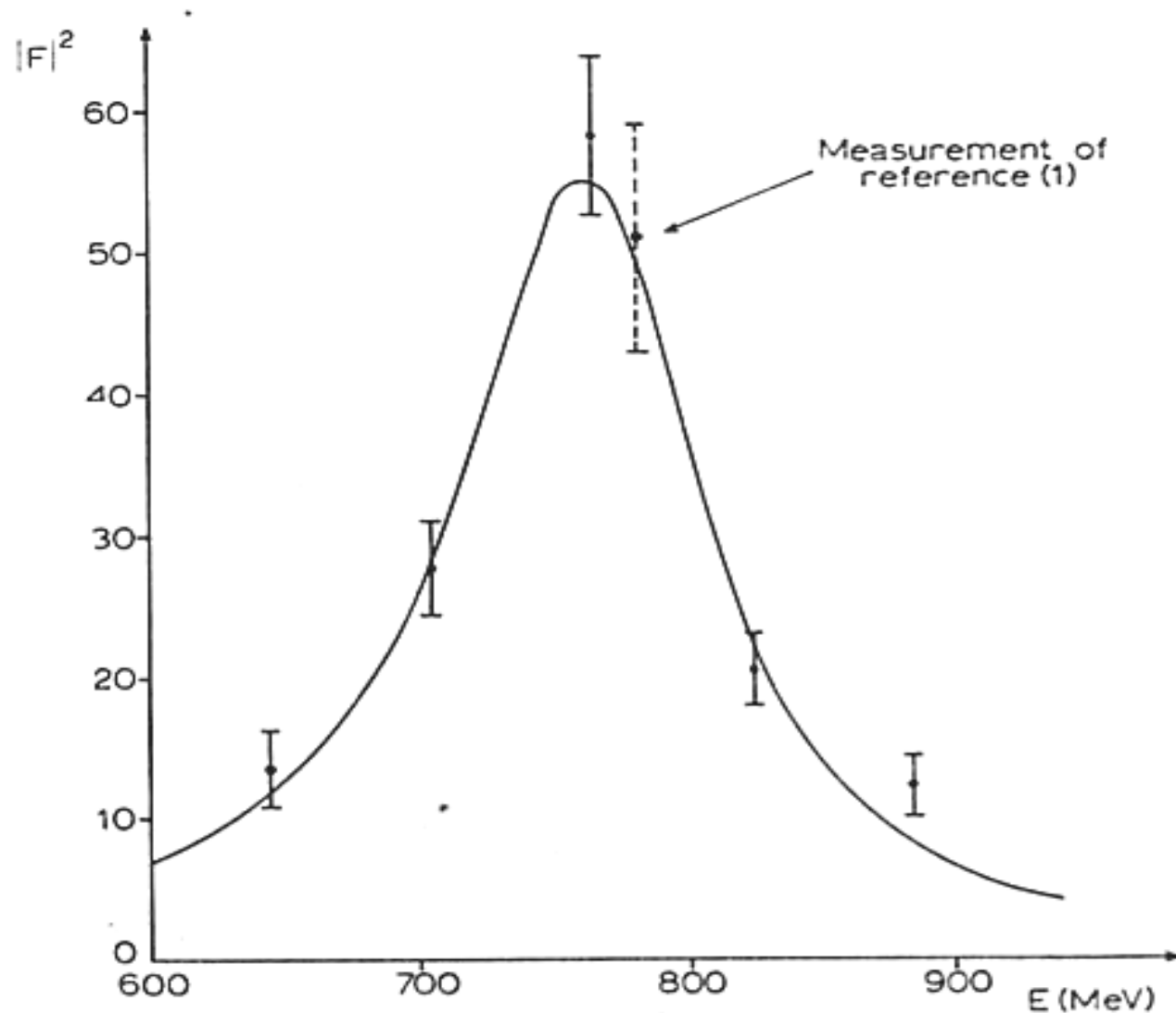
Michel Davier (LAL – Orsay, BaBar Collaboration)

- the muon magnetic anomaly
- $e^+e^-$  and (revisited)  $\tau$  spectral functions
- the BaBar ISR (Initial State Radiation) analysis
- test of the method:  $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$
- results on  $e^+e^- \rightarrow \pi^+\pi^-(\gamma)$
- combination of all  $ee$  data
- discussion and perspectives



# Un petit retour en arrière au LAL il y a ~45 ans

$e^+e^- \rightarrow \pi^+\pi^-$   
sur ACO  
résonance  $\rho$



# Lepton Magnetic Anomaly: from Dirac to QED

$$\vec{\mu} = g \frac{e}{2m} \vec{s},$$

$$a = (g - 2)/2$$

Dirac (1928)  $g_e=2$   $a_e=0$

anomaly discovered:

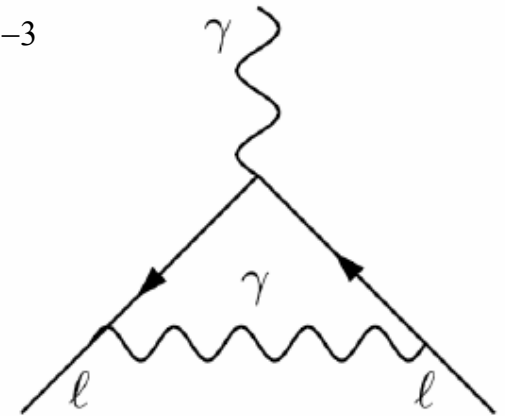
Kusch-Foley (1948)  $a_e = (1.19 \pm 0.05) 10^{-3}$

and explained by  $O(\alpha)$  QED contribution:

Schwinger (1948)  $a_e = \alpha/2\pi = 1.16 10^{-3}$

first triumph of QED

$\Rightarrow a_e$  sensitive to quantum fluctuations of fields



# More Quantum Fluctuations

$$a = a^{\text{QED}} + a^{\text{had}} + a^{\text{weak}} + ? a^{\text{new physics ?}}$$

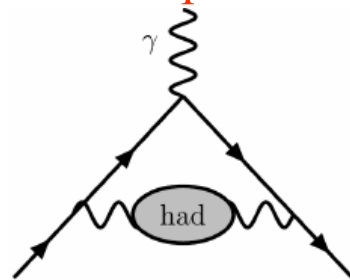
typical contributions:

QED up to  $O(\alpha^4)$ ,  $\alpha^5$  in progress (Kinoshita et al.)

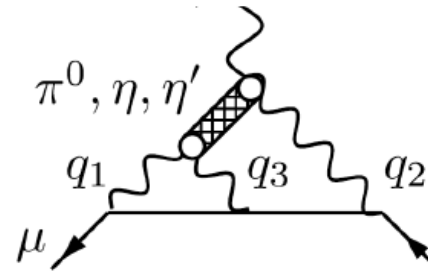


Hadrons

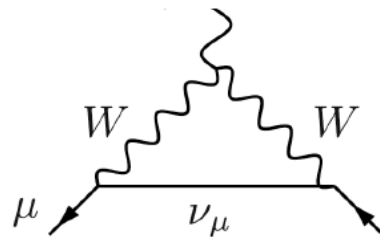
vacuum polarization



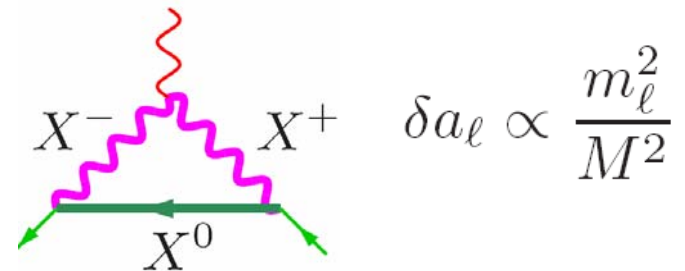
light-by-light (models)



Electroweak



new physics at high mass scale



$$\delta a_\ell \propto \frac{m_\ell^2}{M^2}$$

$\Rightarrow a_\mu$  much more sensitive to high scales

# Hadronic Vacuum Polarization and Muon $(g-2)_\mu$

Dominant uncertainty from lowest-order HVP piece

Cannot be calculated from QCD (low mass scale), but one can use experimental data on  $e^+e^- \rightarrow \text{hadrons}$  cross section

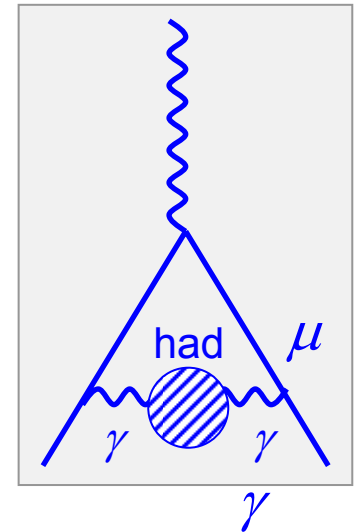
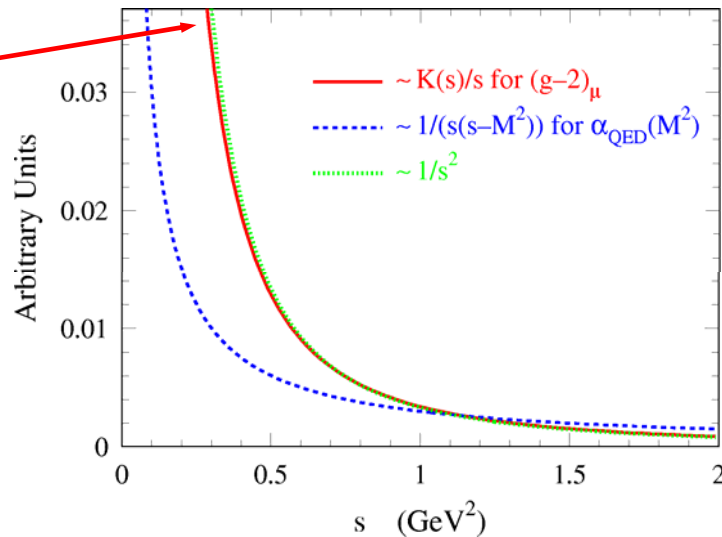
Bouchiat-Michel (1961) Brodsky-de Rafael (1968) Born:  $\sigma^{(0)}(s) = \sigma(s)(\alpha/\alpha(s))^2$

$$12\pi \text{Im}\Pi_\gamma(s) = \frac{\sigma^0[e^+e^- \rightarrow \text{hadrons}(\gamma)]}{\sigma_{pt}} \equiv R(s)$$

$$\text{Im}[\text{Diagram}] \propto |\text{Diagram} \text{ hadrons}|^2$$

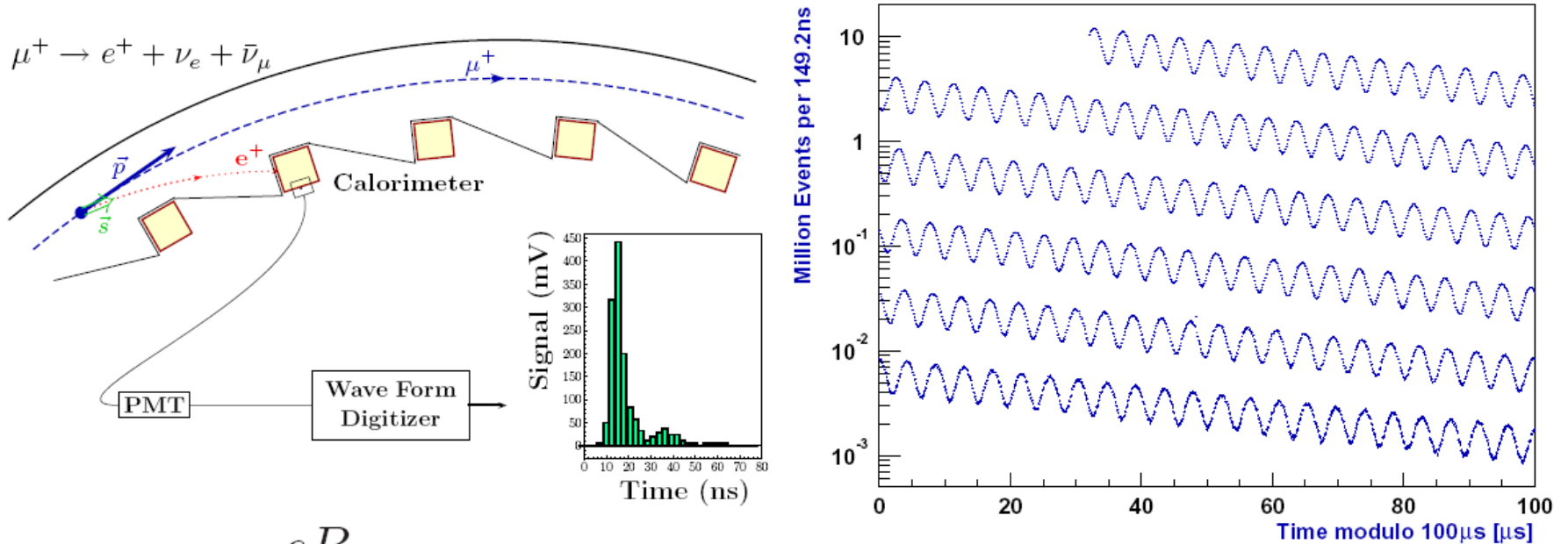
$$a_\mu^{\text{had}} = \frac{\alpha^2}{3\pi^2} \int_{4m_\pi^2}^{\infty} ds \frac{K(s)}{s} R(s)$$

Dispersion relation



# The E-821 Direct $a_\mu$ Measurement at BNL

Storage ring technique pioneered at CERN (Farley-Picasso...)



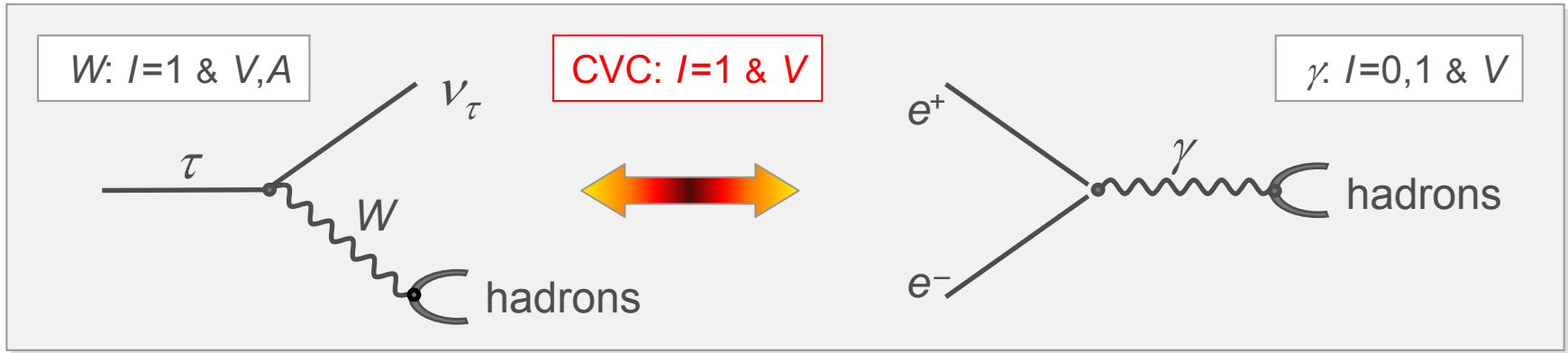
$$\omega_a = a_\mu \frac{eB}{m_\mu}$$

$a_\mu$  obtained from a ratio of frequencies  
 result updated with new value for  $\mu_\mu/\mu_p$  ( $+0.9 \cdot 10^{-10}$ )  
 (see next review in RPP2009 (Hoecker-Marciano))

$$\omega_{\text{precession}} - \omega_{\text{rotation}}$$

$$a_\mu^{\text{exp}} = (11\,659\,208.9 \pm 5.4 \pm 3.3) \cdot 10^{-10} \\ (\pm 6.3) \quad (0.54 \text{ ppm})$$

# The Role of $\tau$ Data through CVC – SU(2)



Hadronic physics factorizes (**spectral Functions**)

$$\sigma^{(I=1)}[e^+e^- \rightarrow \pi^+\pi^-] = \frac{4\pi\alpha^2}{s} \nu[\tau^- \rightarrow \pi^-\pi^0\nu_\tau]$$

$$\nu[\tau^- \rightarrow \pi^-\pi^0\nu_\tau] \propto \underbrace{\frac{\text{BR}[\tau^- \rightarrow \pi^-\pi^0\nu_\tau]}{\text{BR}[\tau^- \rightarrow e^-\bar{\nu}_e\nu_\tau]}}_{\text{branching fractions}} \underbrace{\frac{1}{N_{\pi\pi^0}} \frac{dN_{\pi\pi^0}}{ds}}_{\text{mass spectrum}} \underbrace{\frac{m_\tau^2}{(1-s/m_\tau^2)^2 (1+s/m_\tau^2)}}_{\text{kinematic factor (PS)}}$$

# SU(2) Breaking

Corrections for SU(2) breaking applied to  $\tau$  data for dominant  $\pi^-\pi^+$  contrib.:

## ■ Electroweak radiative corrections:

- ▶ dominant contribution from short distance correction  $S_{EW}$
- ▶ subleading corrections (small)
- ▶ long distance radiative correction  $G_{EM}(s)$

Marciano-Sirlin' 88

Braaten-Li' 90

Cirigliano-Ecker-Neufeld' 02  
Lopez Castro et al.' 06

## ■ Charged/neutral mass splitting:

- ▶  $m_{\pi^-} \neq m_{\pi^0}$  leads to phase space (cross sec.) and width (FF) corrections
- ▶  $\rho$ - $\omega$  mixing (EM  $\omega \rightarrow \pi^-\pi^+$  decay) corrected using FF model
- ▶  $m_{\rho^-} \neq m_{\rho^0}$  \*\*\* and  $\Gamma_{\rho^-} \neq \Gamma_{\rho^0}$  \*\*\*

Alemay-Davier-Höcker' 97, Czyż-Kühn' 01

Flores-Baez-Lopez Castro' 08  
Davier et al.'09

## ■ Electromagnetic decays: $\rho \rightarrow \pi\pi\gamma$ \*\*\*, $\rho \rightarrow \pi\gamma$ , $\rho \rightarrow \eta\gamma$ , $\rho \rightarrow l^+l^-$

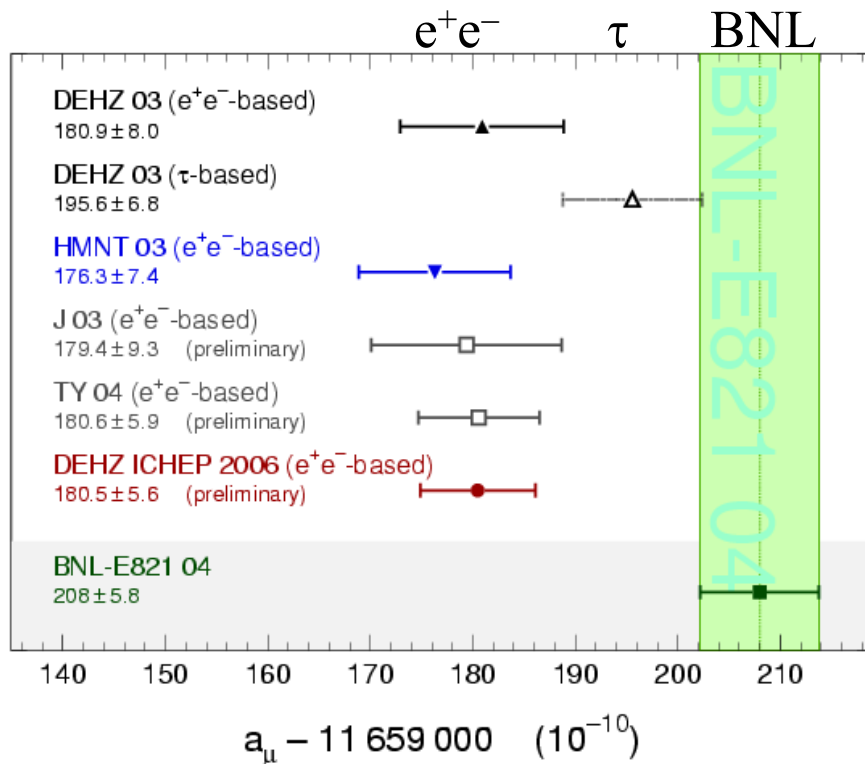
## ■ Quark mass difference $m_u \neq m_d$ (negligible)



# Situation at ICHEP'06 / 08

$$a_{\mu}^{\text{had}} [\text{ee}] = (690.9 \pm 4.4) \times 10^{-10}$$

$$a_{\mu} [\text{ee}] = (11\,659\,180.5 \pm 4.4_{\text{had}} \pm 3.5_{\text{LBL}} \pm 0.2_{\text{QED+EW}}) \times 10^{-10}$$



Hadronic HO  $-(9.8 \pm 0.1) \times 10^{-10}$

Hadronic LBL  $+(12.0 \pm 3.5) \times 10^{-10}$

Electroweak  $(15.4 \pm 0.2) \times 10^{-10}$

QED  $(11\,658\,471.9 \pm 0.1) \times 10^{-10}$

Knecht-Nyffeler (2002), Melnikov-Vainhstein (2003)

Davier-Marciano (2004)

Kinoshita-Nio (2006)

Observed Difference with BNL using  $e^+e^-$ :

$$a_{\mu} [\text{exp}] - a_{\mu} [\text{SM}] = (27.5 \pm 8.4) \times 10^{-10}$$

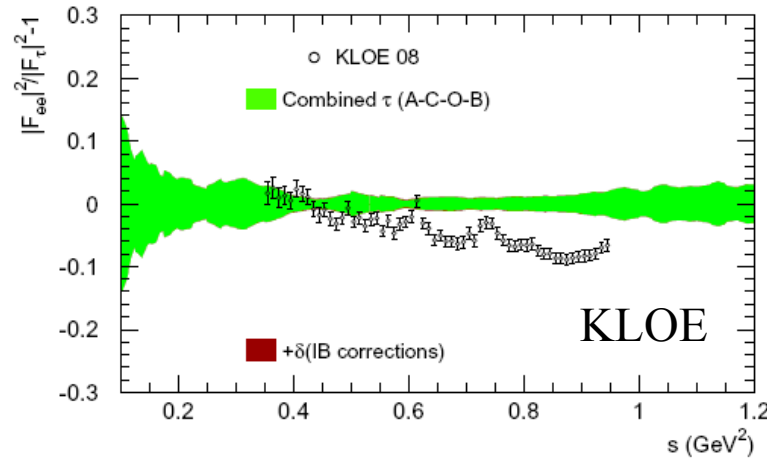
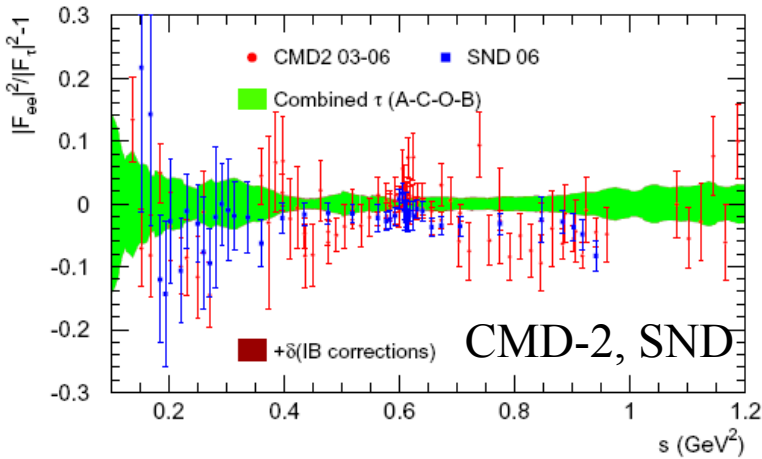
➔ 3.3 „standard deviations“

Estimate using  $\tau$  data consistent with E-821

# Revisited Analysis using $\tau$ Data: Belle + new IB

Relative comparison of  $\tau$  and ee spectral functions  
( $\tau$  green band)

arXiv:0906-5443 MD.Höcker,  
Malaescu,Zhang +IHEP+Mexico

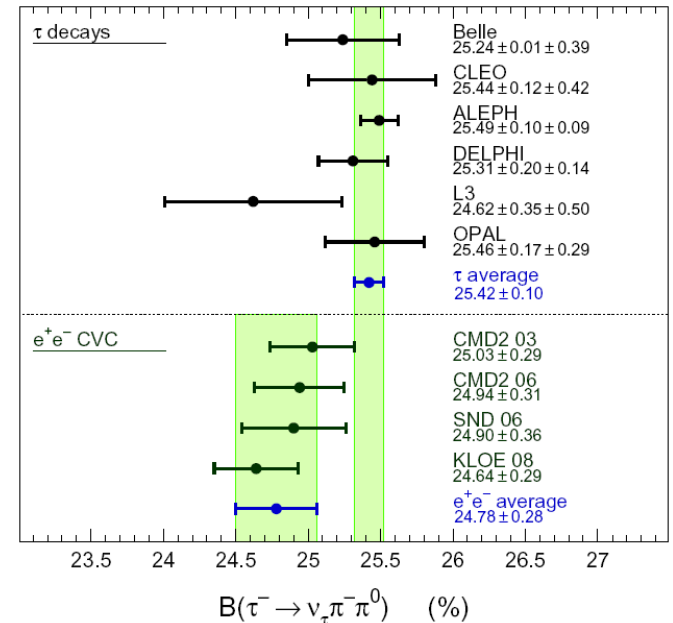


slope...

Global test of spectral functions:  
prediction of  $\tau$  BR using ee data

$$\mathcal{B}_X^{\text{CVC}} = \frac{3 \mathcal{B}_e |V_{ud}|^2}{2 \pi \alpha^2 m_\tau^2} \int_{s_{\min}}^{m_\tau^2} ds s \sigma_{X^0} \left(1 - \frac{s}{m_\tau^2}\right)^2 \left(1 + \frac{2s}{m_\tau^2}\right)$$

$\Rightarrow$  larger disagreement with KLOE



# Goals of the BaBar Analysis

- ❖ Measure  $\sigma[e^+ e^- \rightarrow \pi^+ \pi^- (\gamma)]$  with high accuracy for vacuum polarization calculations, using the ISR method  $e^+ e^- \rightarrow \pi^+ \pi^- \gamma (\gamma)$
  - ❖  $\pi\pi$  channel contributes 73% of  $a_\mu^{\text{had}}$
  - ❖ Dominant uncertainty also from  $\pi\pi$
  - ❖ Also important to increase precision on  $\alpha(M_Z^2)$  (EW tests, ILC)
  - ❖ Present systematic precision of  $e^+e^-$  experiments
    - CMD-2 0.8%      SND 1.5%      in agreement
    - KLOE (ISR from 1.02 GeV) 2005 1.3%      some deviation in shape
    - 2008 0.9%      better agreement
  - ❖ Big advantage of ISR: all mass spectrum covered at once, from threshold to 3 GeV, with same detector and analysis
  - ❖ Measure simultaneously  $\pi^+ \pi^- \gamma (\gamma)$  and  $\mu^+ \mu^- \gamma (\gamma)$
  - ❖ Compare to spectral functions from previous  $e^+ e^-$  data and  $\tau$  decays
- ⇒ aim for a measurement with <1% accuracy (syst. errors at per mil level)

great interest to clarify the situation as magnitude of possible discrepancy with SM is of the order of SUSY contributions with masses of a few 100 GeV

# Analyse faite au LAL

Un travail de longue haleine....

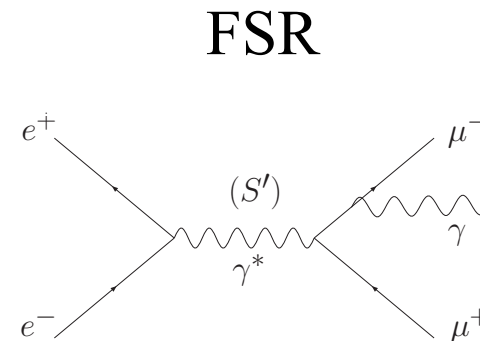
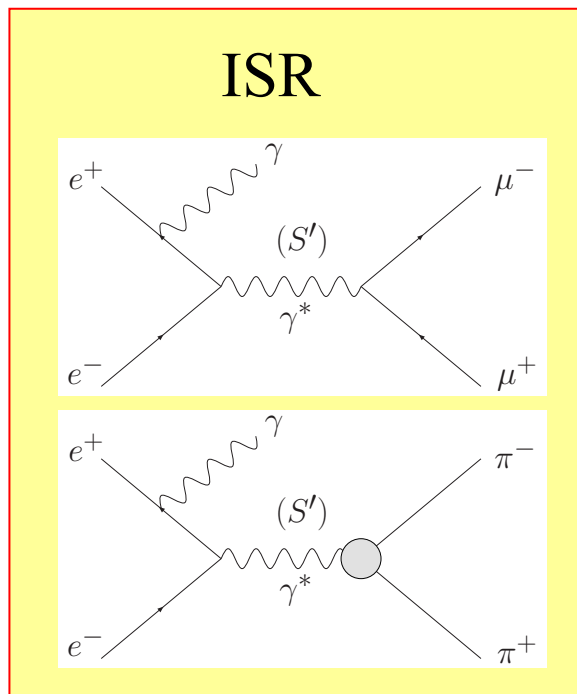
- **Wenfeng Wang** (postdoc): identification  $\pi/\mu/e$   
fits cinématiques  
efficacité tracking
- **Nicolas Arnaud**: identification K
- **Anne-Marie Lutz**: efficacité trigger
- **Liangliang Wang** (thèse co-tutelle 2009): bruits de fond  
analyse finale
- **Bogdan Malaescu** (thèse 2010,  $K^+K^-$ ): unfolding  
outils polarisation du vide
- **MD**

# The Relevant Processes

$e^+ e^- \rightarrow \mu^+ \mu^- \gamma (\gamma)$  and  $\pi^+ \pi^- \gamma (\gamma)$  measured simultaneously

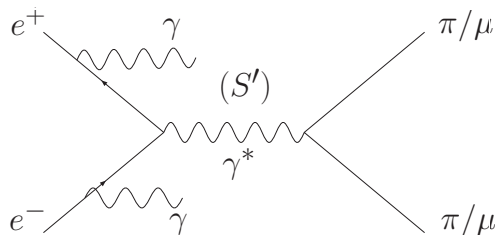
$$x = 2E_\gamma^*/\sqrt{s}$$

$$s' = s(1 - x)$$

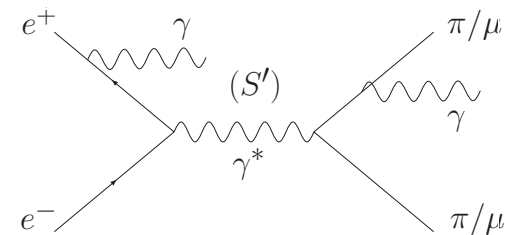


LO FSR negligible for  $\pi\pi$   
at  $s \sim (10.6 \text{ GeV})^2$

**ISR + add. ISR**

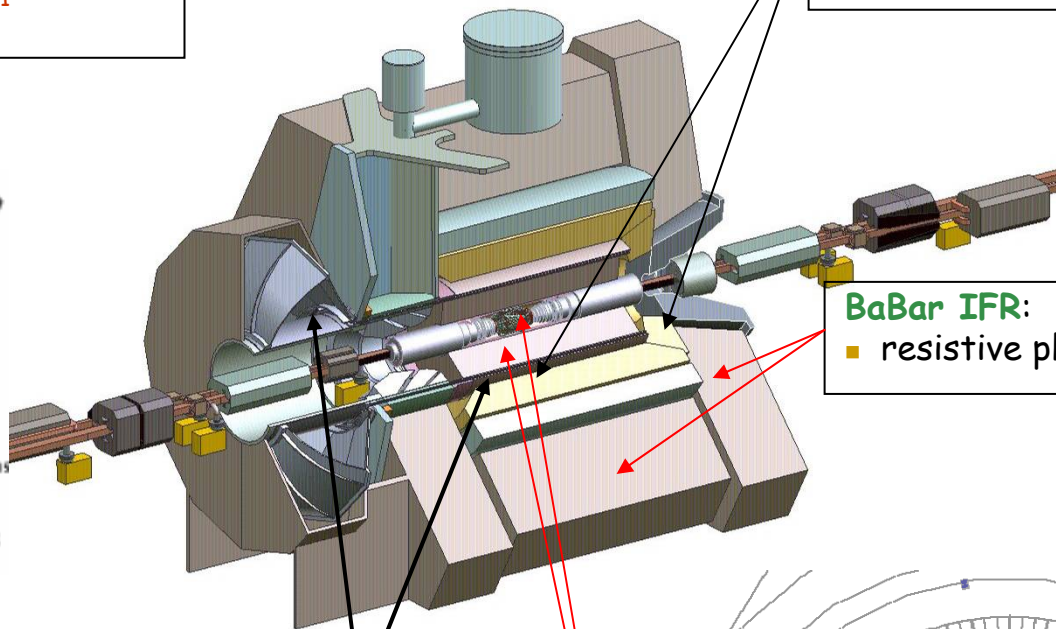
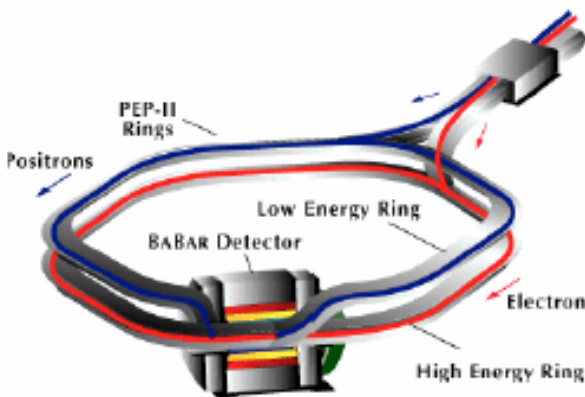


**ISR + add. FSR**



# BaBar / PEP II

- ❖ **PEP-II** is an asymmetric  $e^+e^-$  collider operating at CM energy of  $\Upsilon(4S)$ .
- ❖ Integrated luminosity =  $531 \text{ fb}^{-1}$

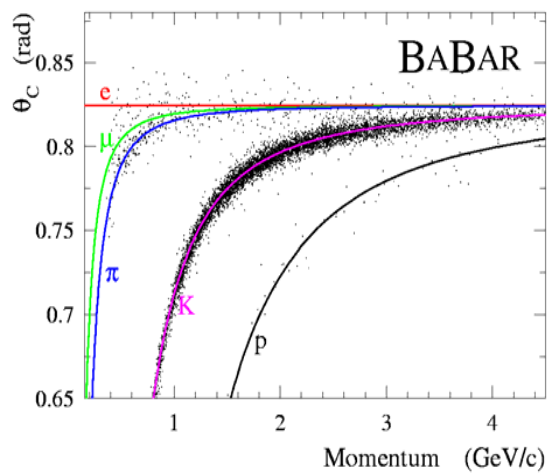


## BaBar EMC:

- 6580 CsI(Tl) crystals, resolution  $\sim 1-2\%$  high E.

## BaBar IFR:

- resistive plate chambers

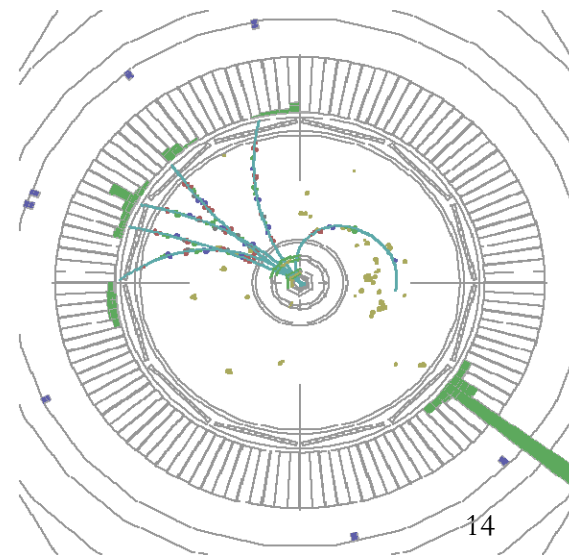


## BaBar DIRC

- particle ID up to  $4-5 \text{ GeV}/c$

## BaBar SVT and DCH

- precision tracking



# Analysis Steps

232 fb<sup>-1</sup> (Y(4S) on-peak & off peak)

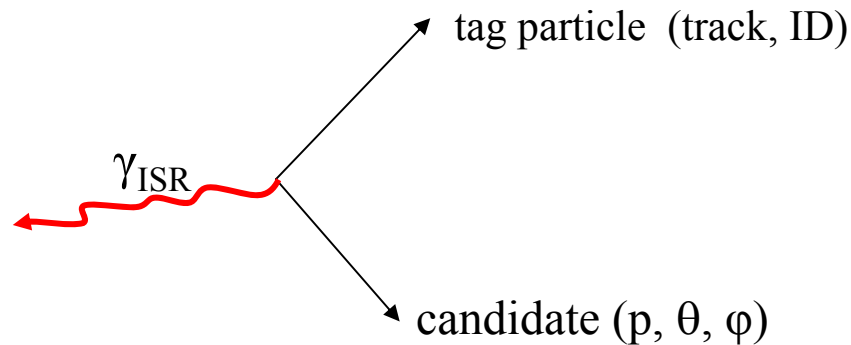
- Measure ratio of  $\pi\pi\gamma(\gamma)$  to  $\mu\mu\gamma(\gamma)$  cross sections to cancel  $ee$  luminosity, additional ISR, vacuum polarization, ISR photon efficiency (otherwise 1-2% syst.)
- ISR photon at large angle in EMC + 2 tracks
  
- Geometrical acceptance (using Monte Carlo simulation)
- All efficiencies measured on data (data/MC corrections)
- Triggers (L1 hardware, L3 software), background-filter efficiencies
- Tracking efficiency
- Particle ID matrix (ID and mis-ID efficiencies):  $\mu$   $\pi$   $K$
- Kinematic fitting
  - reduce non 2-body backgrounds
  - $\chi^2$  cut efficiency: additional radiation (ISR, FSR), secondary interactions
- Unfolding of mass spectra
- Consistency checks for  $\mu\mu$  (QED test, ISR luminosity) and  $\pi\pi$
- Unblinding R  $\Rightarrow$  partial preliminary results (Tau08, Sept. 2008)
- Additional studies and checks
- Final results on  $\pi\pi$  cross section and calculation of dispersion integral

# MC Generators

- Acceptance and efficiencies determined initially from simulation, with data/MC corrections applied
- Large simulated samples, typically  $10 \times$  data, using AfkQed generator
- **AfkQed**: lowest-order (LO) QED with additional radiation:
  - ISR with structure function method,  $\gamma$  assumed collinear to the beams and with limited energy
  - FSR using PHOTOS
- **Phokhara 4.0**: (almost) exact second-order QED matrix element, limited to NLO
- Studies comparing Phokhara and AfkQed at 4-vector level with fast simulation
- QED test with  $\mu\mu\gamma$  ( $\gamma$ ) cross section requires reliable NLO generator
- $\pi\pi(\gamma)$  cross section obtained through  $\pi\pi\gamma / \mu\mu\gamma$  ratio, rather insensitive to detailed description of radiation in MC



# Particle-related Efficiency Measurements



- benefit from pair production for tracking and particle ID
- kinematically constrained events
- efficiency automatically averaged over running periods
- measurement in the same environment as for physics, in fact same events!
- applied to particle ID with  $\pi/K/\mu$  samples, tracking, study of secondary interactions...
- **assumes that efficiencies of the 2 particles are uncorrelated**
- **in practice not true  $\Rightarrow$  study of 2-particle overlap in the detector (trigger, tracking, EMC, IFR) required a large effort to reach per mil accuracies**

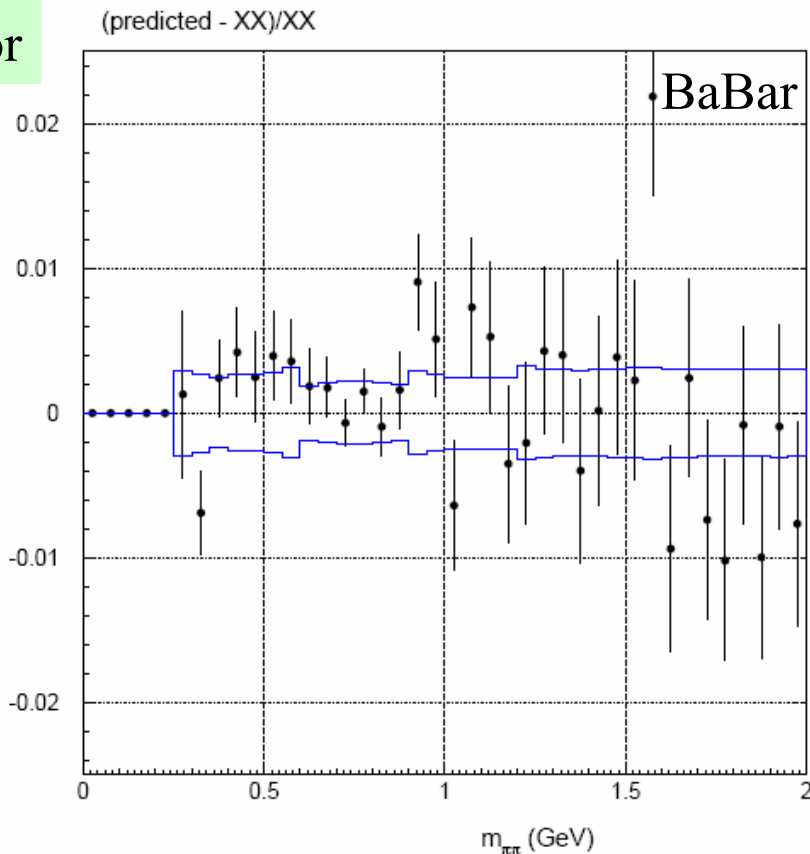
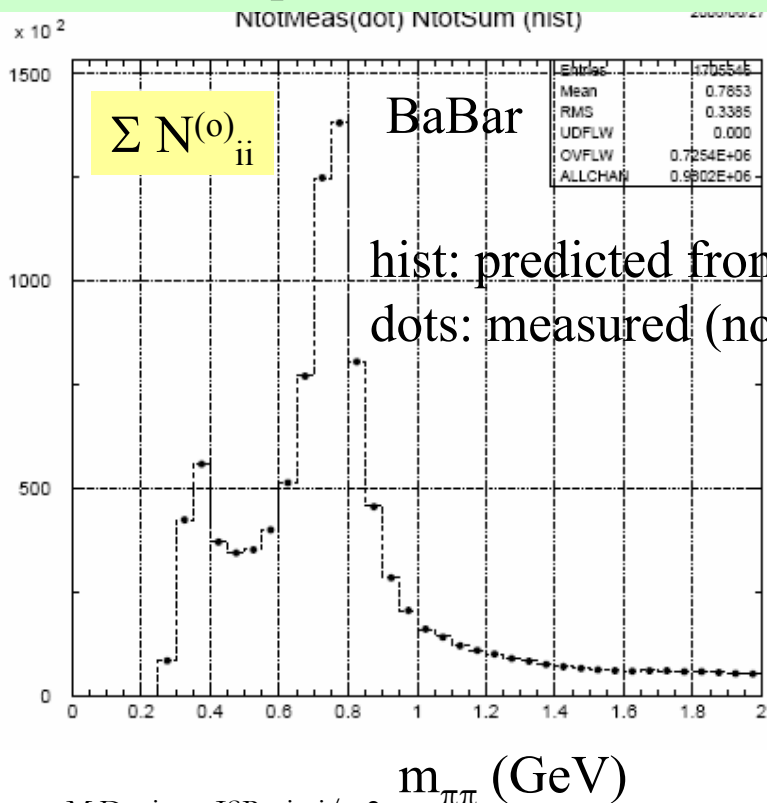
# PID separation and Global Test

$$N_{\pi\pi'} = N_{\mu\mu}^{(0)} \varepsilon_{\mu\mu \rightarrow \pi\pi'} + N_{\pi\pi}^{(0)} \varepsilon_{\pi\pi \rightarrow \pi\pi'} + N_{KK}^{(0)} \varepsilon_{KK \rightarrow \pi\pi'} + N_{ee/\pi\pi'}$$

$$N_{\mu\mu'} = N_{\mu\mu}^{(0)} \varepsilon_{\mu\mu \rightarrow \mu\mu'} + N_{\pi\pi}^{(0)} \varepsilon_{\pi\pi \rightarrow \mu\mu'} + N_{KK}^{(0)} \varepsilon_{KK \rightarrow \mu\mu'}$$

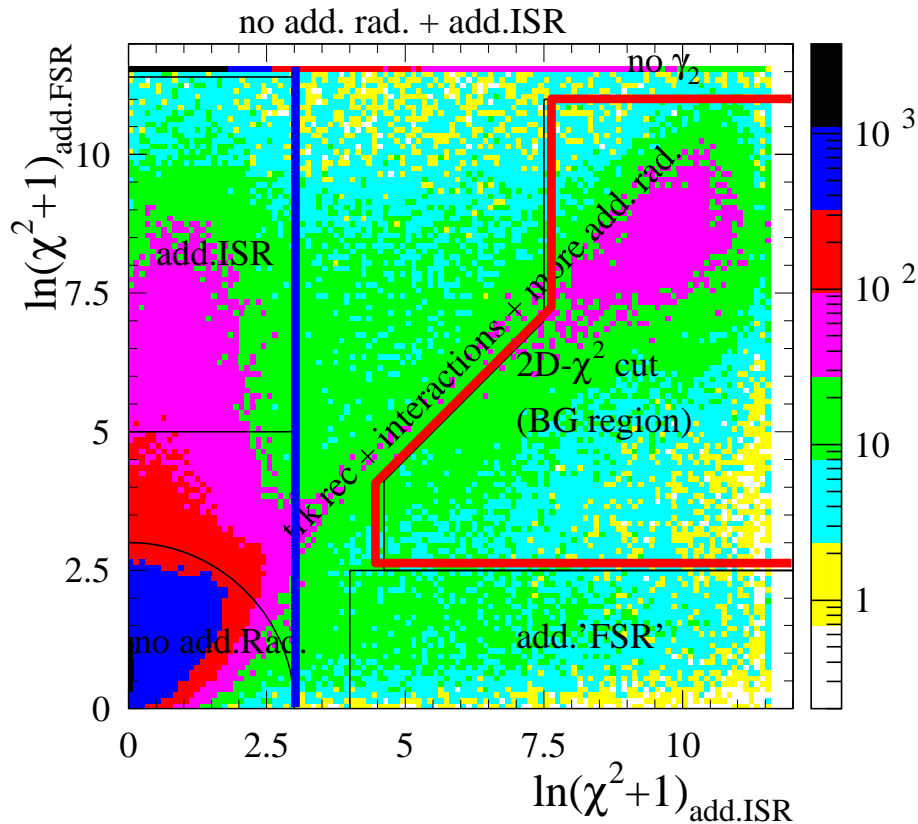
$$N_{KK'} = N_{\mu\mu}^{(0)} \varepsilon_{\mu\mu \rightarrow KK'} + N_{\pi\pi}^{(0)} \varepsilon_{\pi\pi \rightarrow KK'} + N_{KK}^{(0)} \varepsilon_{KK \rightarrow KK'}$$

All 'xx'  $\Rightarrow$  solve for all  $xx^{(0)}$  and compare with no-ID spectrum and estimated syst. error



# Kinematic Fitting

$\pi\pi\gamma(\gamma)$



- Two kinematic fits to  $X X \gamma_{\text{ISR}} \gamma_{\text{add}}$  (ISR photon defined as highest energy)

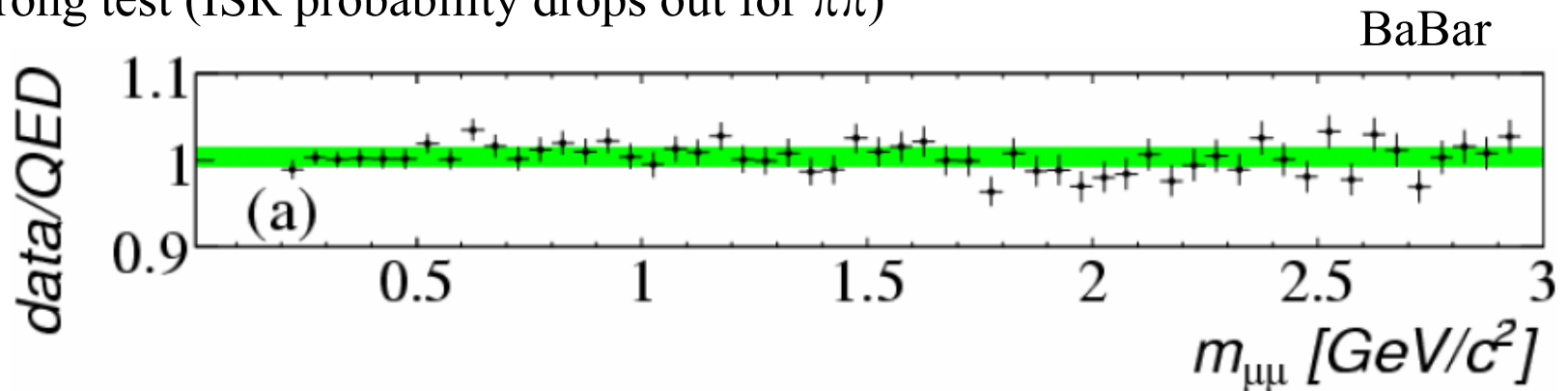
Add. ISR fit:  $\gamma_{\text{add}}$  assumed along beams

Add. 'FSR' if  $\gamma_{\text{add}}$  detected

- First analysis to measure cross section with additional photons (NLO)
- Loose  $\chi^2$  cut (outside BG region in plot) for  $\mu\mu$  and  $\pi\pi$  in central  $\rho$  region
- Tight  $\chi^2$  cut ( $\ln(\chi^2+1) < 3$ ) for  $\pi\pi$  in  $\rho$  tail region
- $q \bar{q}$  and multi-hadronic ISR background from MC samples + normalization from data using signals from  $\pi^0 \rightarrow \gamma_{\text{ISR}} \gamma$  ( $q\bar{q}$ ), and  $\omega$  and  $\phi$  ( $\pi\pi\pi^0\gamma$ )

# QED Test with $\mu\mu\gamma$ sample

- absolute comparison of  $\mu\mu$  mass spectra in data and in simulation
- simulation corrected for data/MC efficiencies
- AfkQed corrected for incomplete NLO using Phokhara
- strong test (ISR probability drops out for  $\pi\pi$ )



$$\frac{\sigma_{\mu\mu\gamma(\gamma)}^{data}}{\sigma_{\mu\mu\gamma(\gamma)}^{NLO QED}} = 1 + (4.0 \pm 1.9 \pm 5.5 \pm 9.4) 10^{-3} \quad (0.2 - 3 \text{ GeV})$$

ISR  $\gamma$  efficiency 3.4 syst.  
trig/track/PID 4.0

BaBar ee luminosity

# Obtaining the $\pi\pi(\gamma)$ cross section

$$\frac{dN_{\pi\pi\gamma(\gamma)}}{d\sqrt{s'}} = \frac{dL_{ISR}^{eff}}{d\sqrt{s'}} \epsilon_{\pi\pi\gamma(\gamma)}(\sqrt{s'}) \sigma_{\pi\pi(\gamma)}^0(\sqrt{s'})$$

Unfolded spectrum

Acceptance from MC + data/MC corrections

Effective ISR luminosity from  $\mu\mu\gamma(\gamma)$  analysis (similar equation + QED)

$\pi\pi$  mass spectrum unfolded (Malaescu arXiv:0907-3791) for detector response

Additional ISR almost cancels in the procedure ( $\pi\pi\gamma(\gamma) / \mu\mu\gamma(\gamma)$  ratio)

Correction  $(2.5 \pm 1.0) 10^{-3} \Rightarrow \pi\pi$  cross section does not rely on accurate description of NLO in the MC generator

ISR luminosity from  $\mu\mu\gamma$  in 50-MeV energy intervals  
(small compared to variation of efficiency corrections)

# Systematic uncertainties

$\sqrt{s}$  intervals (GeV)

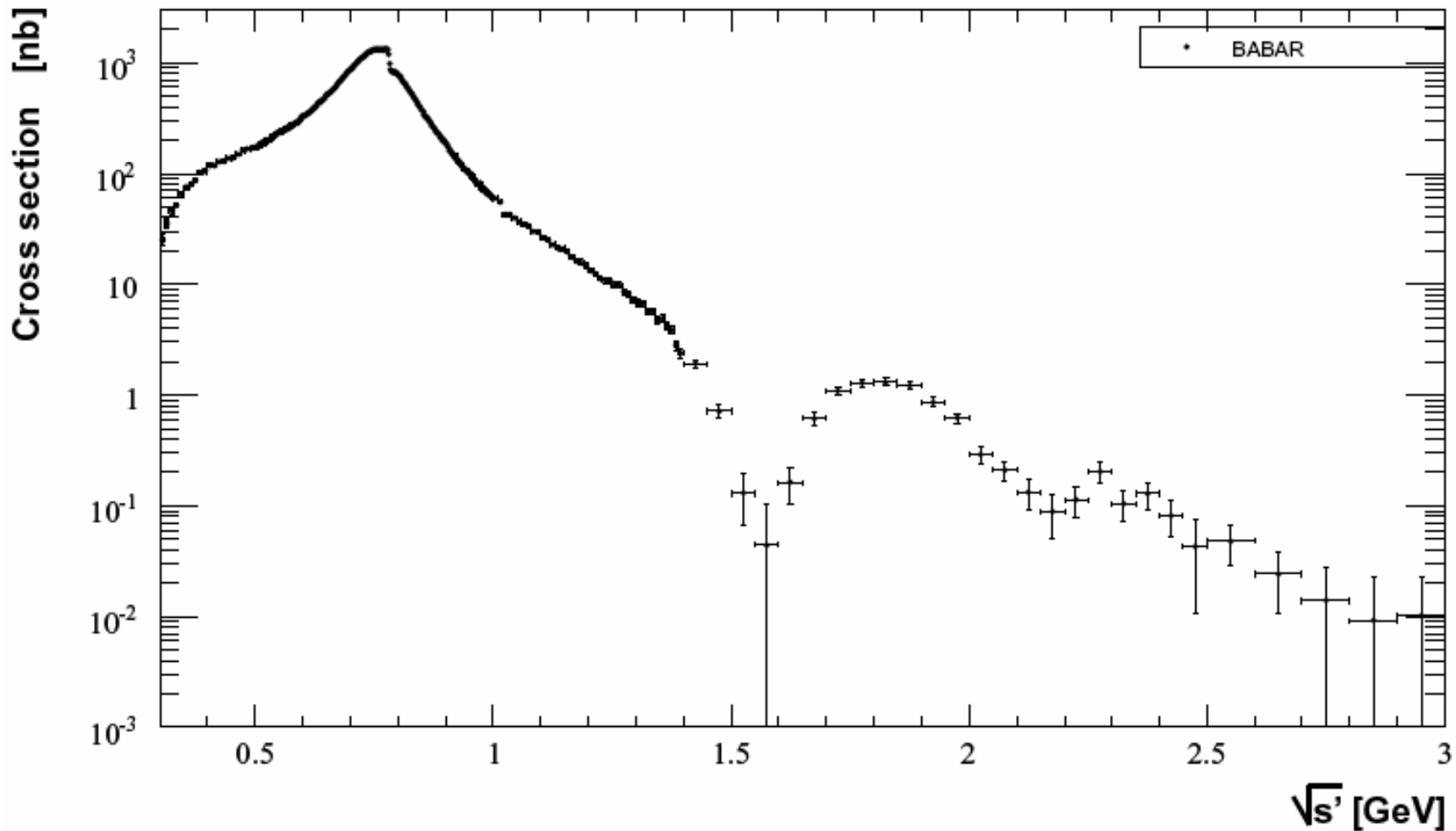
errors in  $10^{-3}$

| sources                    | 0.3-0.4 | 0.4-0.5 | 0.5-0.6 | 0.6-0.9 | 0.9-1.2 | 1.2-1.4 | 1.4-2.0 | 2.0-3.0 |
|----------------------------|---------|---------|---------|---------|---------|---------|---------|---------|
| trigger/ filter            | 5.3     | 2.7     | 1.9     | 1.0     | 0.5     | 0.4     | 0.3     | 0.3     |
| tracking                   | 3.8     | 2.1     | 2.1     | 1.1     | 1.7     | 3.1     | 3.1     | 3.1     |
| $\pi$ -ID                  | 10.1    | 2.5     | 6.2     | 2.4     | 4.2     | 10.1    | 10.1    | 10.1    |
| background                 | 3.5     | 4.3     | 5.2     | 1.0     | 3.0     | 7.0     | 12.0    | 50.0    |
| acceptance                 | 1.6     | 1.6     | 1.0     | 1.0     | 1.6     | 1.6     | 1.6     | 1.6     |
| kinematic fit ( $\chi^2$ ) | 0.9     | 0.9     | 0.3     | 0.3     | 0.9     | 0.9     | 0.9     | 0.9     |
| correl $\mu\mu$ ID loss    | 3.0     | 2.0     | 3.0     | 1.3     | 2.0     | 3.0     | 10.0    | 10.0    |
| $\pi\pi/\mu\mu$ cancel.    | 2.7     | 1.4     | 1.6     | 1.1     | 1.3     | 2.7     | 5.1     | 5.1     |
| unfolding                  | 1.0     | 2.7     | 2.7     | 1.0     | 1.3     | 1.0     | 1.0     | 1.0     |
| ISR luminosity             | 3.4     | 3.4     | 3.4     | 3.4     | 3.4     | 3.4     | 3.4     | 3.4     |
| sum (cross section)        | 13.8    | 8.1     | 10.2    | 5.0     | 6.5     | 13.9    | 19.8    | 52.4    |

Dominated by particle ID ( $\pi$ -ID, correlated  $\mu\mu \rightarrow \pi\pi$ ,  $\mu$ -ID in ISR luminosity)

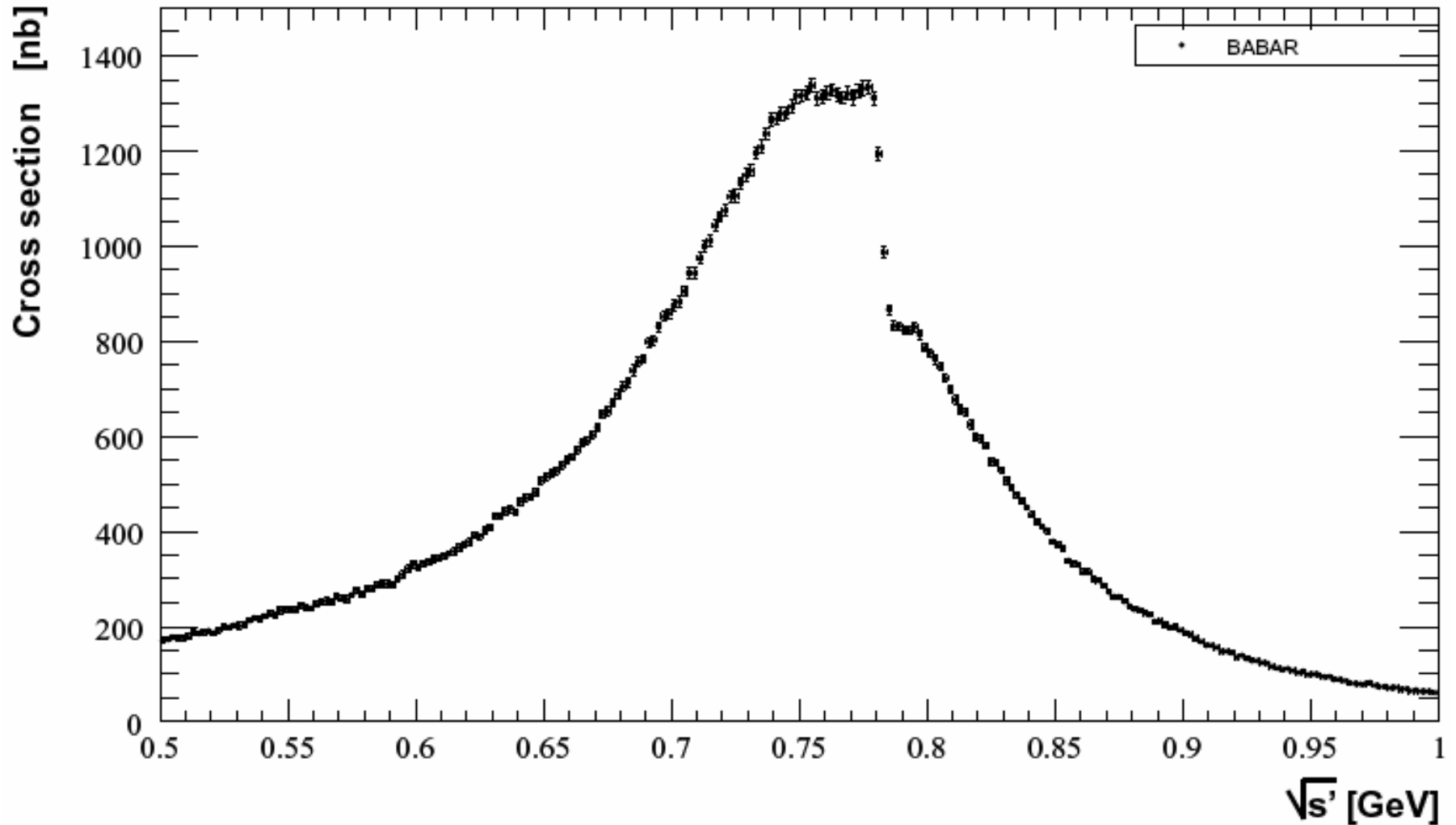
# BaBar results (arXiv:0908.3589)

$e^+ e^- \rightarrow \pi^+ \pi^- (\gamma)$     bare (no VP) cross section    diagonal errors stat+syst



# BaBar results in $\rho$ region

2-MeV energy intervals





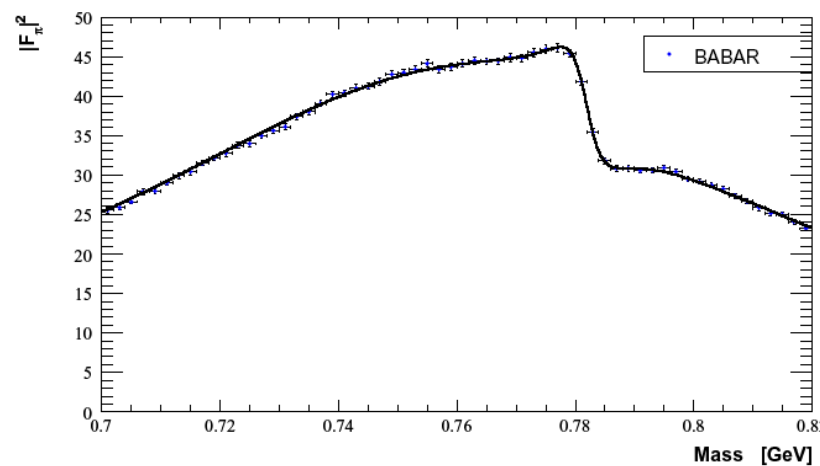
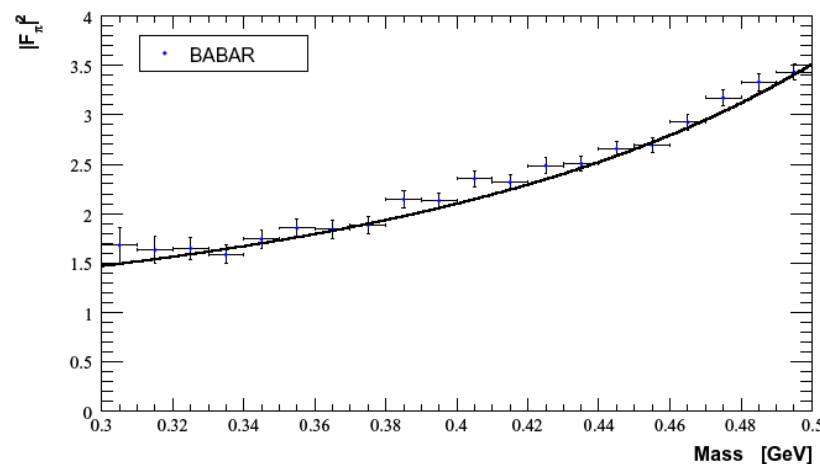
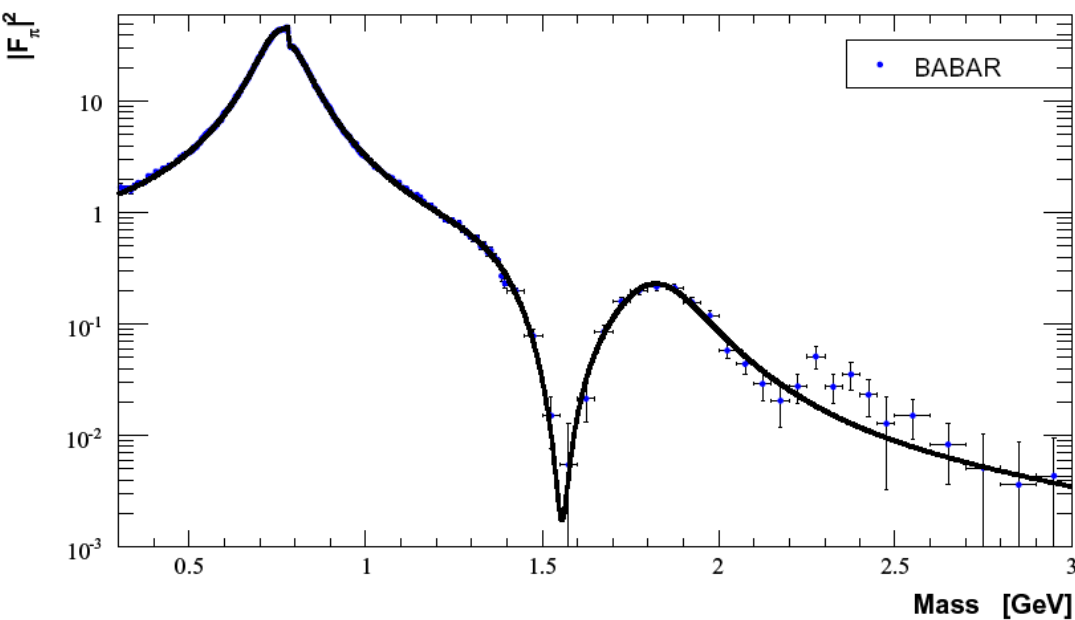
# VDM fit of the pion form factor

$$F_\pi(s) = \frac{BW_\rho^{GS}(s, m_\rho, \Gamma_\rho) \frac{1 + \alpha BW_\omega^{KS}(s, m_\omega, \Gamma_\omega)}{1 + \alpha} + \beta BW_{\rho'}^{GS}(s, m_{\rho'}, \Gamma_{\rho'}) + \gamma BW_{\rho''}^{GS}(s, m_{\rho''}, \Gamma_{\rho''})}{1 + \beta + \gamma}$$

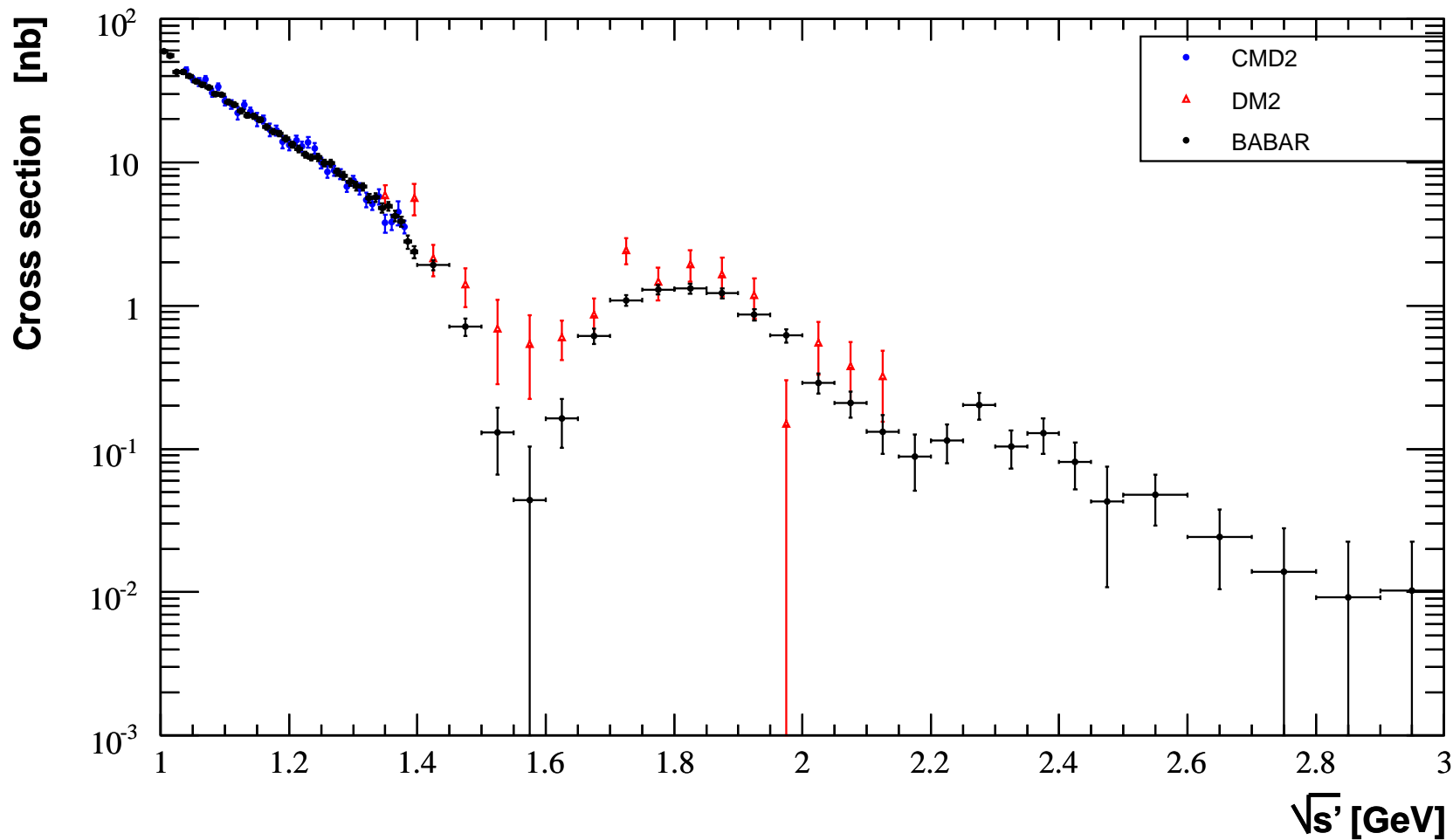
$$|F_\pi|^2(s') = \frac{3s'}{\pi\alpha^2(0)\beta_\pi^3} \sigma_{\pi\pi}(s')$$

$$\sigma_{\pi\pi}(s') = \frac{\sigma_{\pi\pi(\gamma)}^0(s')}{1 + \frac{\alpha}{\pi}\eta(s')} \left( \frac{\alpha(s')}{\alpha(0)} \right)^2$$

add. FSR       $\alpha$  Running (VP)

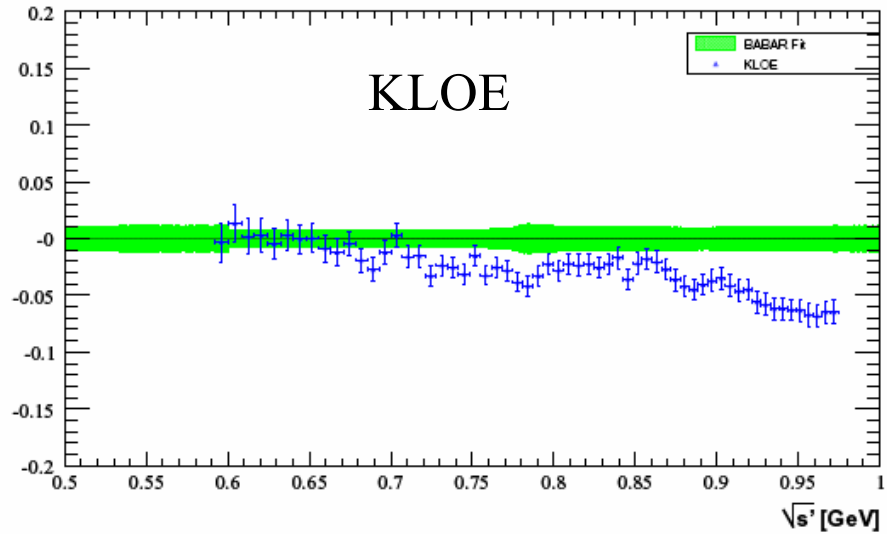
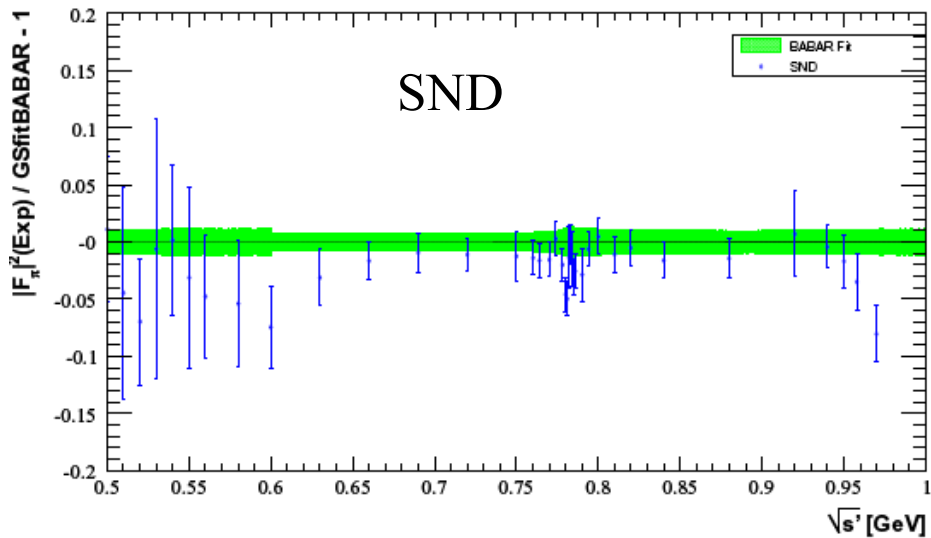
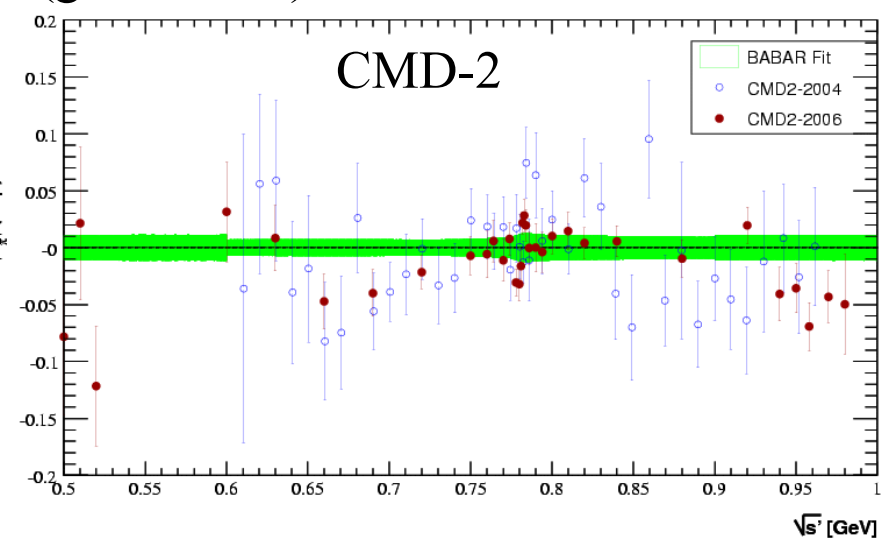
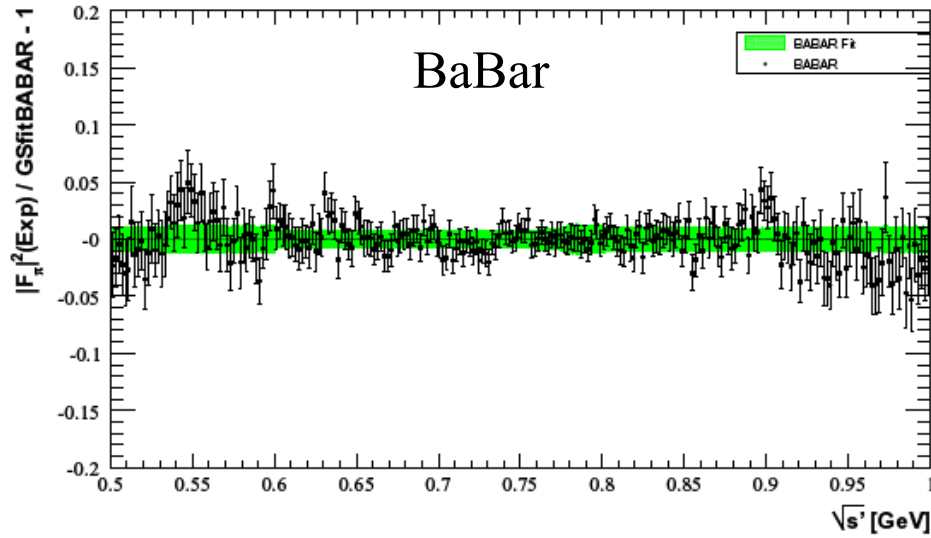


# BaBar vs. other experiments at larger mass

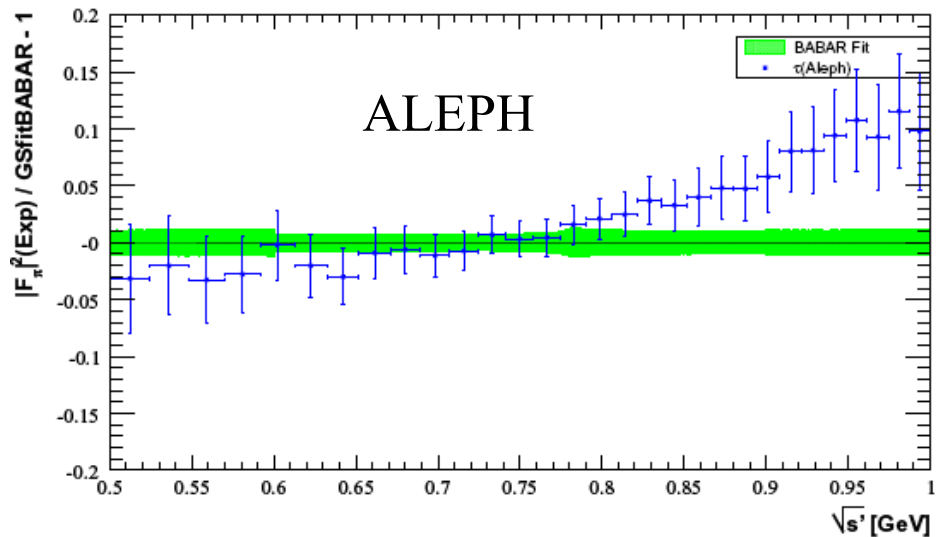


# BaBar vs. other ee data (0.5-1.0 GeV)

direct relative comparison of cross sections with BaBar fit (stat + syst errors included)  
(green band)



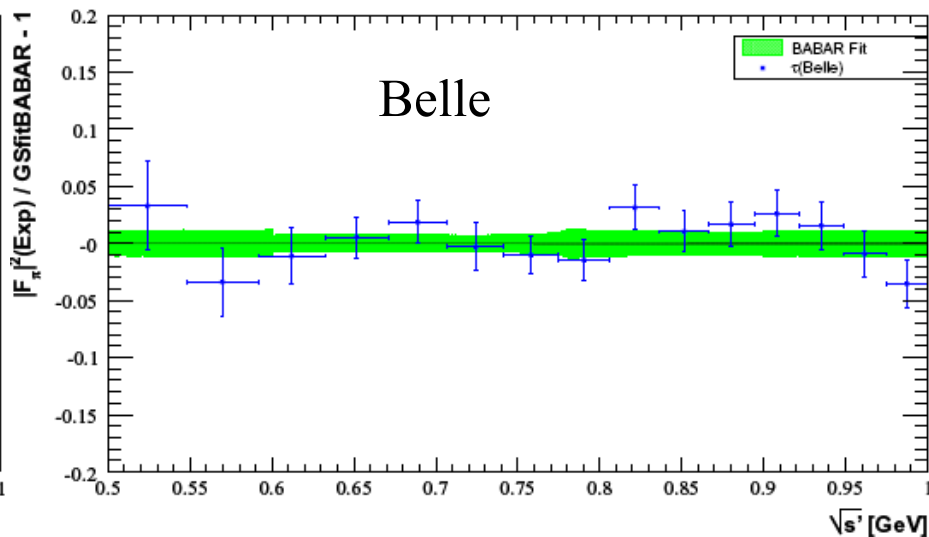
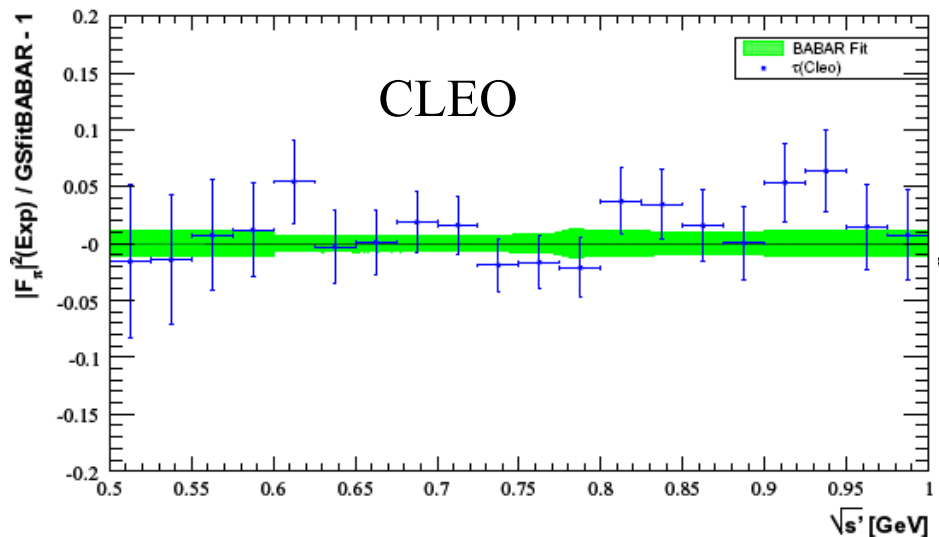
# BaBar vs. IB-corrected $\tau$ data (0.5-1.0 GeV)



relative comparison w.r.t. BaBar of isospin-breaking corrected  $\tau$  spectral functions

IB corrections: radiative corr.,  $\pi$  masses,  $\rho$ - $\omega$  interference,  $\rho$  masses/widths

each  $\tau$  data normalized to its own BR



# Computing $a_{\mu}^{\pi\pi}$

$$a_{\mu}^{\pi\pi(\gamma),LO} = \frac{1}{4\pi^3} \int_{4m_{\pi}^2}^{\infty} ds K(s) \sigma_{\pi\pi(\gamma)}^0(s),$$

where  $K(s)$  is the QED kernel,

$$K(s) = x^2 \left(1 - \frac{x^2}{2}\right) + (1+x)^2 \left(1 + \frac{1}{x^2}\right) \left[ \ln(1+x) - x + \frac{x^2}{2} \right] + x^2 \frac{1+x}{1-x} \ln x,$$

with  $x = (1 - \beta_{\mu})/(1 + \beta_{\mu})$  and  $\beta_{\mu} = (1 - 4m_{\pi}^2/s)^{1/2}$ .

| $m_{\pi\pi}$ range (GeV) | $a_{\mu}^{\pi\pi(\gamma),LO}$ BABAR |
|--------------------------|-------------------------------------|
| 0.28–0.30                | $0.55 \pm 0.01 \pm 0.01$            |
| 0.30–0.50                | $57.62 \pm 0.63 \pm 0.55$           |
| 0.50–1.00                | $445.94 \pm 2.10 \pm 2.51$          |
| 1.00–1.80                | $9.97 \pm 0.10 \pm 0.09$            |
| 0.28–1.80                | $514.09 \pm 2.22 \pm 3.11$          |

( $\times 10^{-10}$ )

0.28–1.8 (GeV)

**BABAR**

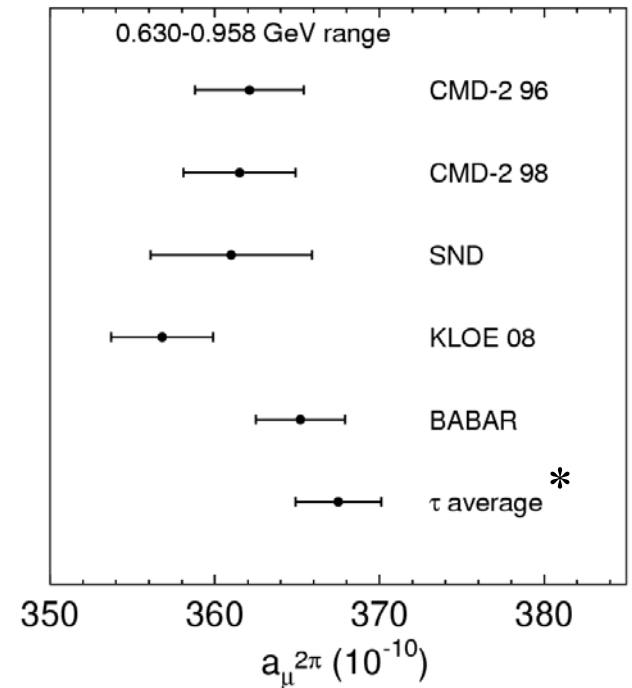
$514.1 \pm 3.8$

previous  $e^+e^-$  combined

$503.5 \pm 3.5$  \*

$\tau$  combined

$515.2 \pm 3.5$  \*



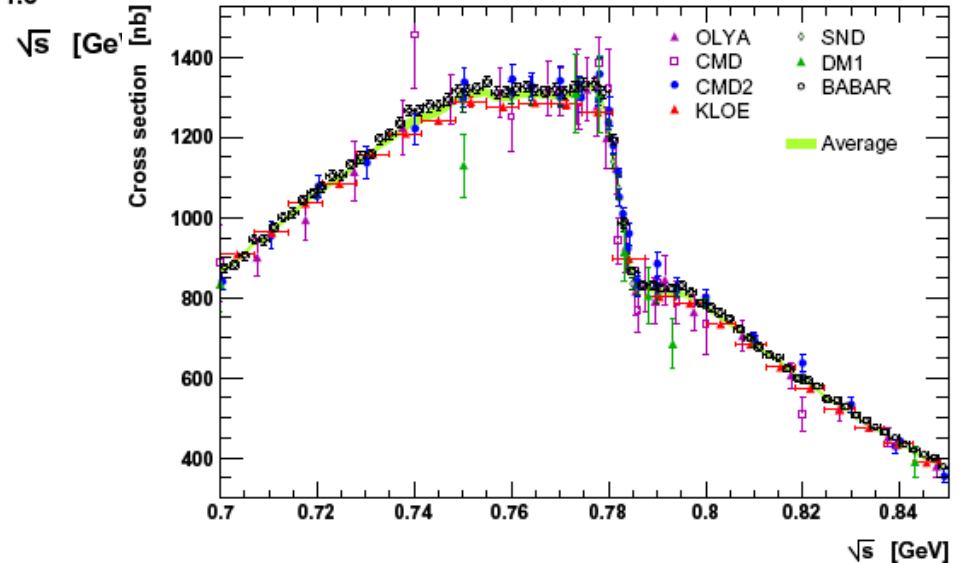
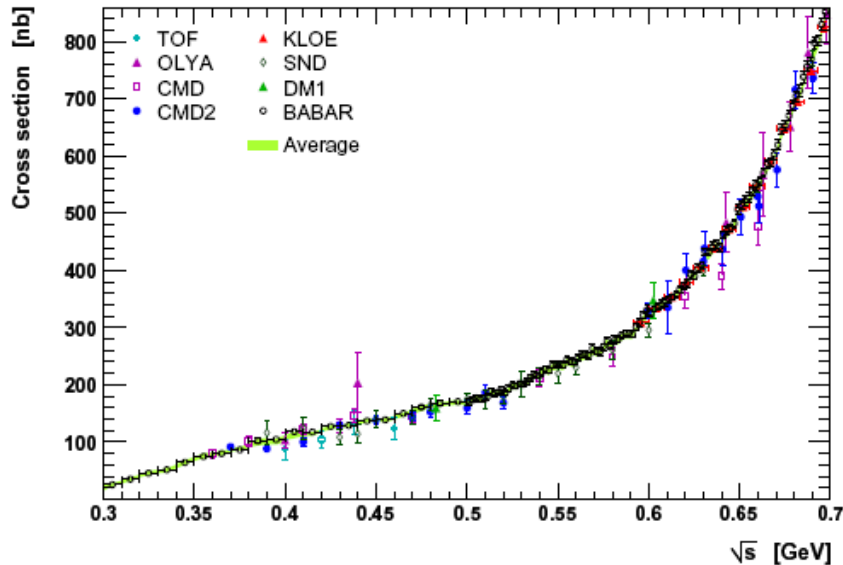
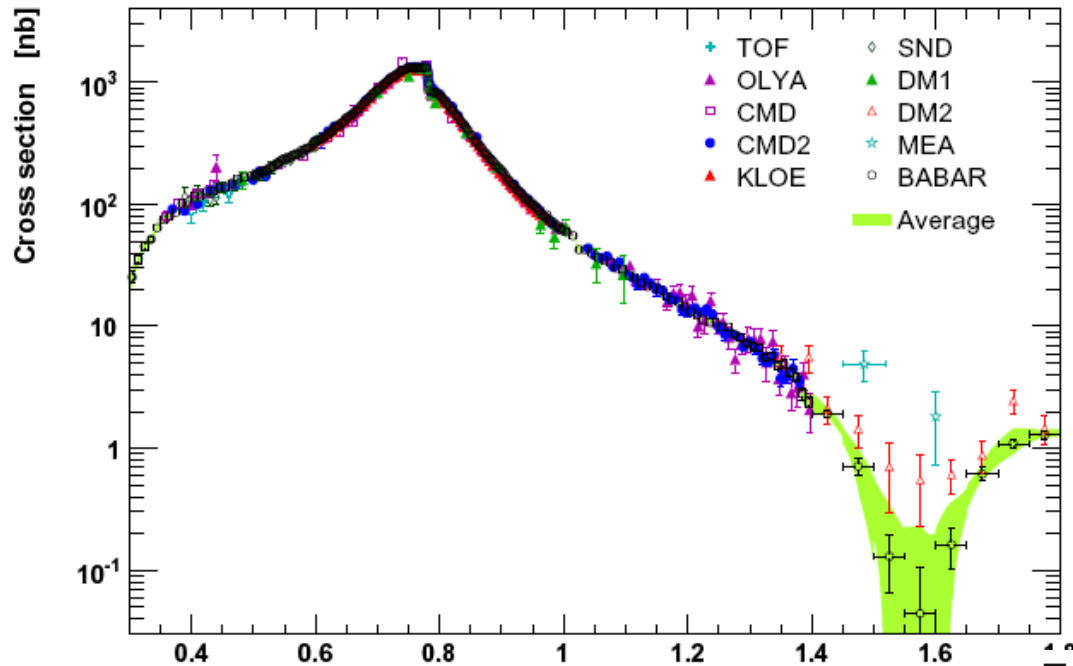
\* arXiv:0906-5443 MD et al.

# Including BaBar in the $e^+e^-$ Combination

arXiv: 0908.4300

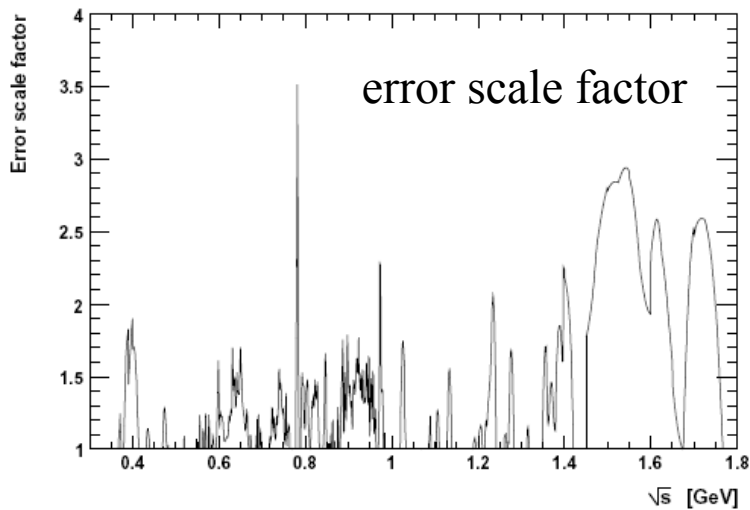
MD-Höcker-Malaescu-Yuan-Zhang

Improved procedure and software (HVPTools) for combining cross section data with arbitrary point spacing/binning

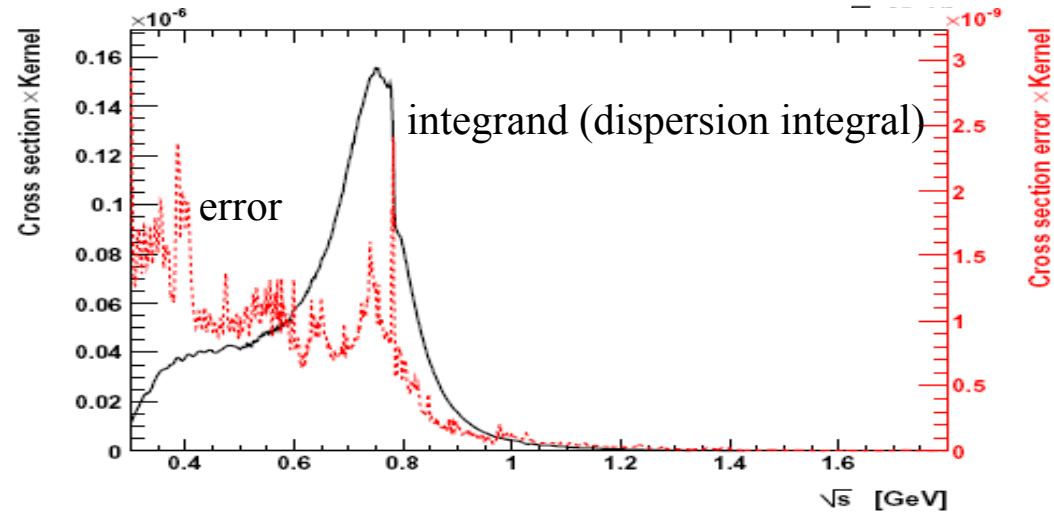
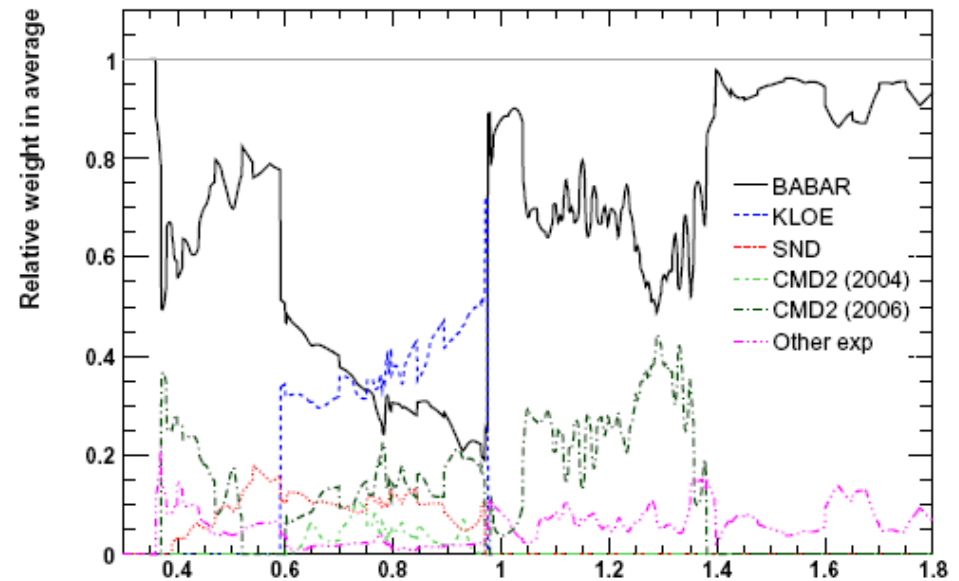


# Obtaining the average cross section

- local weighted average performed
- full covariance matrices
- local  $\chi^2$  used for error rescaling
- average dominated by BaBar and KLOE, BaBar covering full range



relative weights



# Other hadronic contributions

from MD-Eidelman-Hoecker-Zhang (2006)

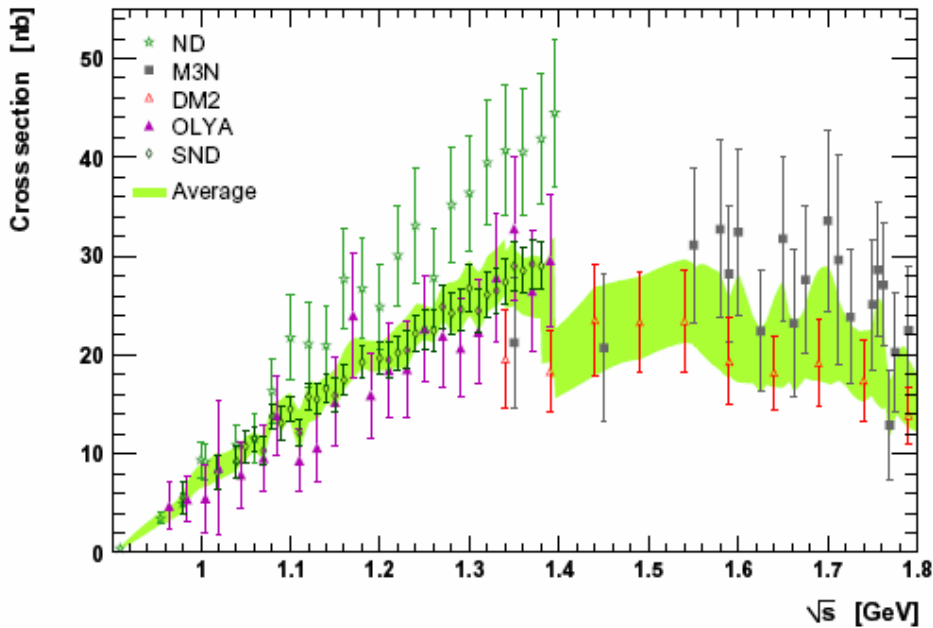
| Modes                          | Energy [GeV]   | $e^+e^-$                            | $\tau$                                |
|--------------------------------|----------------|-------------------------------------|---------------------------------------|
| $\pi^+\pi^-2\pi^0$             | $2m_\pi - 1.8$ | $16.8 \pm 1.3 \pm 0.2_{\text{rad}}$ | $21.4 \pm 1.3 \pm 0.6_{\text{SU}(2)}$ |
| $2\pi^+2\pi^- (+\text{BaBar})$ | $2m_\pi - 1.8$ | $13.1 \pm 0.4 \pm 0.0_{\text{rad}}$ | $12.3 \pm 1.0 \pm 0.4_{\text{SU}(2)}$ |
| $\omega (782)$                 | $0.3 - 0.81$   | $38.0 \pm 1.0 \pm 0.3_{\text{rad}}$ | —                                     |
| $\phi (1020)$                  | $1.0 - 1.055$  | $35.7 \pm 0.8 \pm 0.2_{\text{rad}}$ | —                                     |
| Other excl. (+BaBar)           | $2m_\pi - 1.8$ | $24.3 \pm 1.3 \pm 0.2_{\text{rad}}$ | —                                     |
| $J/\psi, \psi(2S)$             | $3.08 - 3.11$  | $7.4 \pm 0.4 \pm 0.0_{\text{rad}}$  | —                                     |
| $R [\text{QCD}]$               | $1.8 - 3.7$    | $33.9 \pm 0.5_{\text{theo}}$        | —                                     |
| $R [\text{data}]$              | $3.7 - 5.0$    | $7.2 \pm 0.3 \pm 0.0_{\text{rad}}$  | —                                     |
| $R [\text{QCD}]$               | $5.0 - \infty$ | $9.9 \pm 0.2_{\text{theo}}$         | —                                     |

$\Rightarrow$  another large long-standing discrepancy in the  $\pi^+\pi^-2\pi^0$  channel !

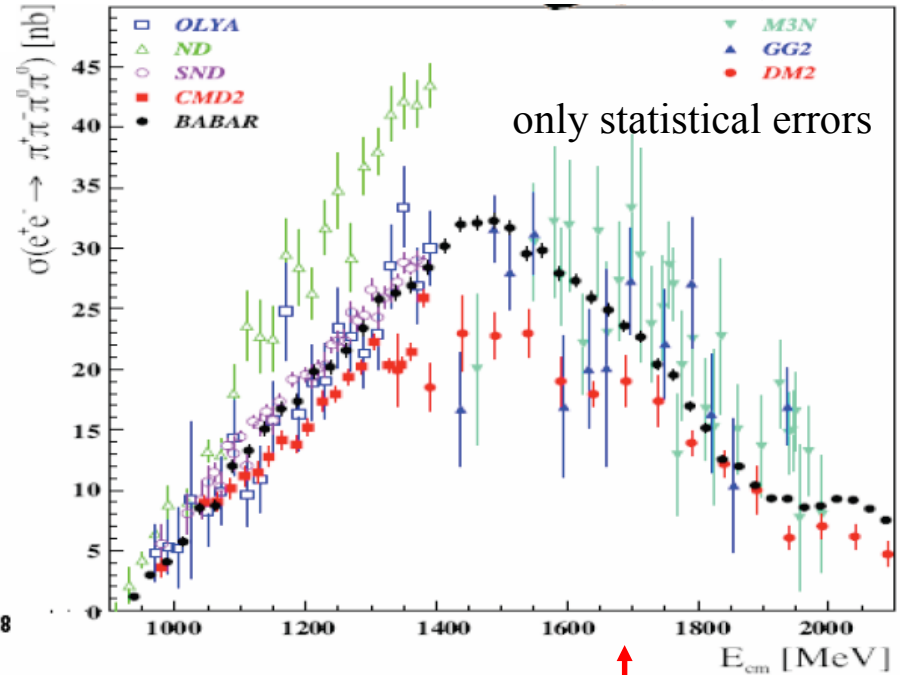


# The Problematic $2\pi 2\pi^0$ Contribution

ee data used now (CMD2 discarded)

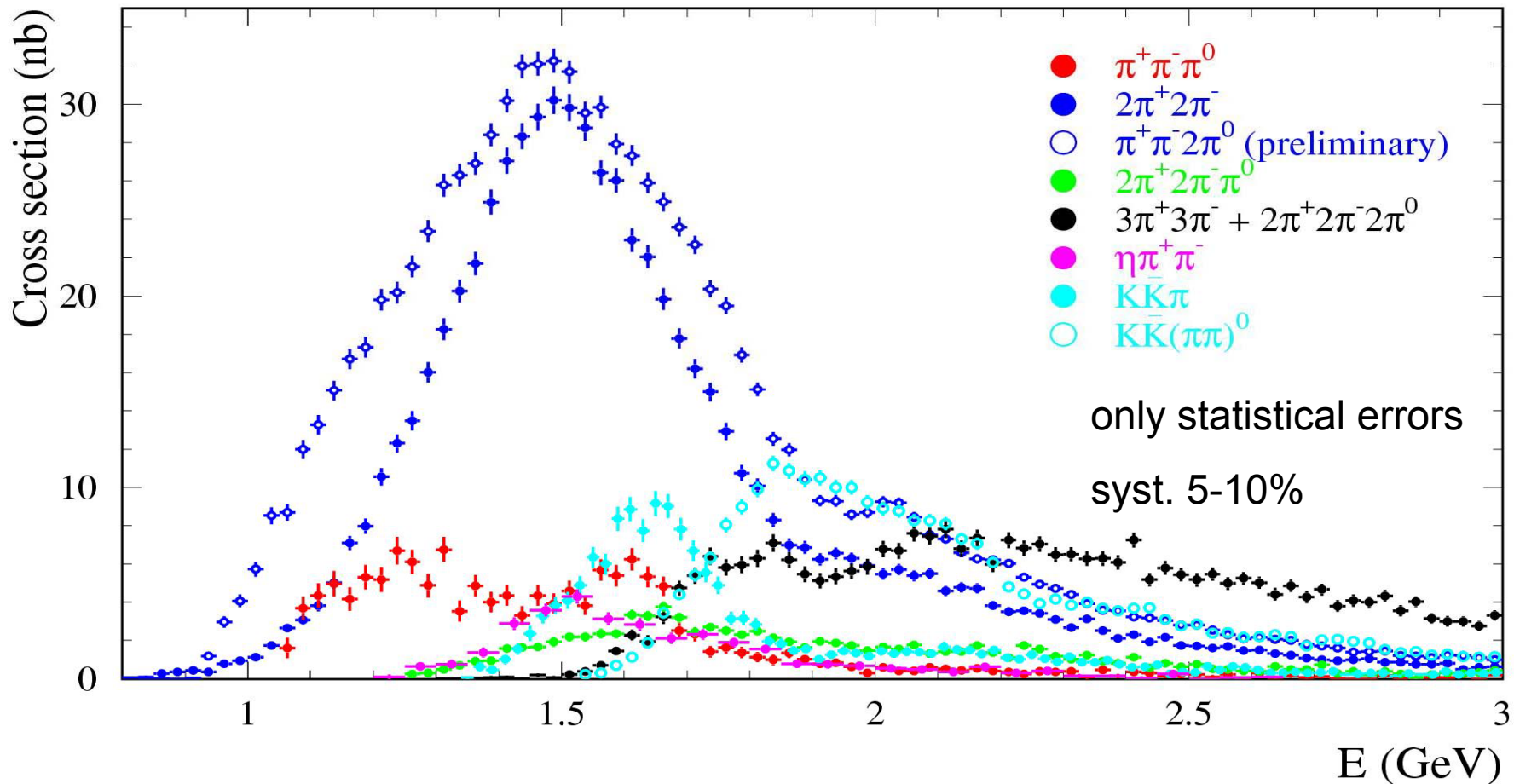


preliminary BaBar data:  
A. Petzold, EPS-HEP (2007)



|                  |                |                                       |
|------------------|----------------|---------------------------------------|
| old contribution | $16.8 \pm 1.3$ |                                       |
| update           | $17.6 \pm 1.7$ | probably still underestimated (BaBar) |
| $\tau$           | $21.4 \pm 1.4$ |                                       |

# BaBar Multi-hadronic Results



Still more channels under analysis:  $K^+K^-$ ,  $K\bar{K}\pi\pi$  with  $K^0$

# Where are we?

- including BaBar  $2\pi$  results in the  $e^+e^-$  combination + estimate of hadronic LBL contribution (Prades-de Rafael-Vainhstein, 2009) yields

$$a_\mu^{\text{SM}}[e^+e^-] = (11\,659\,183.4 \pm 4.1 \pm 2.6 \pm 0.2) 10^{-10}$$

HVP LBL EW ( $\pm 4.9$ )

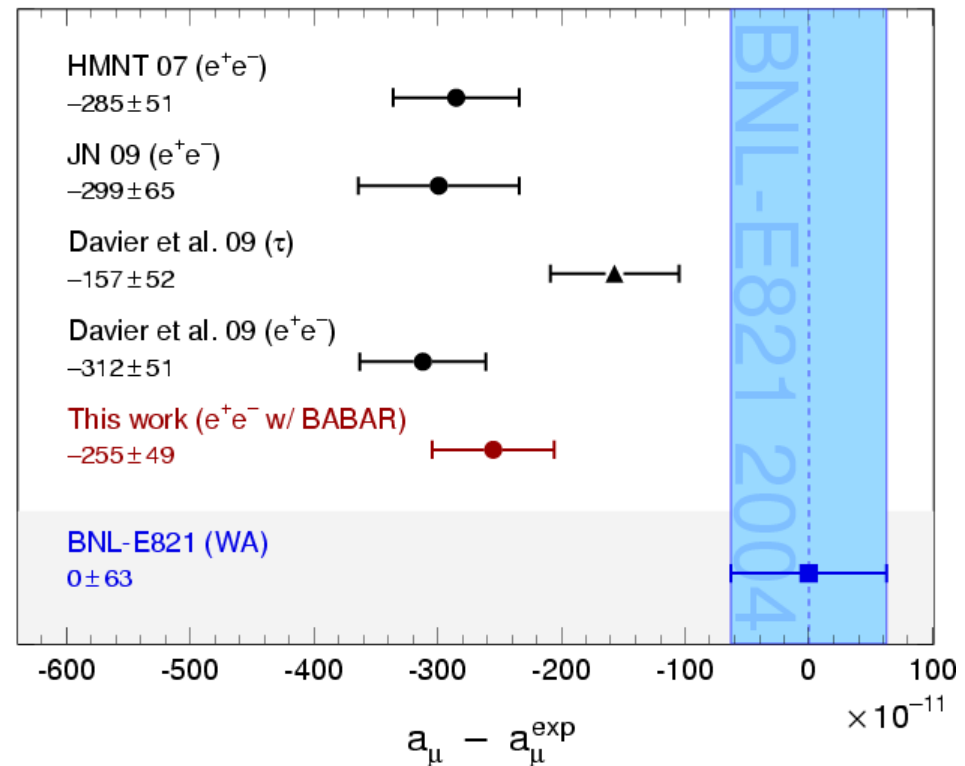
- E-821 updated result

$$11\,659\,208.9 \pm 6.3$$

- deviation (ee)  $25.5 \pm 8.0$   
( $3.2 \sigma$ )

- updated  $\tau$  analysis  
+Belle +revisited IB corrections

- deviation ( $\tau$ )  $15.7 \pm 8.2$   
( $1.9 \sigma$ )



# Discussion

- BaBar  $2\pi$  data complete and the most accurate, but expected precision improvement on the average not reached because of discrepancy with KLOE
- however, previous  $\tau/ee$  disagreement strongly reduced  
2.9 $\sigma$  (2006)  $\rightarrow$  2.4 $\sigma$  ( $\tau$  update)  $\rightarrow$  1.5 $\sigma$  (including BaBar)
- a range of values for the deviation from the SM can be obtained, depending on the  $2\pi$  data used:

|               |              |
|---------------|--------------|
| BaBar         | 2.4 $\sigma$ |
| all ee        | 3.2 $\sigma$ |
| all ee -BaBar | 3.7 $\sigma$ |
| all ee -KLOE  | 2.9 $\sigma$ |
| $\tau$        | 1.9 $\sigma$ |

- all approaches yield a deviation, but SM test limited by systematic effects not well accounted for in the experimental analyses (ee) and/or the corrections to  $\tau$  data
- at the moment some evidence for a deviation ( $\sim 3\sigma$ ), but not sufficient to establish a contribution from new physics. However valuable information if NP found at LHC

# Perspectives

- **first priority is a clarification of the BaBar/KLOE discrepancy:**
  - origin of the ‘slope’ (was very pronounced with the 2004 KLOE results, reduced now with the 2008 results)
  - normalization difference on  $\rho$  peak (most direct effect on  $a_\mu$ )
  - Novosibirsk results in-between, closer to BaBar
  - slope also seen in KLOE/ $\tau$  comparison; BaBar agrees with  $\tau$
- further checks of the KLOE results are possible: as method is based on MC simulation for ISR and additional ISR/ISR probabilities  $\Rightarrow$  **long-awaited test with  $\mu\mu\gamma$  analysis**
- contribution from multi-hadronic channels will continue to be updated with more results forthcoming from BaBar, **particularly  $2\pi 2\pi^0$**
- more ee data expected from VEPP-2000 in Novosibirsk
- experimental error of E-821 direct  $a_\mu$  measurement is a limitation, already now
  - $\Rightarrow$  new proposal submitted to Fermilab to improve accuracy by a factor 4
  - $\Rightarrow$  project at JPARC

# Conclusions

- BaBar analysis of  $\pi\pi$  and  $\mu\mu$  ISR processes completed
- Precision goal has been achieved: 0.5% in  $\rho$  region (0.6-0.9 GeV)
- Absolute  $\mu\mu$  cross section agrees with NLO QED within 1.1%
- $ee \rightarrow \pi\pi(\gamma)$  cross section very insensitive to MC generator
- full range of interest covered from 0.3 to 3 GeV
- Structures observed in pion form factor at large masses
- Comparison with data from earlier experiments
  - fair agreement with CMD-2 and SND, poor with KLOE
  - agreement with  $\tau$  data
- Contribution to  $a_\mu$  from BaBar is  $(514.1 \pm 2.2 \pm 3.1) \times 10^{-10}$  in 0.28-1.8 GeV
- BaBar result has comparable accuracy (0.7%) to combined previous results
- Deviation between BNL measurement and theory prediction reduced using BaBar  $\pi\pi$  data

$$a_\mu [\text{exp}] - a_\mu [\text{SM}] = (19.8 \pm 8.4) \times 10^{-10}$$

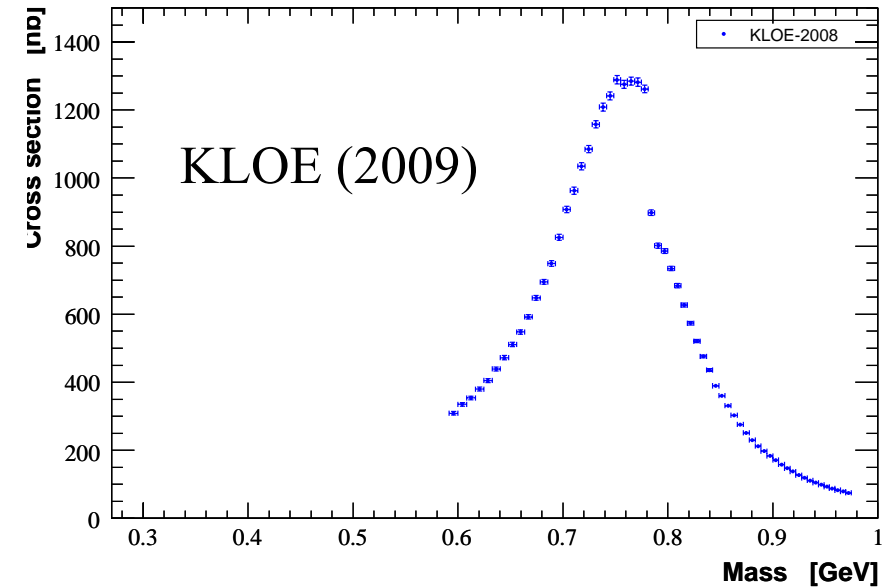
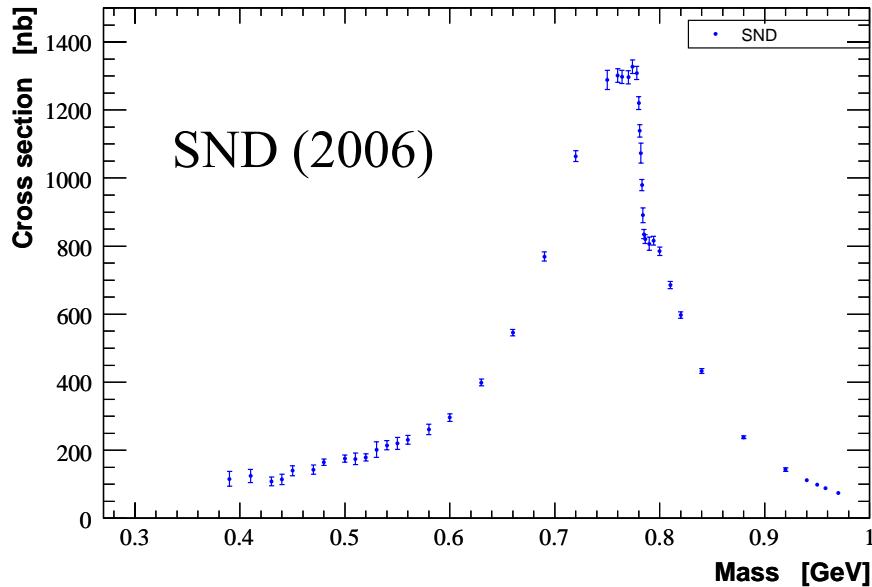
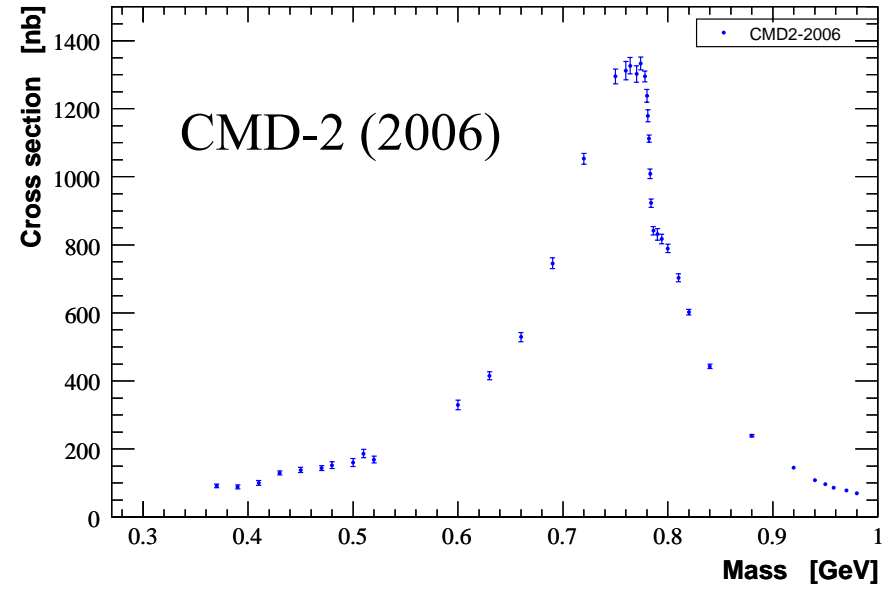
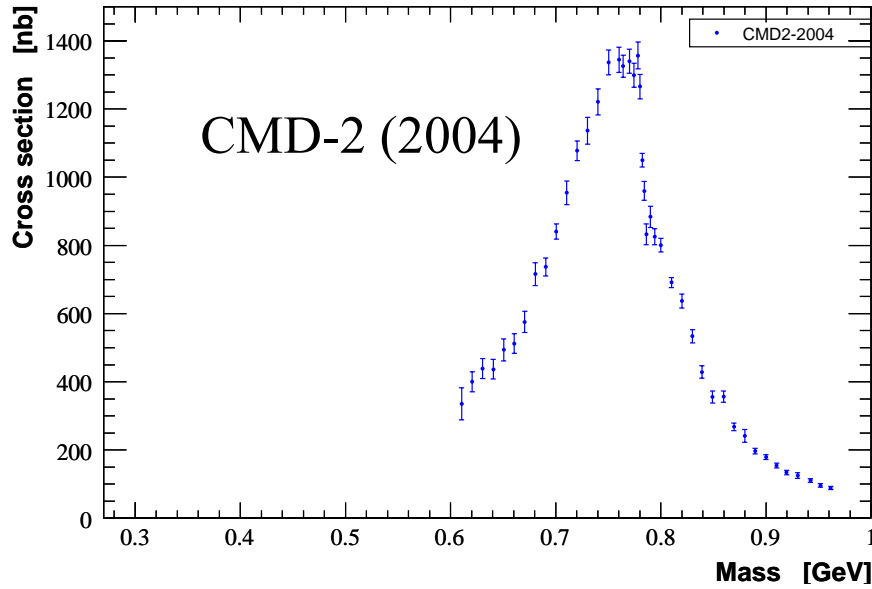
$$25.5 \pm 8.0$$

$2\pi$  from BaBar only

combined ee including BaBar

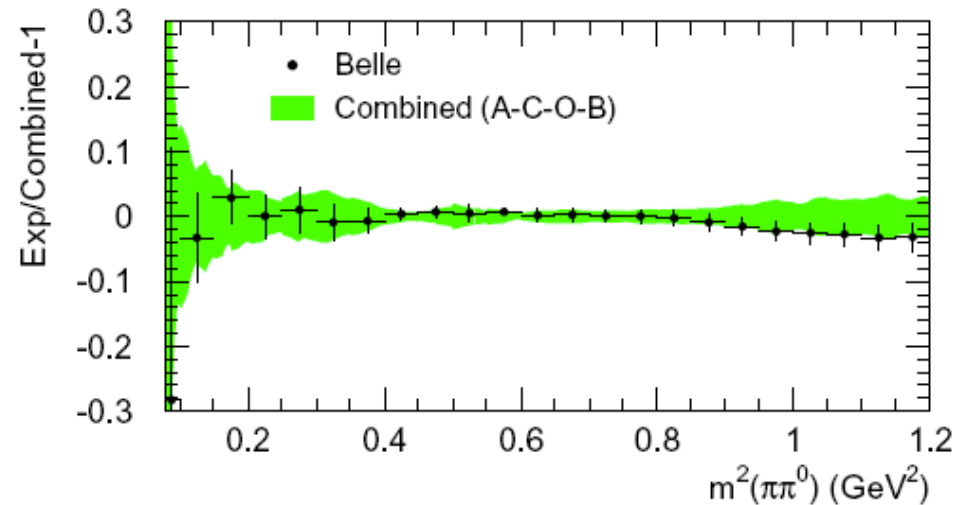
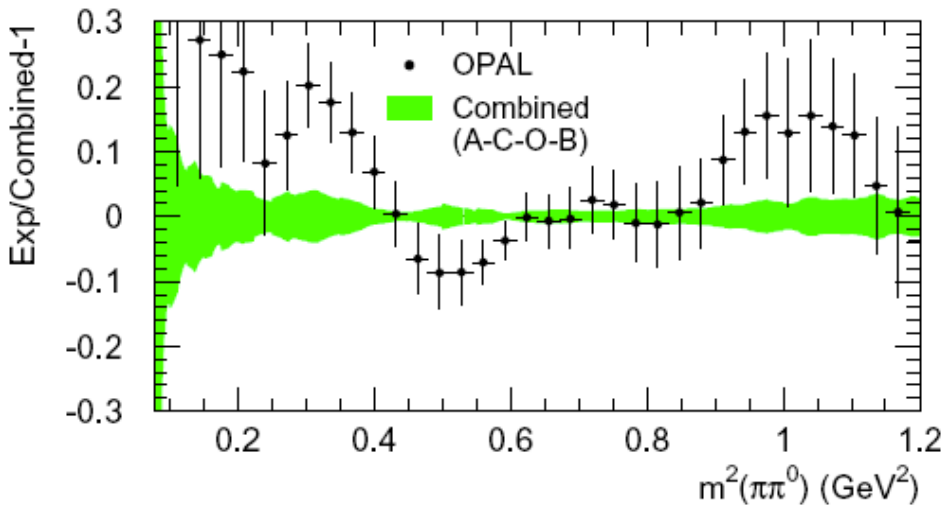
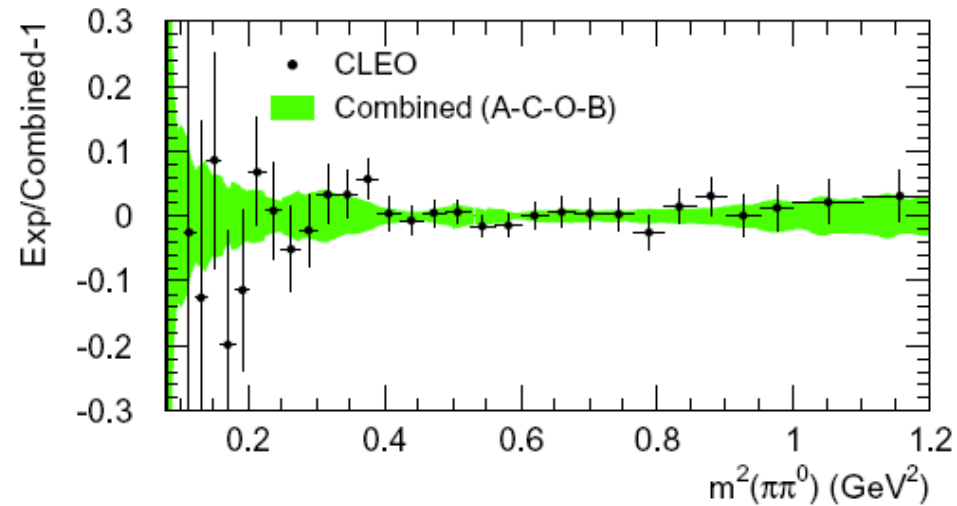
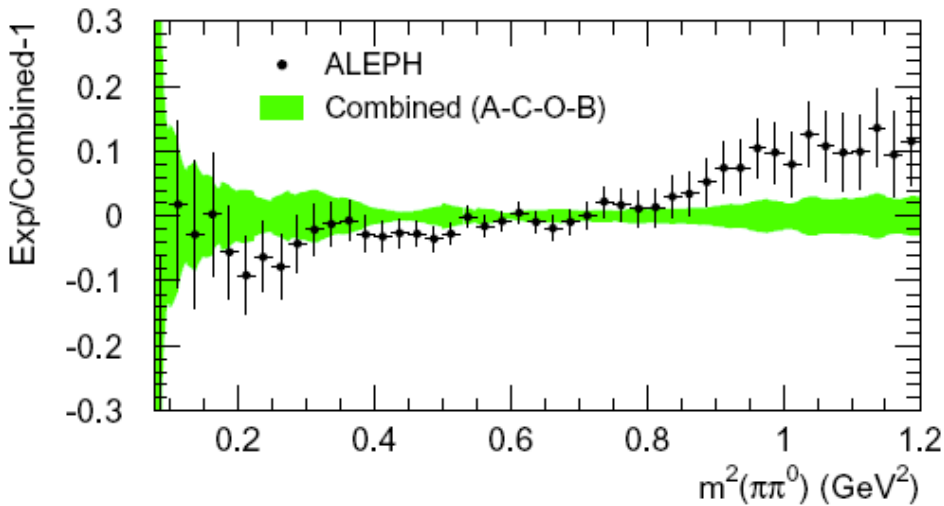
# Backup Slides

# Data on $e^+e^- \rightarrow \text{hadrons}$





# Revisited Analysis using $\tau$ Data: including Belle



# Revisited Analysis $\tau$ Data: new IB corrections

| Source  | $\Delta a_\mu^{\text{had,LO}}[\pi\pi, \tau] (10^{-10})$ |                        |
|---|---|------------------------|
|   | GS model  | KS model               |
| $S_{\text{EW}}$                                   | $-12.21 \pm 0.15$                                       |                        |
| $G_{\text{EM}}$                                   | $-1.92 \pm 0.90$  |                        |
| FSR   | $+4.67 \pm 0.47$  |                        |
| $\rho$ - $\omega$ interference                    | $+2.80 \pm 0.19$  | $+2.80 \pm 0.15$       |
| $m_{\pi^\pm} - m_{\pi^0}$ effect on $\sigma$      | $-7.88$   |                        |
| $m_{\pi^\pm} - m_{\pi^0}$ effect on $\Gamma_\rho$ | $+4.09$   | $+4.02$                |
| $m_{\rho^\pm} - m_{\rho_{\text{bare}}^0}$         | $0.20^{+0.27}_{-0.19}$                                  | $0.11^{+0.19}_{-0.11}$ |
| $\pi\pi\gamma$ , electrom. decays                 | $-5.91 \pm 0.59$  | $-6.39 \pm 0.64$       |
| Total   | $-16.07 \pm 1.22$                                       | $-16.70 \pm 1.23$      |
|   | $-16.07 \pm 1.85$                                       |                        |

# The Measurement

- ISR photon at large angle in EMC
  - 1 (for efficiency) or 2 (for physics) tracks of good quality
  - identification of the charged particles
  - separate  $\pi\pi/\text{KK}/\mu\mu$  event samples
  - kinematic fit (not using ISR photon energy) including 1 additional photon
  - obtain all efficiencies (trigger, filter, tracking, ID, fit) from same data
  - **measure ratio of  $\pi\pi\gamma(\gamma)$  to  $\mu\mu\gamma(\gamma)$  cross sections to cancel**
    - ee luminosity
    - additional ISR
    - vacuum polarization
    - ISR photon efficiency
- } otherwise ~2% syst error
- correct for  $|\text{FSR}|^2$  contribution in  $\mu\mu\gamma(\gamma)$  (QED, <1% below 1 GeV)
  - additional FSR photons measured

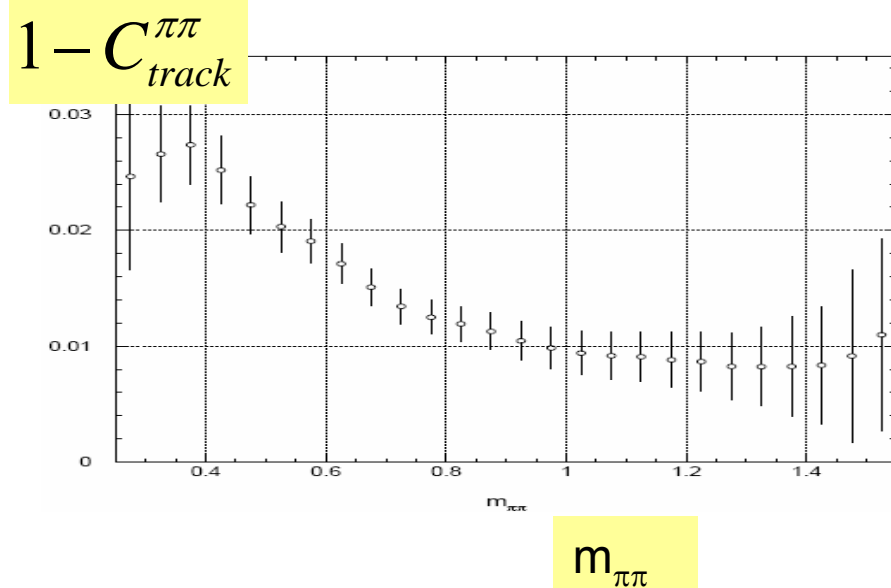
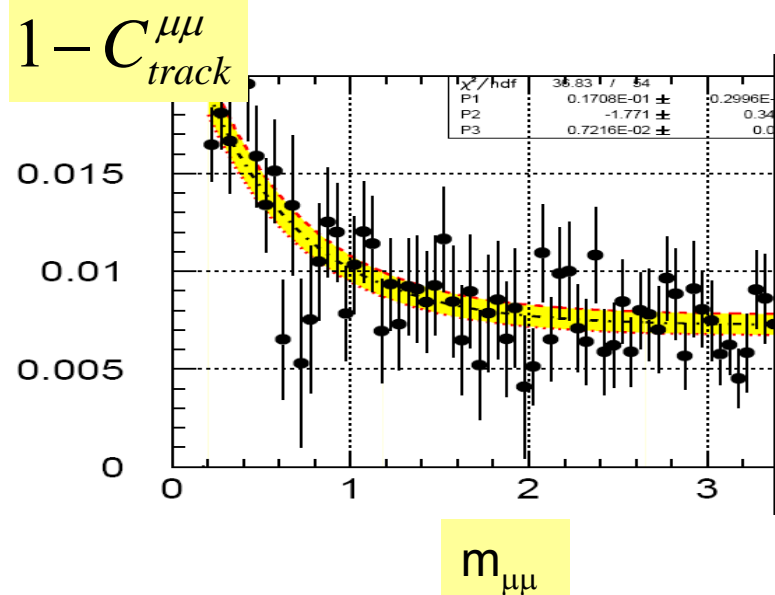
$$R_{\text{exp}}(s') = \frac{\sigma_{[\pi\pi\gamma(\gamma)]}(s')}{\sigma_{[\mu\mu\gamma(\gamma)]}(s')} = \frac{\sigma_{[\pi\pi(\gamma)]}^0(s')}{(1 + \delta_{\text{FSR}}^{\mu\mu})\sigma_{[\mu\mu(\gamma)]}^0(s')} = \frac{R(s')}{(1 + \delta_{\text{FSR}}^{\mu\mu})(1 + \delta_{\text{add,FSR}}^{\mu\mu})}$$

# Data/MC Tracking Correction to $\pi\pi\gamma, \mu\mu\gamma$ cross sections

- single track efficiency
- correlated loss probability  $f_0$
- probability to produce more than 2 tracks  $f_3$

$$C_{track}^{\mu\mu} = \left( \frac{\mathcal{E}_{track}^{data}}{\mathcal{E}_{track}^{MC}} \right)^2 \frac{(1 - f_0 - f_3)^{data}}{(1 - f_0 - f_3)^{MC}}$$

and similarly for  $\pi\pi$



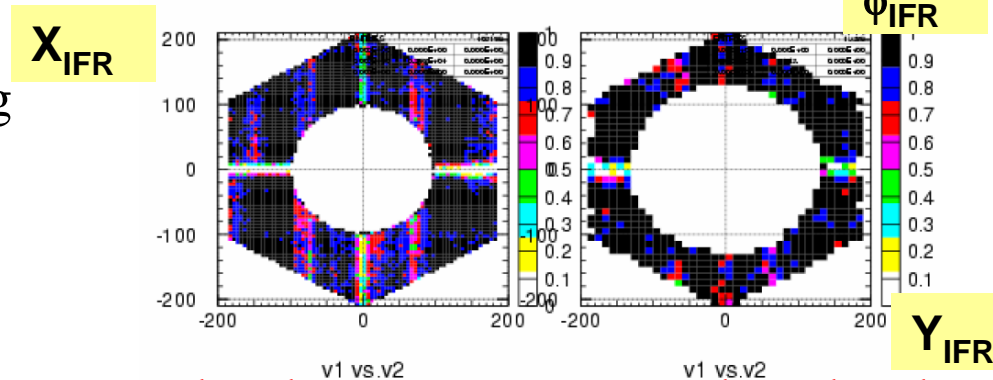
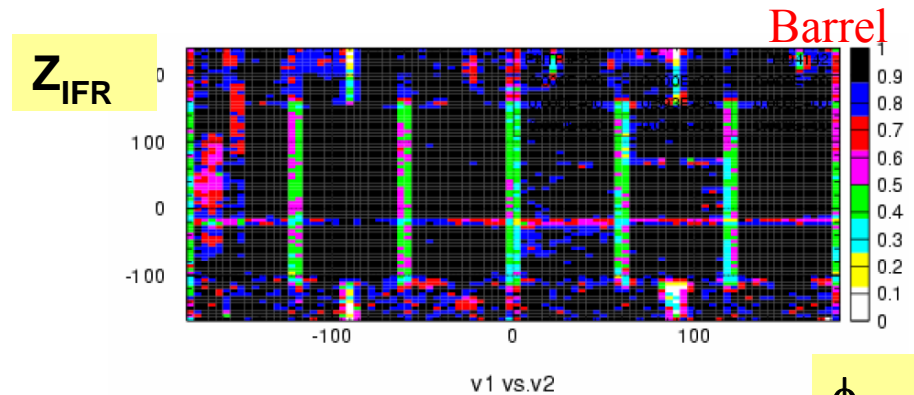
# Particle Identification

- Particle identification required to separate  $XX\gamma$  final processes
- Define 5 ID classes using cuts and PID selectors (complete and orthogonal set)
- Electrons rejected at track definition level ( $E_{cal}$ ,  $dE/dx$ )
- All ID efficiencies measured

$$\varepsilon_{X \rightarrow I}$$

- a tighter  $\pi$  ID ( $\pi_h$ ) is used for tagging in efficiency measurements and to further reject background in low cross section regions.

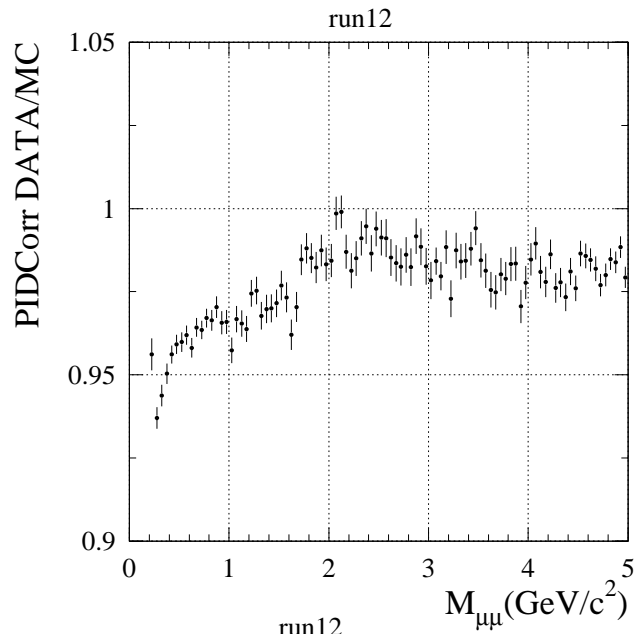
- \* isolated muons  $M_{\mu\mu} > 2.5 \text{ GeV}$   
→ efficiency maps ( $p, v_1, v_2$ )  
impurity  $(1.1 \pm 0.1) 10^{-3}$
- \* correlated efficiencies/close tracks  
→ maps ( $dv_1, dv_2$ )



Forward Endcap

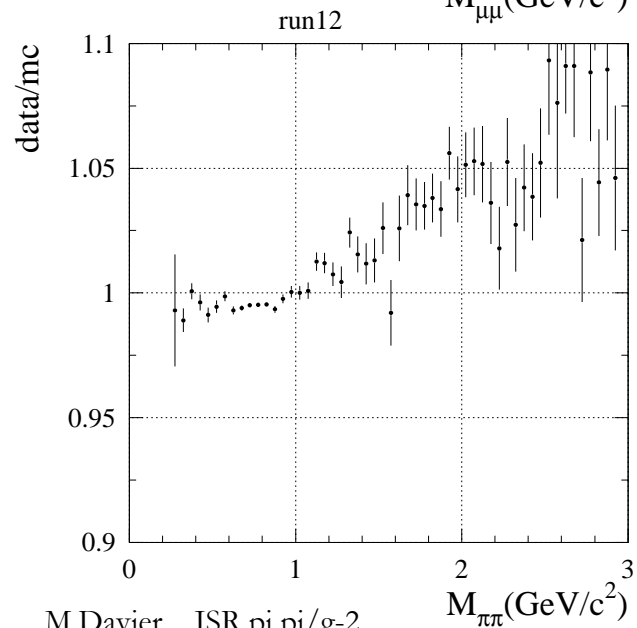
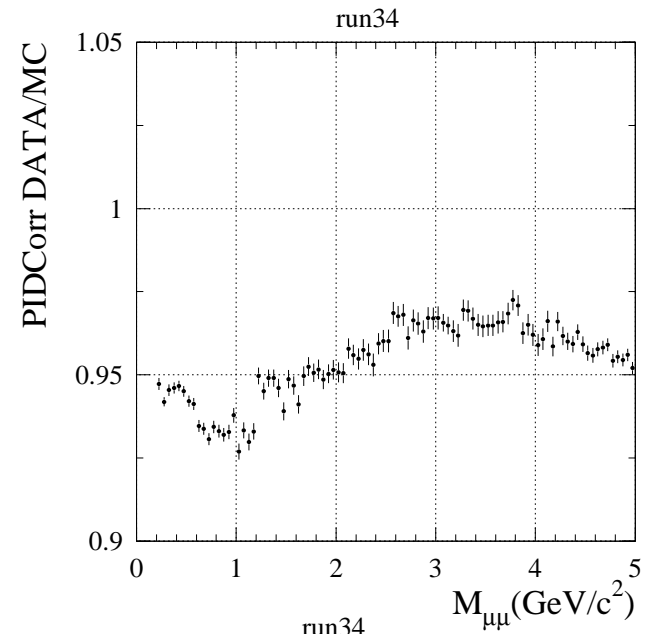
Backward Endcap

# Data/MC PID corrections to $\mu\mu$ and $\pi\pi$ cross sections

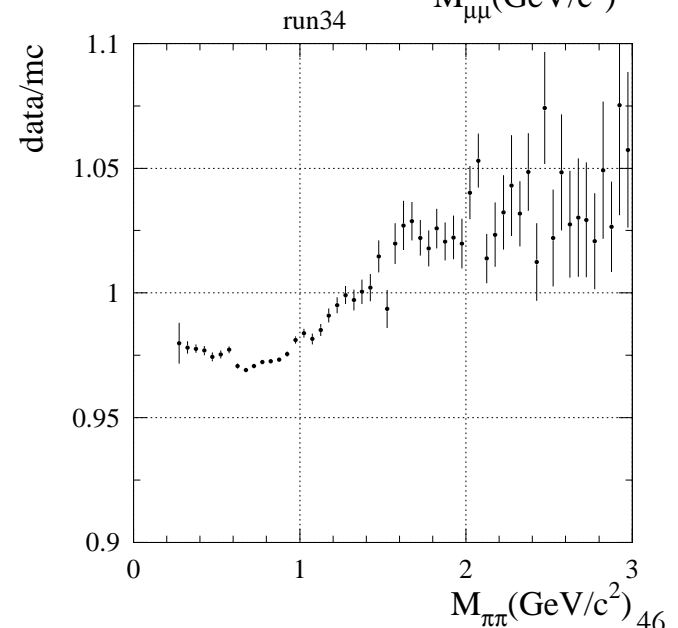


$\mu\mu\gamma$

Two running periods with different IFR performance



$\pi\pi\gamma$

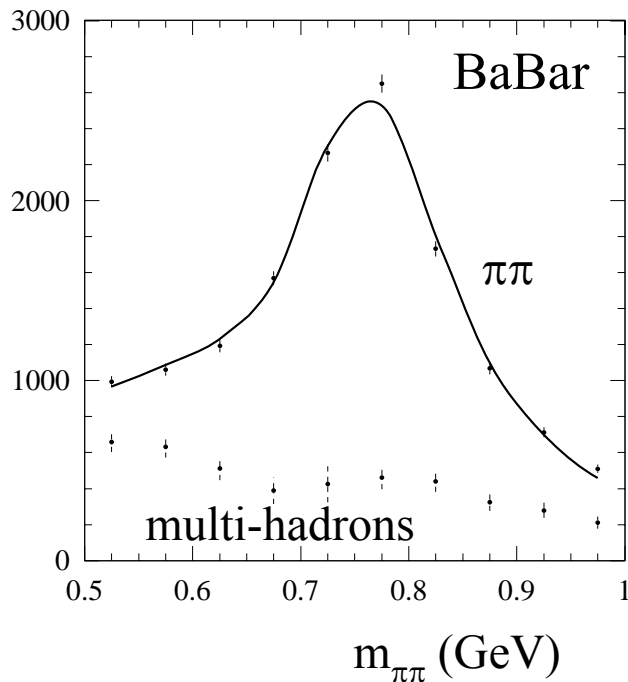


# Backgrounds

- background larger with loose  $\chi^2$  cut used in 0.5-1.0 GeV mass range
- $q\bar{q}$  and multi-hadronic ISR background from MC samples + normalization from data using signals from  $\pi^0 \rightarrow \gamma_{\text{ISR}} \gamma$  ( $q\bar{q}$ ), and  $\omega$  and  $\phi$  ( $\pi\pi\pi^0\gamma$ )
- global test in background-rich region near cut boundary

BG fractions in  $10^{-2}$  at  $m_{\pi\pi}$  values

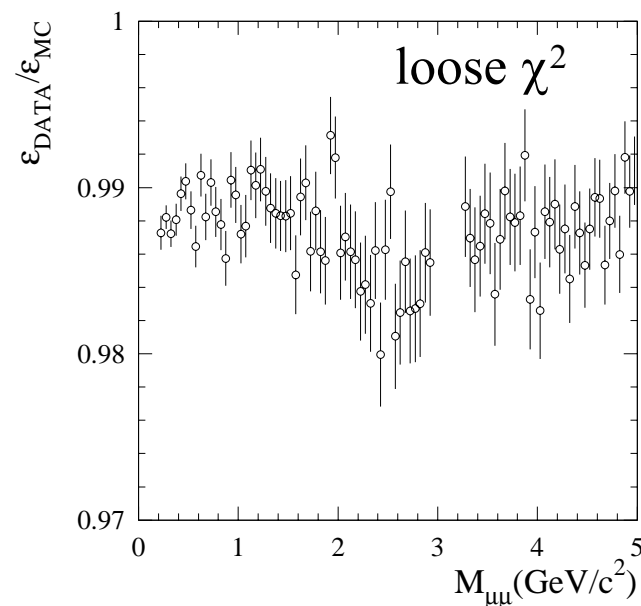
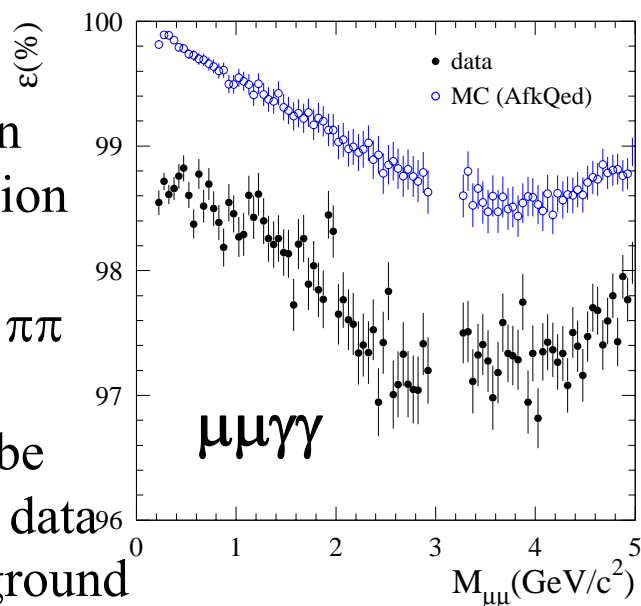
Fitted BG/predicted =  $0.968 \pm 0.037$



| process              | 0.525 GeV        | 0.775 GeV       | 0.975 GeV       |
|----------------------|------------------|-----------------|-----------------|
| $\mu\mu$             | $3.48 \pm 0.36$  | $0.37 \pm 0.23$ | $2.71 \pm 0.31$ |
| $KK$                 | $0.08 \pm 0.01$  | $0.01 \pm 0.01$ | $0.08 \pm 0.01$ |
| $\gamma 2\pi\pi^0$   | $8.04 \pm 0.41$  | $0.39 \pm 0.05$ | $0.88 \pm 0.19$ |
| $q\bar{q}$           | $1.11 \pm 0.17$  | $0.26 \pm 0.03$ | $1.81 \pm 0.19$ |
| $\gamma 2\pi 2\pi^0$ | $1.29 \pm 0.16$  | $0.06 \pm 0.01$ | $0.46 \pm 0.09$ |
| $\gamma 4\pi$        | $0.20 \pm 0.04$  | $0.09 \pm 0.01$ | $0.24 \pm 0.06$ |
| $\gamma p\bar{p}$    | $0.22 \pm 0.02$  | $0.04 \pm 0.01$ | $0.52 \pm 0.06$ |
| $\gamma \eta 2\pi$   | $0.02 \pm 0.01$  | $0.03 \pm 0.01$ | $0.09 \pm 0.01$ |
| $\gamma K_S K_L$     | $0.18 \pm 0.03$  | $0.01 \pm 0.01$ | $0.10 \pm 0.02$ |
| $\gamma 4\pi 2\pi^0$ | $< 0.01$         | $< 0.01$        | $< 0.01$        |
| $\tau\tau$           | $0.17 \pm 0.03$  | $0.04 \pm 0.01$ | $0.31 \pm 0.05$ |
| $\gamma ee$          | $0.63 \pm 0.63$  | $0.03 \pm 0.03$ | $0.27 \pm 0.27$ |
| total                | $15.38 \pm 0.87$ | $1.31 \pm 0.24$ | $7.37 \pm 0.51$ |

# $\chi^2$ cut Efficiency Correction

- depends on simulation of ISR (FSR), resolution effects (mostly ISR  $\gamma$  direction) for  $\mu\mu$  and  $\pi\pi$
- $\chi^2$  cut efficiency can be well measured in  $\mu\mu$  data because of low background

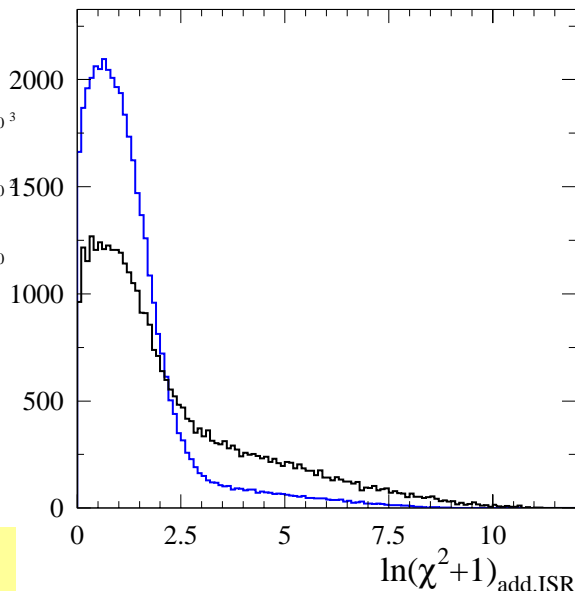
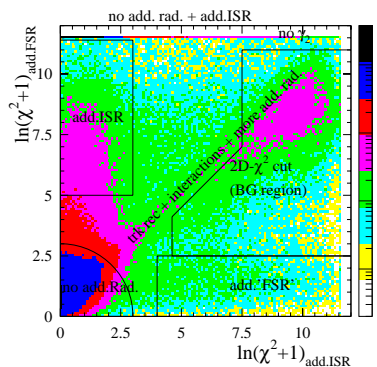


- main correction from lack of angular distribution for additional ISR in AfkQed
- common correction: 1% for loose  $\chi^2$ , 7% for tight  $\chi^2$
- additional loss for  $\pi\pi$  because of interactions studied with sample of interacting events  
much better study now, 2 independent methods

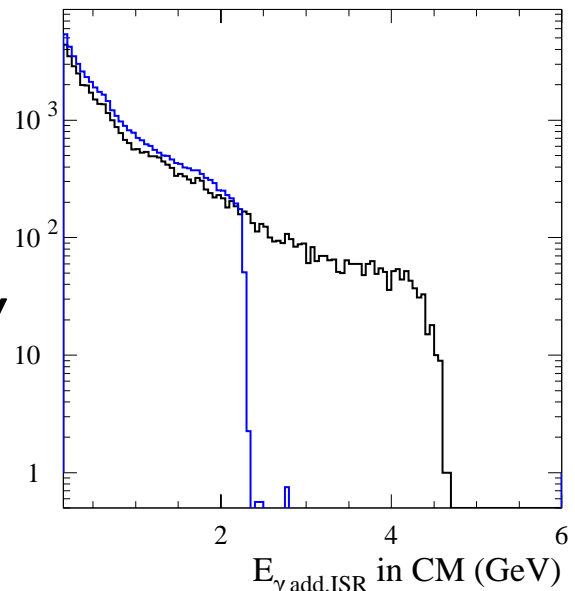
secondary interactions  
 data/MC  $1.51 \pm 0.03$   
 syst error  $0.3 - 0.9 \times 10^{-3}$



# Additional ISR

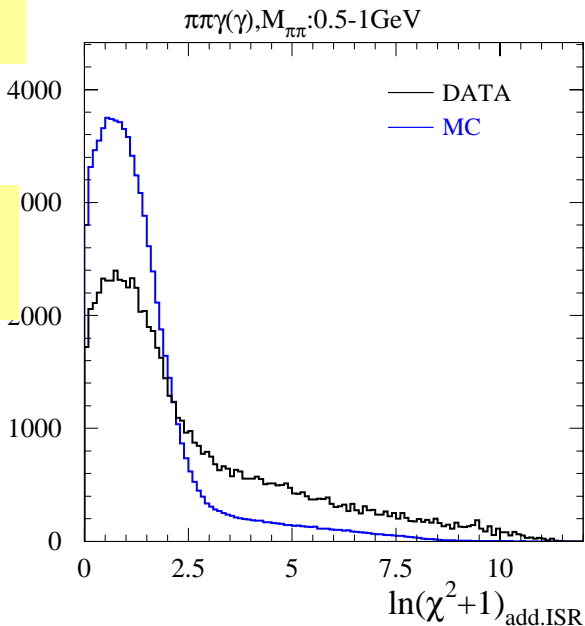


$\mu\mu\gamma\gamma$

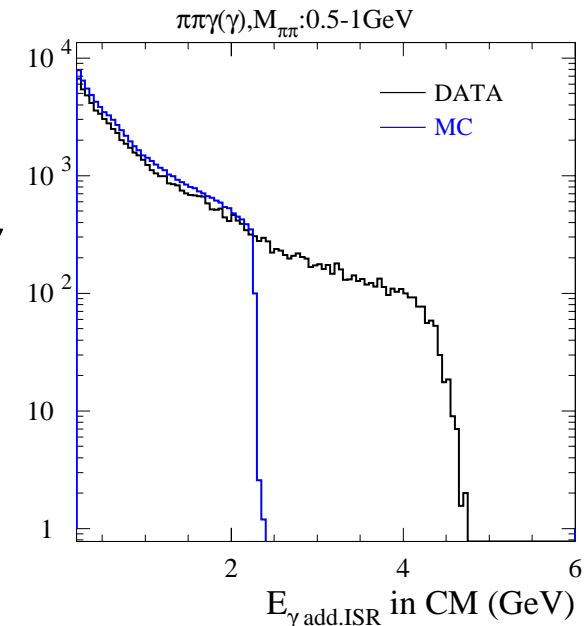


Angular distribution of add. ISR /beams!

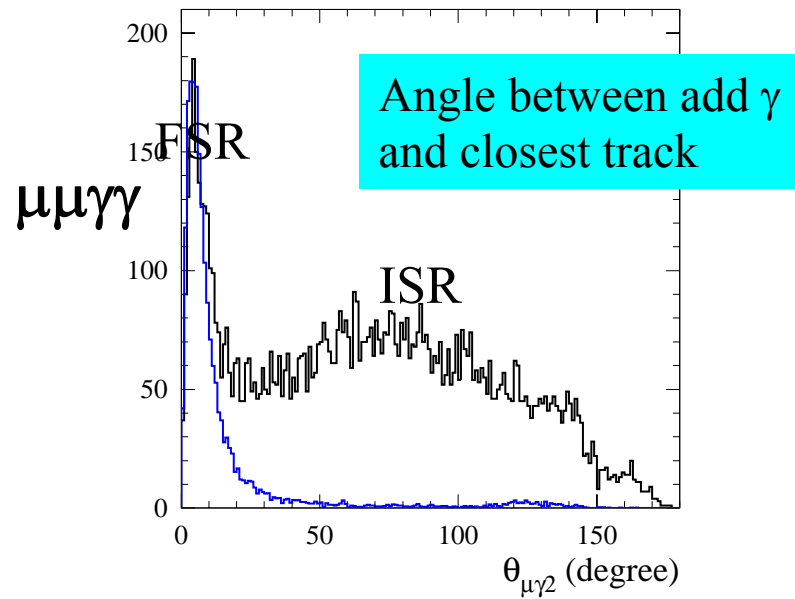
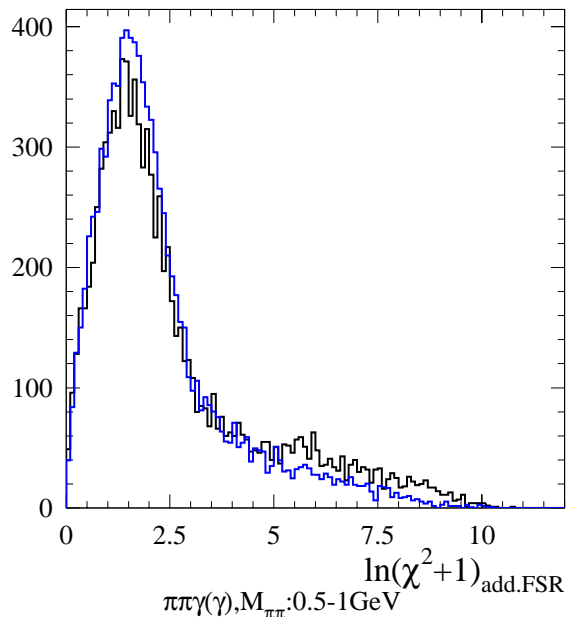
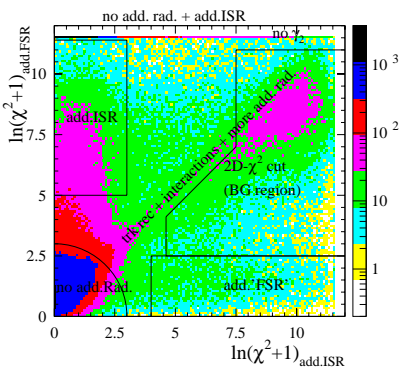
Energy cut-off for add. ISR in AfkQed



$\pi\pi\gamma\gamma$



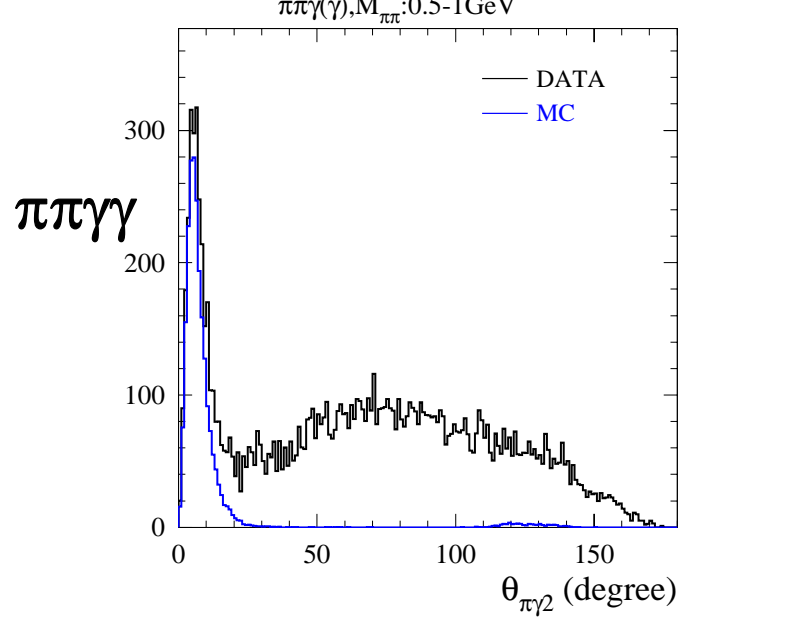
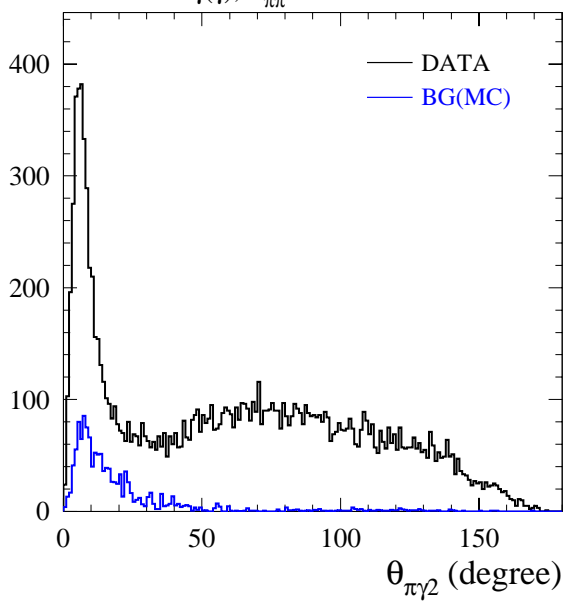
# Additional FSR



Large-angle add.ISR  
in data  $\neq$  AfkQed

Evidence for FSR  
data  $\sim$  AfkQed

data/MC  
 $\mu\mu$   $0.96 \pm 0.06$   
 $\pi\pi$   $1.21 \pm 0.05$



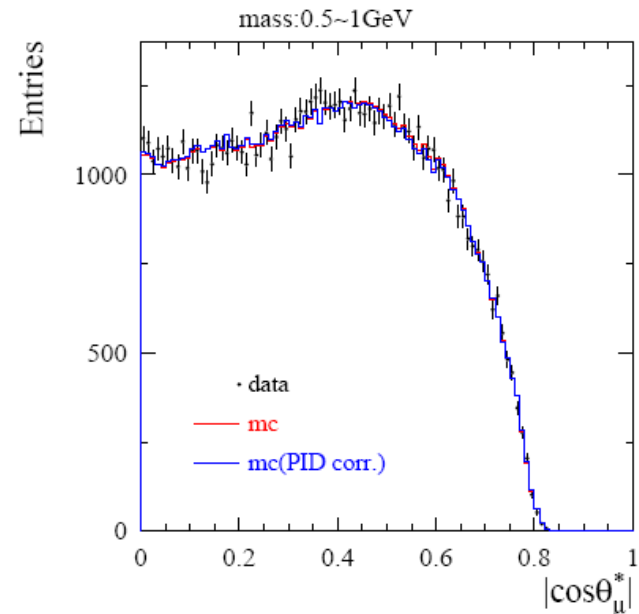
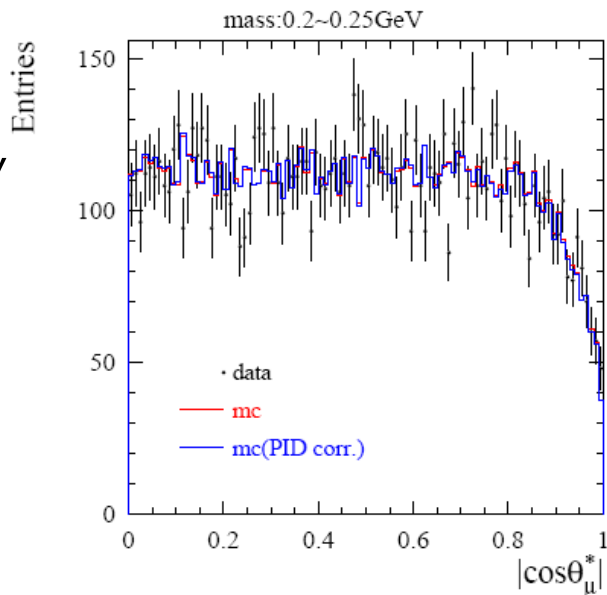
# Checking Known Distributions

$\text{Cos}\theta^*$  in XX CM /  $\gamma$

$\mu\mu$

flat at threshold

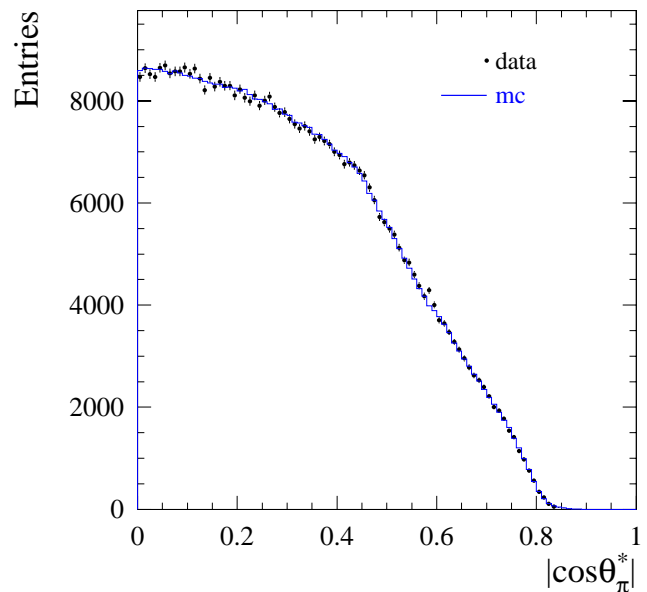
$1 + \cos^2\theta^* \quad \beta_\mu \rightarrow 1$



$\pi\pi$

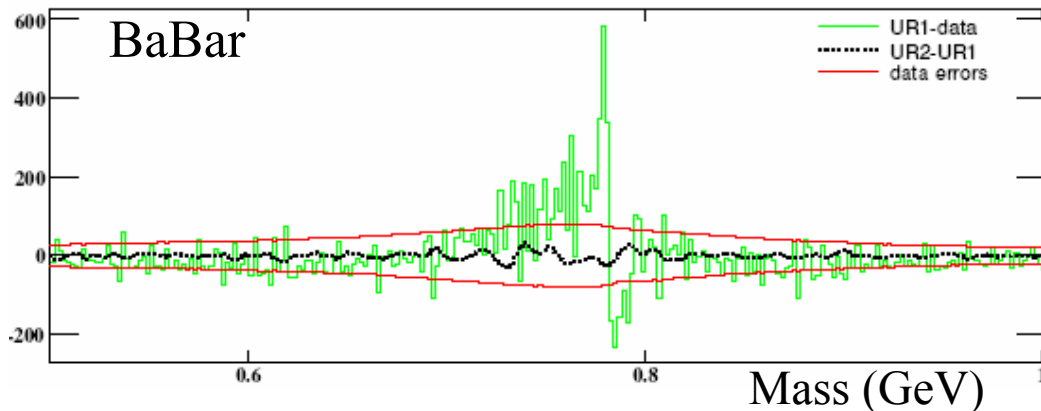
$\sin^2\theta^* \quad \forall \beta_\pi$

$P > 1 \text{ GeV}$  track requirement  $\Rightarrow$  loss at  $\text{cos}\theta^* \sim 1$

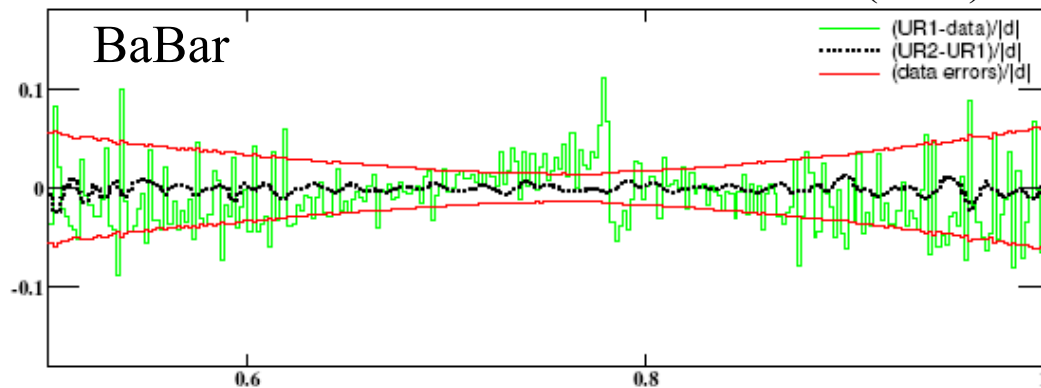


# Unfolding $\pi\pi$ Mass Spectrum

- measured mass spectrum distorted by resolution effects and FSR ( $m_{\pi\pi}$  vs.  $\sqrt{s}$ )
- iterative unfolding method (B. Malaescu arXiv:0907-3791)
- mass-transfer matrix from simulation with corrections from data
- 2 MeV bins in 0.5-1.0 GeV mass range, 10 MeV bins outside
- most salient effect in  $\rho$ - $\omega$  interference region (little effect on  $a_{\mu}^{\pi\pi}$ )



Absolute difference  
unfolded(1) – raw data  
unfolded(2) – unfolded(1)  
Statistical errors (band)



Relative difference

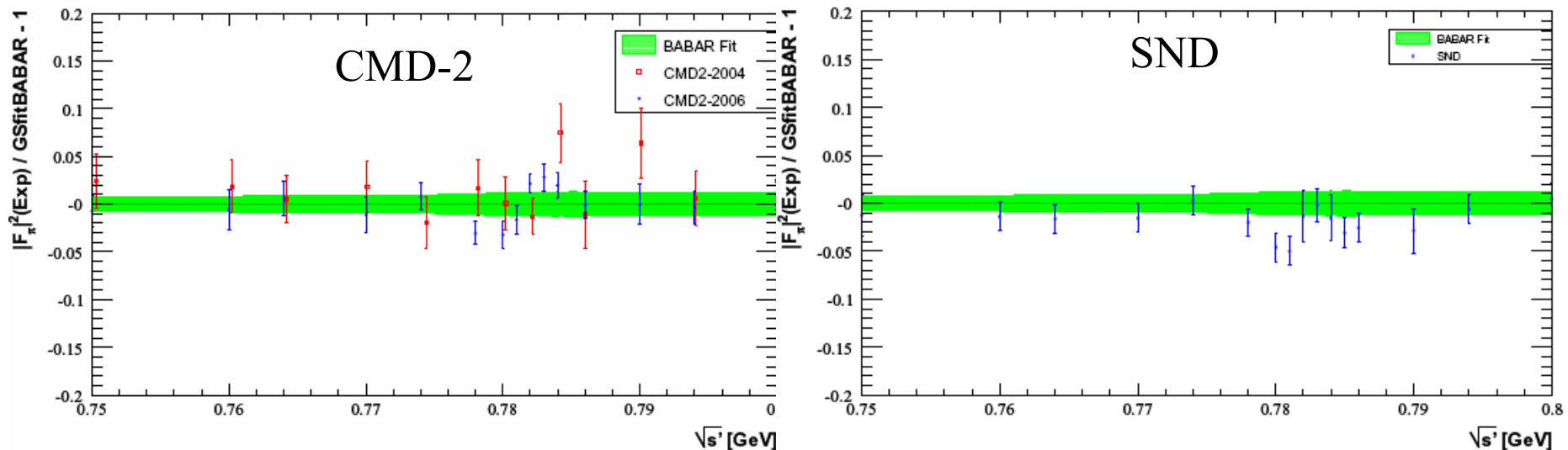
# Changes since preliminary results at Tau08

- preliminary results Sept. 2008: only 0.5-3 GeV (excess/expect. near threshold)
- problem explored (Oct. 2008- Feb. 2009): trigger/BGFilter, ee background
- $\mu\mu \rightarrow \pi\pi$  re-investigated  $\Rightarrow$  direct measurement achieved using ID probabilities  
before: model for correlated loss, no precise direct check  
 $\Rightarrow$  significant changes  $\mu\mu$  efficiency for ISR lumi  $\uparrow\uparrow$  +0.9%  
 $\mu\mu$  contamination in  $\pi\pi$  sample  $\downarrow\downarrow$   
 $\Rightarrow \pi\pi$  cross section  $\downarrow\downarrow$ 

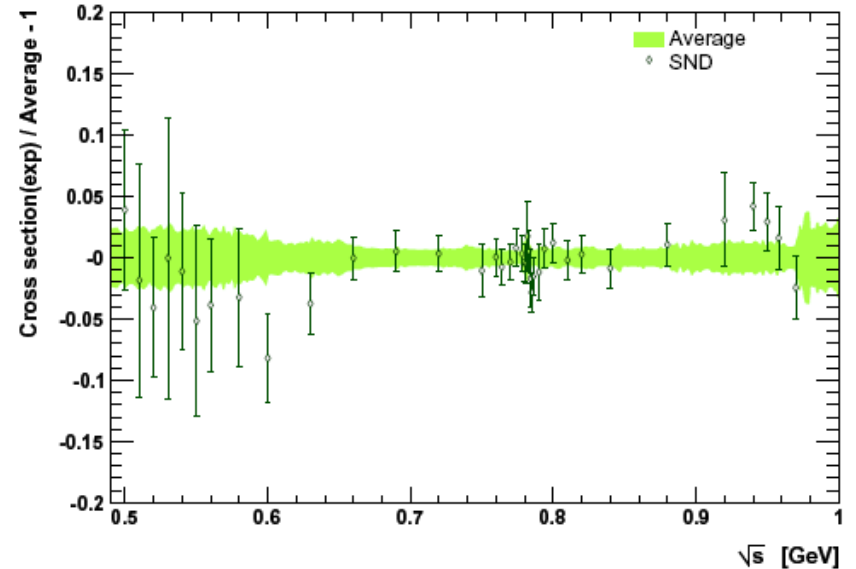
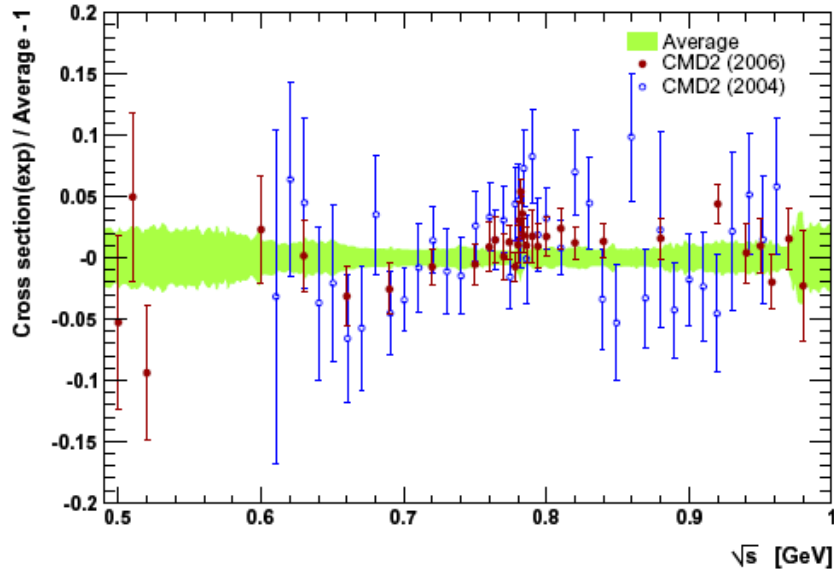
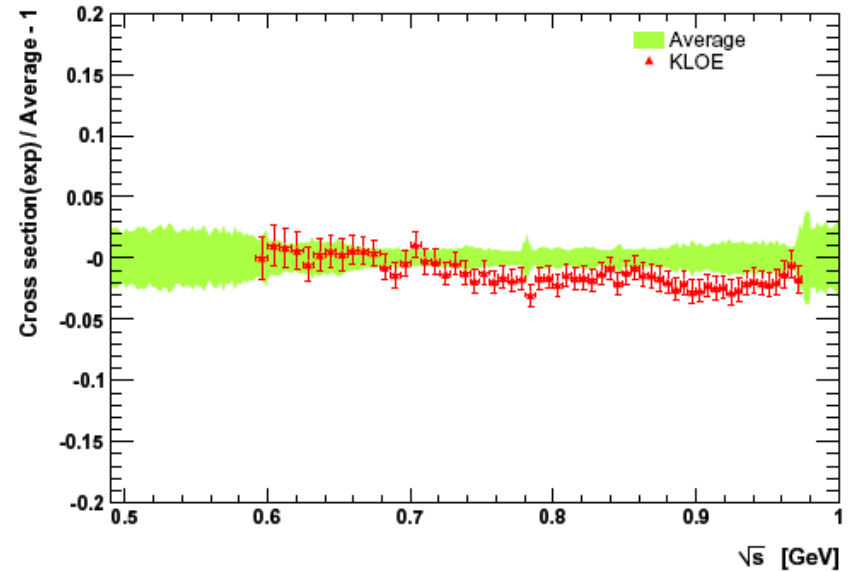
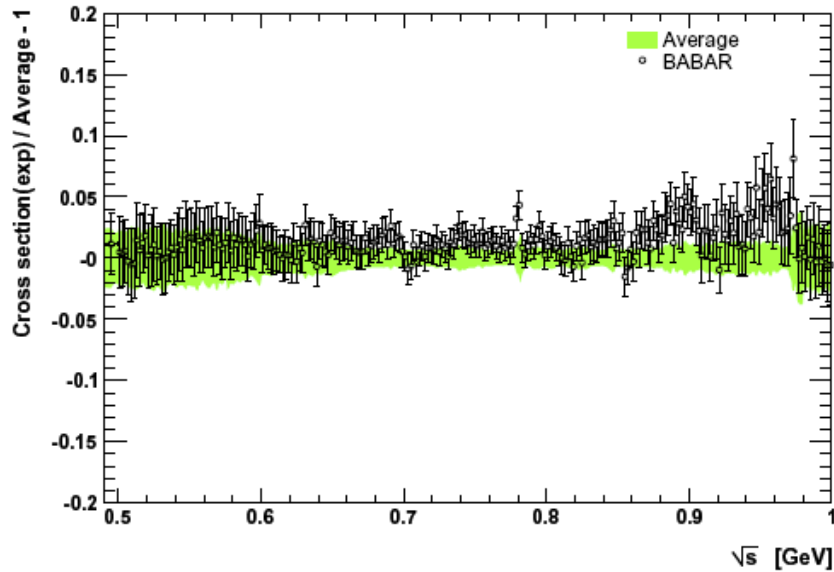
|       |           |
|-------|-----------|
| -1.8% | 0.525 GeV |
| -1.0% | 0.775 GeV |
| -1.4% | 0.975 GeV |
- other changes: - MC unfolding mass matrix corrected for data/MC differences (small)
  - ISR lumi now used in 50-MeV sliding bins, instead of global fit
  - cancellation of add ISR in  $\pi\pi/\mu\mu$  ratio studied/corrected
- extensive review

# BaBar vs. other ee data ( $\rho$ - $\omega$ interference region)

- mass calibration of BaBar checked with ISR-produced  $J/\psi \rightarrow \mu\mu$
- expect  $-(0.16 \pm 0.16)$  MeV at  $\rho$  peak
- $\omega$  mass determined through VDM mass fit
$$m_{\omega}^{\text{fit}} - m_{\omega}^{\text{PDG}} = -(0.12 \pm 0.29) \text{ MeV}$$
- Novosibirsk data precisely calibrated using resonant depolarization
- comparison BaBar/CMD-2/SND in  $\rho$ - $\omega$  interference region shows no evidence for a mass shift



# Consistency of Experiments with Average



# Backup Slides

| Energy range (GeV)     | Experiment                  | $a_{\mu}^{\text{had,LO}}[\pi\pi] (10^{-10})$   |
|------------------------|-----------------------------|--|
| $2m_{\pi^{\pm}} - 0.3$ | Combined $e^{+}e^{-}$ (fit) | $0.55 \pm 0.01$  |
| 0.30 – 0.63            | Combined $e^{+}e^{-}$       | $132.6 \pm 0.8 \pm 1.0 (1.3_{\text{tot}})$   |
| 0.63 – 0.958           | CMD2 03                     | $361.8 \pm 2.4 \pm 2.1 (3.2_{\text{tot}})$   |
|                        | CMD2 06                     | $360.2 \pm 1.8 \pm 2.8 (3.3_{\text{tot}})$   |
|                        | SND 06                      | $360.7 \pm 1.4 \pm 4.7 (4.9_{\text{tot}})$   |
|                        | KLOE 08                     | $356.8 \pm 0.4 \pm 3.1 (3.1_{\text{tot}})$   |
|                        | BABAR 09                    | $365.2 \pm 1.9 \pm 1.9 (2.7_{\text{tot}})$   |
|                        | Combined $e^{+}e^{-}$       | $360.8 \pm 0.9 \pm 1.8 (2.0_{\text{tot}})$   |
| 0.958 – 1.8            | Combined $e^{+}e^{-}$       | $14.4 \pm 0.1 \pm 0.1 (0.2_{\text{tot}})$  |
| Total                  | Combined $e^{+}e^{-}$       | $508.4 \pm 1.3 \pm 2.6 (2.9_{\text{tot}})$   |
| Total                  | Combined $\tau$ [1]         | $515.2 \pm 2.0_{\text{exp}} \pm 2.2_{\text{B}} \pm 1.6_{\text{IB}} (3.4_{\text{tot}})$ |



# Backup Slides

